

Magnetic Microscopy

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<http://spin.ijl.cnrs.fr>

Special thanks !



Jeffrey McCord



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Thomas Hauet

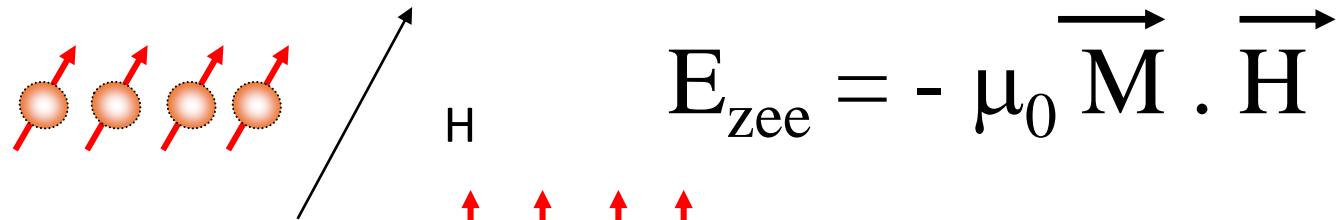


Daniel Lacour



Interactions

Zeeman Energy



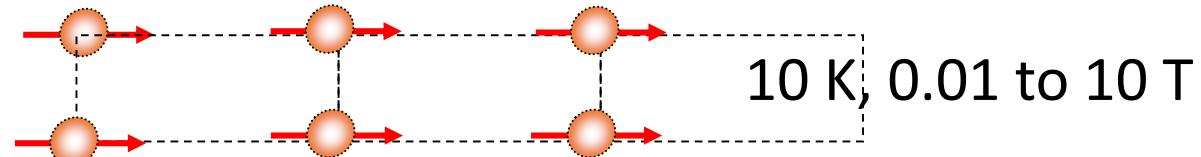
Exchange



1000 K, 100 T

$$E_{\text{exc}} = -J \vec{S}_1 \cdot \vec{S}_2$$

Magneto-crystalline
anisotropy



$$E_K = -K \cos^2(\theta)$$

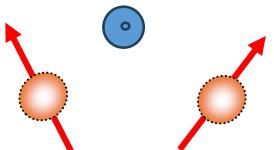
Dipolar



1 K, 10 mT

$$E_{\text{dip}} = -\mu_0 \vec{M} \cdot \vec{H}_{\text{dip}}$$

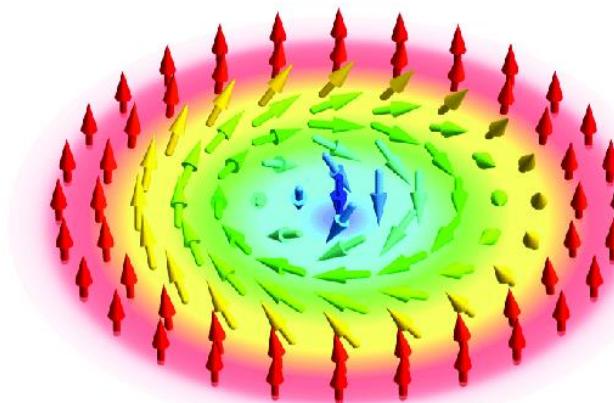
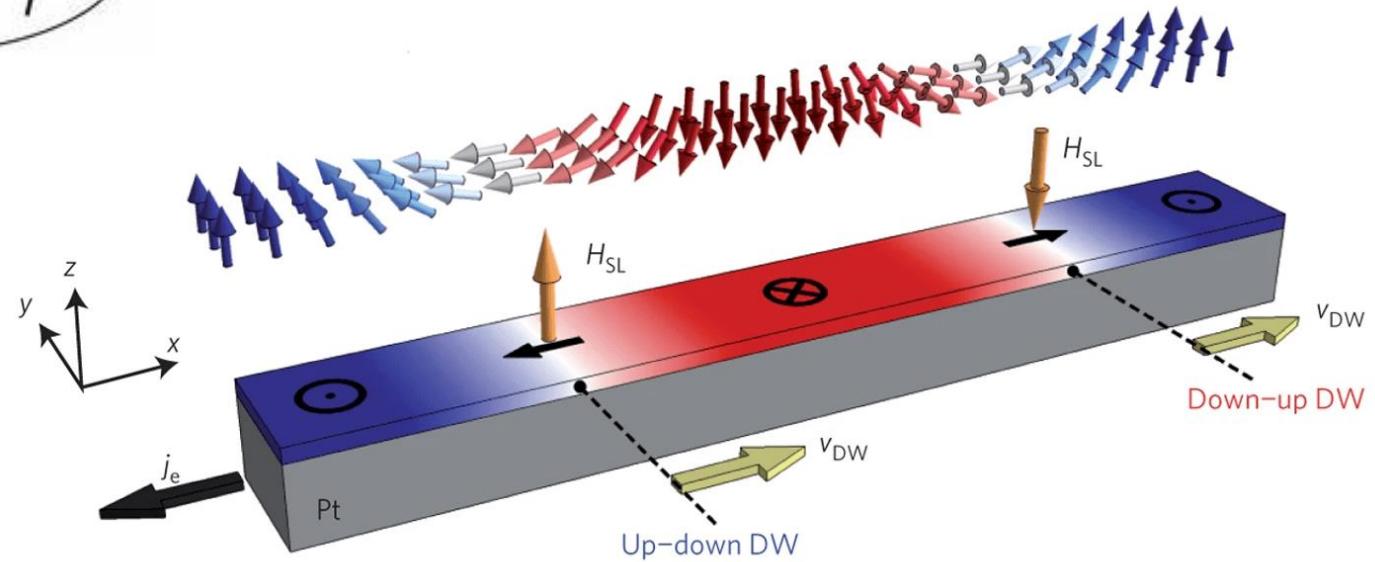
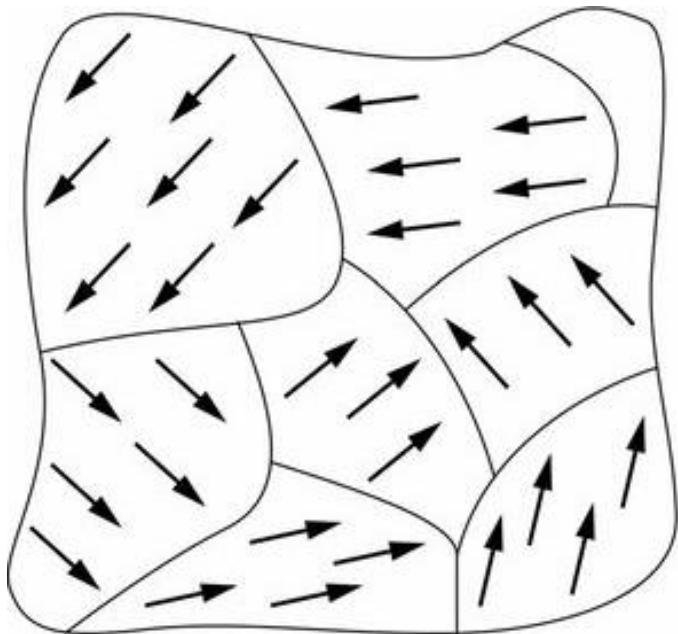
Dzyaloshinskii–Moriya interaction (DMI)



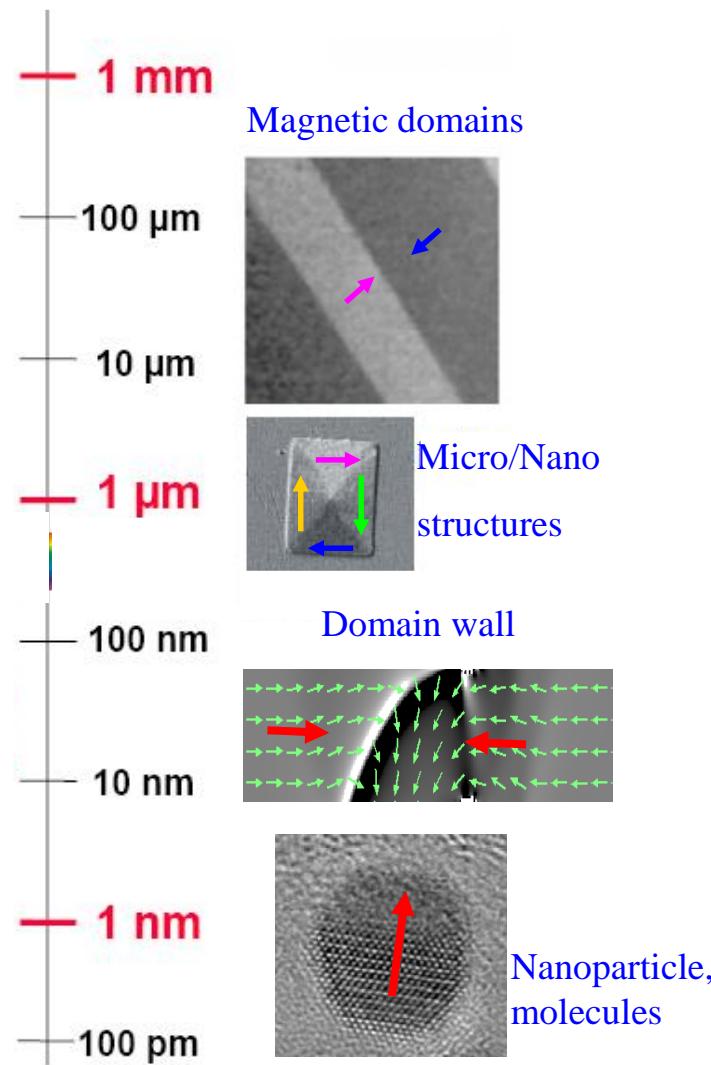
$$E_{\text{DMI}} = D_{12} \cdot (\vec{S}_1 \times \vec{S}_2)$$

Configuration results from competition of the different interactions

Magnetic configurations



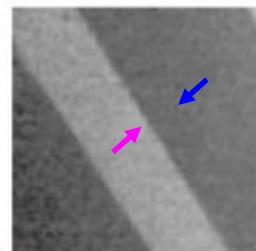
Spatial scale



Spatial scale

— 1 mm

Magnetic domains



100 µm

10 µm

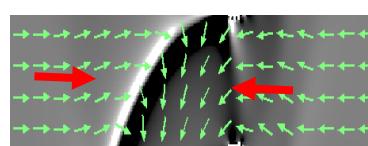
— 1 µm

Micro/Nano structures



100 nm

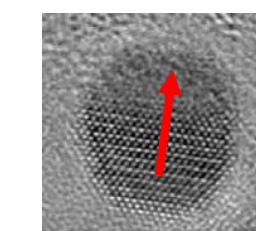
Domain wall



10 nm

— 1 nm

Nanoparticle,
molecules



100 pm

Magneto-optical microscopy (MO)

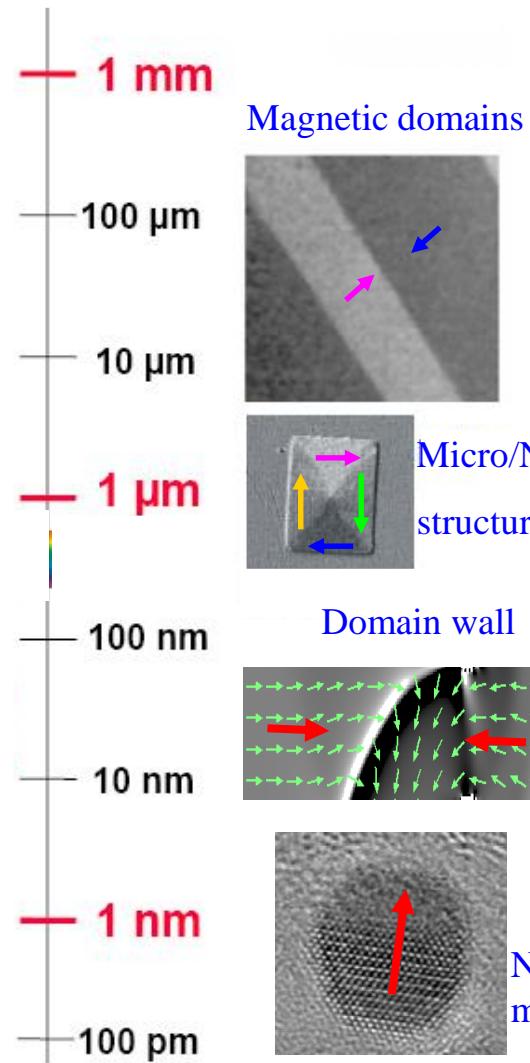
Scanning electron microscopy (SEMPA)

Transmission electron microscopy (TEM)

X-Ray microscopy

Magnetic force microscopy (MFM)

Spatial scale



What is measured?

- ❑ Magnetization, induction, stray field?
- ❑ Elemental resolution
- ❑ Direct or indirect?
- ❑ Quantitative or not?

Environmental conditions

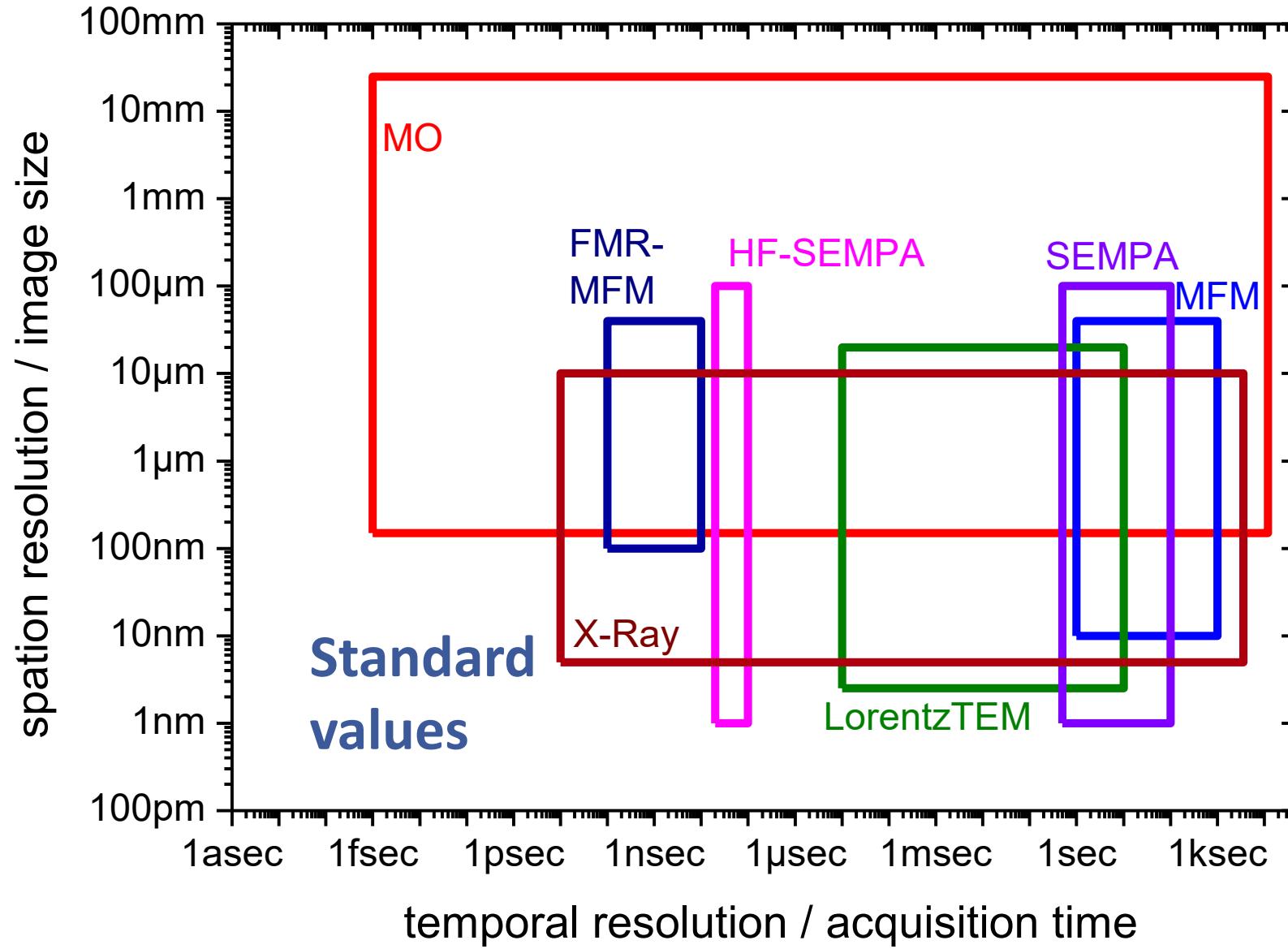
- ❑ Temperature
- ❑ Field: magnetic field, electric
- ❑ Electric current, light etc.
- ❑ Strain
- ❑ Additional measuring techniques

Which specifications?

- ❑ Magnetization: 1D, 2D, 3D
- ❑ Depth resolution: surface or volume?
- ❑ Lateral resolution
- ❑ Sensitivity
- ❑ Time/Spectral resolution

Versatility

- ❑ Sample preparation needed
- ❑ Time per one measurement
- ❑ In situ / ex situ
- ❑ Large-scale or in-lab?
- ❑ Expensive or cheap?



Magneto-optical microscopy (MO)

Scanning electron microscopy (SEMPA)

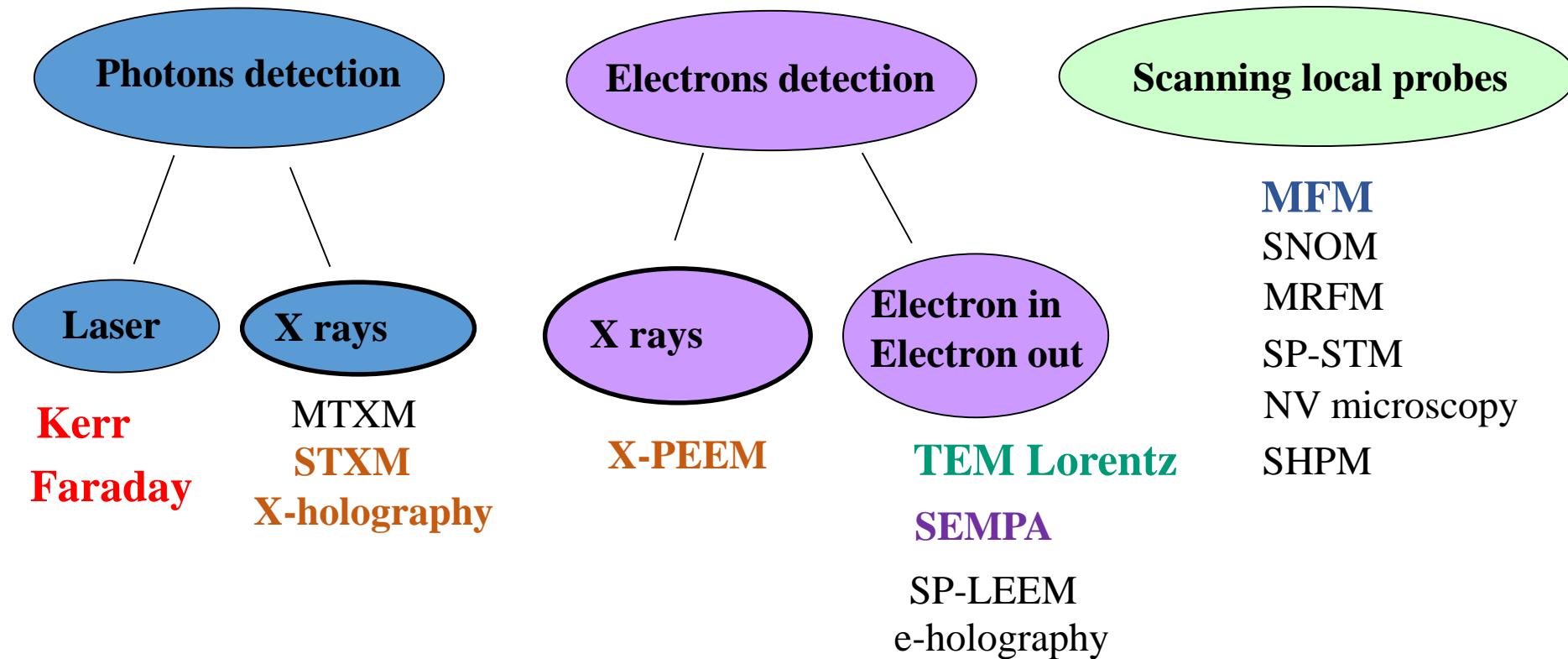
Transmission electron microscopy (TEM)

X-Ray microscopy

Magnetic force microscopy (MFM)

	Bitter pattern	MFM	SEM-I Secondary	TEM Fresnel and Foucault	TEM DPC	TEM Holography	SEM-II Back-scattered	SEMPA	SPLEEM	MOKE (Kerr microscopy)	XPEEM	STXM ^(a)
Contrast mechanism	∇B_{ext}	∇B_{ext}	∇B_{ext}	B	B	B, Φ_B	B	M	M	M	M	M
Evaluation of the magnetization, $M(r)$	Indirect	Indirect	Q	Indirect	Q	Q	Q	Q	Q	Q	Q	Q
Spatial resolution (nm) <small>Typical Limit</small>	$\frac{300}{80}$	$\frac{60}{20}$	$\frac{1000}{800}$	$\frac{50}{\sim 10}$	$\frac{10}{2}$	$\frac{20}{5}$	$\frac{2000}{1000}$	$\frac{150}{20}$	$\frac{40}{20}$	$\frac{800}{250}$	$\frac{300}{50}$	$\frac{30}{15}$
Depth of information (nm)	500–1000	20–500	10–50 nm	Thickness integrated <150 nm	Thickness integrated <100 nm	Thickness integrated <100 nm	10,000	1–2	<1	<20 (metals)	<5 nm	Thickness integrated <100 nm
Time for image acquisition	30 msec	5–20 mins	10–60 sec	50 msec–60 sec	5–60 secs	50 msec–10 sec	10–60 sec	1–100 min	~1sec	1 msec–5 sec	~1sec	~1sec
Limits on applied magnetic fields	None	<500 kA/m	Not advised	~100–500 kA/m	~100–500 kA/m	50 kA/m	Not advised	Not advised	Not advised	None	Not advised	None
Imaging conditions	None	In air	HV	HV	HV	HV	UHV	UHV	In air	UHV	None	
Max thickness	None	None	None	<150 nm	<100 nm	<100 nm	None	None	None			60–100 nm
Sample smoothness	R	R	NR	Preferred	Preferred	Preferred	NR	NR	R	R	NR	NR
Sample clean surface	NR	NR		Preferred	Preferred	Preferred	NR	R	R	NR	Preferred	NR

Type of measurements



NV = NV center of diamond probe

MFM = magnetic force microscopy

MRFM = magnetoc resonance force microscopy

MTXM = magnetic transmission X-ray microscopy

SEMPA = scanning electron microscopy with polarization analysis

SNOM = scanning near field optical microscopy

SP-LEEM = spin polarized low energy electron microscopy

SHPM = scanning all probe microscopy

Outlines

Magneto-optical microscopy (MO)

Scanning electron microscopy (SEMPA)

Transmission electron microscopy (TEM)

X-Ray microscopy

Magnetic force microscopy (MFM)

Outlines

Magneto-optical microscopy (MO)

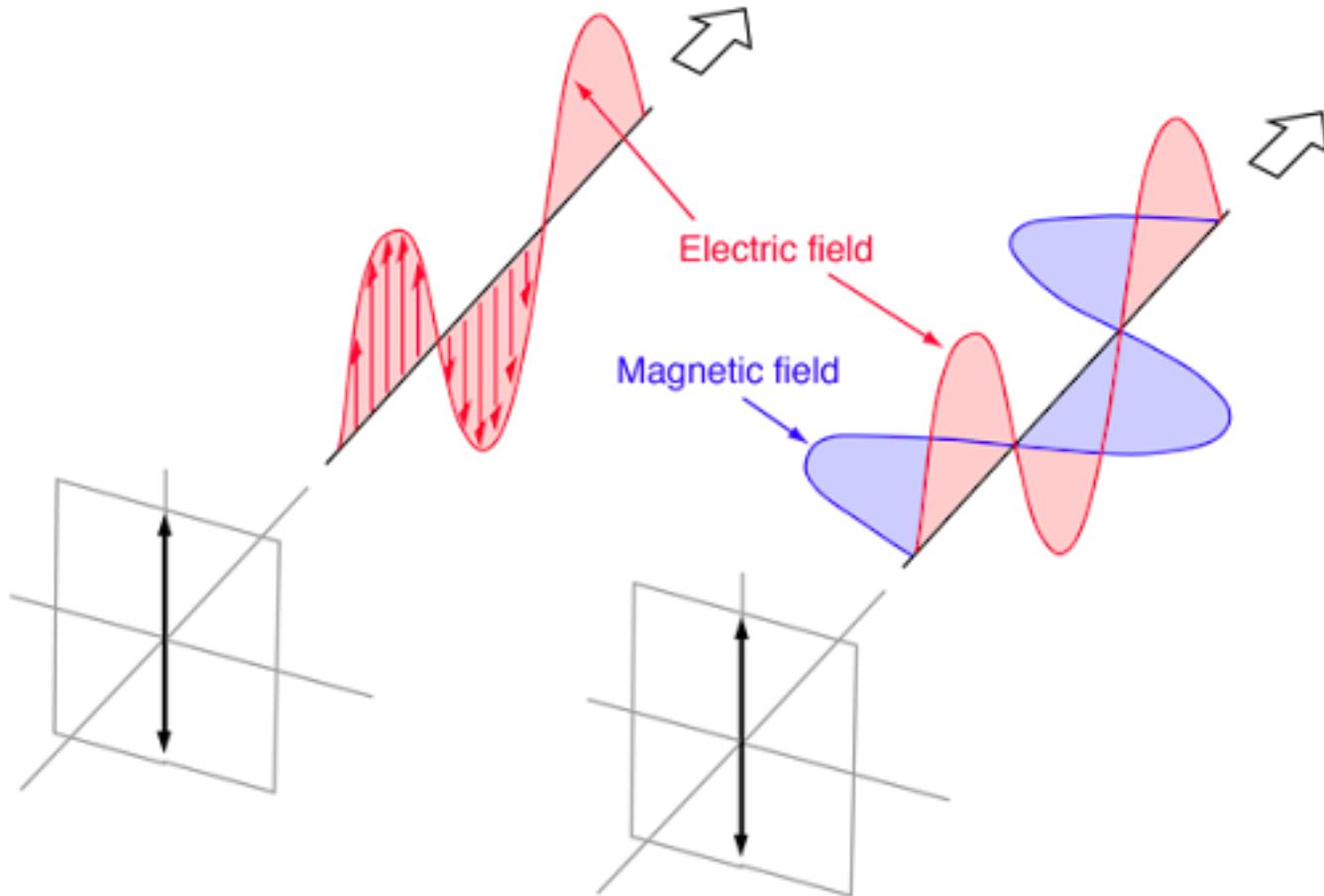
Scanning electron microscopy (SEMPA)

Transmission electron microscopy (TEM)

