

Stabilizing skyrmions in multiferroics materials

Bertrand Dupé

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www.tom.uliege.be

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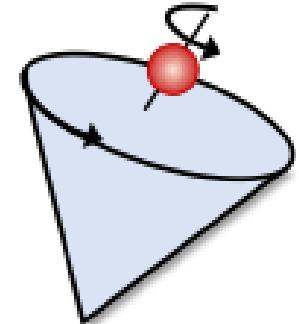
Lobbying and networking – STF, magnetometry...



European School on Magnetism 2026

Spin-orbit driven magnetic phenomena

Ångström laboratory, Uppsala University, Sweden
August 17-28, 2026



Enjoy ten days of fascinating topics around magnetism at the oldest university of Scandinavia. Lectures and hands-on sessions will cover fundamental aspects, theoretical modelling as well as experimental characterization of a variety of topics:

- Nanomagnetism
- Ultrafast magnetization dynamics
- Spin-orbit torques
- Spin-dependent transport
- Spin and orbital Hall effect
- Skyrmions
- Permanent magnets
- 2D magnets
- AFM spintronics
- Altermagnetism...



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Onsite: 700 €, Online: 300 €

Information: [WEBSITE](#)

Organization:

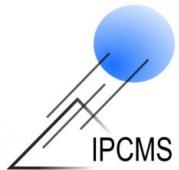
ESM chair: Assoc. Prof. Biplab Sanyal
ESM co-chair: Dr. Heike Herper



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Hervieux



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Philippe Ghosez
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Sebastian Meyer
Patrick Buhl

Alejandro Silhanek
Peter Schlagheck



Stefan Heinze
Charles Paillard
Markus Hoffmann
Stephan von Malottki

Bertrand Dupé



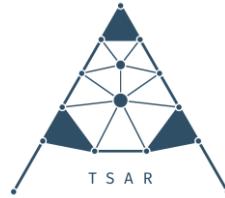
Wulf Wulfhekel
Marie Hervé
Loic Mougel



Geoffrey Beach
Felix Bütner
Ivan Lemesh



Stefan Blügel
Gustav Bihlmayer
Yuriy Mokrousov
Samir Lounis



Michel Viret
Jean-Yves Chaleau
Vincent Garcia
Aurore Finco
Vincent Jacques



Bin Xu Laurent Bellaiche

Topological orders in Matter (TOM – tom.uliege.be)

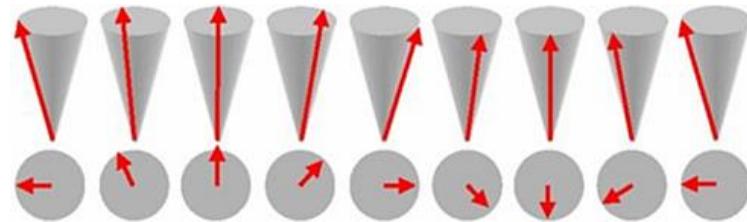
Magnonics and
thermal driven long
range excitations

Mexx Regout

In collaboration with
Matthieu Verstraete

Topology and transport
properties (Majorana
states...)

In collaboration with
Marie Hervé
Tristan Cren
Wulf Wulfhekel

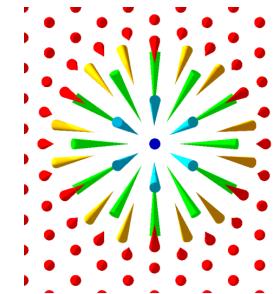


Topological orders in matter
[Github.com/bertdupe/Matjes](https://github.com/bertdupe/Matjes)



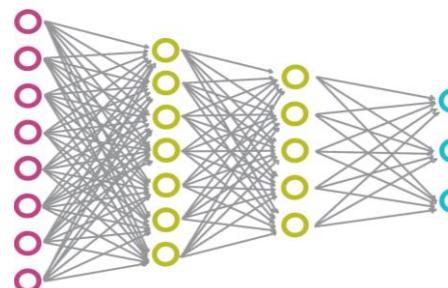
Bertrand Dupé

Topological magnetic
textures in real space
(skyrmions, merons...)



Sebastian Meyer
Olivier Gonnet

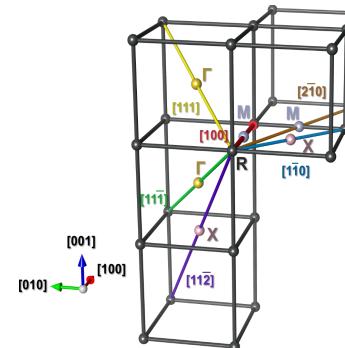
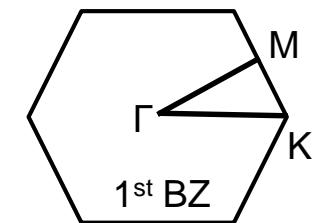
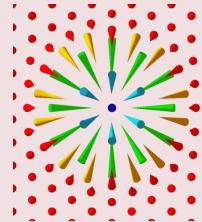
Artificial intelligence
and topology



Xavier Bosch

Outline

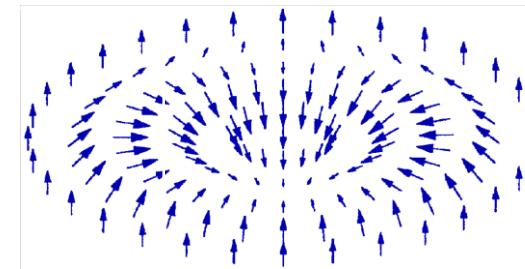
- Introduction on magnetic skyrmions
 - The discovery
 - The racetrack memory
 - Topology and stability
- The different magnetic interactions
 - Origin of the DM interaction
 - Obtaining magnetic interactions from density functional theory
 - Some examples of use
- Isolated skyrmions in Multiferroics
 - BiFeO₃ (BFO) as a good playground
 - Determining the magnetic interactions in BFO
 - Using strain to tune the interactions in BFO