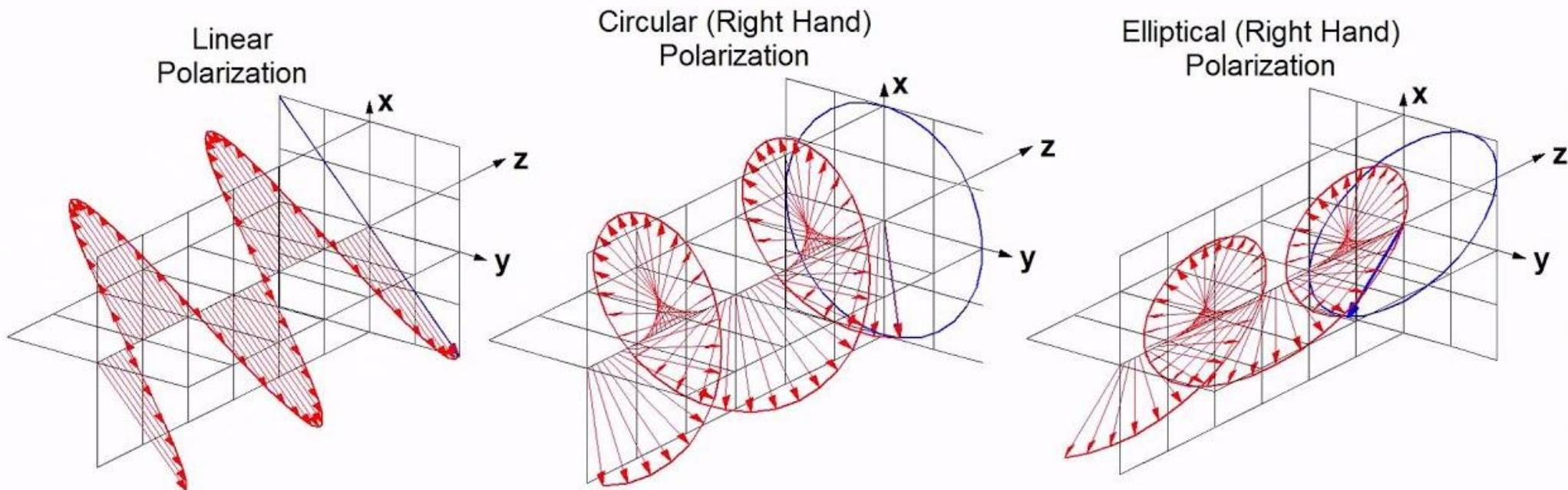
X-Ray microscopy

Magnetic force microscopy (MFM)

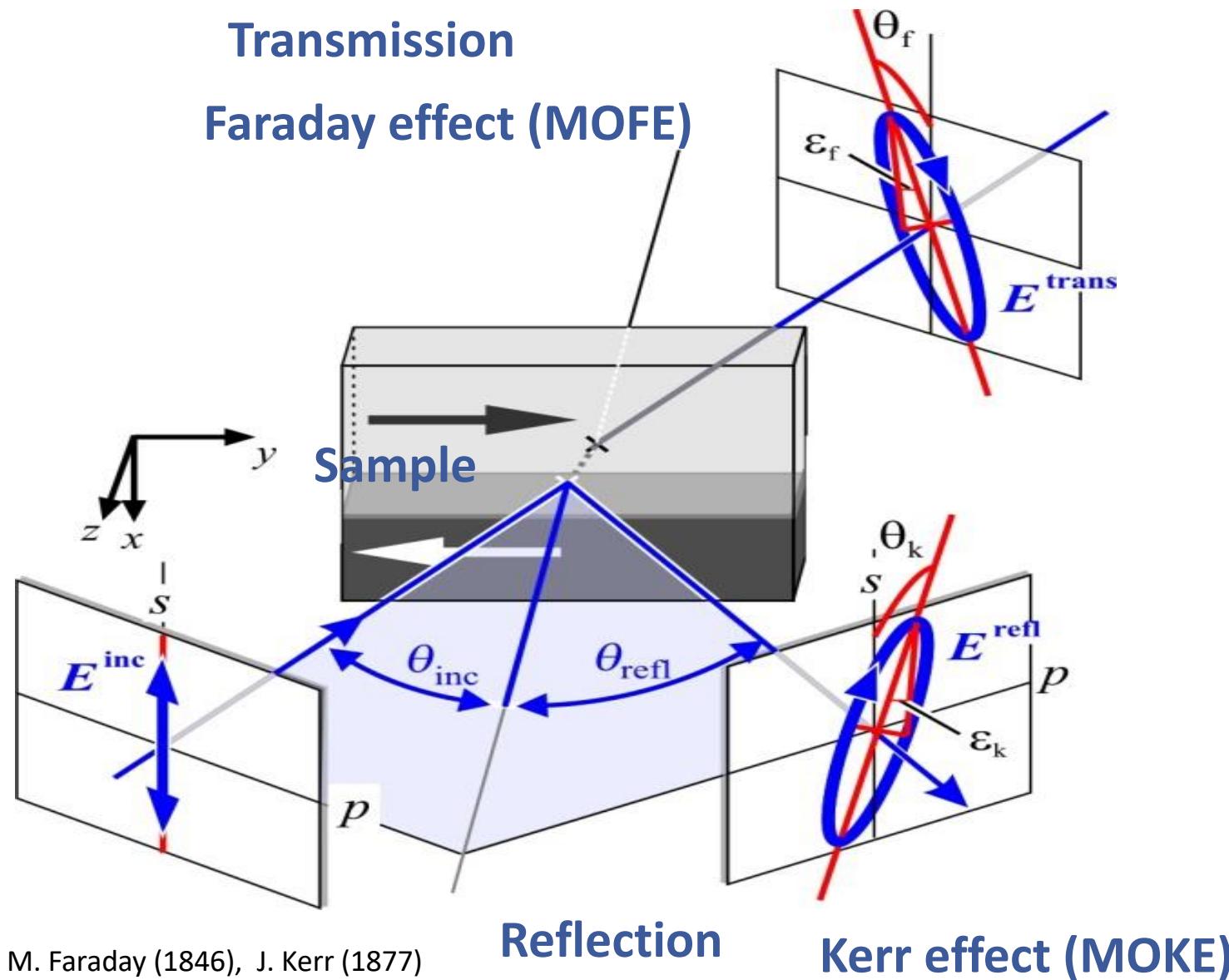
Linearly polarized light



polarized light



Magneto-optic effect



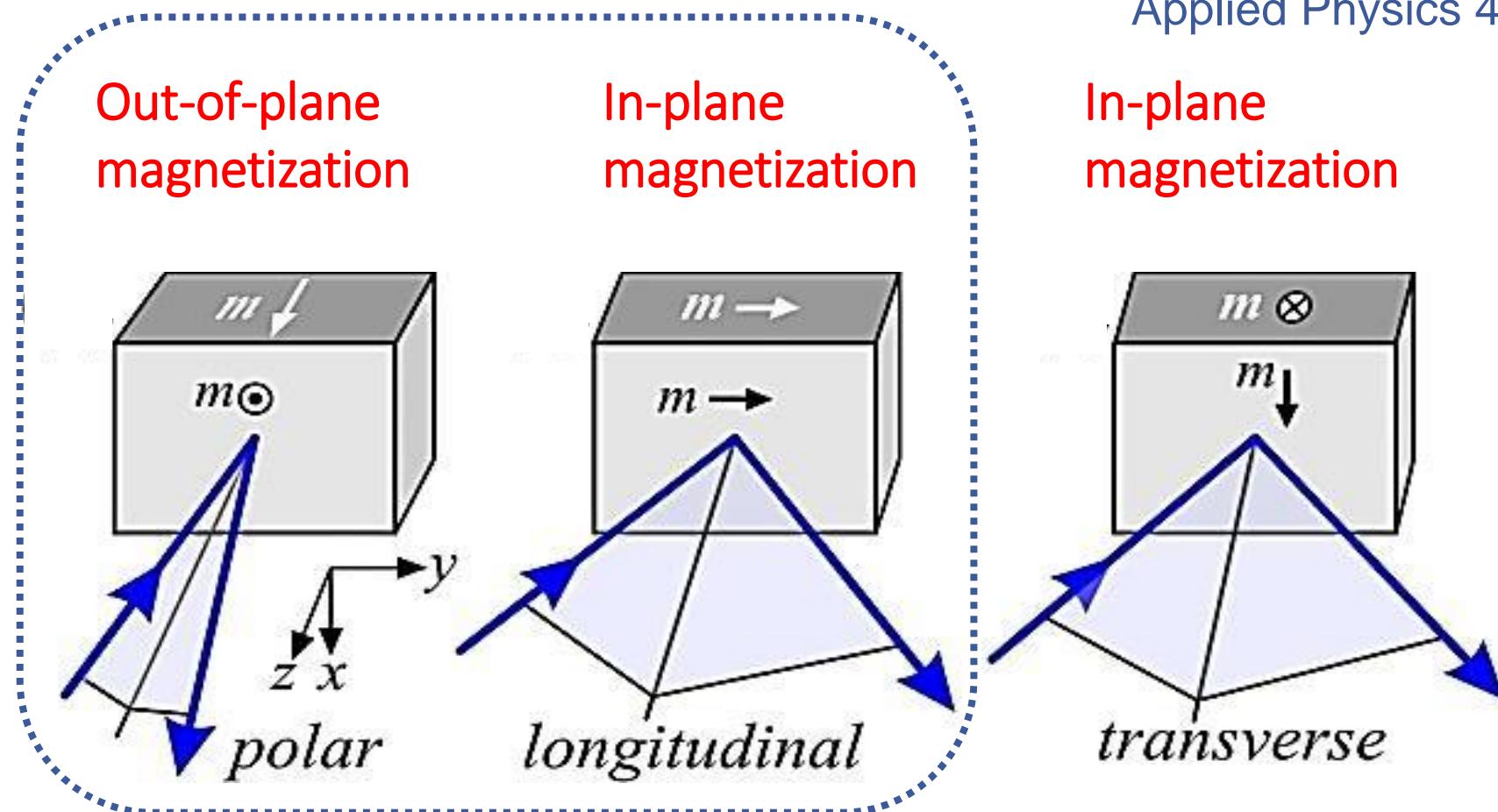
Longitudinal Faraday and Kerr effect under an angle of incidence ϑ_{inc} relative to the surface normal. The case of s-polarization is sketched. By the MO interaction with the magnetic medium the linearly polarized incoming light (E^{inc}) is transformed to an elliptically polarized light E^{trans} and E^{refl} . The resulting Faraday rotation ϑ_f and ellipticity e_f , respectively, Kerr rotation ϑ_k and ellipticity e_k are shown. ϑ_{refl} is the angle of reflection of light.

J.McCord, Journal of Physics D:
Applied Physics 48, 333001 (2015)

Magneto-optic effect

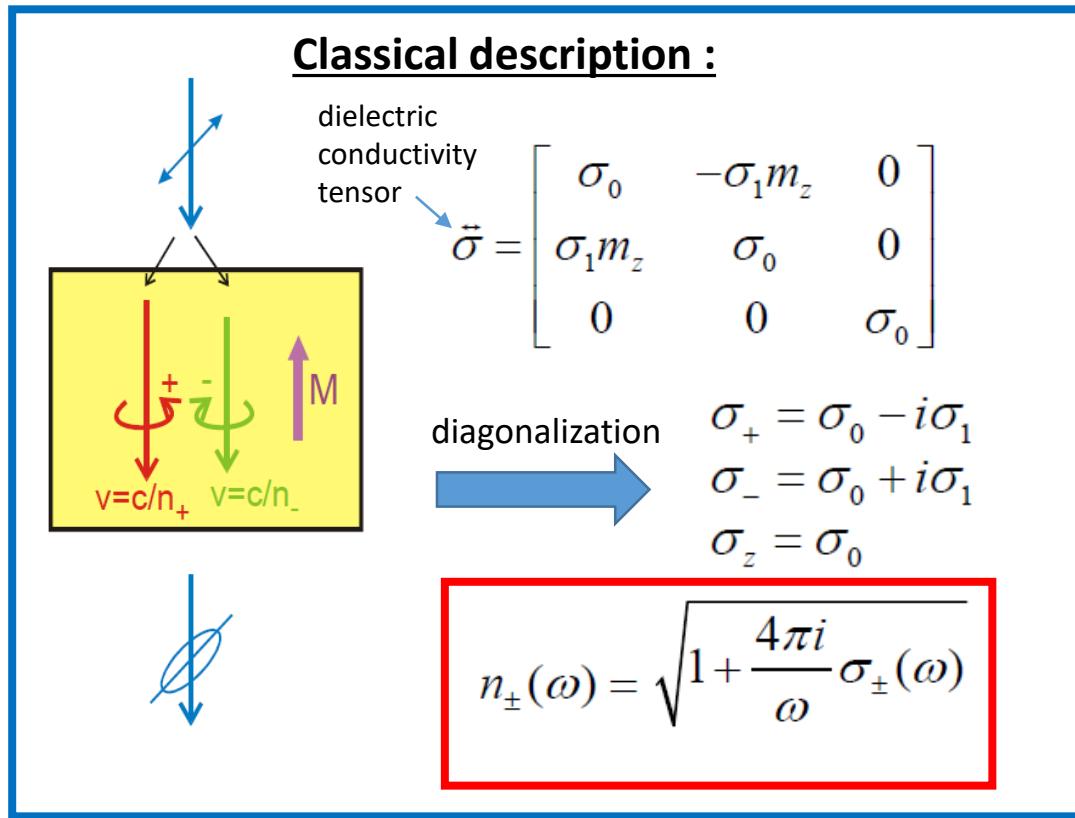
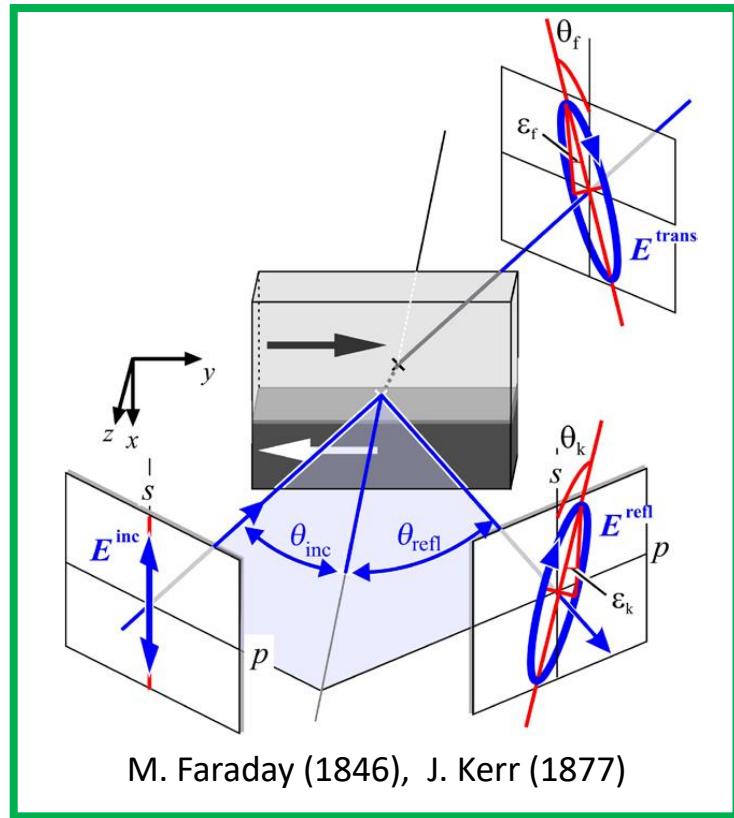
The effects might come together!

J.McCord, Journal of Physics D:
Applied Physics 48, 333001 (2015)



The three basic configurations of the (a) polar, (b) longitudinal, and (c) transverse magneto-optical Kerr effect. The unit vector of magnetization \mathbf{m} is lying along the corresponding sensitivity axes (as indicated).

Magneto-optic effect

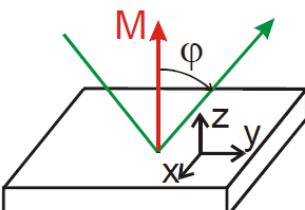


More generally : 3 useful configurations

$$\vec{\sigma}(M) = \begin{bmatrix} \sigma_0 & -\sigma_1 m_z & \sigma_1 m_y \\ \sigma_1 m_z & \sigma_0 & -\sigma_1 m_x \\ -\sigma_1 m_y & \sigma_1 m_x & \sigma_0 \end{bmatrix}$$

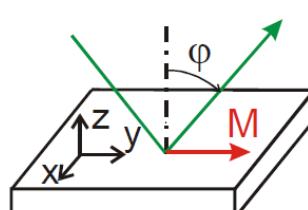
Polar Kerr effect
(PMOKE)

$M \perp$ sample surface



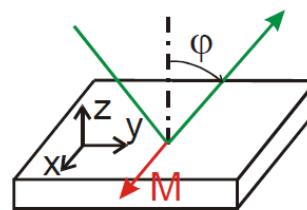
Longitudinal Kerr effect
(LMOKE)

$M \parallel$ plane of incidence

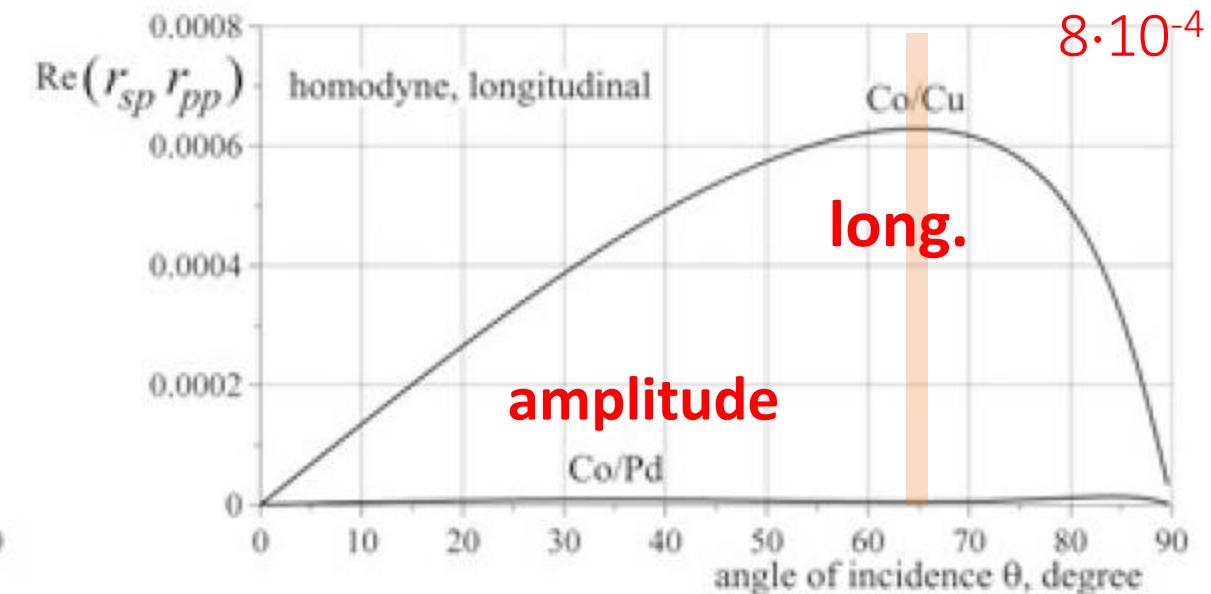
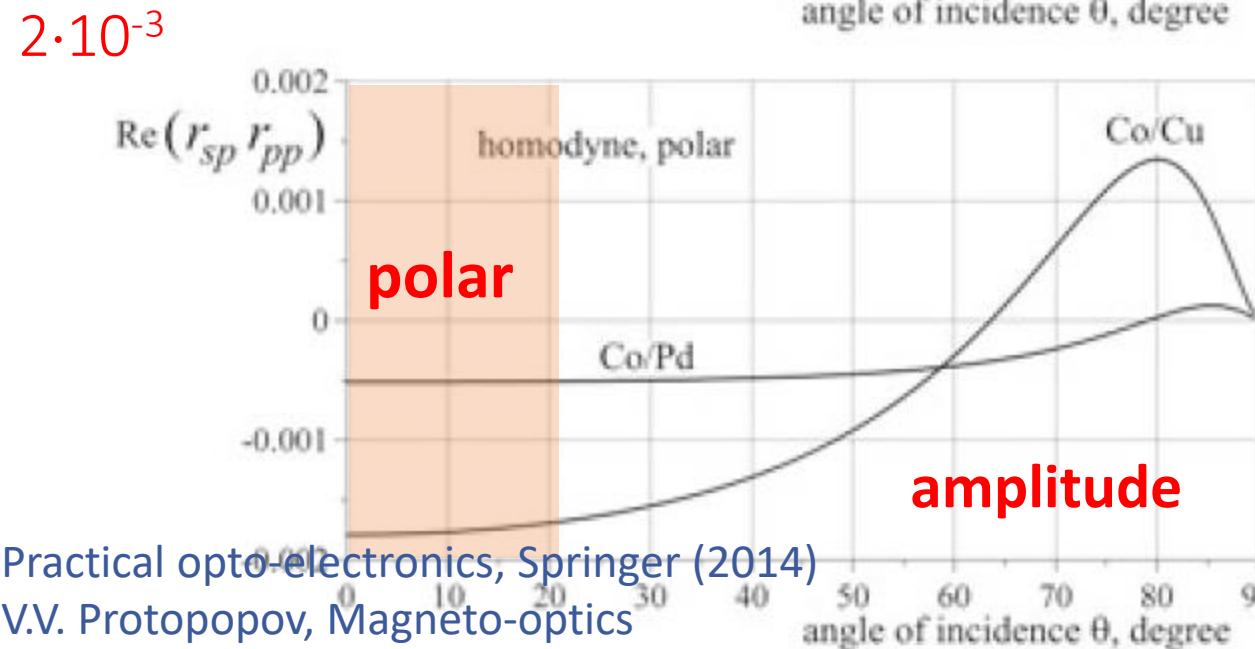
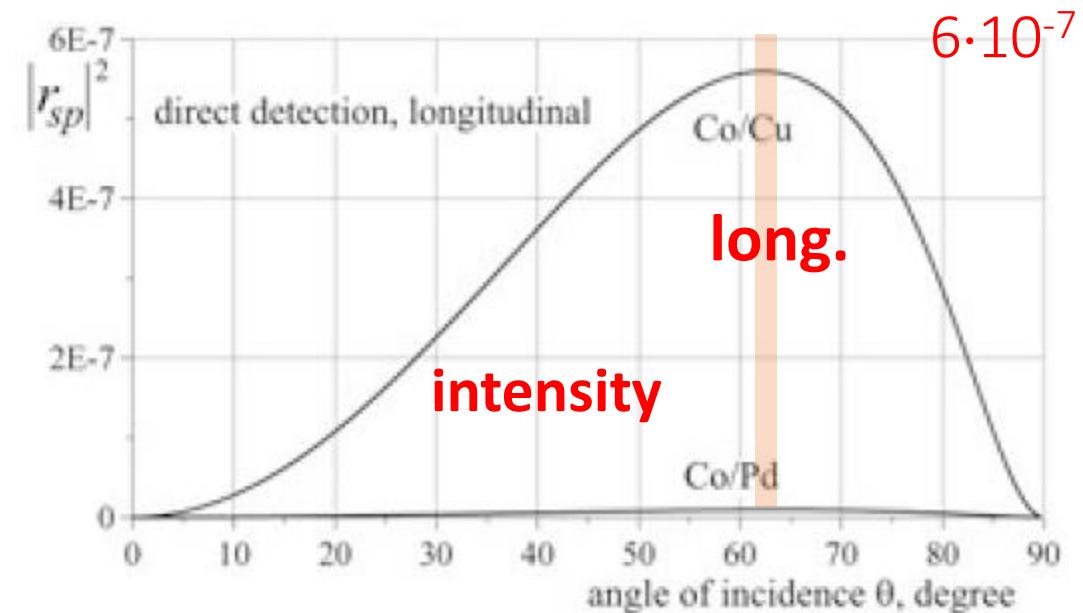
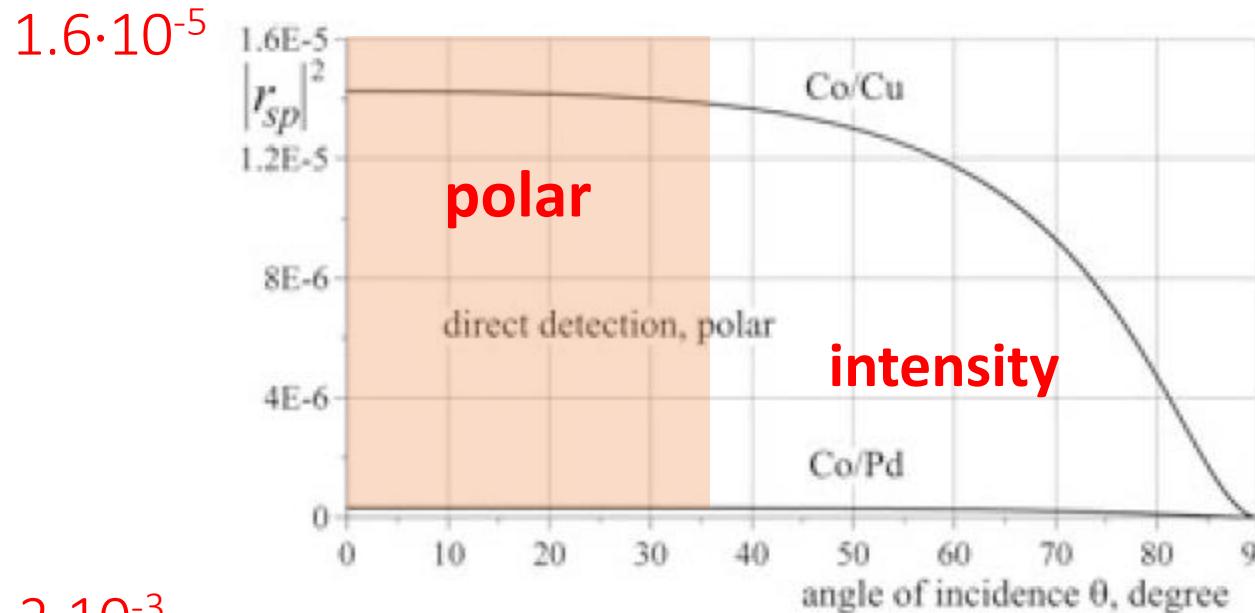


Transversal Kerr effect
(TMOKE)

$M \perp$ plane of incidence



Magneto-optic effect



**MOKE
(Kerr
microscopy)**

Contrast mechanism **M**

Evaluation of the magnetization, **M(r)**

Spatial resolution (nm) $\frac{\text{Typical}}{\text{Limit}}$ $\frac{800}{250}$

Depth of information (nm) <20 (metals)

Time for image acquisition 1 msec–5 sec

Limits on applied magnetic fields None

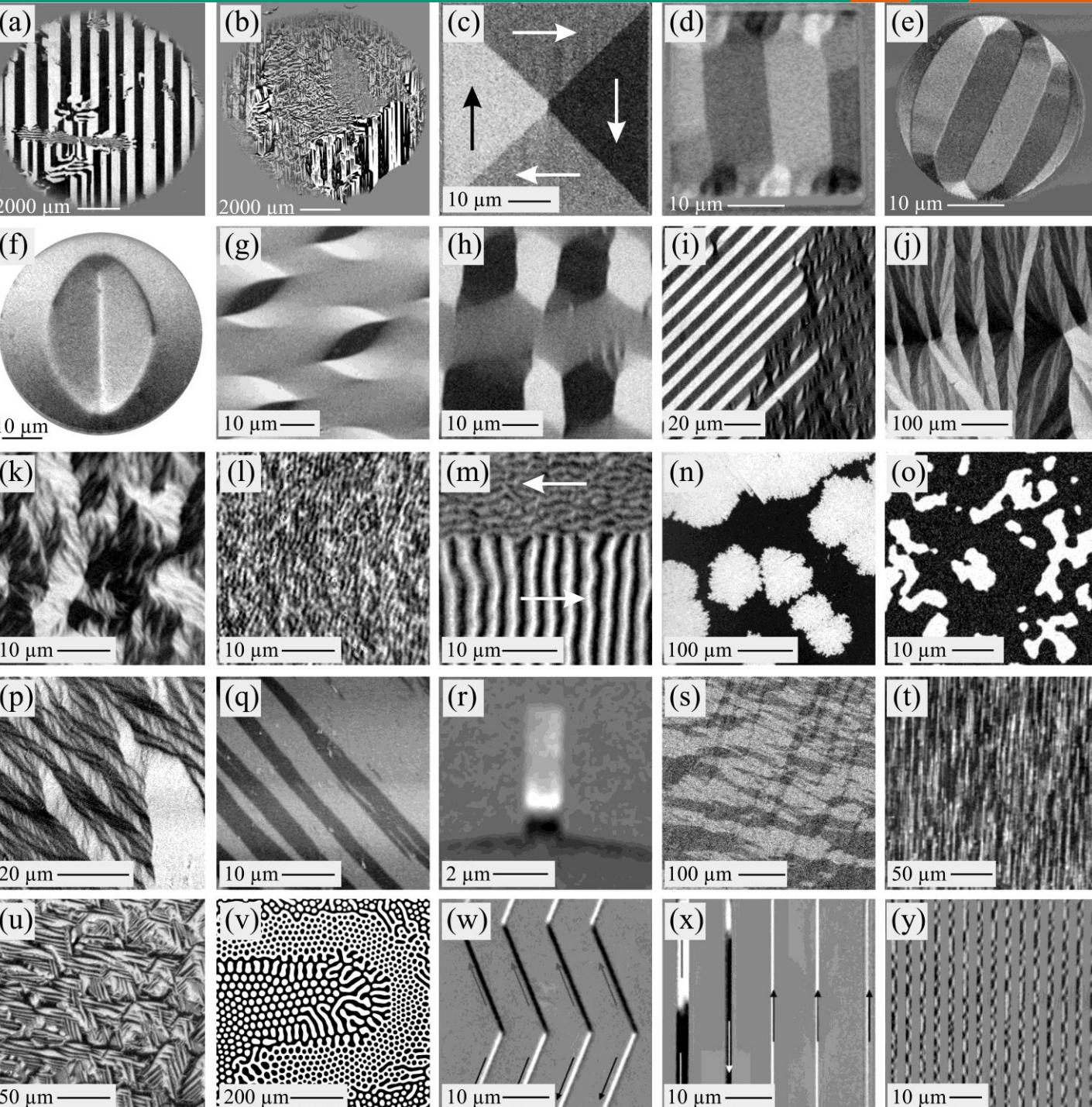
Imaging conditions In air

Max thickness None

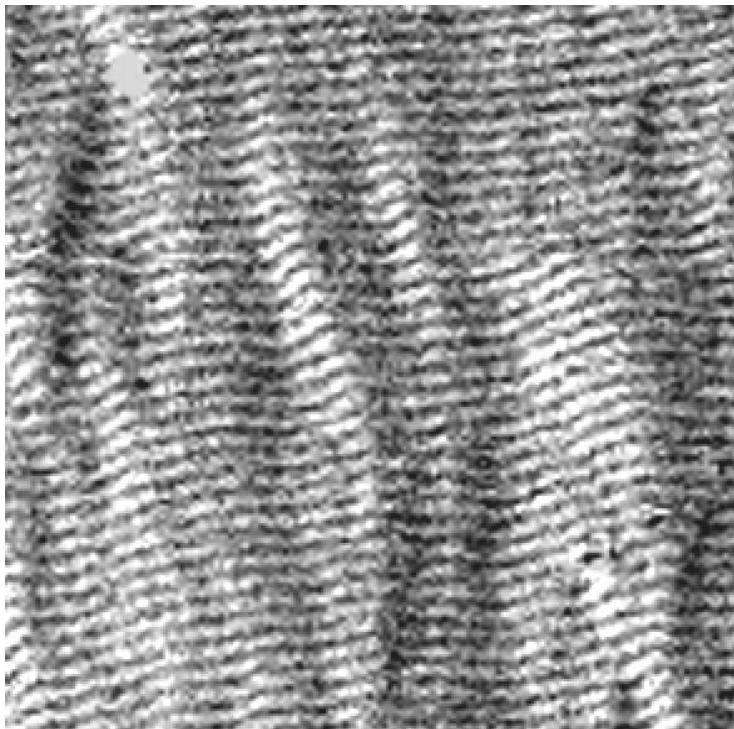
Sample smoothness R

Sample clean surface NR

Topical Review
J. McCord,
J. Phys. D: Appl.
Phys. 48,
333001 (2015)

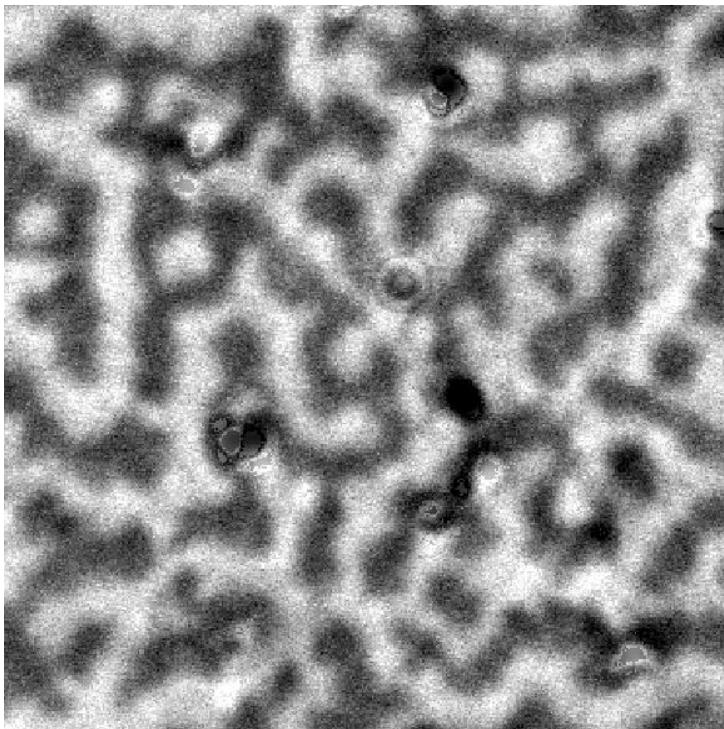


Ultimate resolution



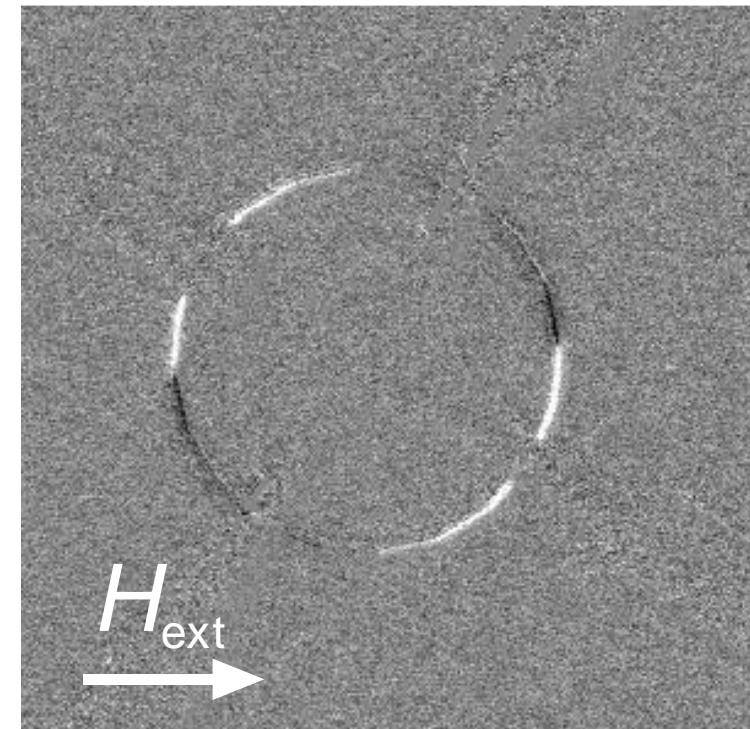
Stripe domains in $\text{Ni}_{81}\text{Fe}_{19}$
Domain width 250 nm

**150 nm
resolution**



Interaction domains in $\text{Nd}_2\text{Fe}_{14}\text{B}$
Domain width 400 nm

(sample O. Gutfleisch, TU
Darmstadt)

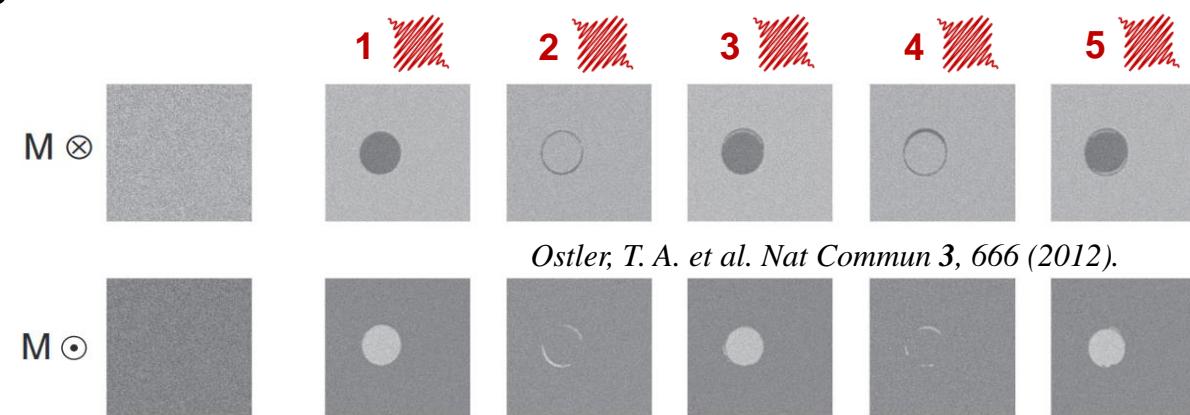
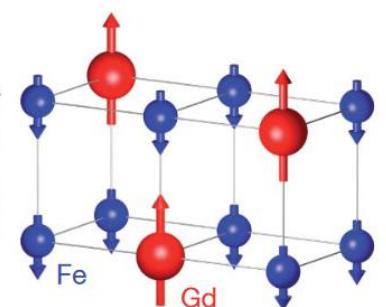


Magnetic domains in a angle sensor
Stripe width 300 nm
Localization accuracy 10 nm

(sample R. Mattheis, IPHT Jena)

All Optical – Helicity Independent switching

Characteristics

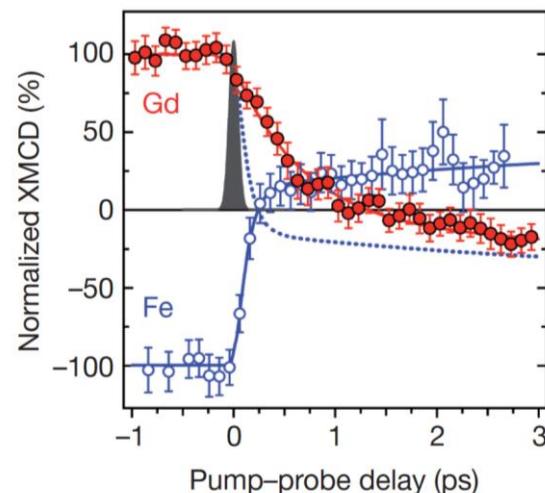


Specific materials

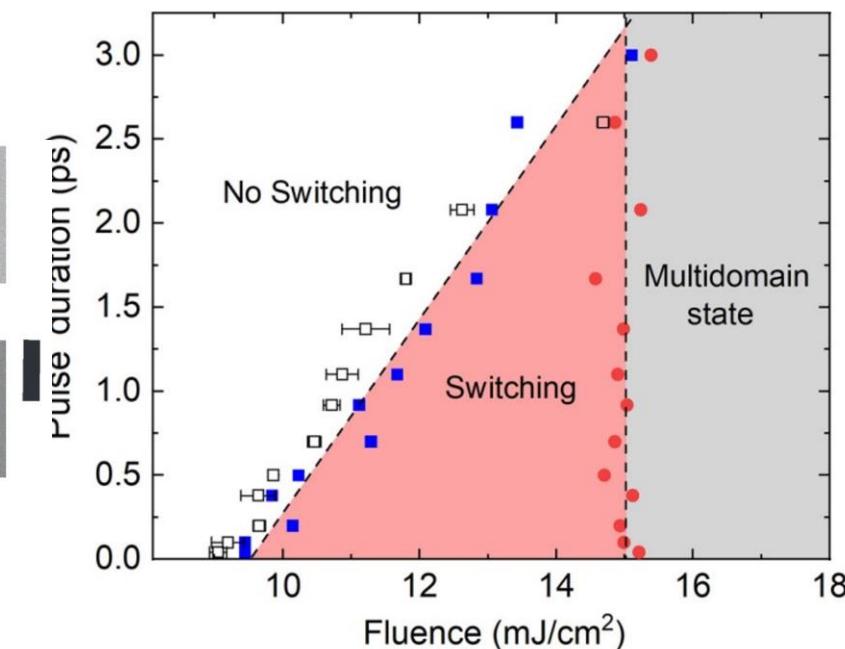
→ Gd based Material

→ MnRuGa

Single pulse & Fast



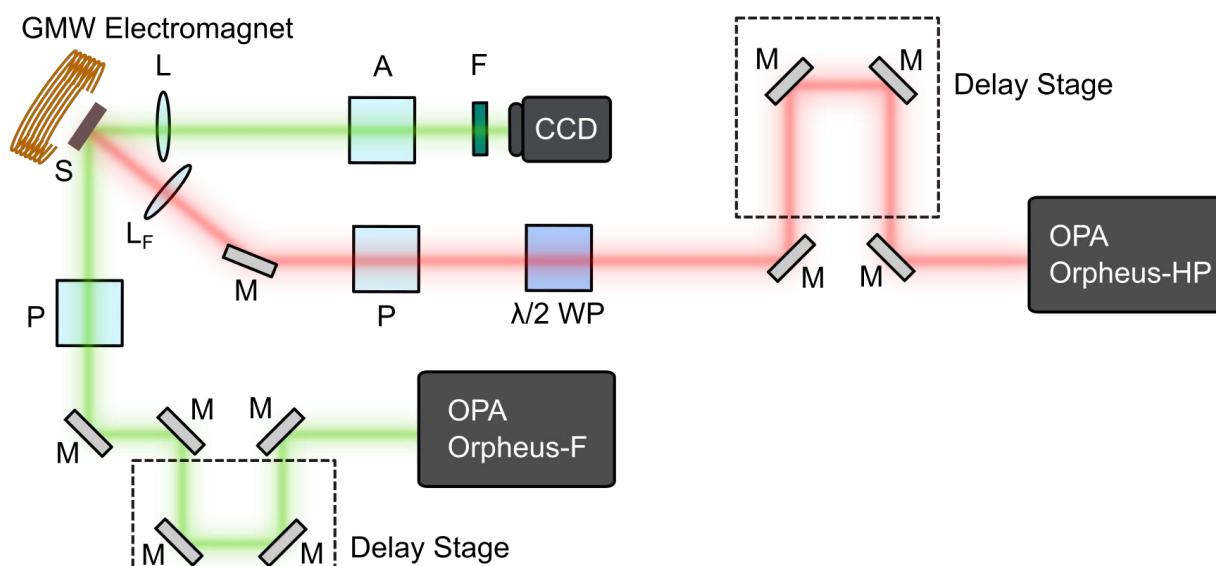
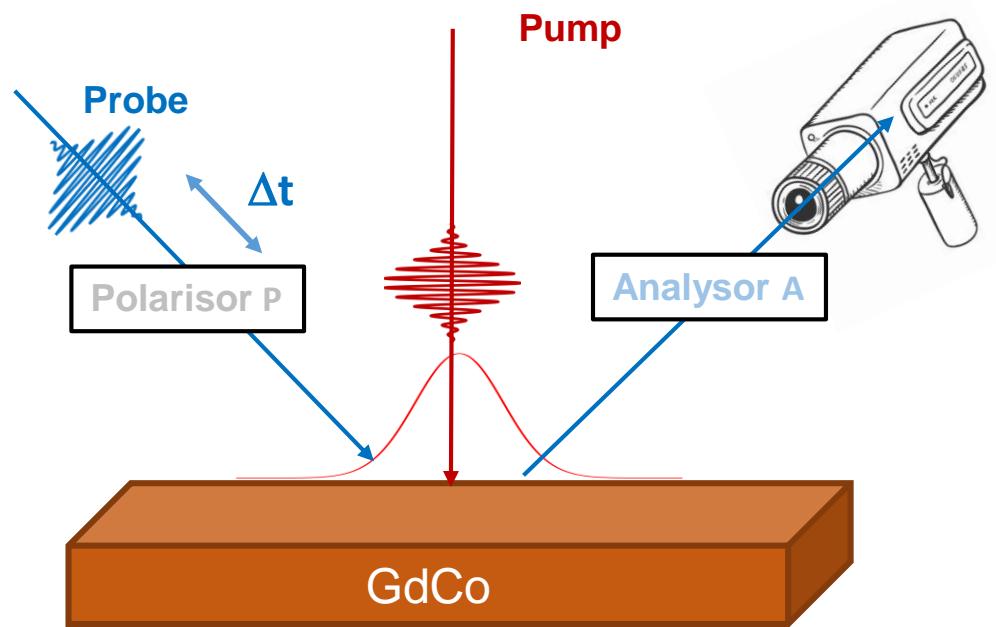
Radu, I. et al. *Nature* 472, 205–208 (2011).



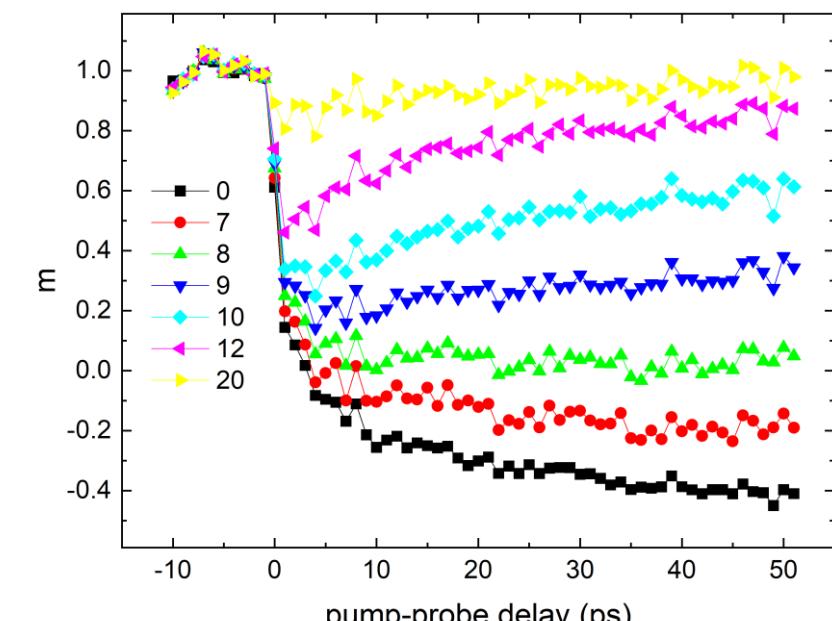
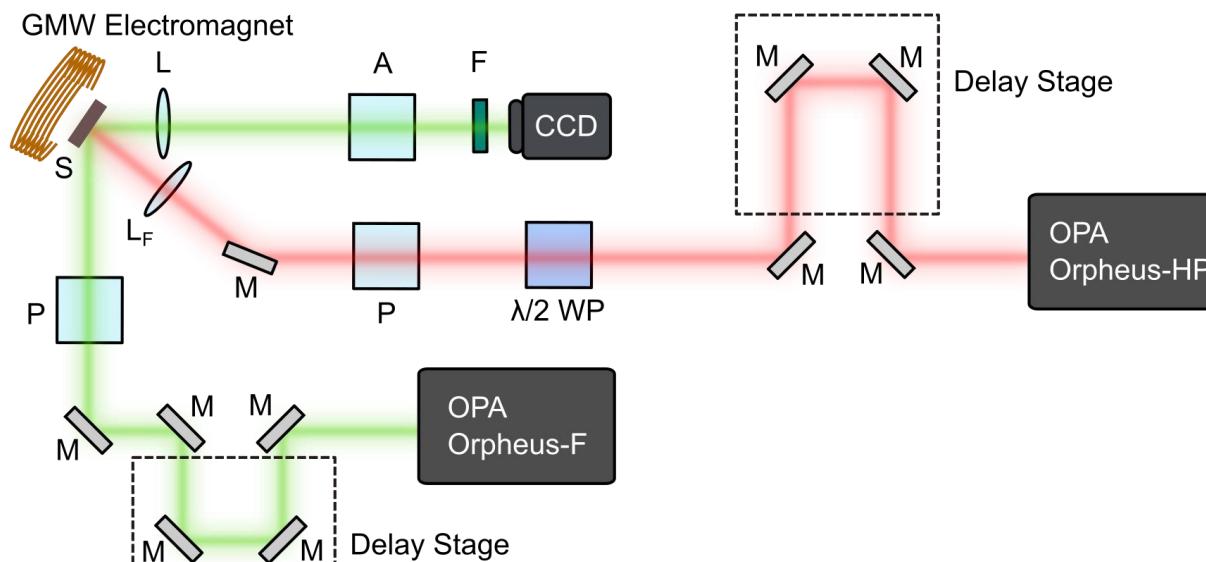
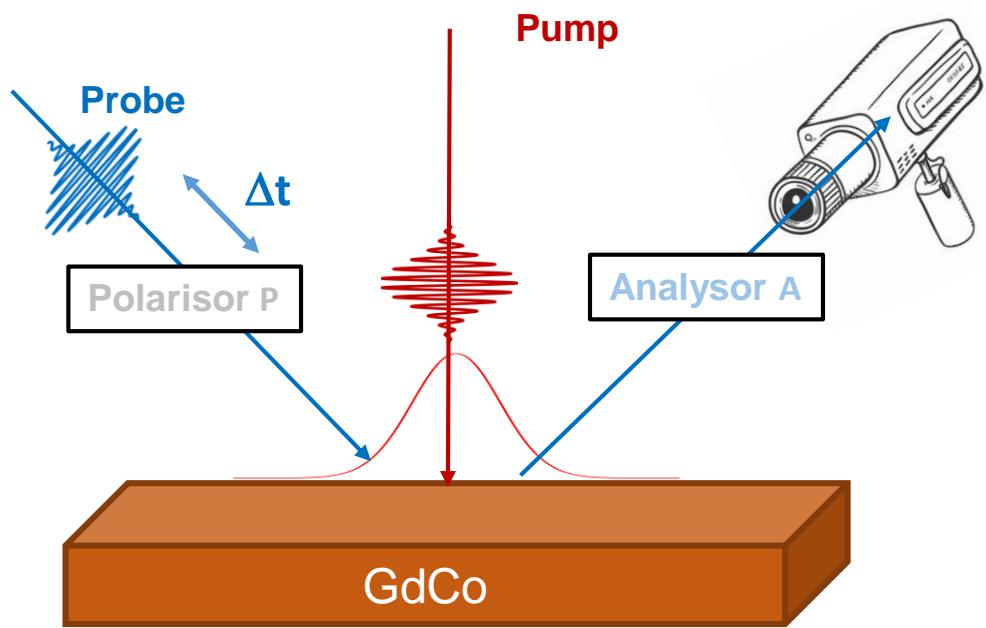
Characteristic State diagram

Wei, J. et al.
Phys Rev Applied 15, 054065 (2021).

Dynamic



Dynamic



Magneto-optical imaging

- Flat and smooth surface required
- Imaging through substrate and covering layers (devices)
- Spatial resolution below 200 nm
- Magnetization can be observed directly
- Quantitative measurements possible
- Almost no influence on magnetization (but light induced heat)
- Straightforward sample manipulation (fields, temperature, stress)
- Surface sensitive (approx. 30 nm)

Outlines

Magneto-optical microscopy (MO)

Scanning electron microscopy (SEMPA)

Transmission electron microscopy (TEM)

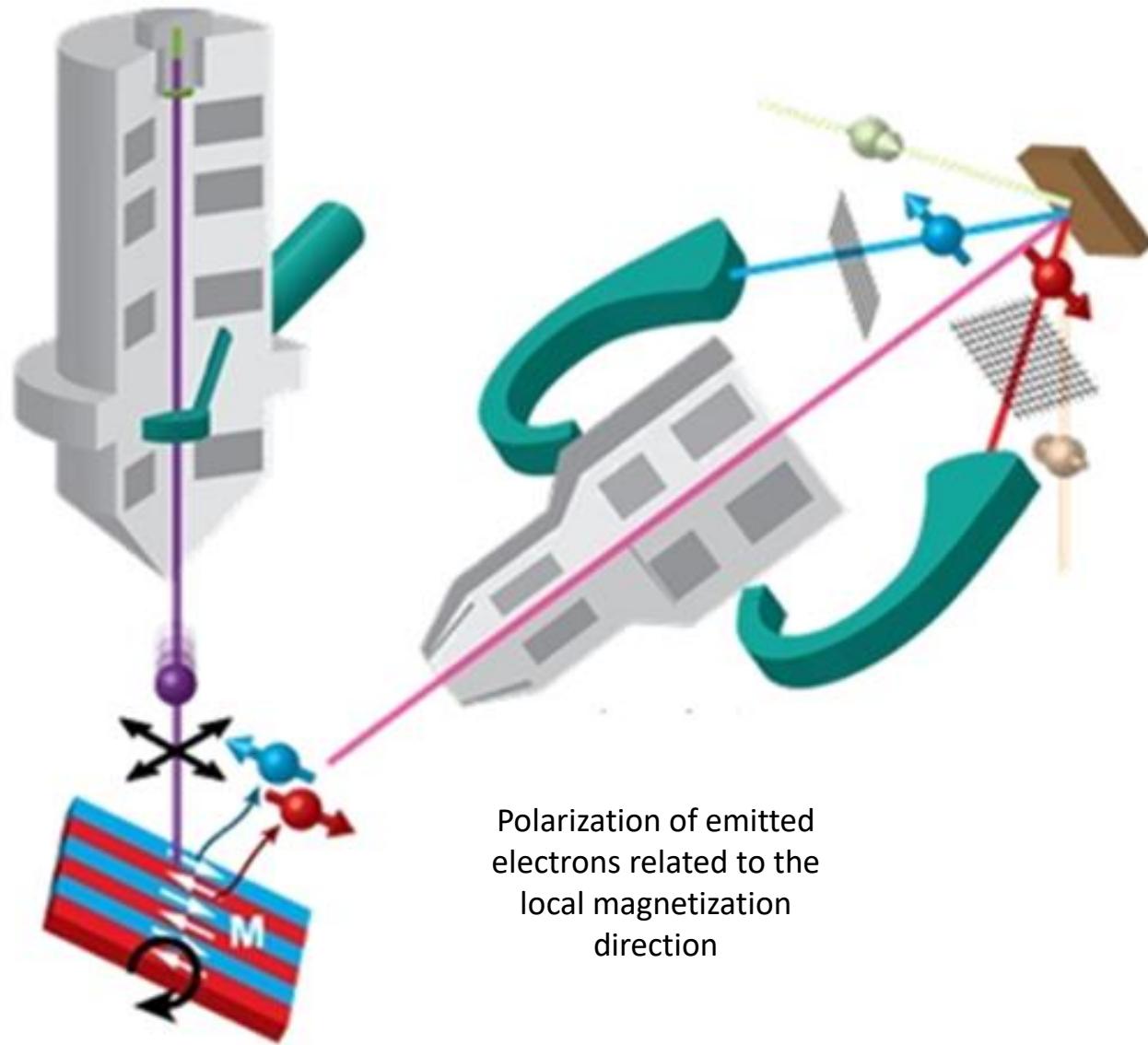
X-Ray microscopy

Magnetic force microscopy (MFM)