Skyrmins in bulk magnetic materials

Micromagnetic model prediction

Existence of magnetic skyrmions
on a micrometer length scale

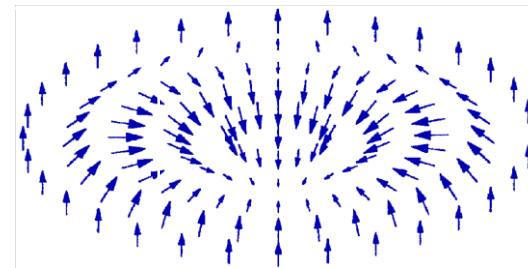


A. N. Bogdanov & D. A. Yablonskii, Sov. Phys. JETP 68, 101 (1989)

Skyrmins in bulk magnetic materials

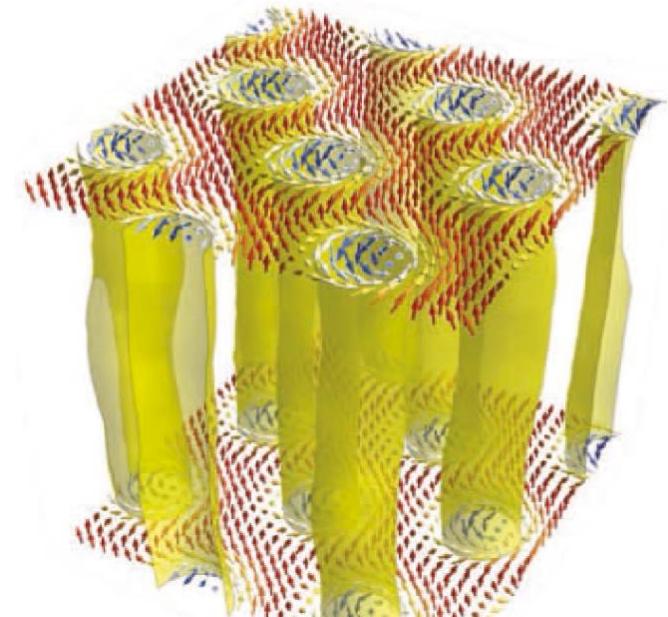
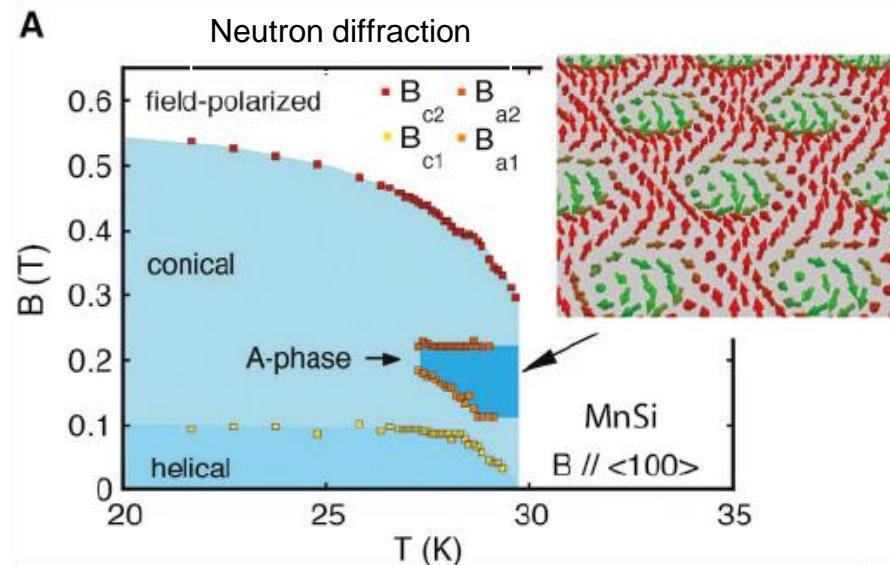
Micromagnetic model prediction

Existence of magnetic skyrmions
on a micrometer length scale



A. N. Bogdanov & D. A. Yablonskii, Sov. Phys. JETP **68**, 101 (1989)

Experimental discovery



S. Mühlbauer *et al.*, Science **323**, 915 (2009)
A. Neubauer *et al.*, PRL **102**, 186602 (2009)

X. Z. Yu *et al.*, Nature **465**, 901 (2010)
M. Lee *et al.*, PRL **102**, 186601 (2009)

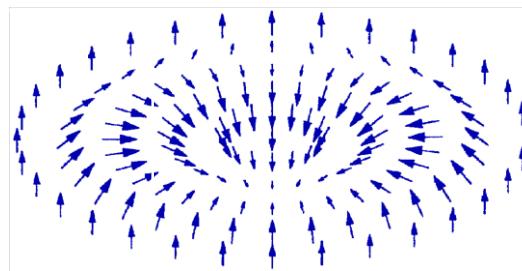
P. Milde *et al.*, Science **340**, 1076 (2013)

Skyrmins in bulk magnetic materials

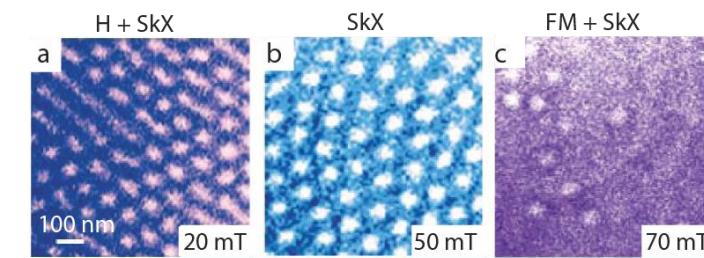
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Existence of magnetic skyrmions
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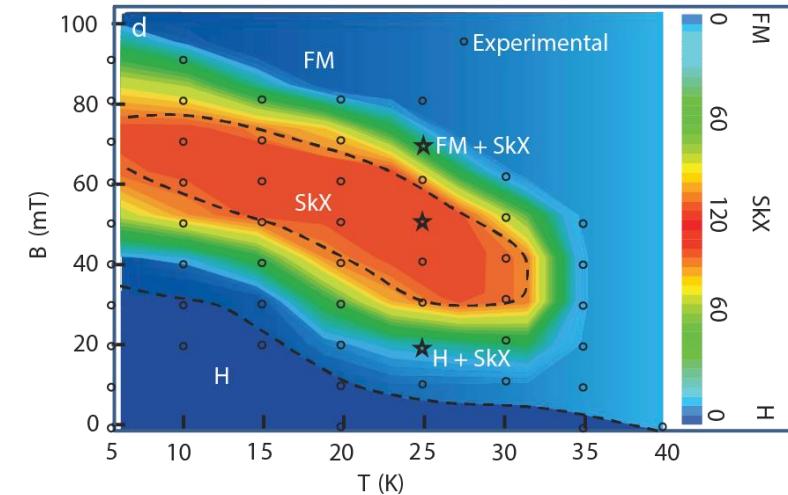
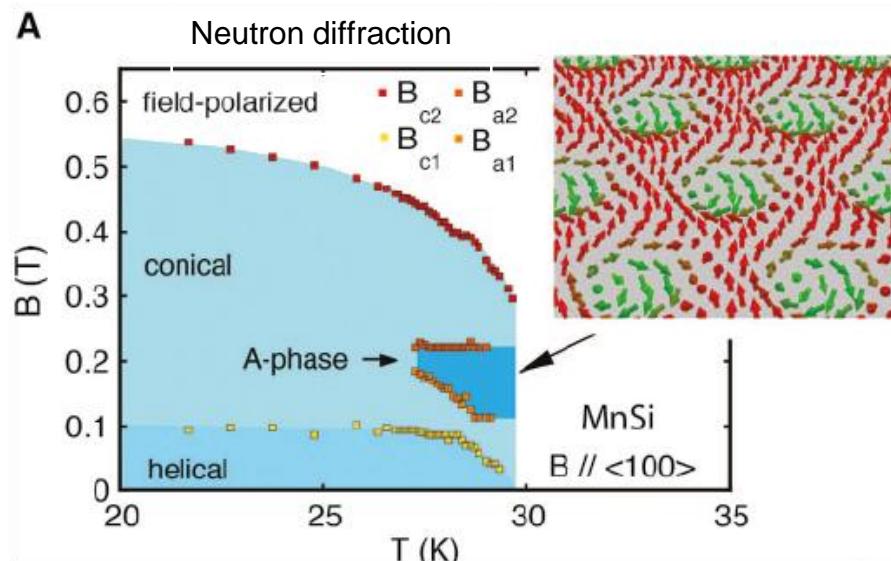
A. N. Bogdanov & D. A. Yablonskii, Sov. Phys. JETP **68**, 101 (1989)



Lorentz TEM



Experimental discovery



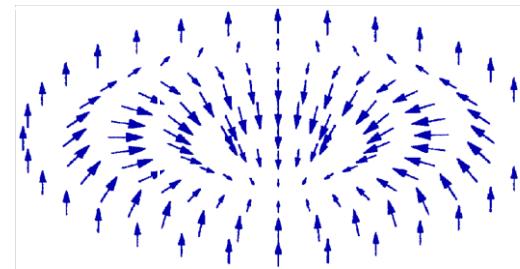
S. Mühlbauer *et al.*, Science **323**, 915 (2009)
A. Neubauer *et al.*, PRL **102**, 186602 (2009)

X. Z. Yu *et al.*, Nature **465**, 901 (2010)
M. Lee *et al.*, PRL **102**, 186601 (2009)

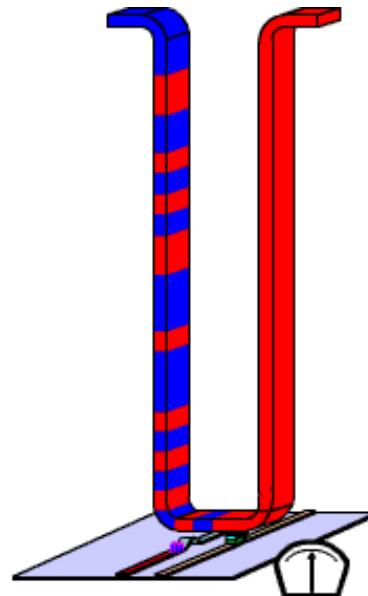
Skyrmins in bulk magnetic materials

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A. N. Bogdanov & D. A. Yablonskii, Sov. Phys. JETP **68**, 101 (1989)



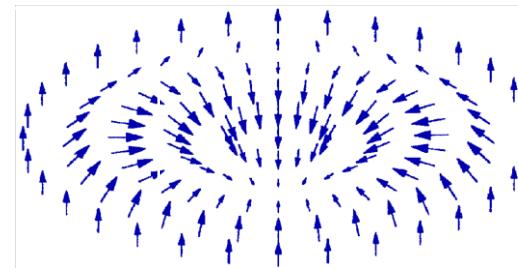
race-track

S. Parkin et al., Science **320**, 190 (2008)

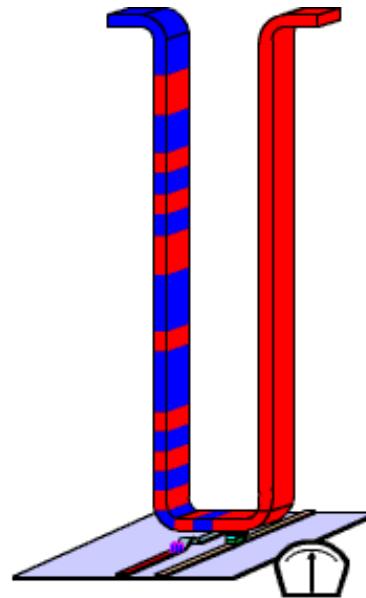
Skyrmins in bulk magnetic materials

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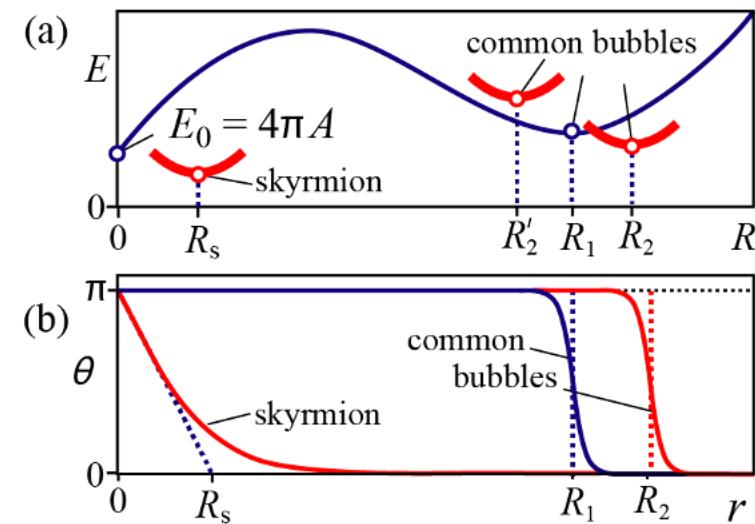
Existence of magnetic skyrmions
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A. N. Bogdanov & D. A. Yablonskii, Sov. Phys. JETP **68**, 101 (1989)