Scanning Electron Microscopy with Polarization Analysis

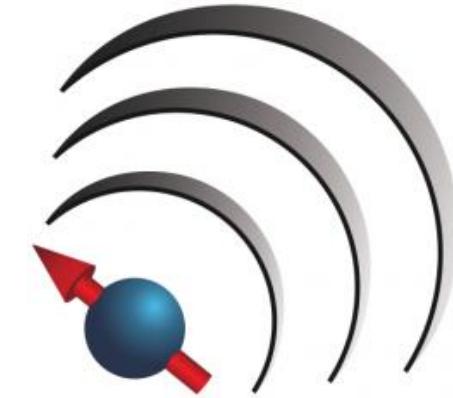
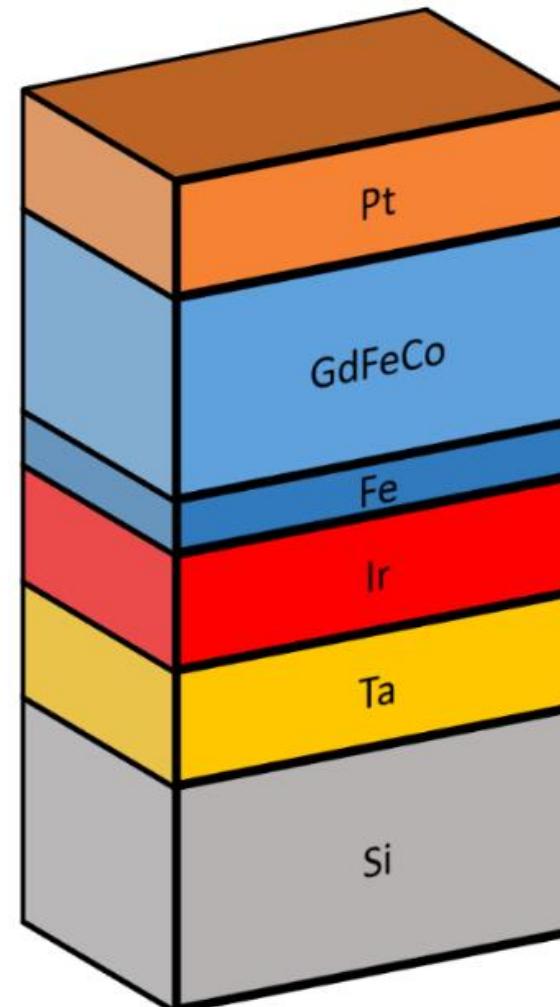
SEMPA

Contrast mechanism	M
Evaluation of the magnetization, $M(r)$	Q
Spatial resolution (nm) <small>Typical Limit</small>	$\frac{150}{20}$
Depth of information (nm)	1–2
Time for image acquisition	1–100 min
Limits on applied magnetic fields	Not advised
Imaging conditions	UHV
Max thickness	None
Sample smoothness	NR
Sample clean surface	R



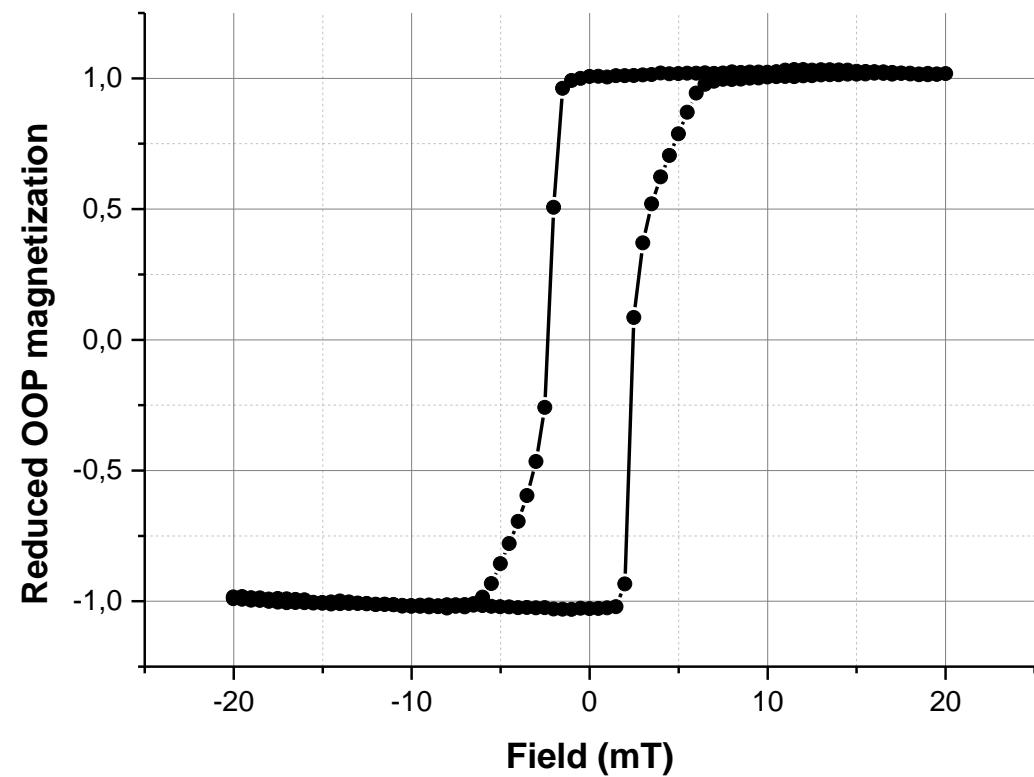
One exemple

- ❖ GdFeCo ferrimagnet
- ❖ DMI enhancement: Fe dusting layer for interfacial (Ir/Fe) and Pt capping layer
- ❖ Small Pt layer for surface sensitive imaging technique
- ❖ Si//Ta(5)/Ir(5)/Fe(0.3)/[Gd_{26.1}Fe_{65.5}Co_{8.3}](8)/Pt(1.5)



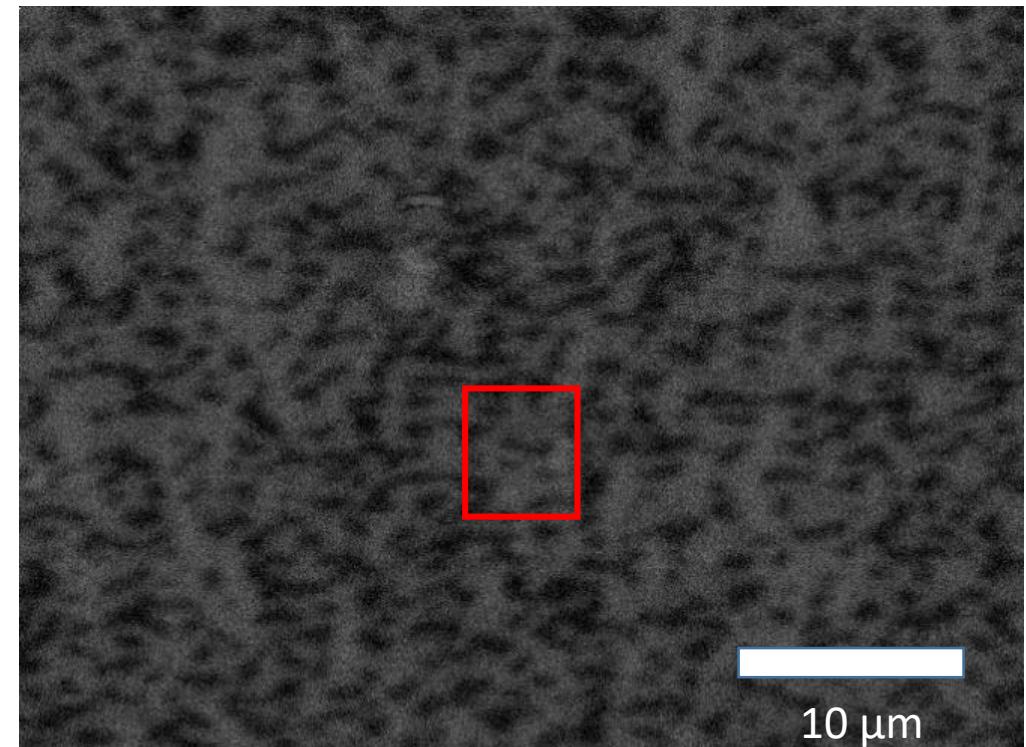
KLÄUI-LAB

- ❖ OOP anisotropy
- ❖ Nucleation using relaxation after IP saturation



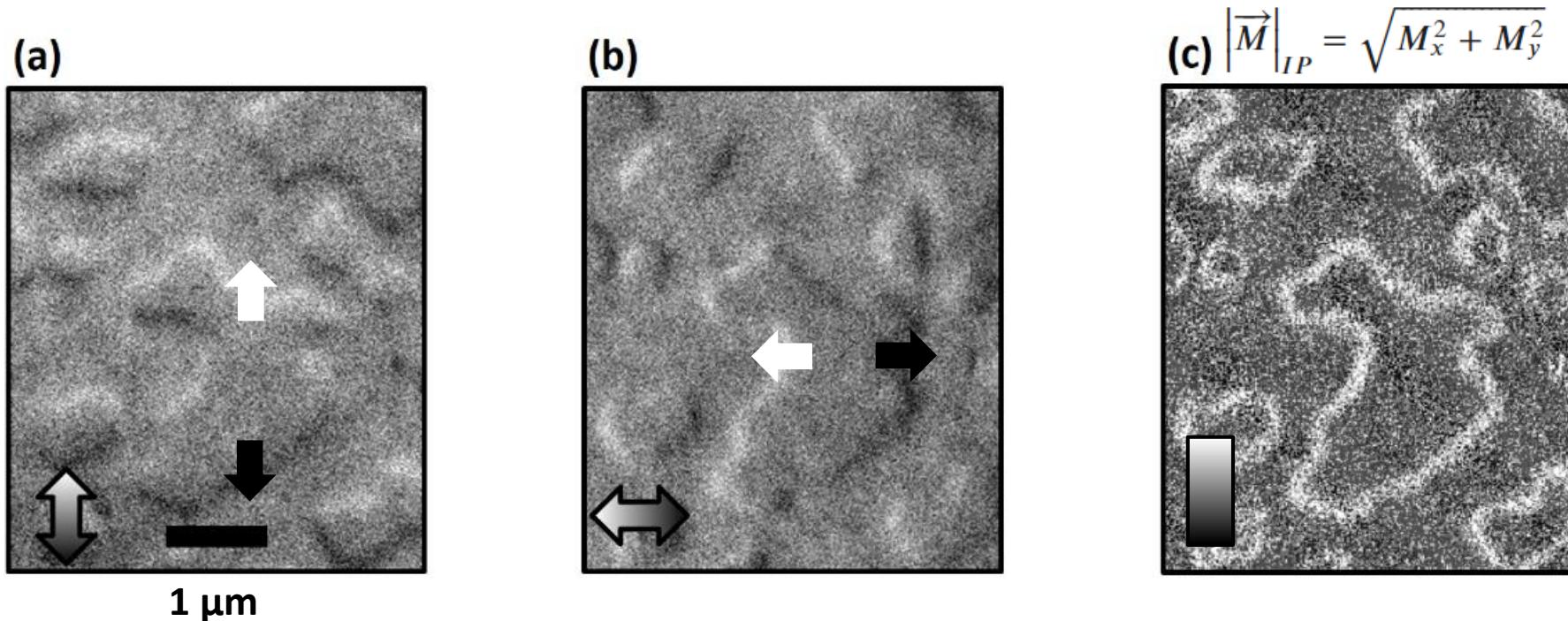
Spin textures observed at room

- ❖ OOP anisotropy
- ❖ Nucleation using relaxation after IP saturation
- ❖ μm -sized spin textures nucleated
- ❖ To determine the chirality, observation of the domain wall spin configuration is necessary



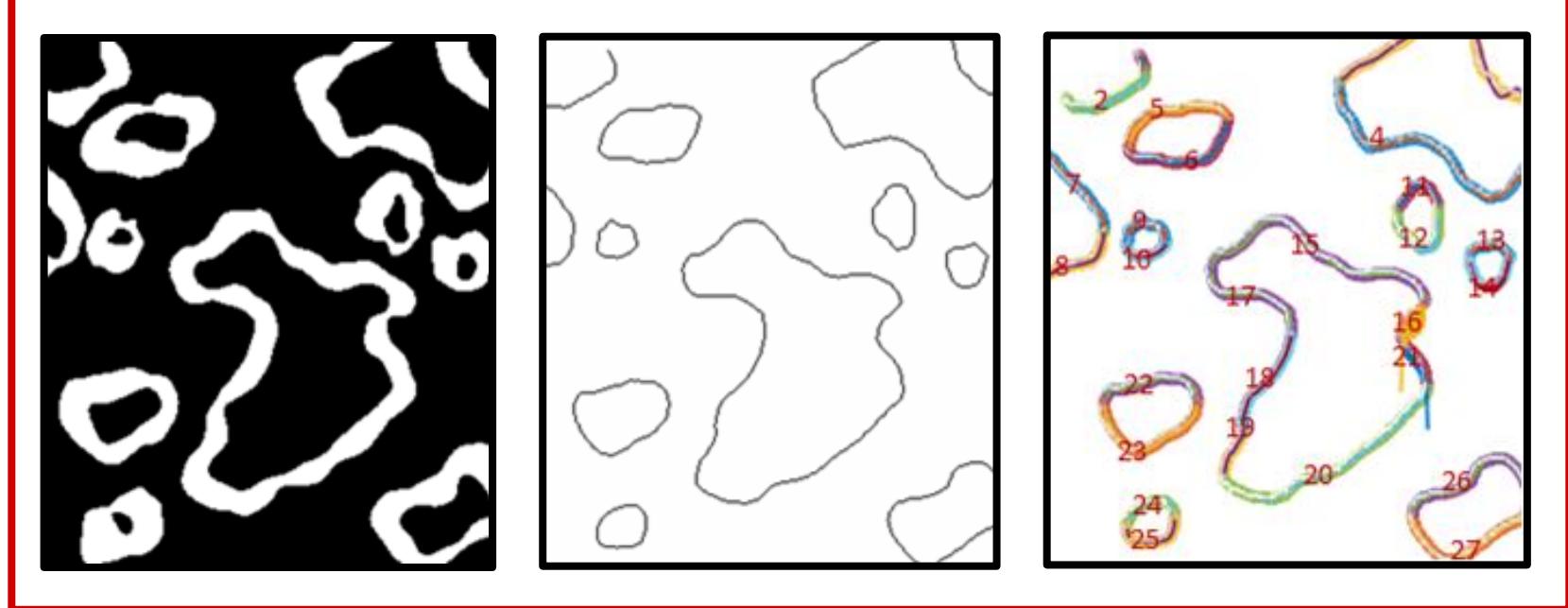
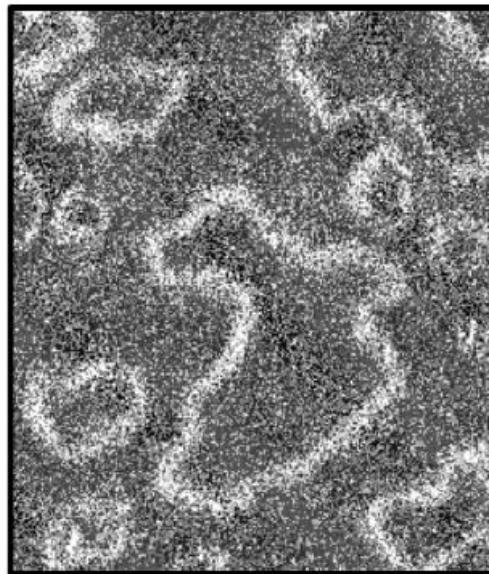
Kerr microscopy at RT, 0 mT

Determination of the domain wall width



- ❖ Observation of the $IP|_x$ and $IP|_y$ components of the magnetization
- ❖ Localization of the domain walls

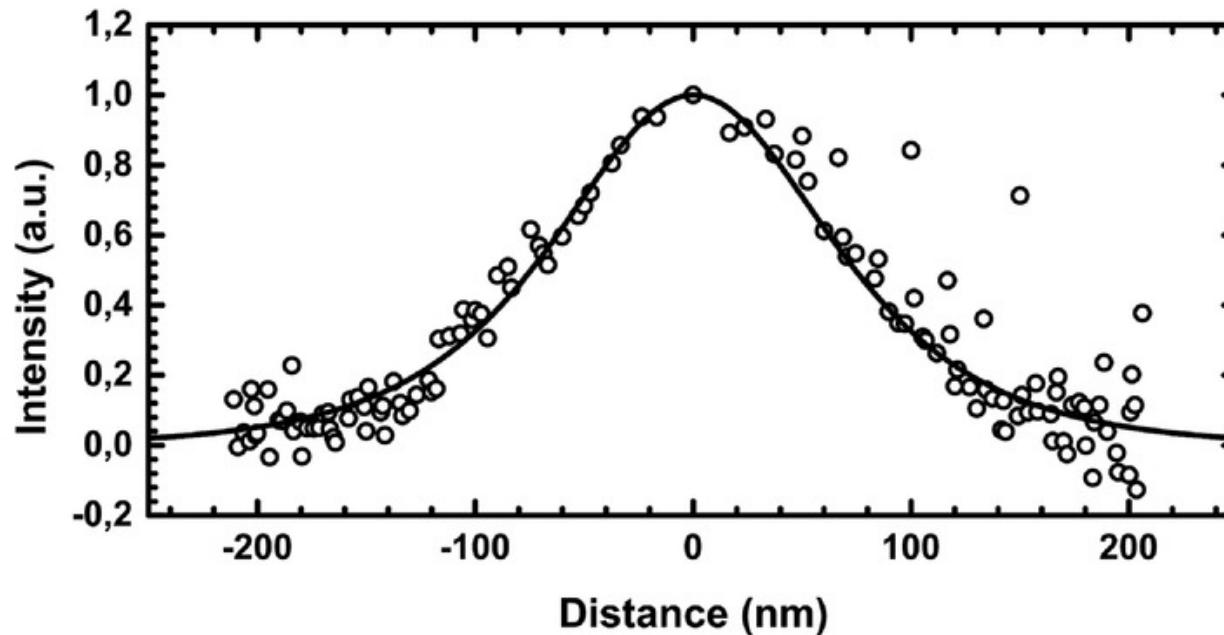
Determination of the domain wall width



Binarization, skeletonize, polynomial fitting

→ Determination of the local normal of the skeleton

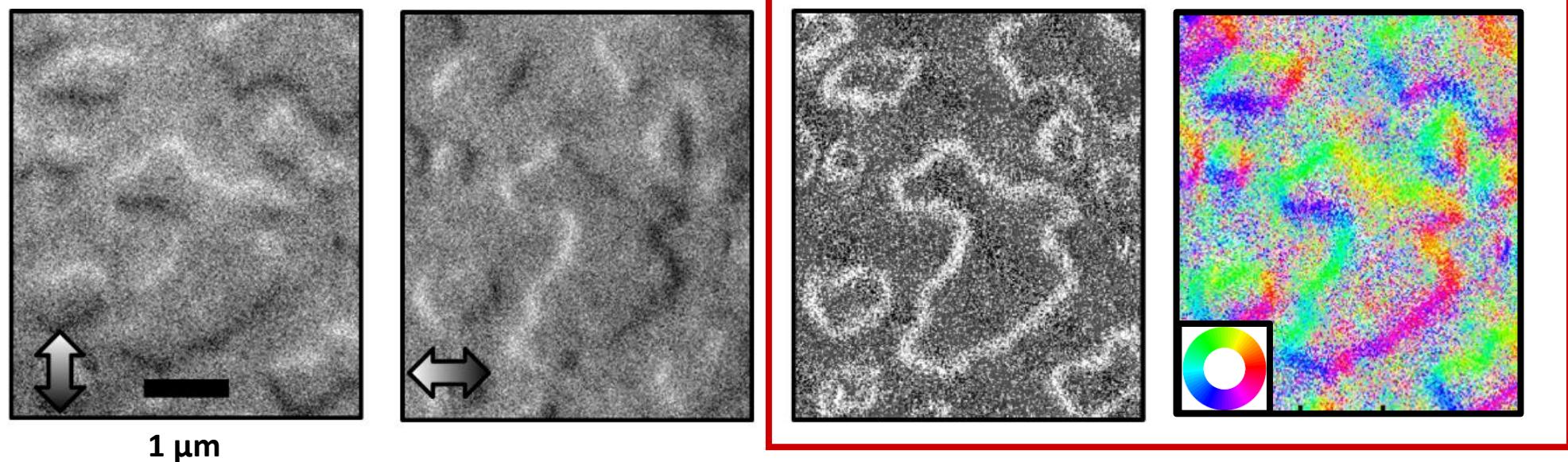
Determination of the domain wall width



Distribution of the domain wall profile: $\text{Intensity} \propto \cosh^{-1}(x/\Delta) \otimes e^{-(x^2/2\sigma^2)}$

$$\rightarrow \delta_{\text{real}} = \pi \Delta = 175 \pm 5 \text{ nm}$$

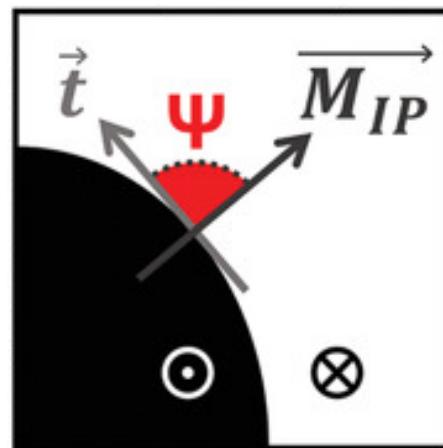
Determination of the chirality



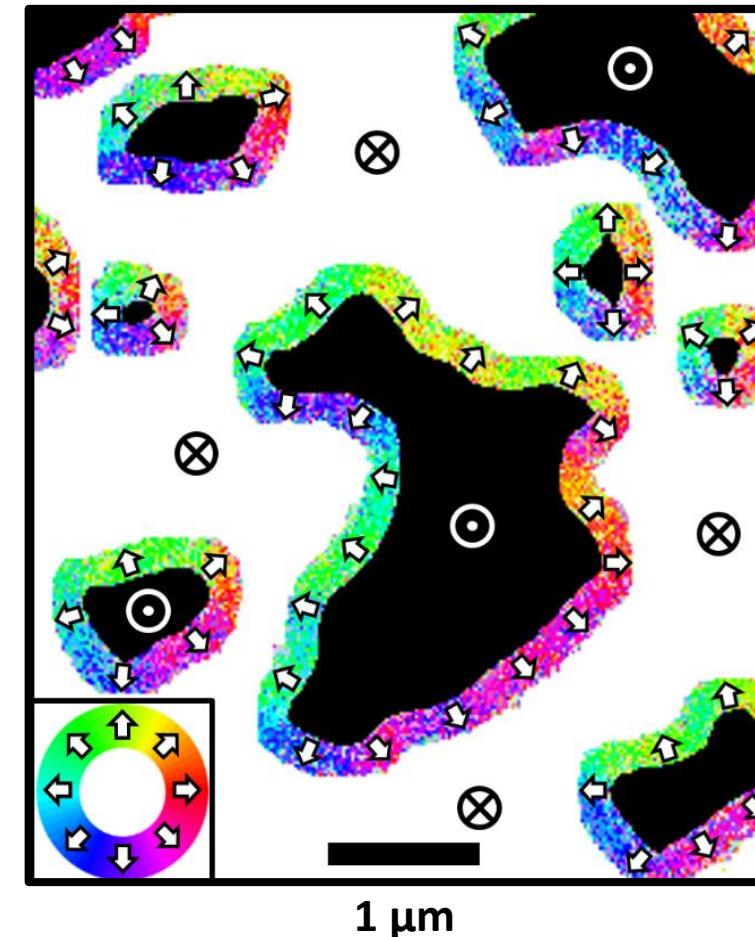
- ❖ We determined firstly the position of the DW
- ❖ We can also deduct the direction of the local magnetization

Determination of the chirality

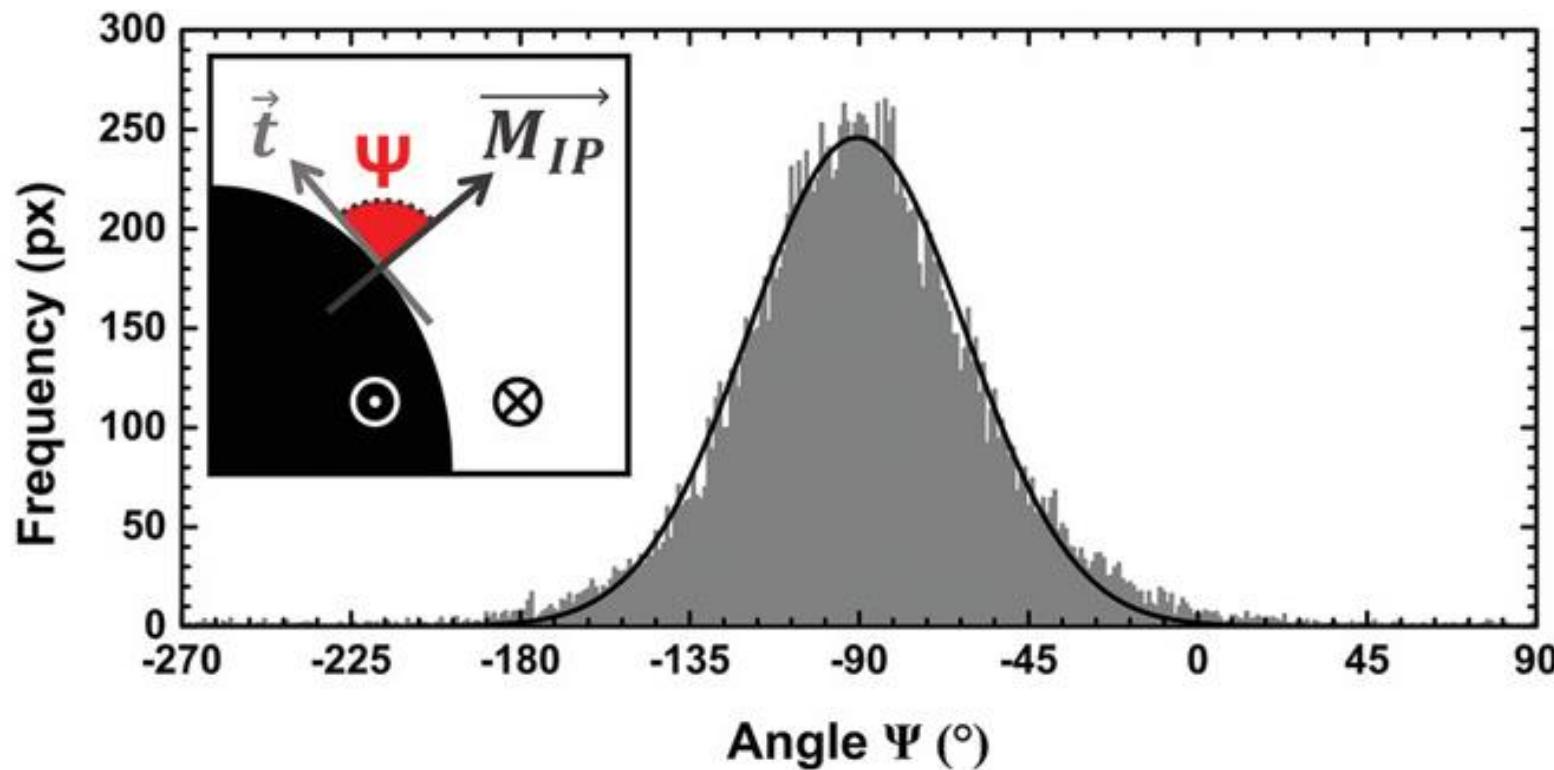
- ❖ Qualitatively, Néel-type spin textures



- ❖ Homochirality



Determination of the chirality



→ Pure right-hand Néel-type chirality

Determination of the exchange stiffness A

$$\Delta = \Delta_0 - \frac{1}{\frac{2\pi(Q-1)}{d} + \frac{1}{\Delta_0 - \Delta_\infty}}$$

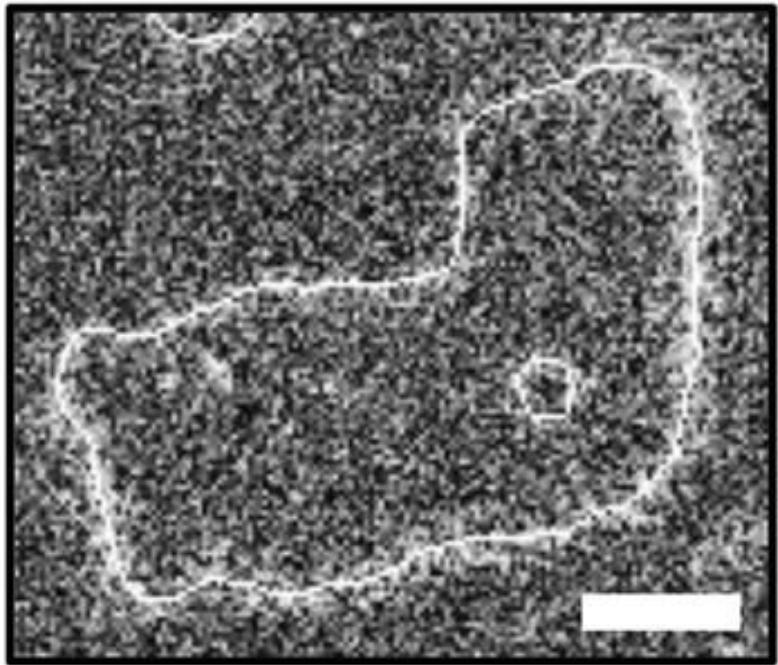
$$Q = \frac{2K_u}{\mu_0 M_s^2}, \quad \Delta_0 = \sqrt{\frac{A}{K_{eff}}}, \quad K_{eff} = K_u - \frac{\mu_0 M_s^2}{2}, \quad \Delta_\infty = \sqrt{\frac{A}{K_u + \frac{\mu_0 M_s^2}{2} \sin^2(\Psi)}}$$

$$\Delta = f(A, K_u, M_s, d, \Psi)$$

- ❖ Δ, Ψ : measured using SEMPA imaging
- ❖ Thickness d known, measurement of the uniaxial anisotropy K_u and the saturation magnetization M_s using magnetometer.