Skyrmion race-track



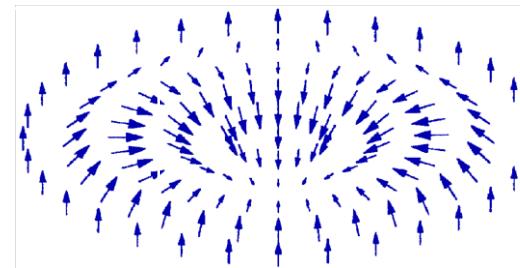
S. Parkin *et al.*, Science **320**, 190 (2008)
A. Fert *et al.*, Nature Nanotech. **8**, 152 (2013)
W. Jiang *et al.*, Science **349**, 283 (2015)
K. Litzius *et al.*, Nature Phys. **13**, 170 (2016)

N. S. Kiselev *et al.*, J. Phys D **44**, 39201 (2011)

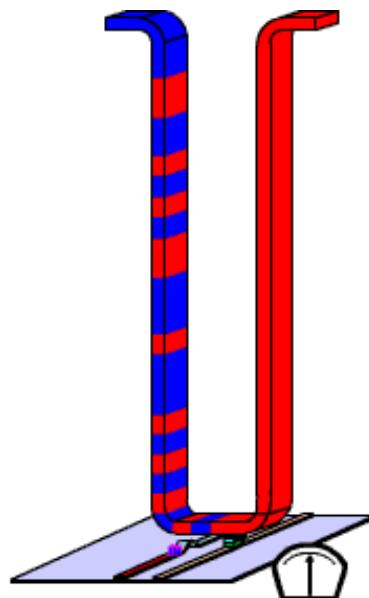
Skyrmins in bulk magnetic materials

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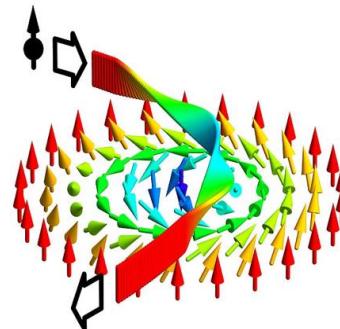
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A. N. Bogdanov & D. A. Yablonskii, Sov. Phys. JETP **68**, 101 (1989)



Skyrmion race-track

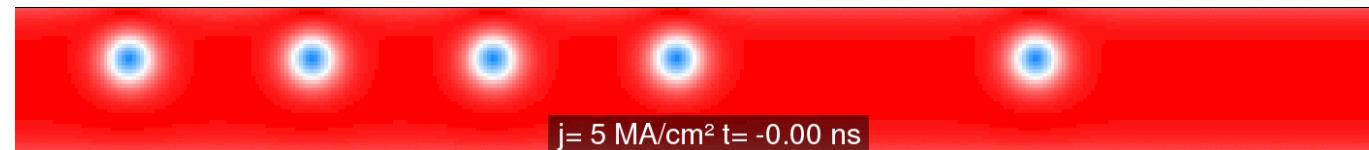


$$\mathbf{F}_{\sigma k} = e\mathbf{E} + \mathbf{F}_H + q_{\sigma}^e \cdot \mathbf{v}_k \times \mathbf{B}^e$$

$$\mathbf{B}^e = \frac{\hbar}{2} \mathbf{n} (\nabla_x \mathbf{n} \times \nabla_y \mathbf{n})$$

$$\mathbf{E} = \hbar \mathbf{n} (\nabla_r \mathbf{n} \times \nabla_t \mathbf{n})$$

T. Schulz et al., Nature Physics **8**, 301 (2012)



S. Parkin et al., Science **320**, 190 (2008)
A. Fert et al., Nature Nanotech. **8**, 152 (2013)
W. Jiang et al., Science **349**, 283 (2015)
K. Litzius et al., Nature Phys. **13**, 170 (2016)

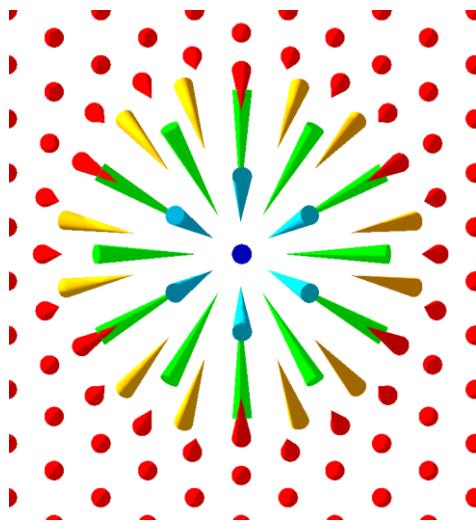
Skyrmions and topological charge

Skyrmion number (topological charge) of a vector field $\mathbf{n}(x,y)$:

$$S = \frac{1}{4\pi} \int \mathbf{n} \cdot (\nabla_x \mathbf{n} \times \nabla_y \mathbf{n}) dA$$

Ferromagnet ($S=0$): topologically trivial state

Skyrmion ($S=+1$)



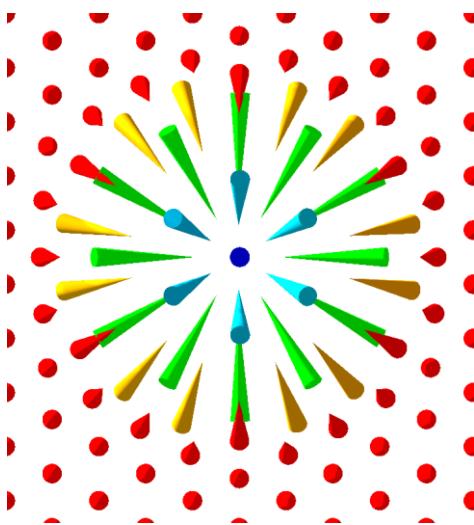
Skyrmions and topological charge

Skyrmion number (topological charge) of a vector field $\mathbf{n}(x,y)$:

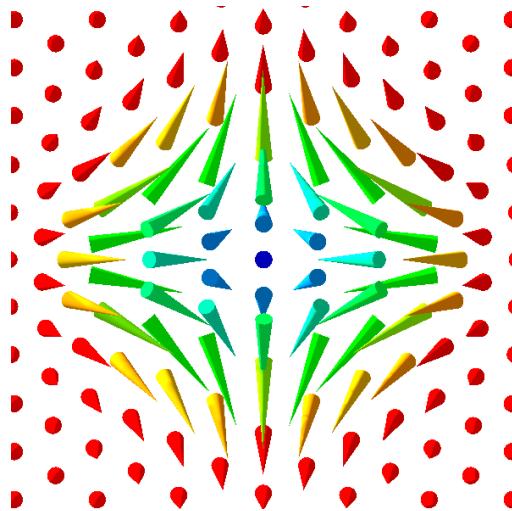
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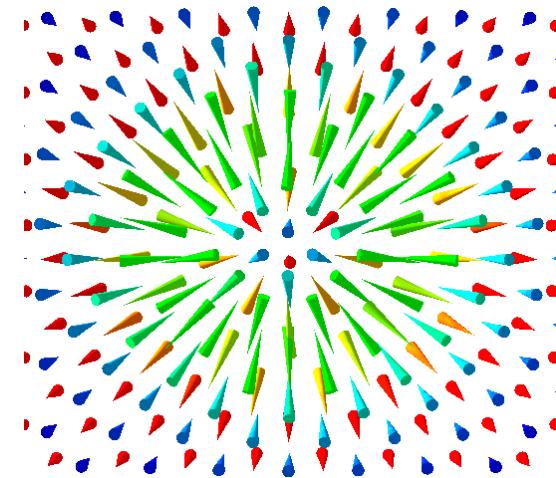
Skyrmion ($S=+1$)



Antiskyrmion ($S=-1$)



Skyrmion AFM ($S=+1$)

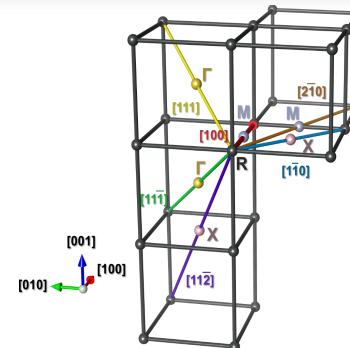
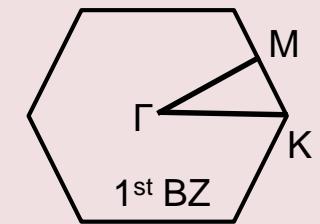
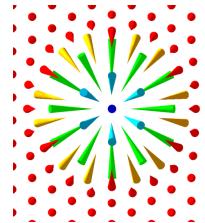


- L. Camosi *et al.*, Phys. Rev. B **95**, 214422 (2017)
M. Hoffmann *et al.*, Nature Commun. **8**, 308 (2017)
A. Nayak *et al.*, Nature **548**, 561 (2017)

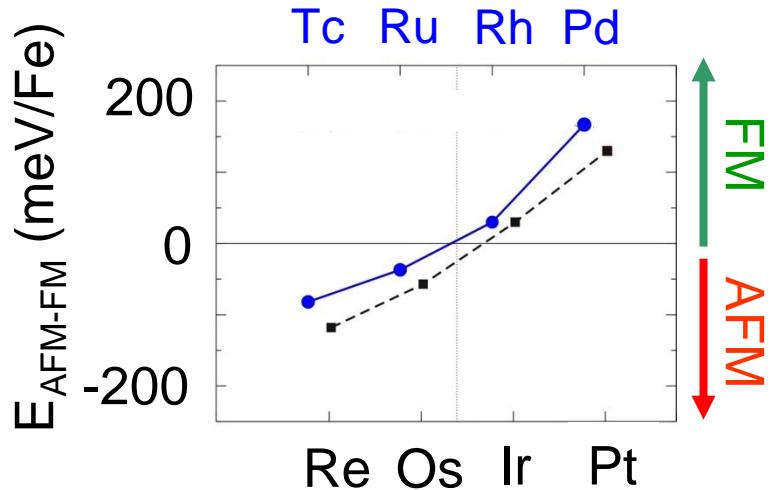
- J. Barker *et al.*, Phys. Rev. Lett. **116**, 147203 (2016)
S. Meyer *et al.*, Phys. Rev. B **96**, 094408 (2017)
W. Legrand *et al.*, Nat. Materials (2019)
T. Dohi *et al.*, Nat. Commun (2019)
L. Desplat *et al.*, Phys. Rev. B **104**, L060409 (2021)

Outline

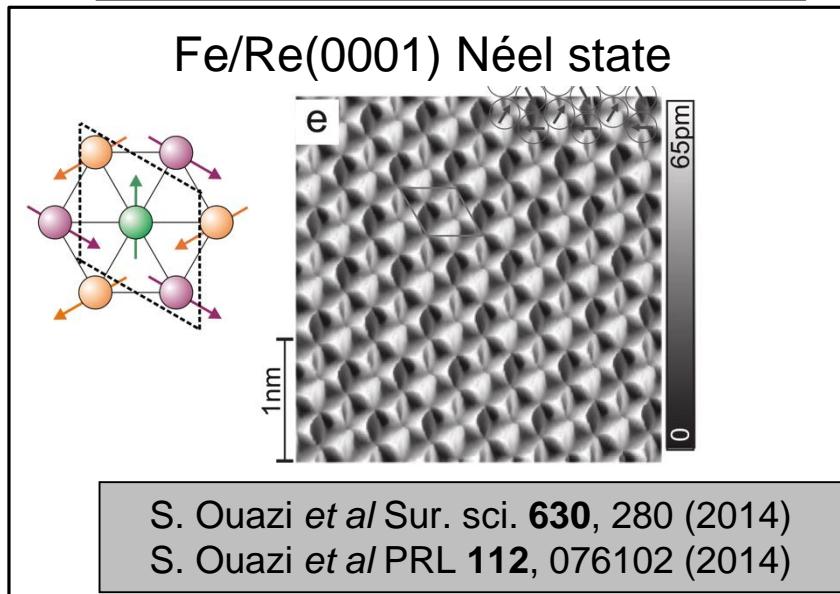
- Introduction on magnetic skyrmions
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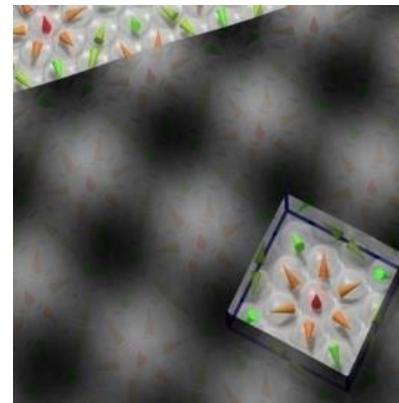
Tuning the magnetic exchange interaction in Fe monolayer



B. Hardrat et al PRB **79**, 094411 (2009)

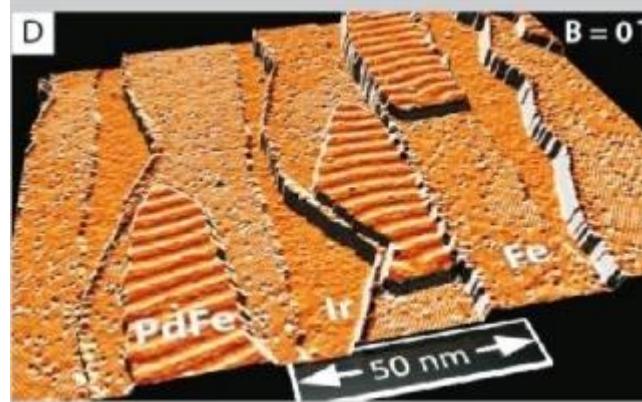


Fe/Ir(111): nano-skyrmion lattice



S. Heinze et al Nat. Phys. **7**, 713 (2011)

Pd/Fe/Ir(111) spin spiral ground state



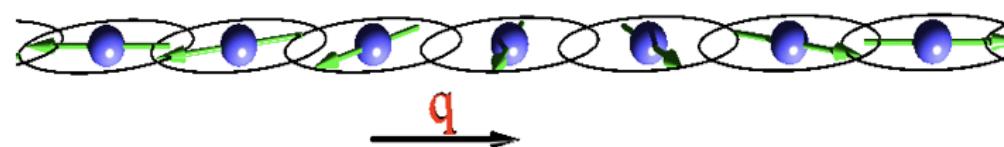
N. Romming et al Science **341**, 636 (2013)
B. Dupé et al Nature Comm. **5**, 4030 (2014)

Spin spiral energy calculation

Density-functional theory (DFT) using the FLEUR code:

- energy of non-collinear magnetic structures
- energies of spiral spin-density waves

Spin spirals



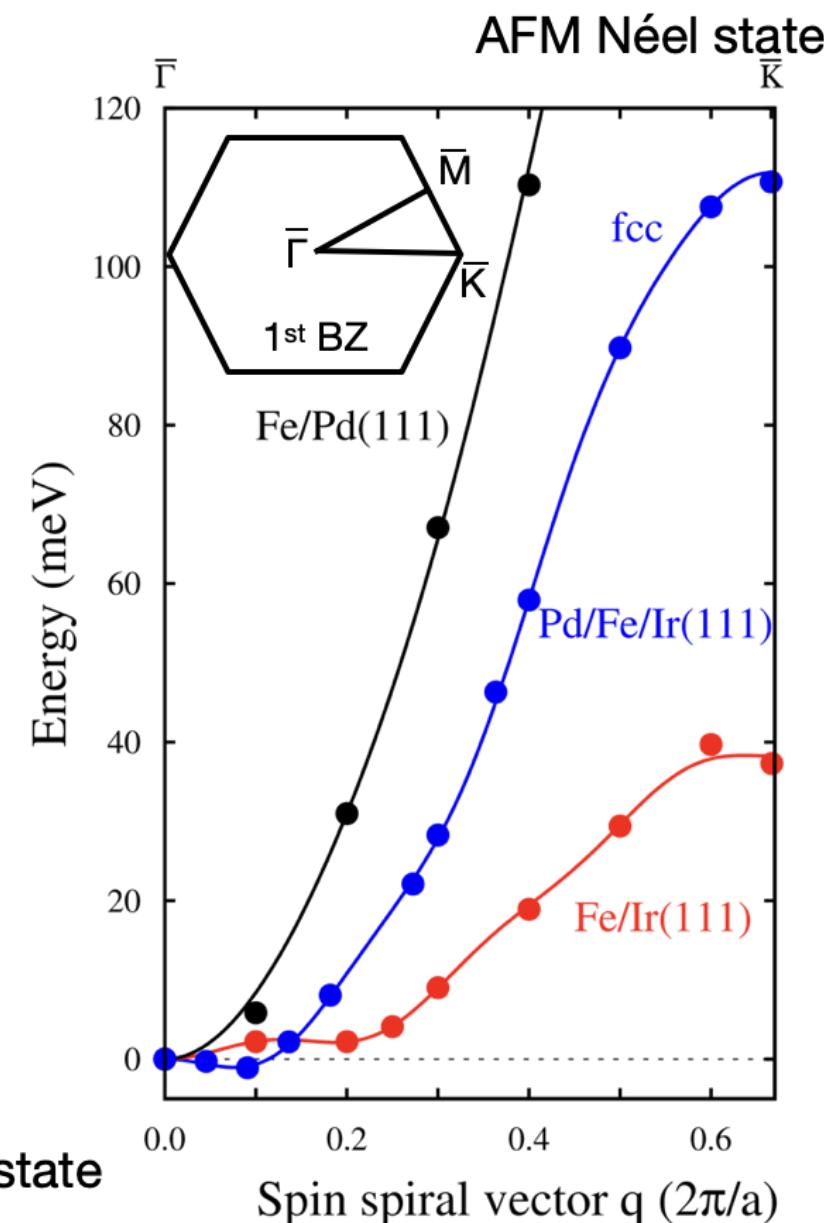
$$E(\mathbf{q}) = -N \sum_{\delta} J_{0,\delta} e^{-i\mathbf{R}_{\delta}\mathbf{q}}$$