→ The exchange stiffness is found numerically and equal to: $A = 8,0 \pm 0.5. pJ.m^{-1}$

Observation of a ferrimagnetic skyrmionium



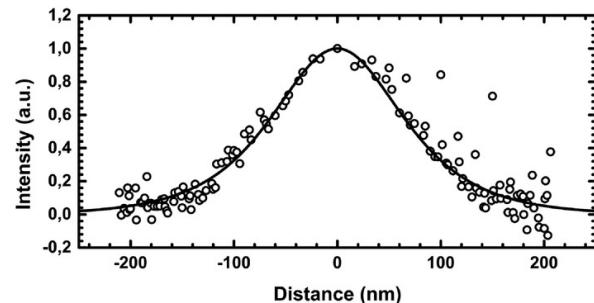
500 nm



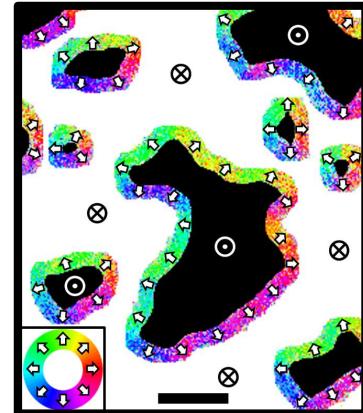
→ First observation of a ferrimagnetic skyrmionium in ferrimagnetic materials

Conclusion of our SEMPA study

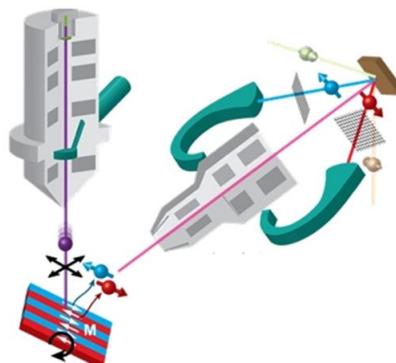
- ❖ Determination of the domain wall width



- ❖ Determination of the chiral character of the spin textures: pure right-hand Néel-type



- ❖ Extraction of the exchange stiffness could be possible with SEMPA



- ❖ Observation of a ferrimagnetic skyrmionium



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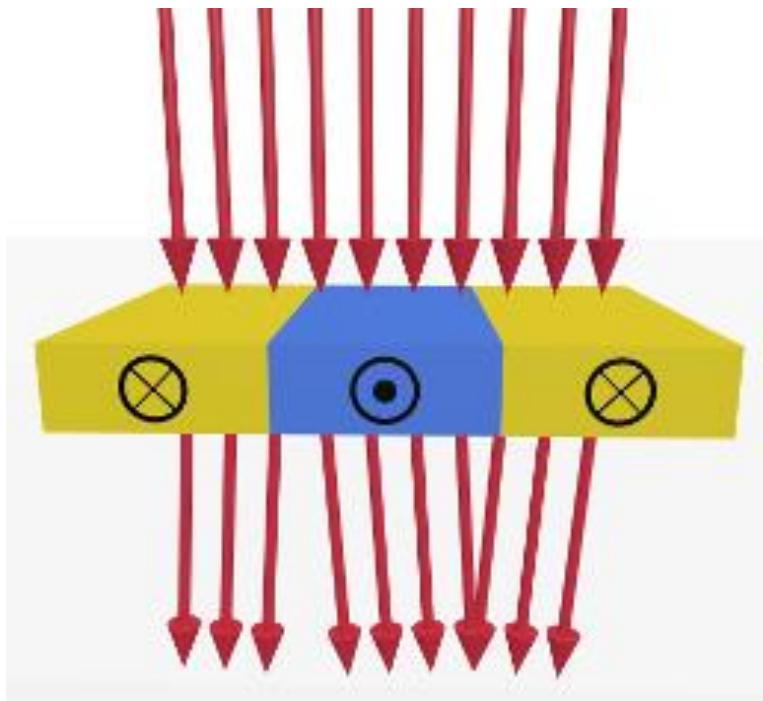
Magnetic force microscopy (MFM)

TEM Lorentz microscopy

	TEM Fresnel and Foucault	TEM DPC
Contrast mechanism	B	B
Evaluation of the magnetization, $M(\mathbf{r})$	Indirect	Q
Spatial resolution (nm)	Typical $\frac{50}{\sim 10}$	Limit $\frac{10}{2}$
Depth of information (nm)	Thickness integrated $< 150 \text{ nm}$	Thickness integrated $< 100 \text{ nm}$
Time for image acquisition	50 msec– 60 sec	5–60 secs
Limits on applied magnetic fields	~ 100 – 500 kA/m	~ 100 – 500 kA/m
Imaging conditions	HV	HV
Max thickness	$< 150 \text{ nm}$	$< 100 \text{ nm}$
Sample smoothness	Preferred	Preferred
Sample clean surface	Preferred	Preferred

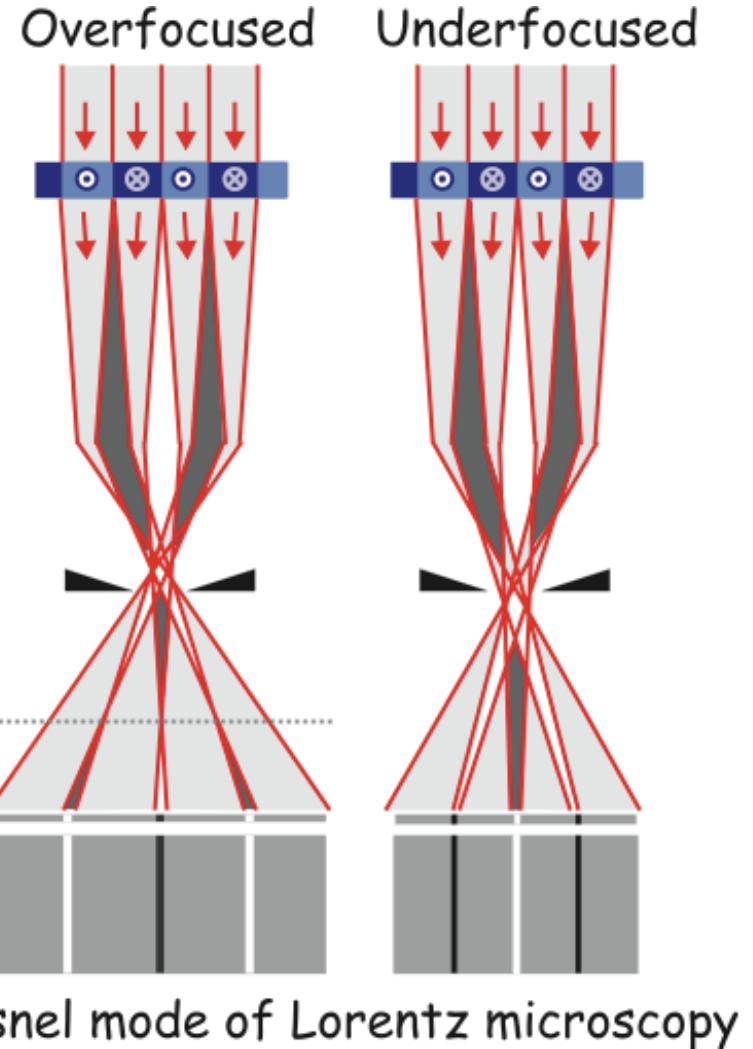
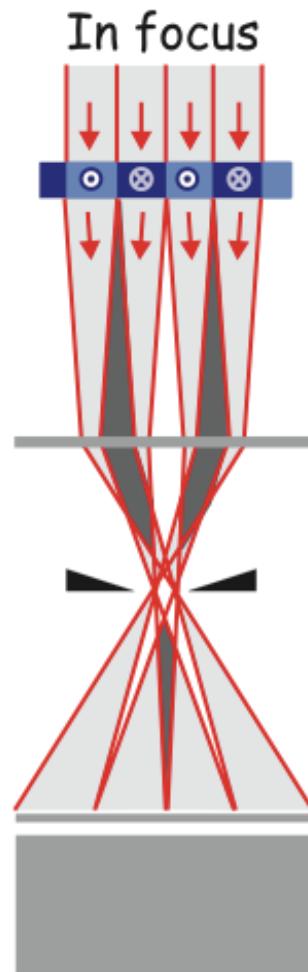
$$F = |e|(\mathbf{v} \times \mathbf{B})$$

Lorentz force

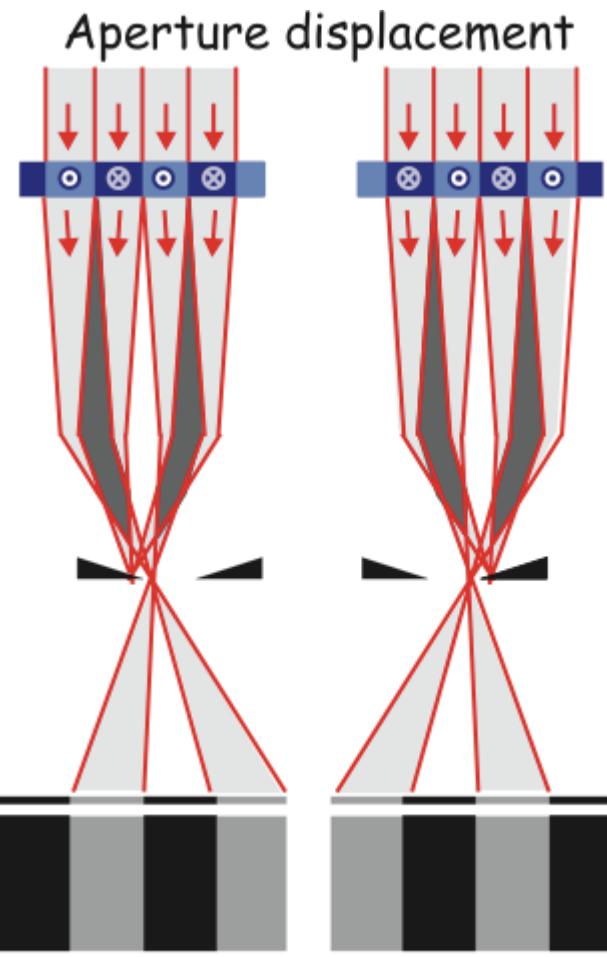


Lorentz deflection angle

$$\beta_L = \frac{e\lambda(\mathbf{B} \times \mathbf{n})}{h} t \approx 100 \mu\text{rad}$$

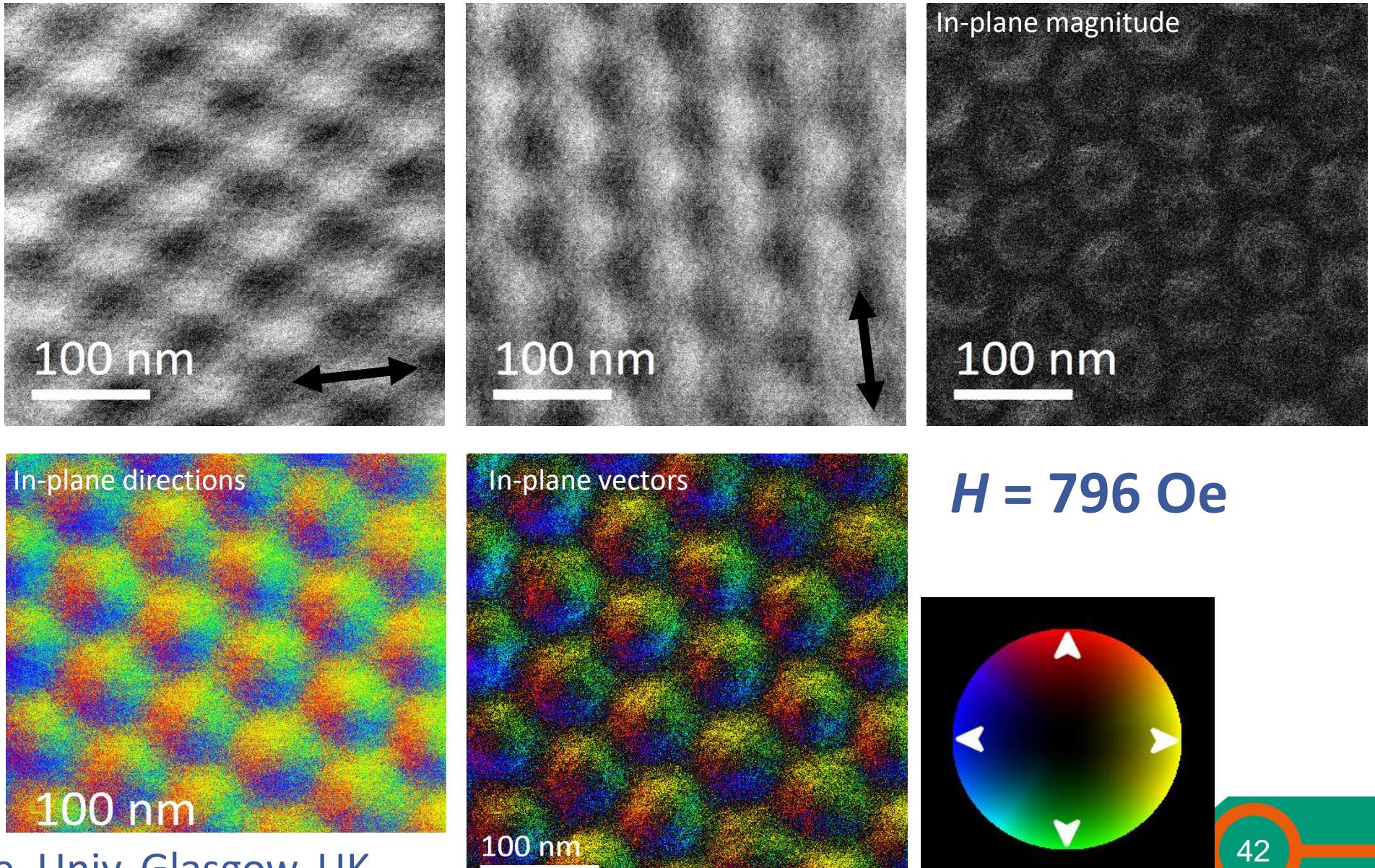
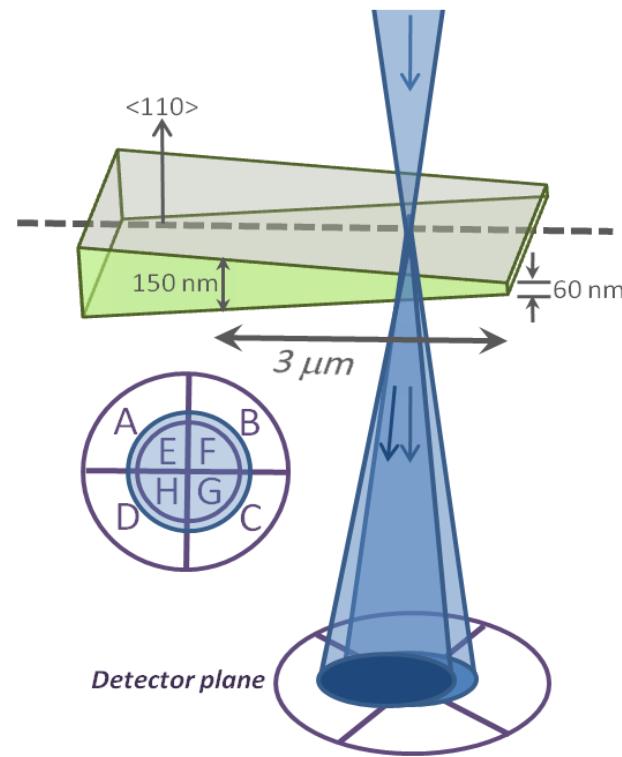


Highlight domain walls

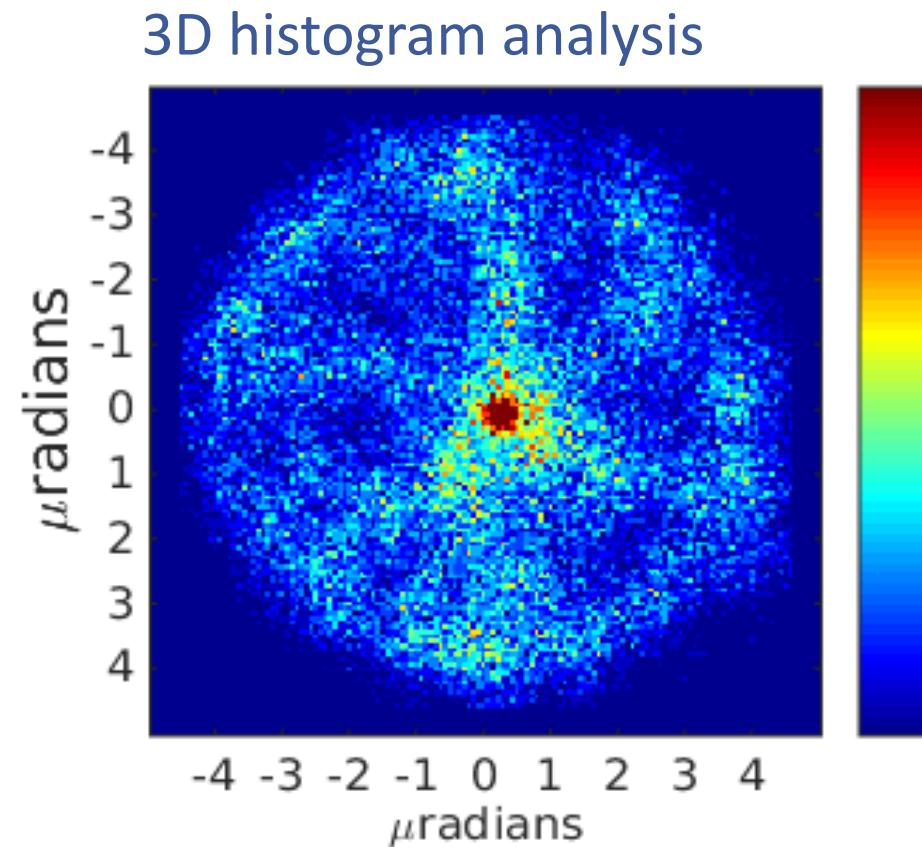
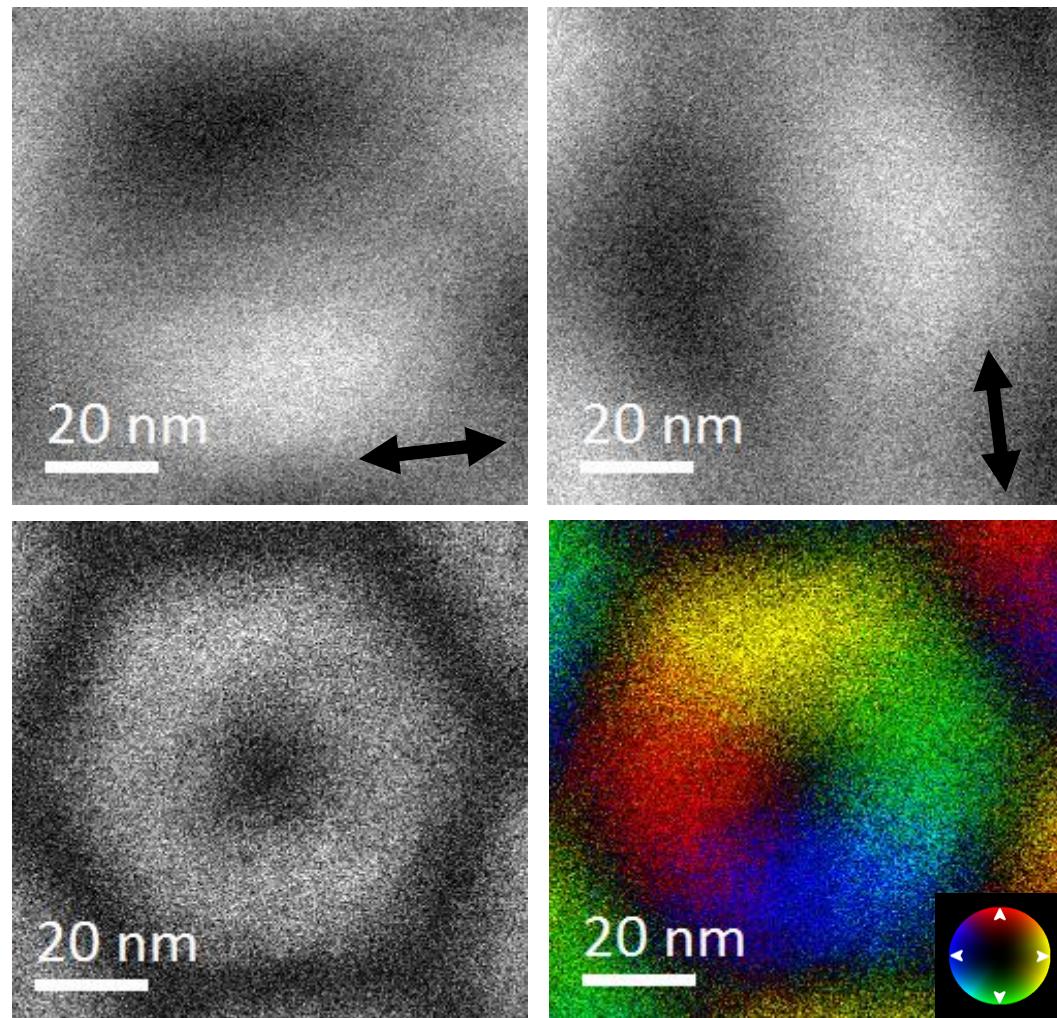


Highlight domains

Skermion lattice



Material from S. McVitie, Univ. Glasgow, UK



- Lorentz deflection angle $+/- 4 \mu\text{radians}$ – equiv. to $B_S \sim 0.2$ Tesla
- Six-fold symmetry

Material from S. McVitie, Univ. Glasgow, UK

Outlines

Magneto-optical microscopy (MO)

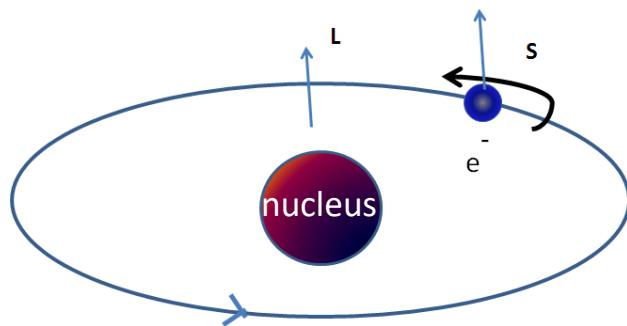
Scanning electron microscopy (SEMPA)

Transmission electron microscopy (TEM)

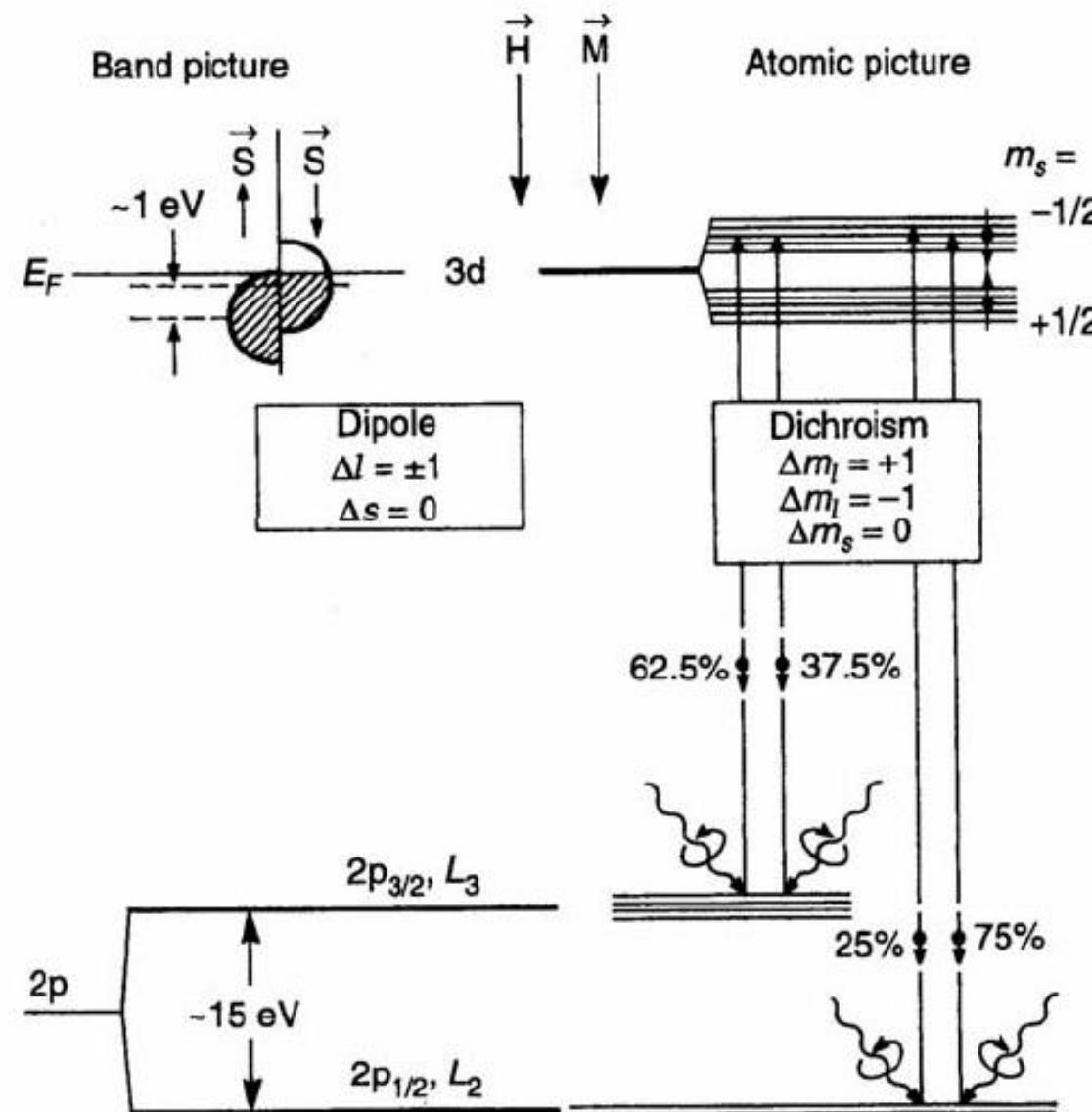
X-Ray microscopy

Magnetic force microscopy (MFM)