developed @ FZ Jülich

Bertrand Dupé

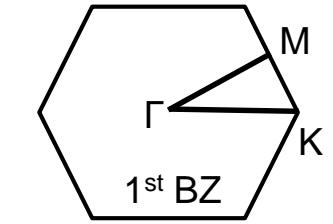
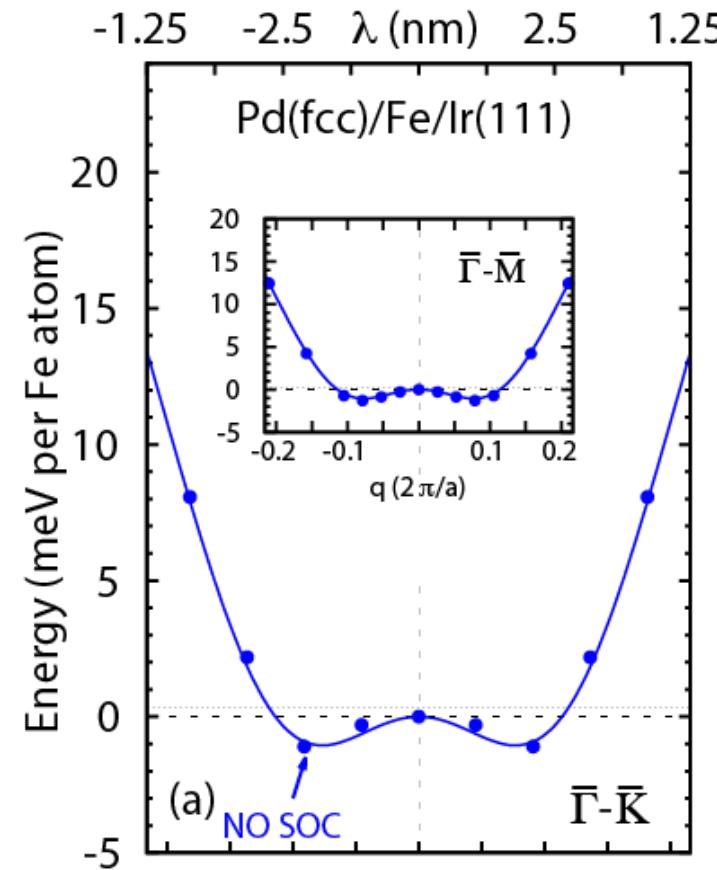
FM state



Heisenberg Hamiltonian parametrization Pd/Fe/Ir(111)

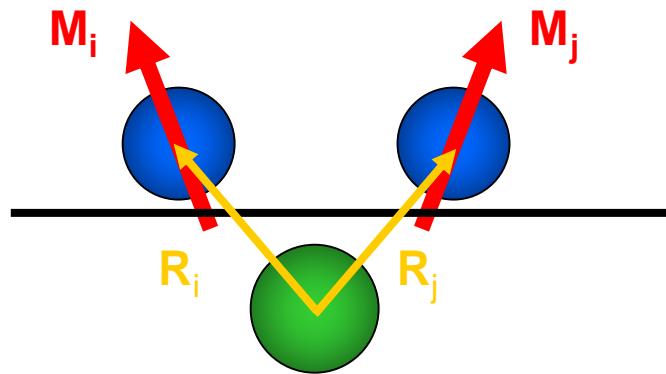
Spin Hamiltonian

$$H = - \sum_{i,j} \mathbf{M}_i \textcolor{teal}{J}_{ij} \mathbf{M}_j$$



Origin of the DM interaction at metal surface

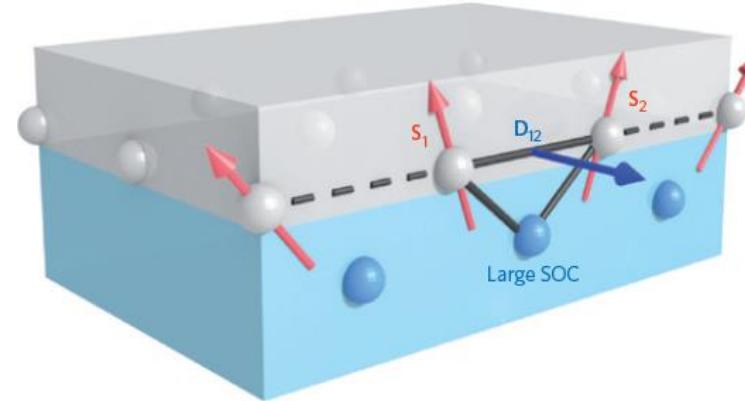
Interaction of two magnetic atoms via a surface atom with strong spin-orbit coupling



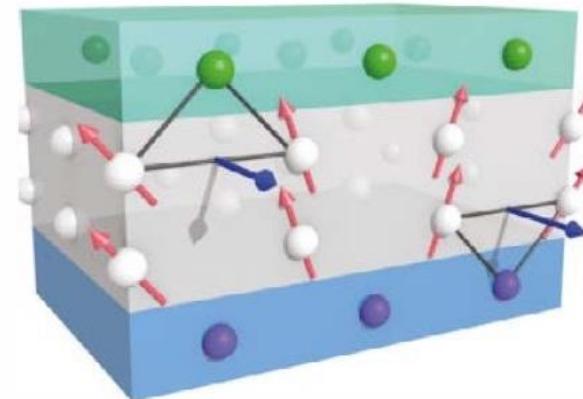
$$H_{DM} \propto -V(\xi)(\mathbf{R}_i \times \mathbf{R}_j)(\mathbf{M}_i \times \mathbf{M}_j)$$

$$H_{DM} \propto -\mathbf{D}_{ij}(\mathbf{M}_i \times \mathbf{M}_j)$$

Levy & Fert, Phys. Rev Lett. **44**, 1538 (1980)