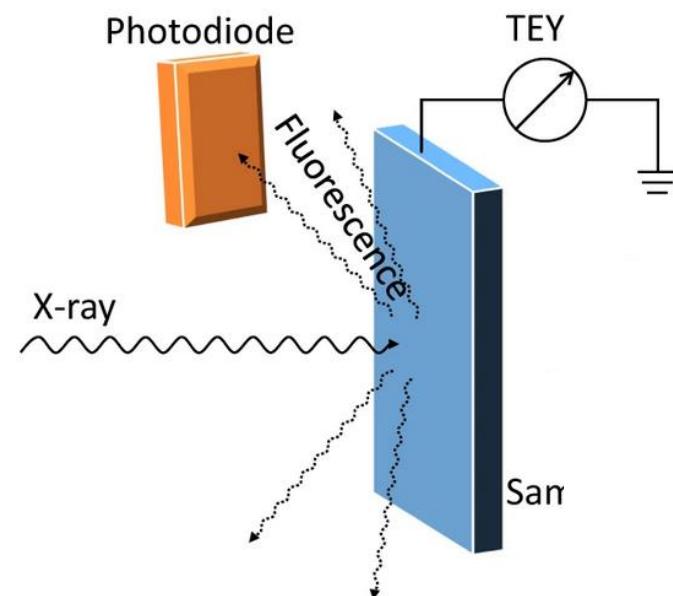
X-ray magnetic circular dichroism (XMCD)



- XMCD disentangles spin and orbital magnetic moment
- XMCD disentangle the moment from specific atoms in an alloy or a multilayer
- XMCD requires to work in synchrotron to get enough X-ray flux (700 - 900 eV for Fe,Co,Ni)



X-ray magnetic circular dichroism (XMCD)

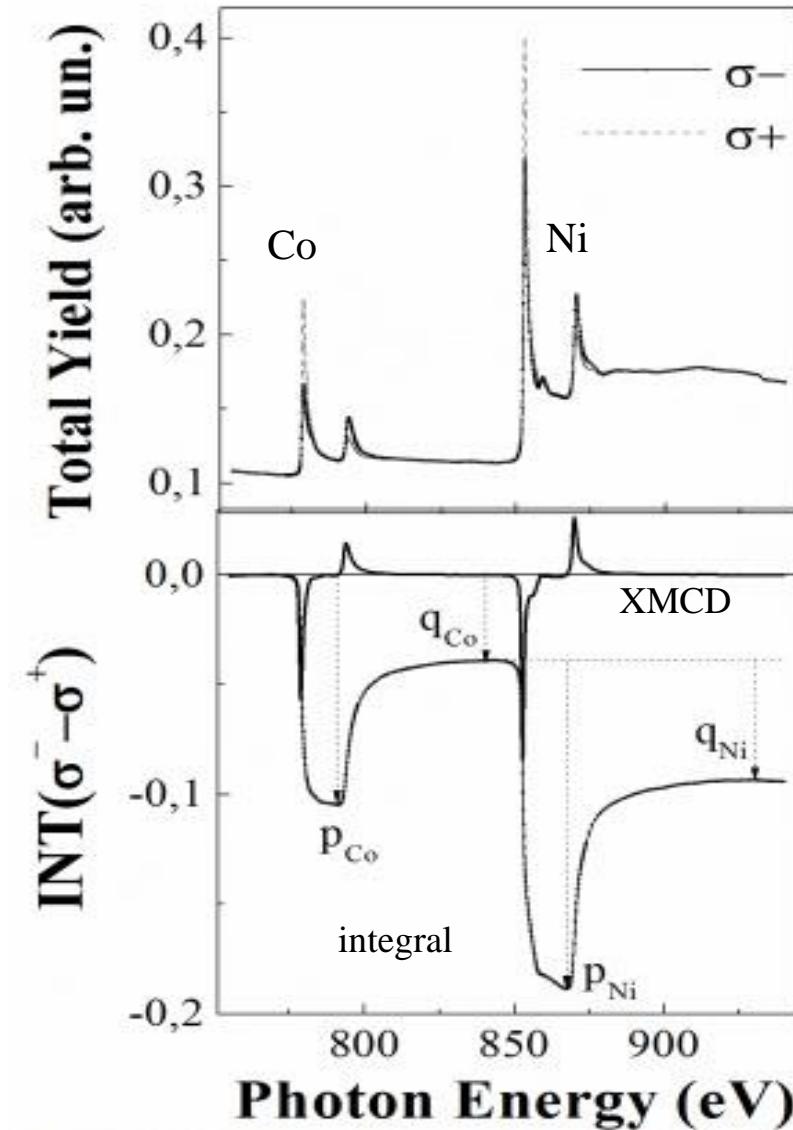


$$m_{\text{spin}}^{\text{eff}} = 2 \langle S_z^{\text{eff}} \rangle \frac{\mu_B}{\hbar} = n_h \cdot \left(\frac{3p - 2q}{r} \right) \mu_B$$

$$m_{\text{orb}} = \langle L_z \rangle \frac{\mu_B}{\hbar} = n_h \cdot \left(\frac{2q}{3r} \right) \mu_B$$



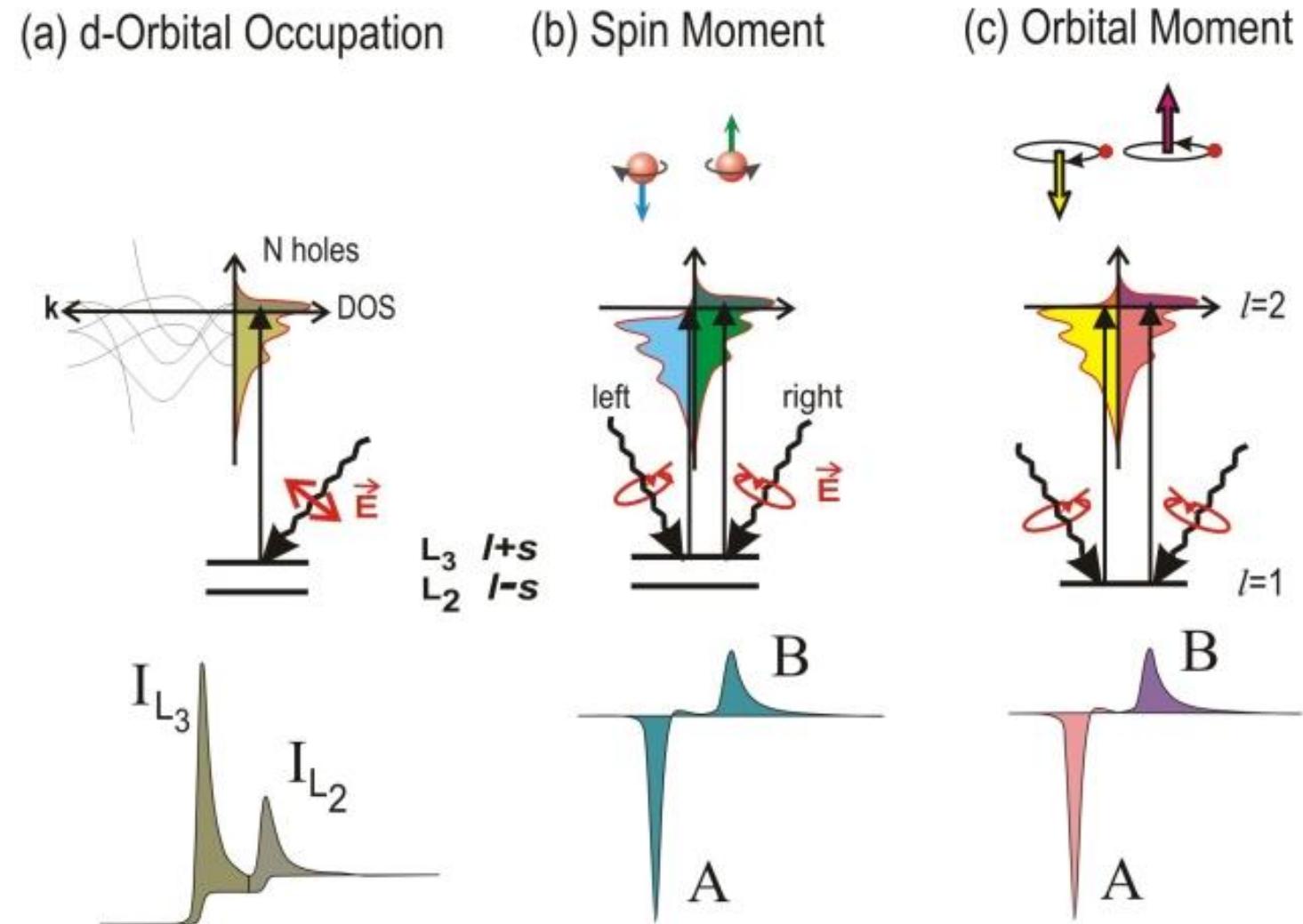
« Surface » sensitive technic (< 50 nm)



X-ray magnetic circular dichroism (XMCD)

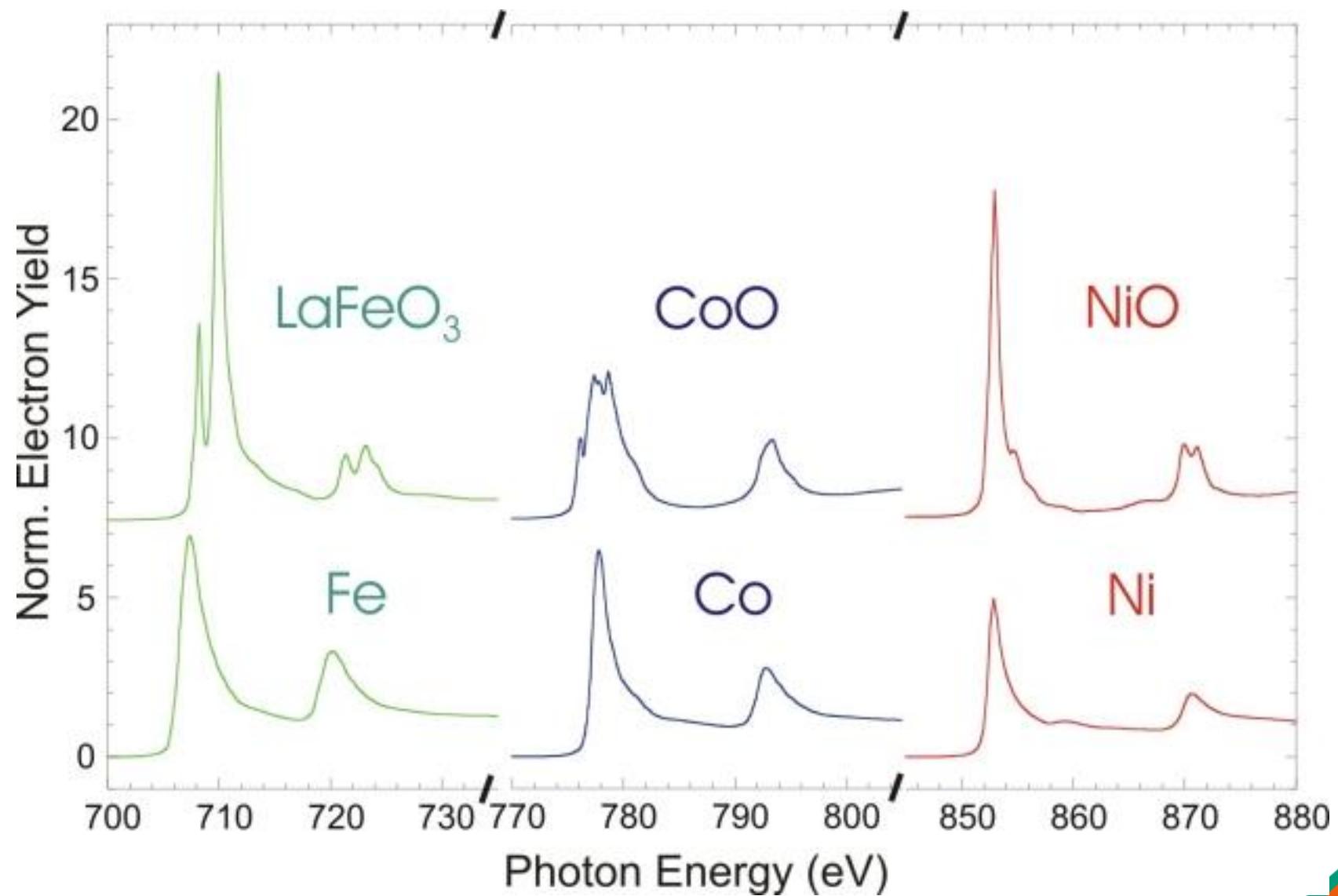
Electronic transitions in conventional L-edge x-ray absorption (a), and x-ray magnetic circular x-ray dichroism (b,c), illustrated in a one-electron model. The transitions occur from the spin-orbit split 2p core shell to empty conduction band states. In conventional x-ray absorption the total transition intensity of the two peaks is proportional to the number of d holes (first sum rule). By use of circularly polarized x-rays the spin moment (b) and orbital moment (c) can be determined from linear combinations of the dichroic difference intensities A and B, according to other sum rules

Spin and Orbital Moments: X-Ray Magnetic Circular Dichroism

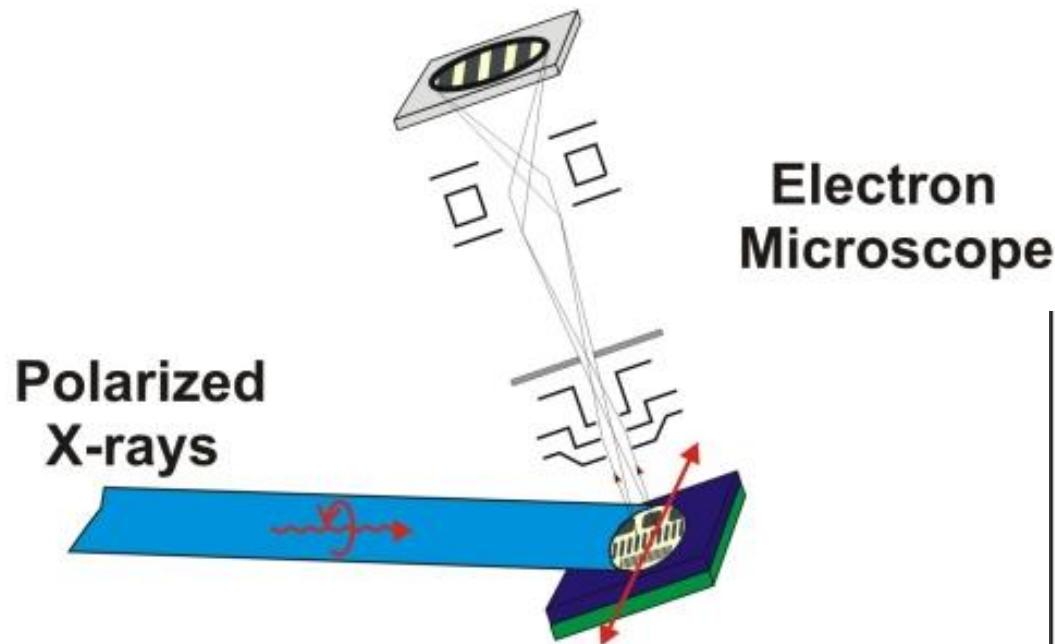


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X-ray magnetic circular dichroism (XMCD)



X-Ray Spectro-Microscopy



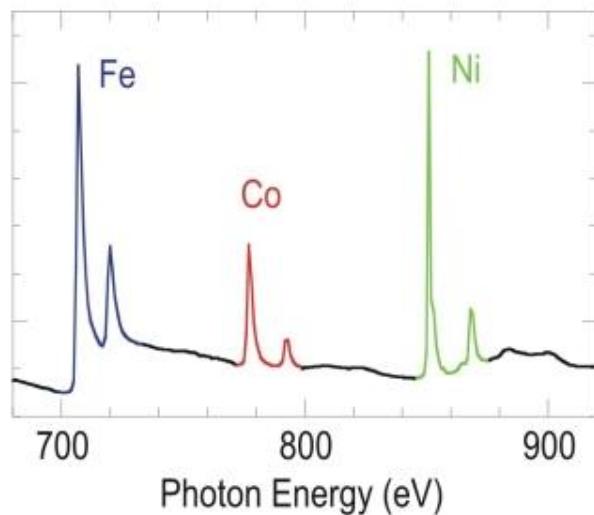
Polarized
X-rays

Electron
Microscope

Magnetic imaging by means of **PEEM**. A layer in the sample is selected by tuning the x-ray energy to the desired element. X-ray polarization contrast at an absorption peak is used for imaging contrast. The local electron yield from a sample region, imaged by PEEM, depends on the relative orientation of the magnetic direction or axis and the polarization, as illustrated on the right.

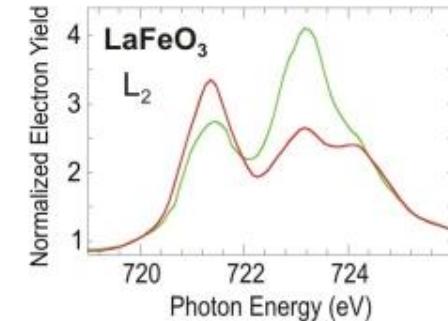
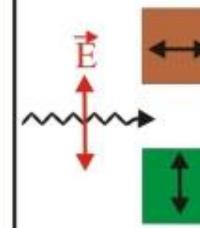
Photoemission electron microscopy (PEEM,

Tune x-ray **energy**
for elemental specificity

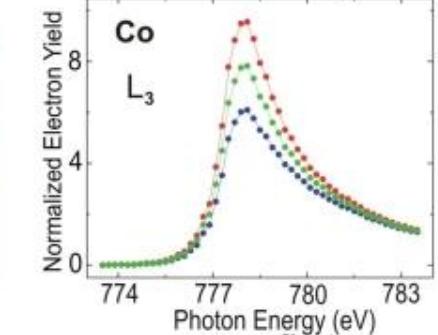
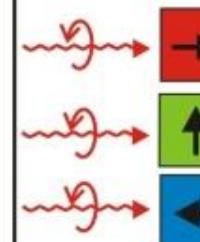


Tune x-ray **polarization**
for magnetic specificity

Linear Dichroism - Antiferromagnets

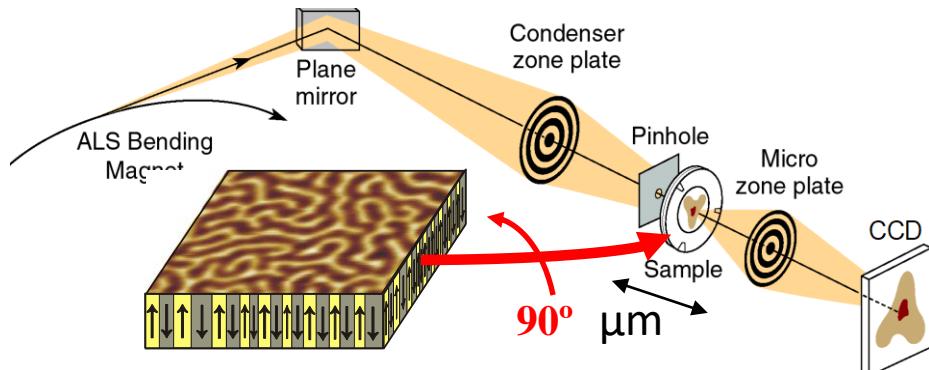


Circular Dichroism - Ferromagnets



Transmission X-ray microscopy (TXM)

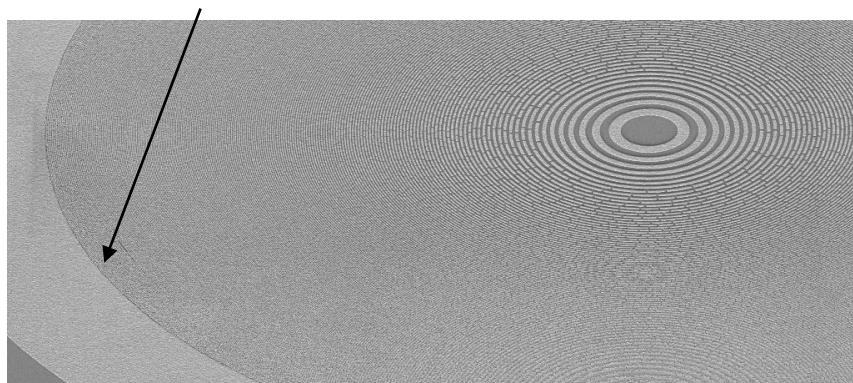
(ALS, SLS, BESSY II, ANKA)



Advantages : large image ($10 \mu\text{m}$)
with good, 50ps time resolution

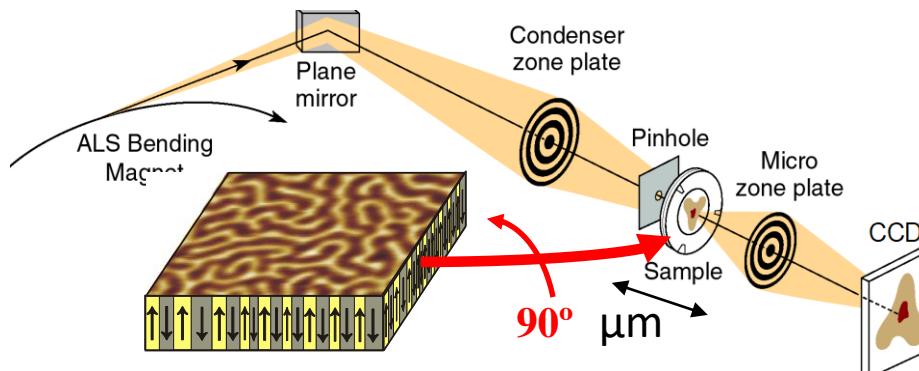
Disadvantages : mostly 300K, small field, lenses

Distance between 2 circles => resolution (here 15 nm)



Transmission X-ray microscopy (TXM)

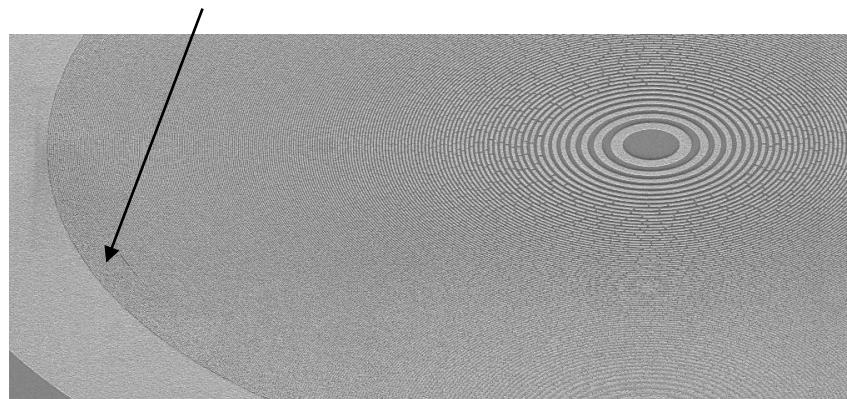
(ALS, SLS, SOLEIL, BESSY II, ANKA)



Advantages : large image ($10 \mu\text{m}$)
with good, 50ps time resolution

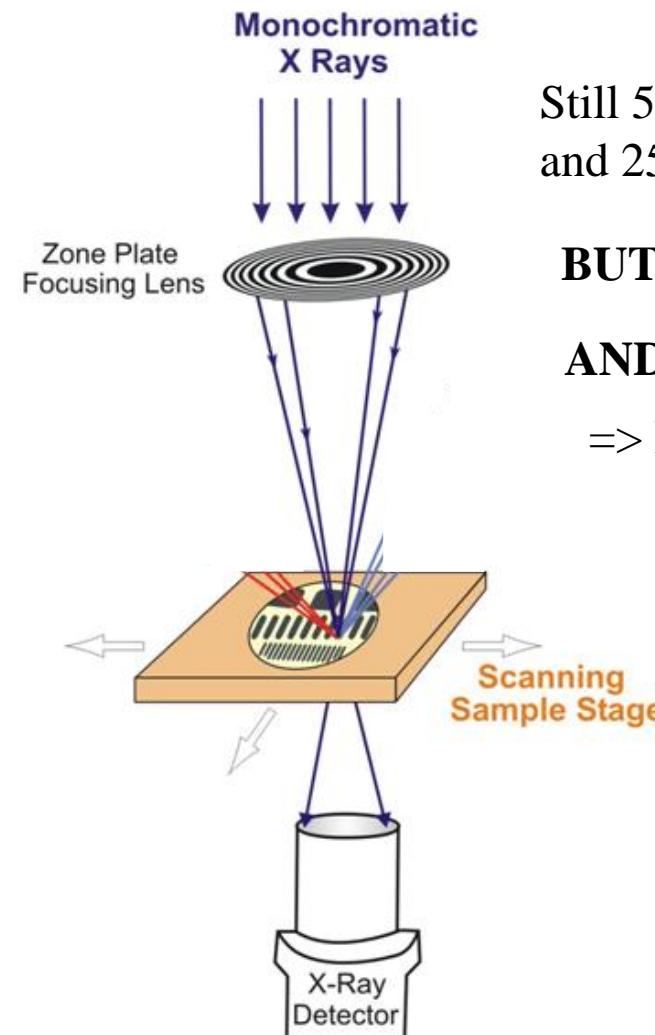
Disadvantages : mostly 300K, small field, lenses

Distance between 2 circles => resolution (here 15 nm)



Scanning TXM

(ALS, SSRL, SLS, Soleil)



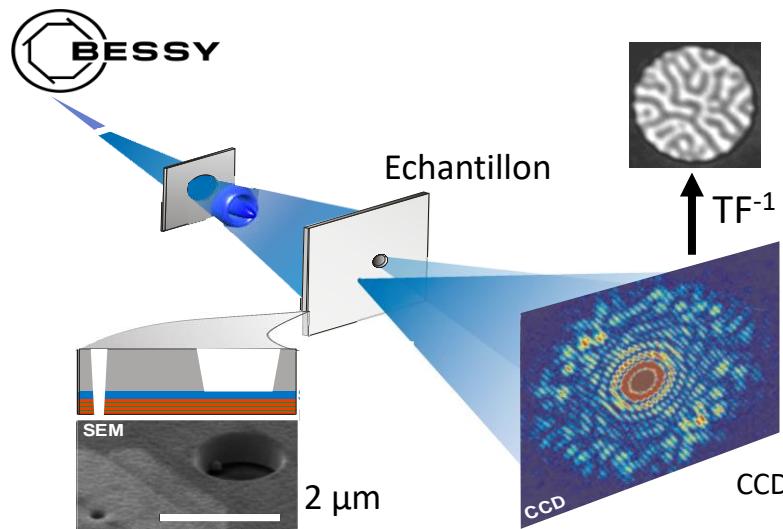
Still 50 ps time resolution
and 25 nm resolution

BUT Only one lens

AND Scanning

=> More flux locally

X-ray Holography



Advantage : 400K-10K, more space around the sample

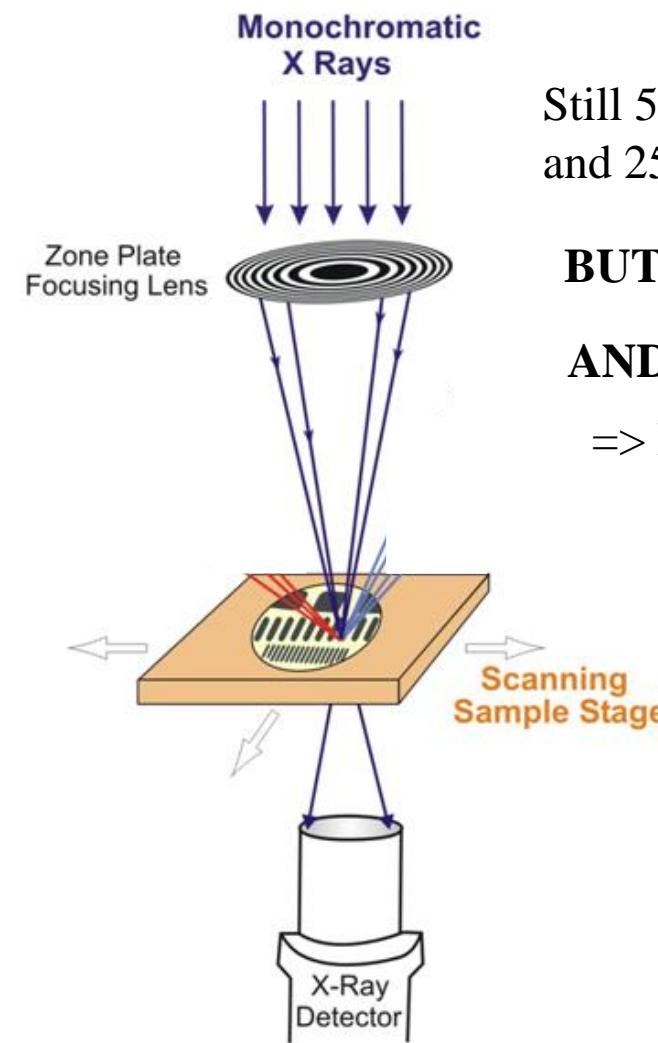
Disadvantage : sample preparation,
limited image size ($< 2 \mu\text{m}$)
Loss in resolution (50nm)
Phase retrieval



**Dynamics in MTXM, STXM,
Holography requieres stroboscopy**

Scanning TXM

(ALS, SSRL, SLS, Soleil)



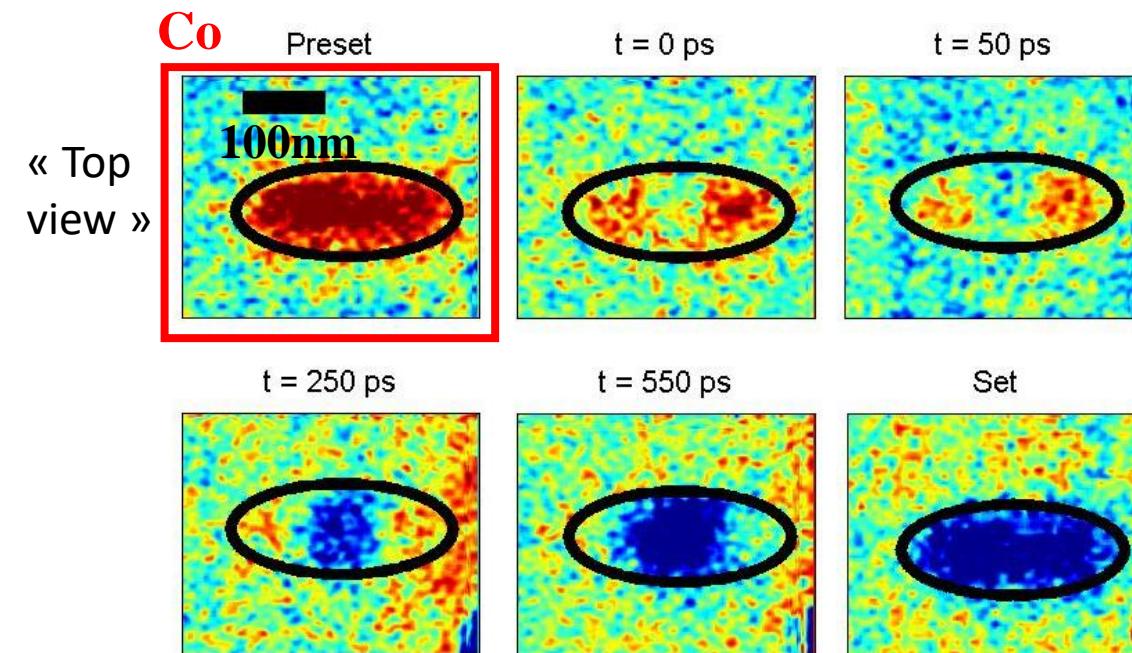
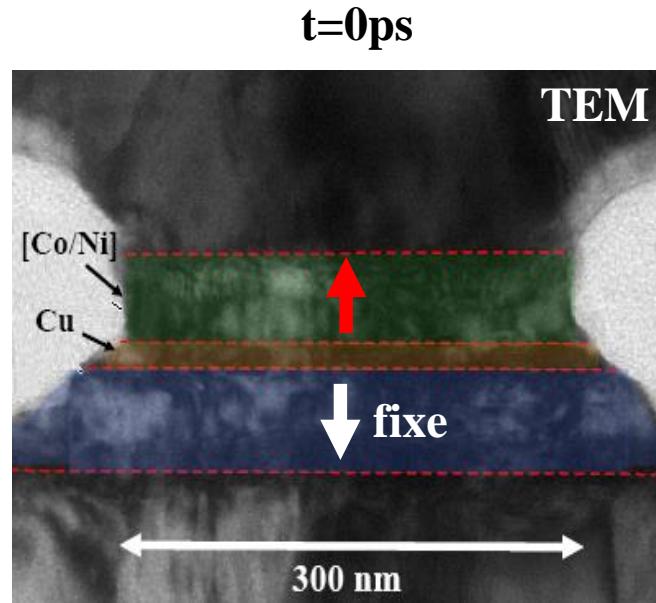
Still 50 ps time resolution
and 25 nm resolution

BUT Only one lense

AND Scanning

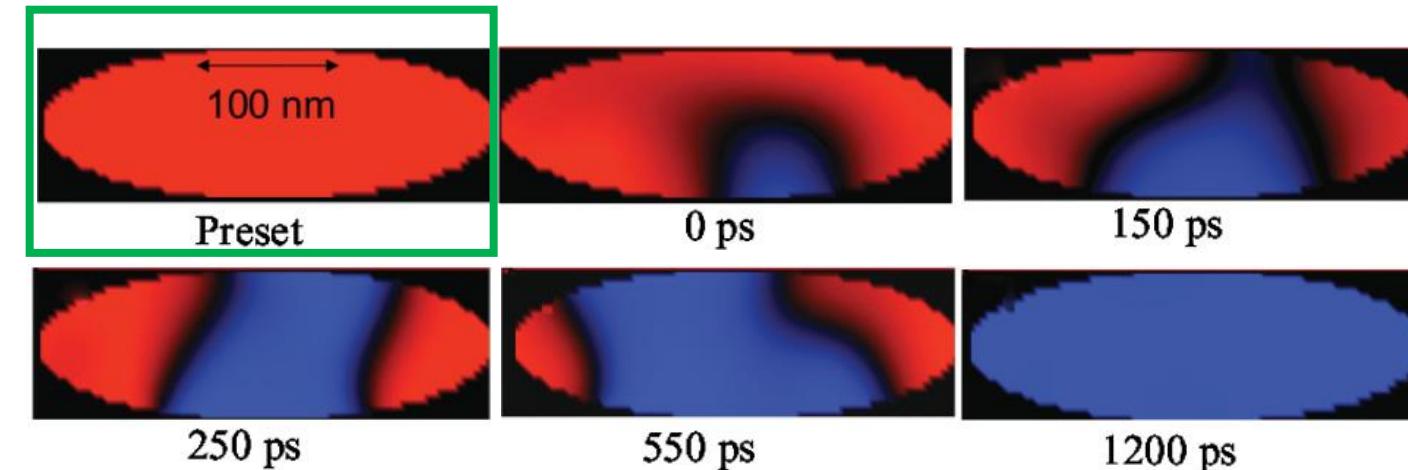
=> More flux locally

STT induced switching - STXM

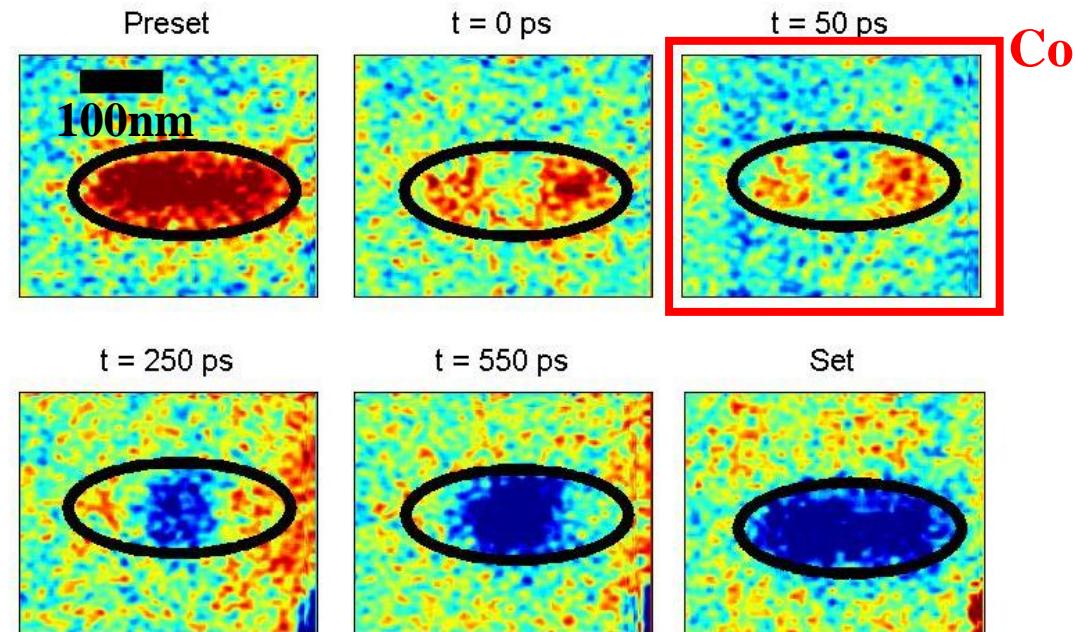
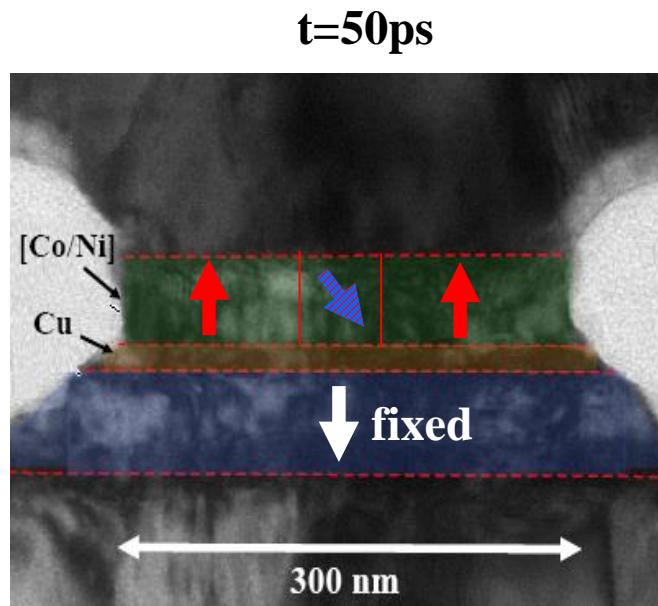


Excitation : Current pulsed at t=0ps

Micromagnetic simulation
(Scheifein code)

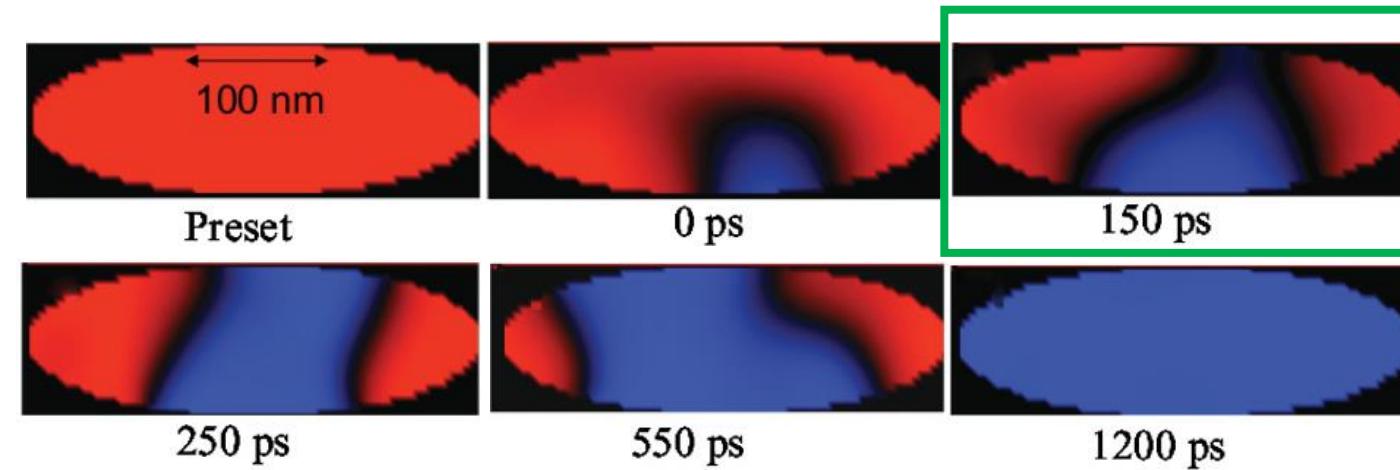


STT induced switching - STXM

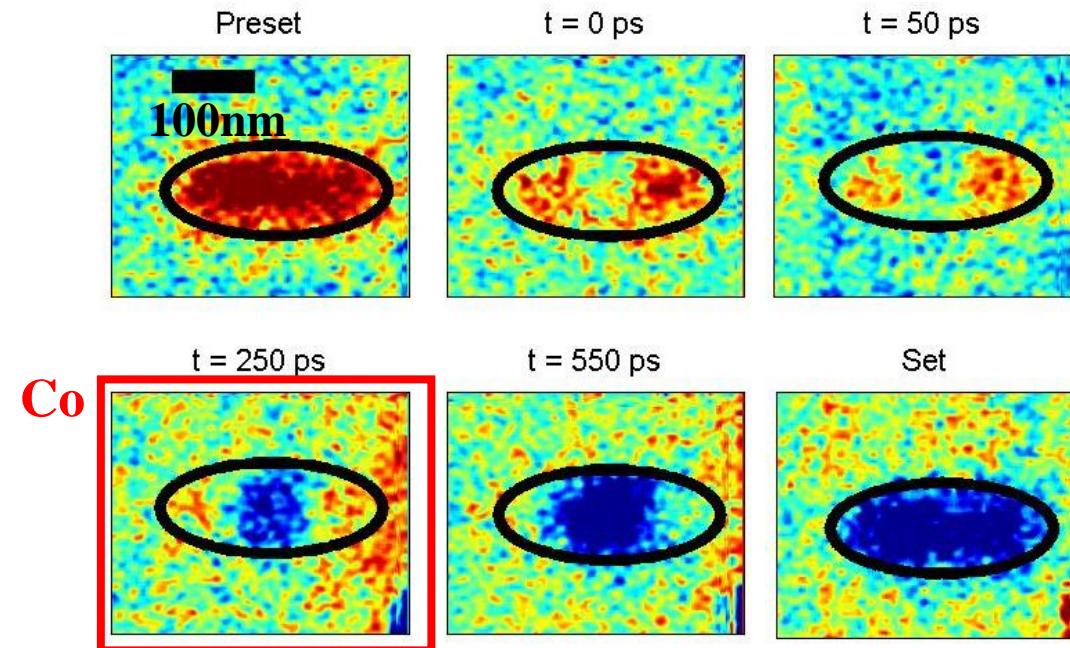
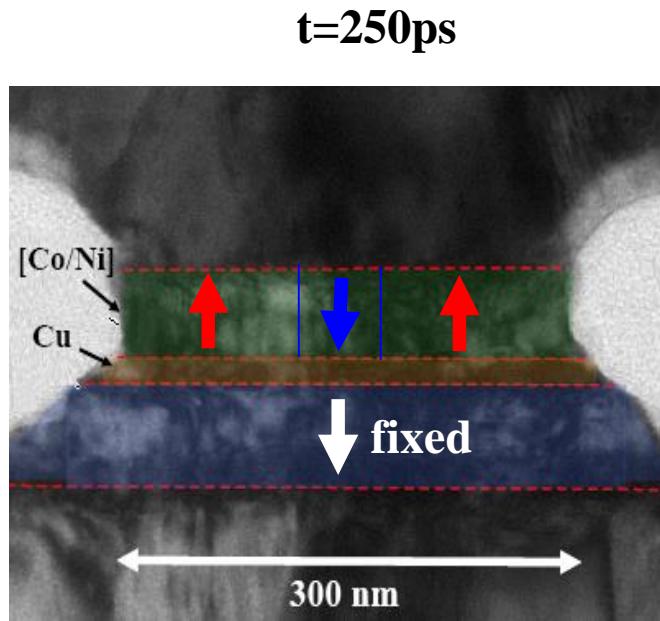


Excitation : Current pulsed at t=0ps

Micromagnetic simulation
(Scheifele code)

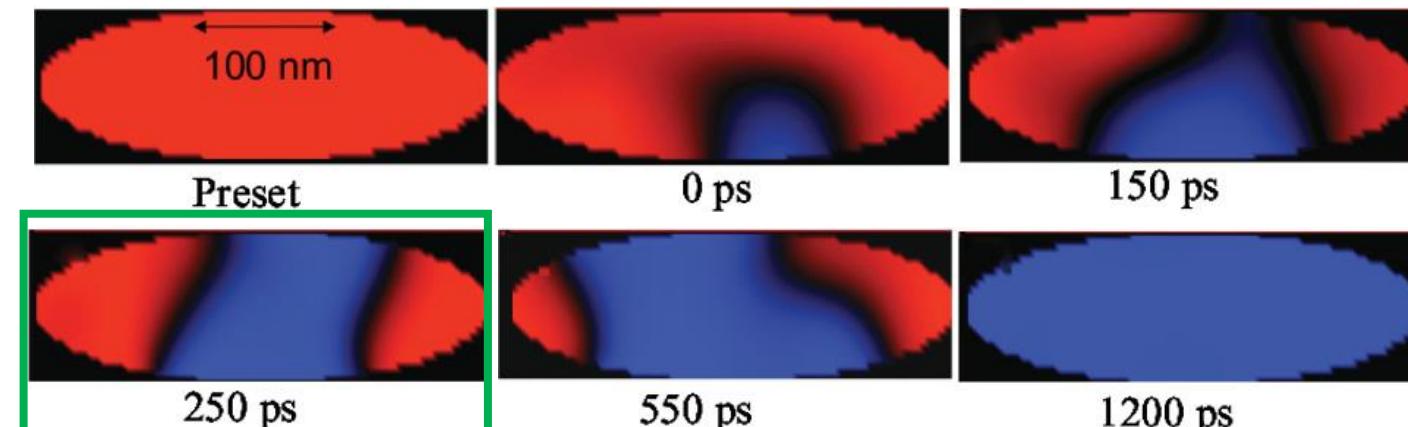


STT induced switching - STXM

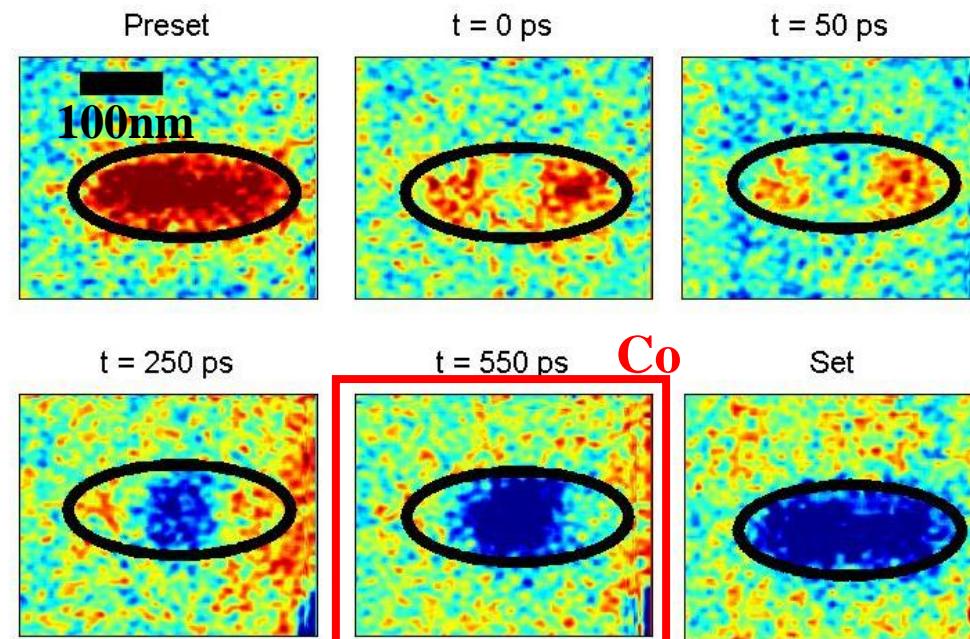
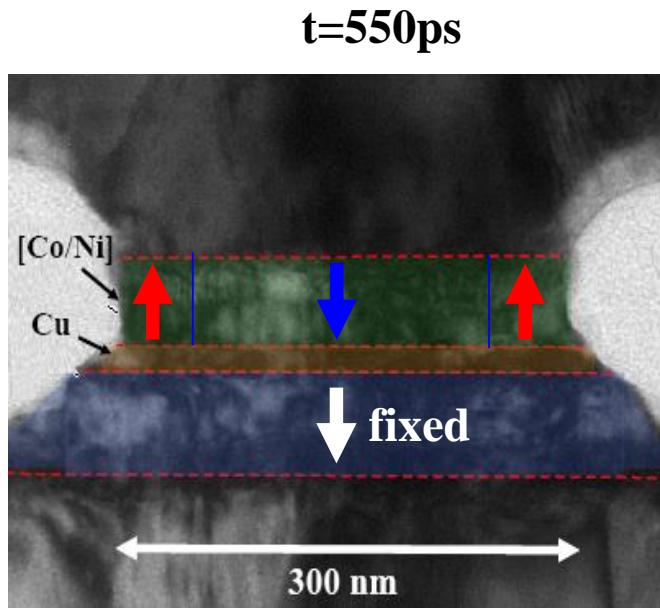


Excitation : Current pulsed at t=0ps

Micromagnetic simulation
(Scheifein code)

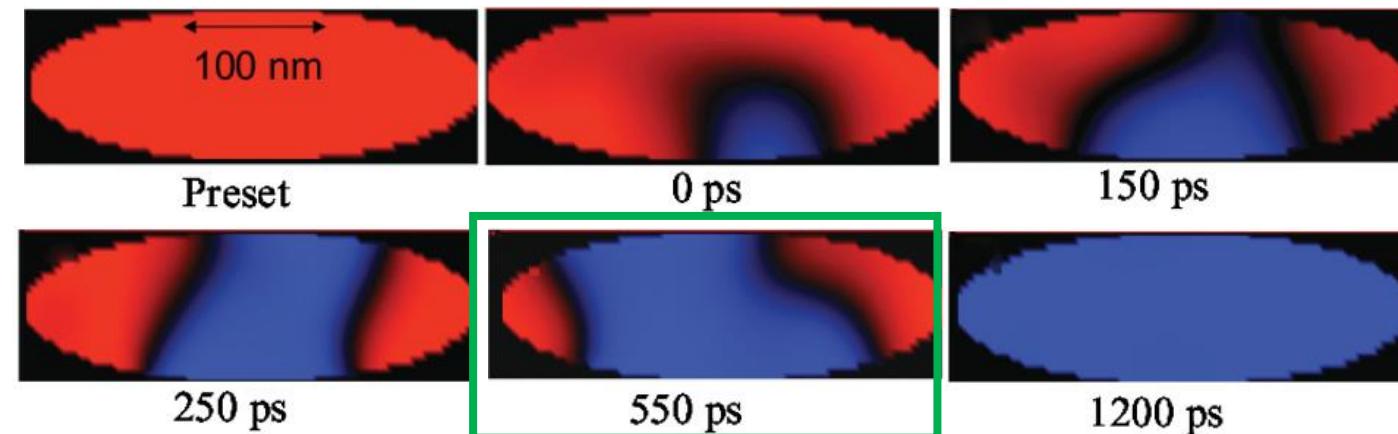


STT induced switching - STXM

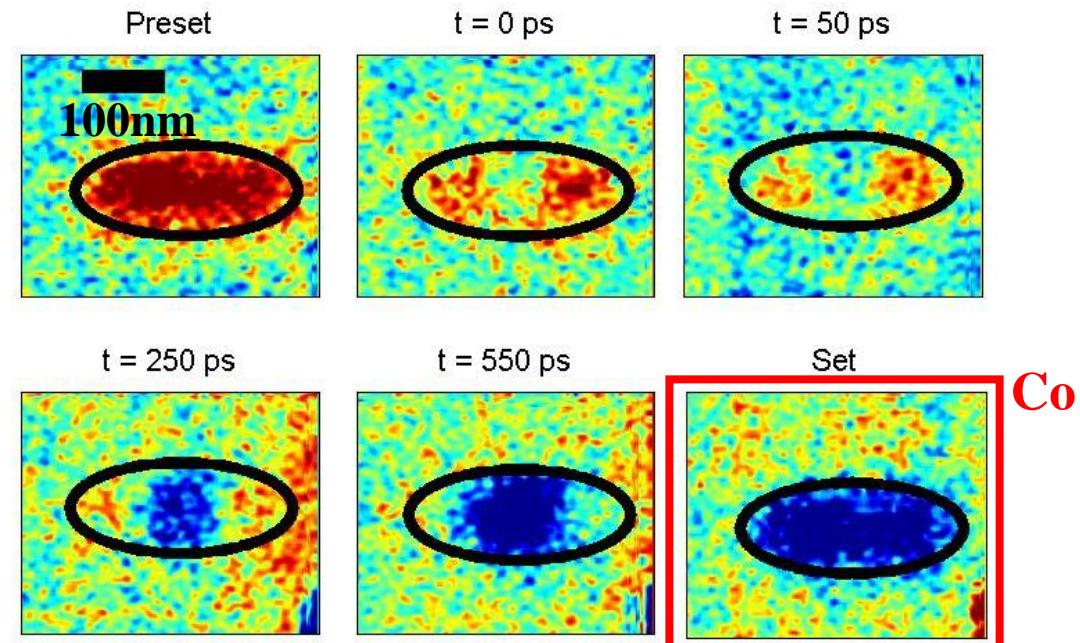
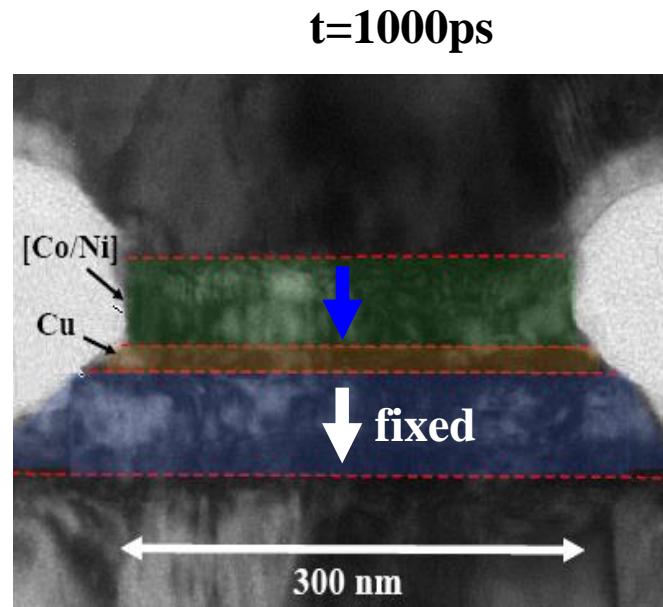


Excitation : Current pulsed at t=0ps

Micromagnetic simulation
(Scheinfein code)

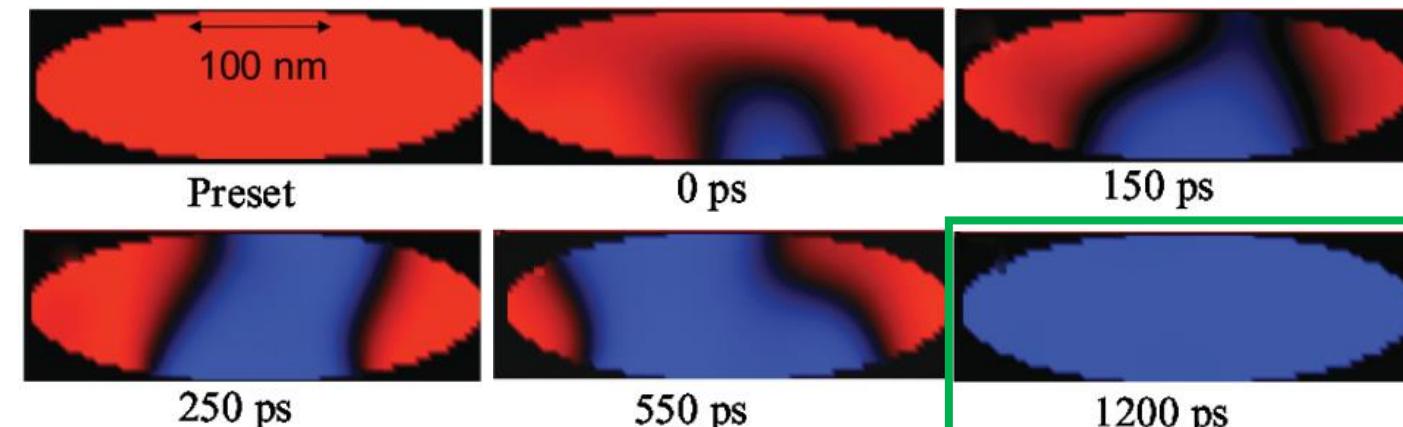


STT induced switching - STXM



Excitation : Current pulsed at $t=0\text{ps}$

Micromagnetic simulation
(Scheifelein code)



What is measured?

- Magnetization component
- Elemental resolution
- Direct
- Quantitative

Environmental conditions

- Temperature 
- Field: magnetic field (not PEEM) 
- Electric current, light etc. 
- Strain 
- Additional measuring techniques

Which specifications?

- Magnetization: 1D, 2D 
- Depth resolution: surface/volume 
- Lateral resolution 25 nm 
- Sensitivity: <single layer 
- Time/Spectral resolution 

Versatility

- No sample preparation
- Time per measurement: s – min
- In situ
- Synchrotron radiation

Outlines

Magneto-optical microscopy (MO)

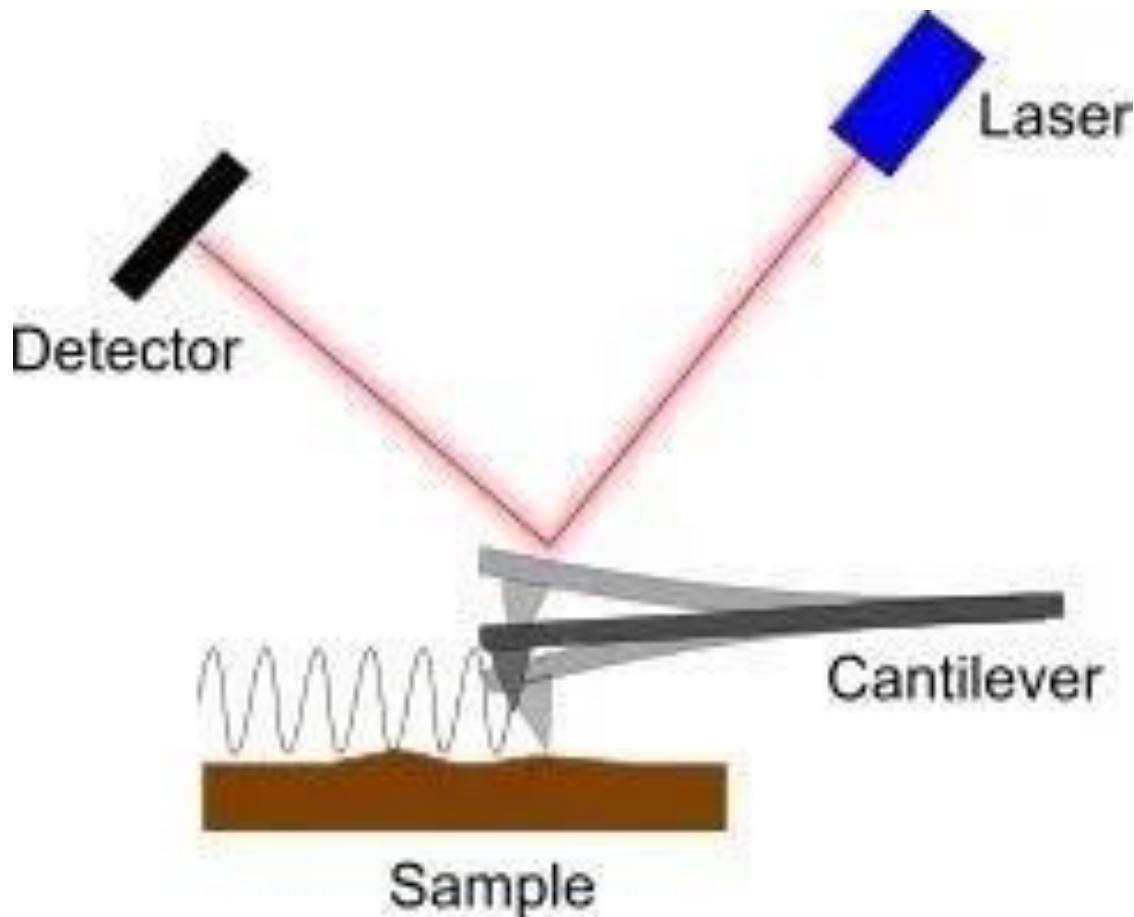
Scanning electron microscopy (SEMPA)

Transmission electron microscopy (TEM)

X-Ray microscopy

Magnetic force microscopy (MFM)

Scanning probe microscopy



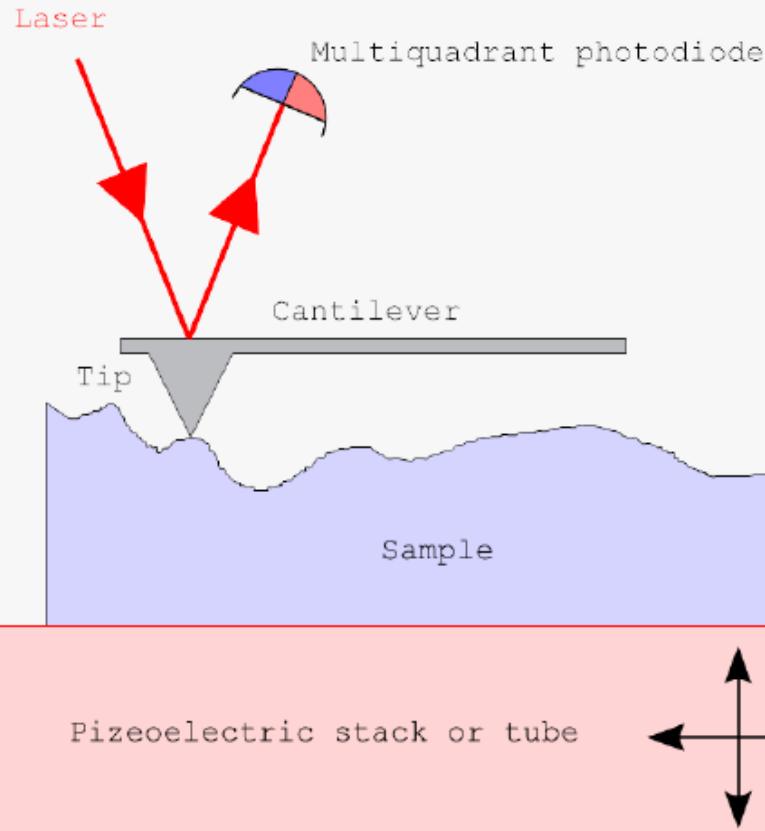
Interaction between the Tip and the sample

Different interaction = different technique

Making tip is an art !

Atomic Force Microscopy

The Atomic Force Microscope (AFM)



G. Binnig et al., Phys. Rev. Lett. 56, 930 (1986)

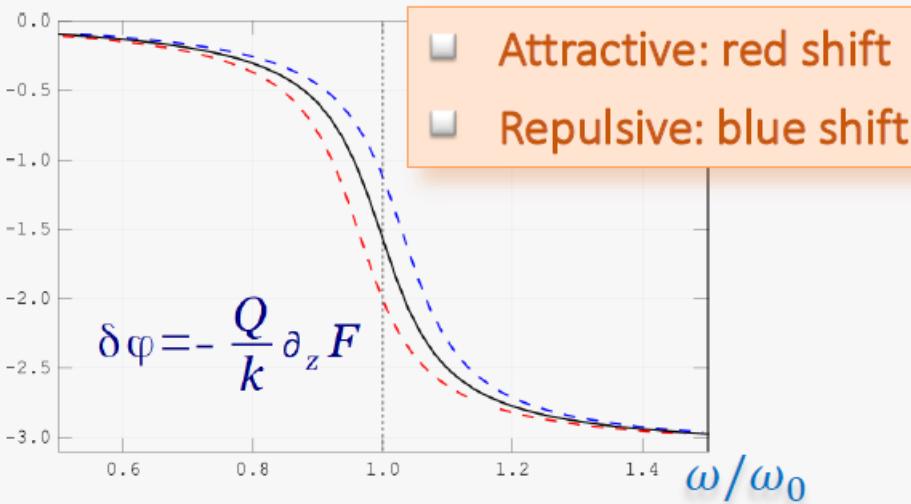
The cantilever as an oscillator

$$m \ddot{z} + \Gamma \dot{z} + k z = F(z)$$

$$\text{with: } F(z) = F(z_0) + (z - z_0) \partial_z F$$

$$\text{Mere renormalization: } \omega_{0,\text{eff}} = \omega_0 \left(1 - \frac{1}{2k} \partial_z F \right)$$

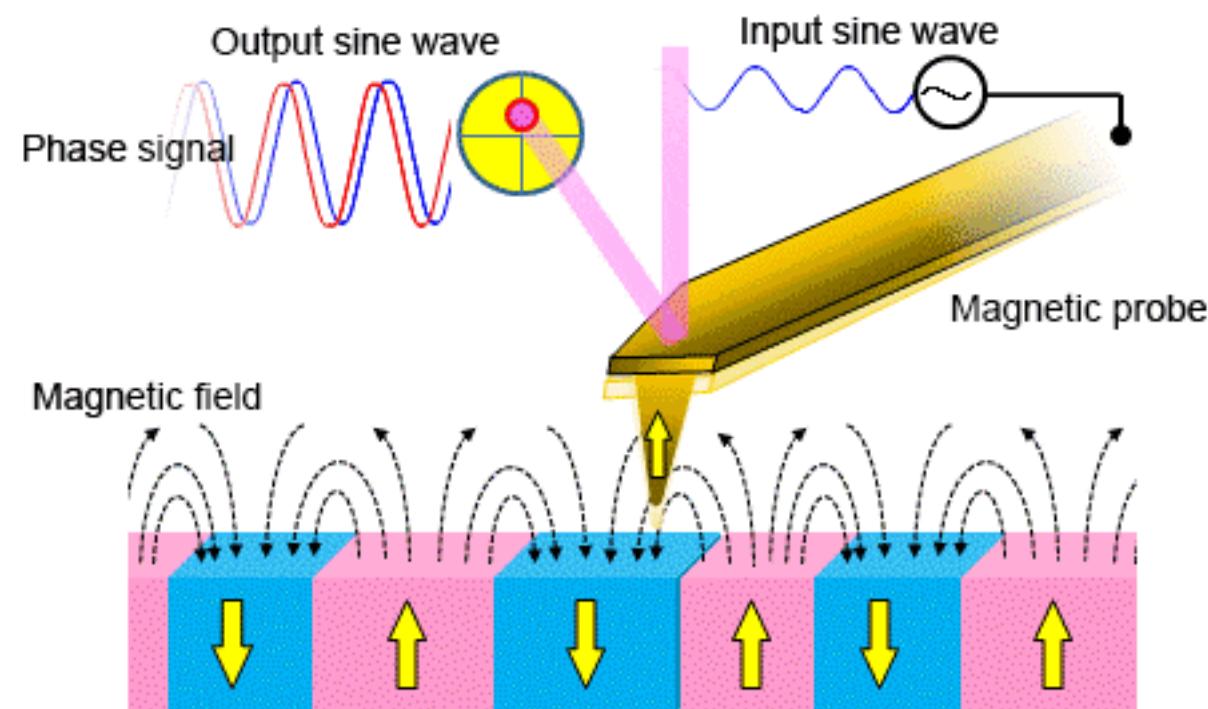
Probing forces with the phase shift



AFM characterizes topography

Magnetic Force Microscopy

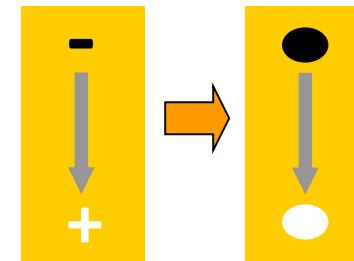
$$\vec{F} = \nabla(\vec{m} \bullet \vec{H}_D)$$



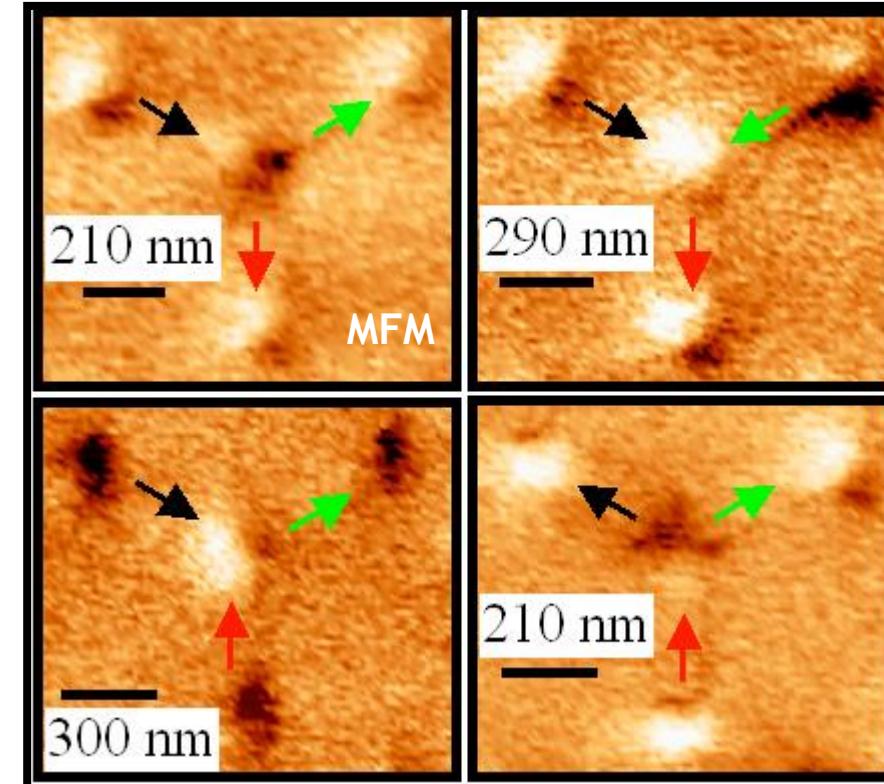
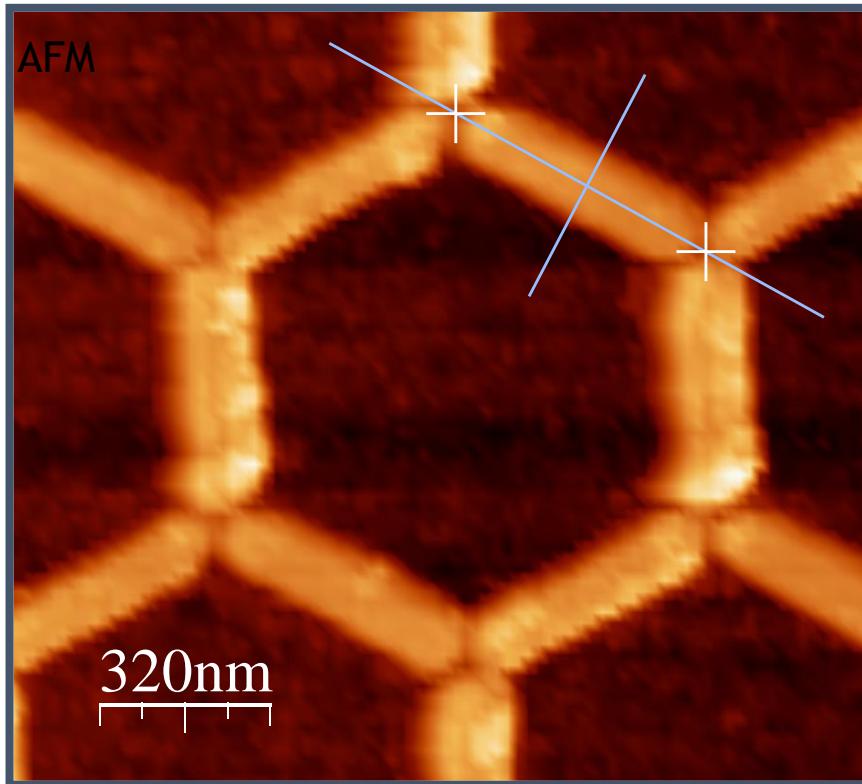
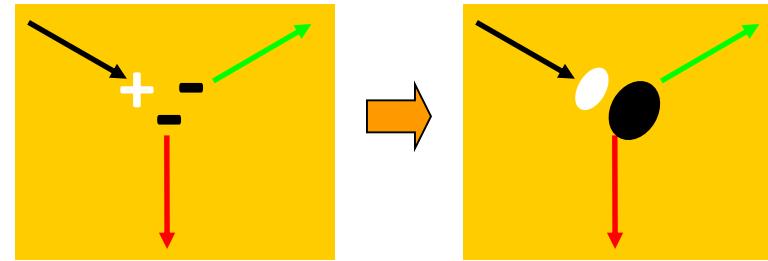
$$\rho = \operatorname{div}(\vec{M}), \quad \sigma = \vec{M} \bullet \vec{n}$$

$$\sigma = \vec{M} \bullet \vec{n}$$

1 Spin



3 Spins :

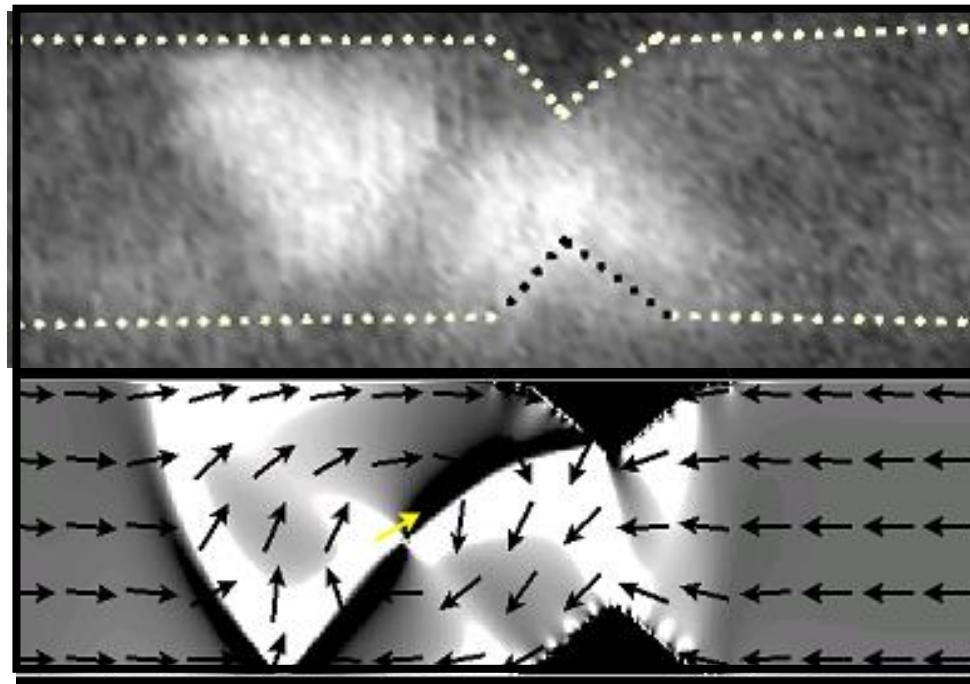


$$\rho = \operatorname{div} (\vec{M})$$

MFM

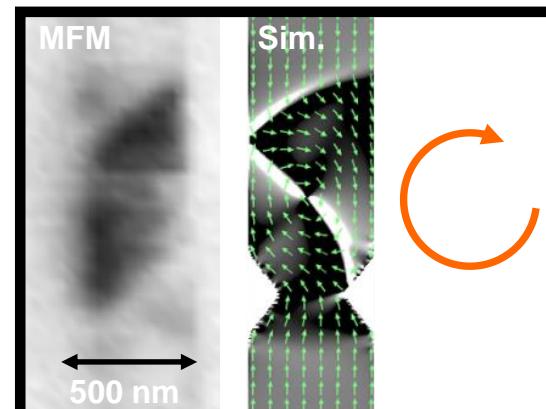
Simulation

Domain wall Vortex

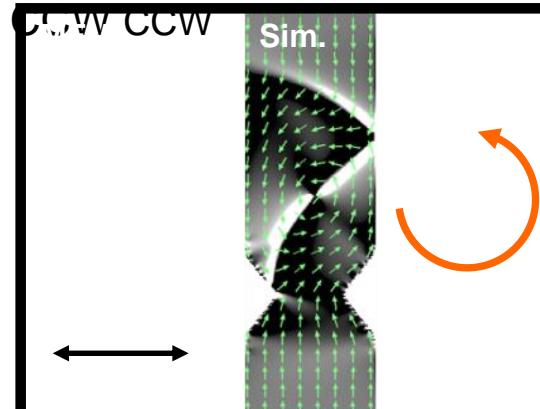


500 nm

Domain wall Chirality CW



Domain wall Chirality



MFM - Characteristic

Contrast mechanism	∇B_{ext}
Evaluation of the magnetization, $M(r)$	Indire
Spatial resolution (nm)	$\frac{300}{80}$
Depth of information (nm)	500–1000
Time for image acquisition	30 ms
Limits on applied magnetic fields	None
Imaging conditions	None
Max thickness	None
Sample smoothness	R
Sample clean surface	NR

Maps the derivative of the magnetic stray field
Spatial resolution down to 10 nm (vacuum)

Non-destructive

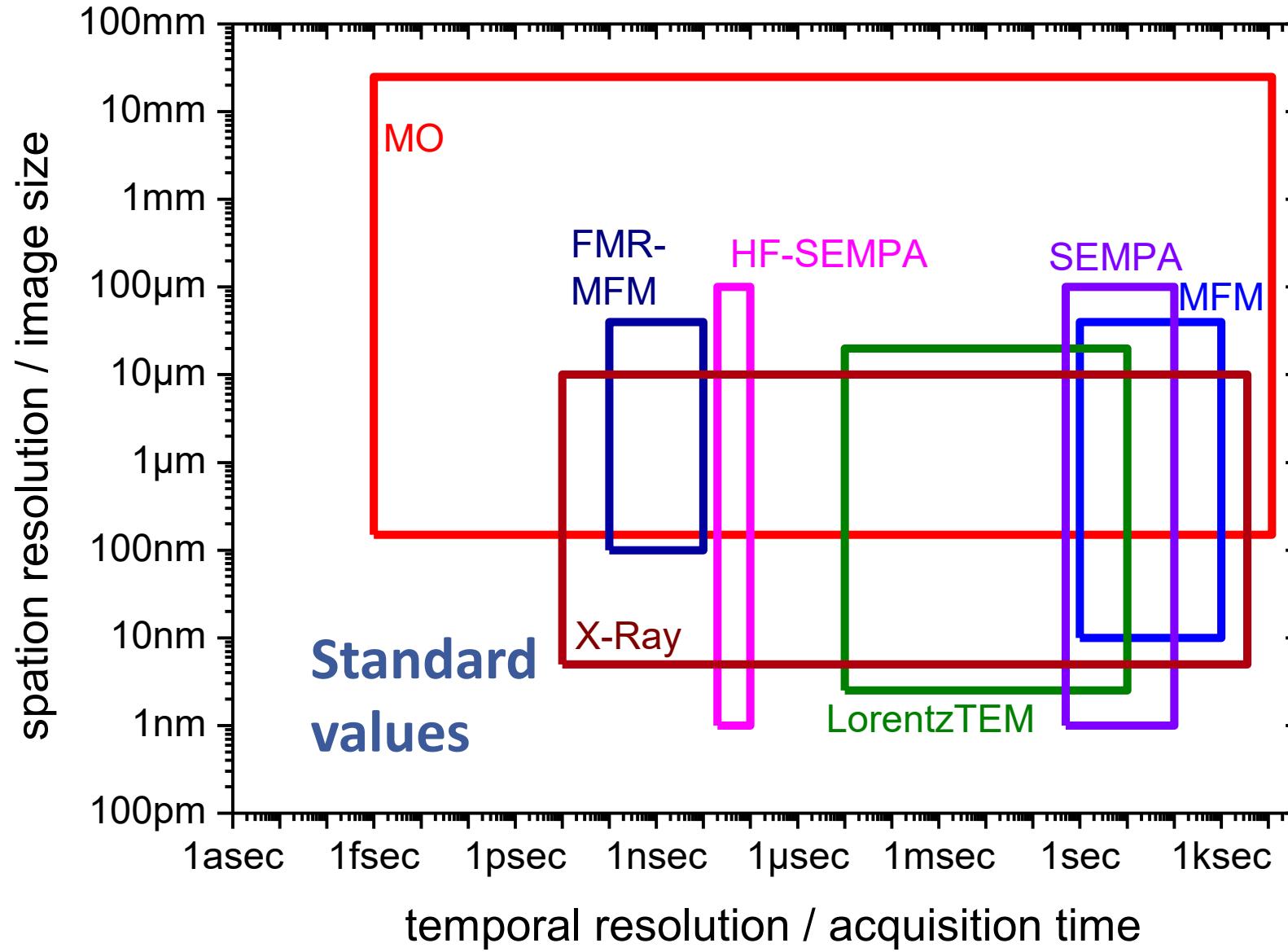
Mostly sensitive to the z-component of stray field (depending on tip)

No sample preparation needed
Surface should be relatively flat

Tip quality is critical

Tip-sample interaction: induced change of magnetic state
Limitations to measure magnetically soft samples

$$\vec{F} = \nabla(\vec{m} \bullet \vec{H}_D)$$



Magneto-optical microscopy (MO)

Scanning electron microscopy (SEMPA)

Transmission electron microscopy (TEM)

X-Ray microscopy

Magnetic force microscopy (MFM)

Thank you !



THE EUROPEAN SCHOOL ON
MAGNETISM