J. Sampaio *et al.*, Nature Nanotech. **8**, 839 (2013)
O. Boule *et al.*, Nature Nanotech. **5**, 449 (2016)



C. Moreau-Luchaire *et al.*, Nature Nanotech. **11**, 444 (2016)

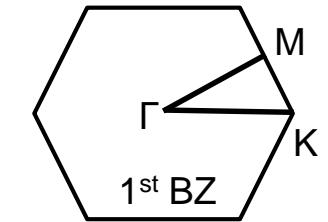
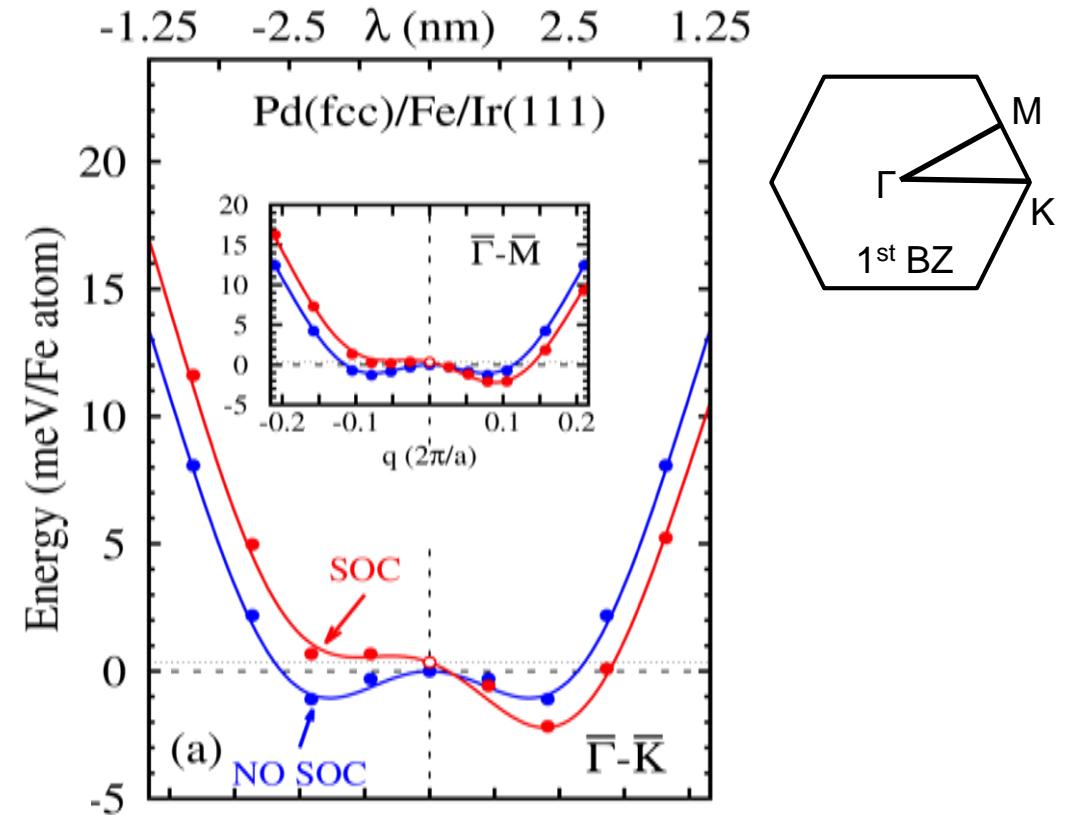
Heisenberg Hamiltonian parametrization: DMI

Spin Hamiltonian

$$H = - \sum_{i,j} \mathbf{M}_i \textcolor{teal}{J}_{ij} \mathbf{M}_j$$

$$- \sum_i \textcolor{red}{K} M_z^2$$

$$- \sum_{i,j} \mathbf{D}_{ij} \cdot (\mathbf{M}_i \times \mathbf{M}_j)$$



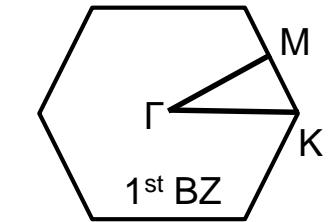
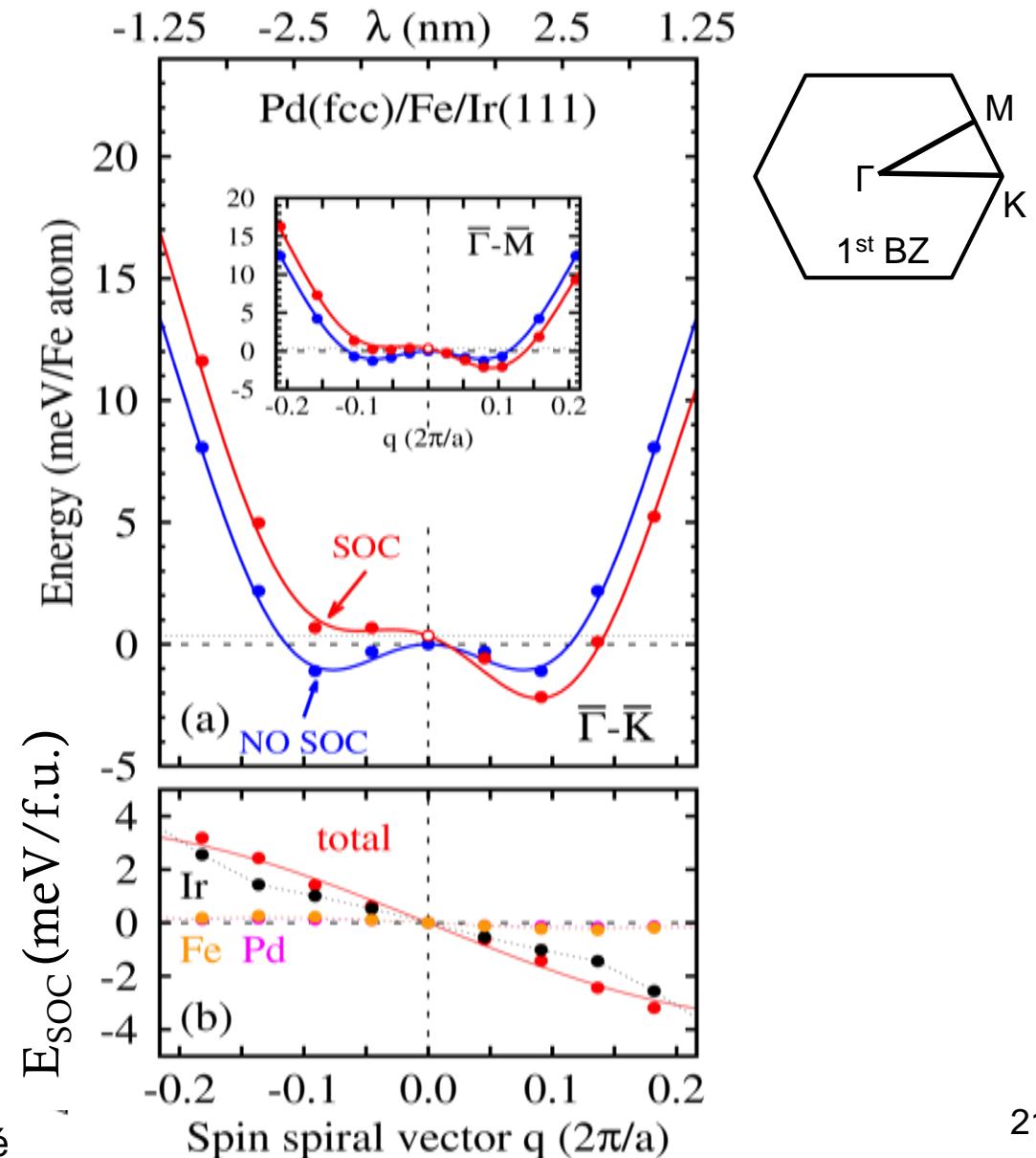
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$$- \sum_{i,j} \mathbf{D}_{ij} \cdot (\mathbf{M}_i \times \mathbf{M}_j)$$



Heisenberg Hamiltonian parametrization

Spin Hamiltonian solved by Monte-Carlo & spin dynamics

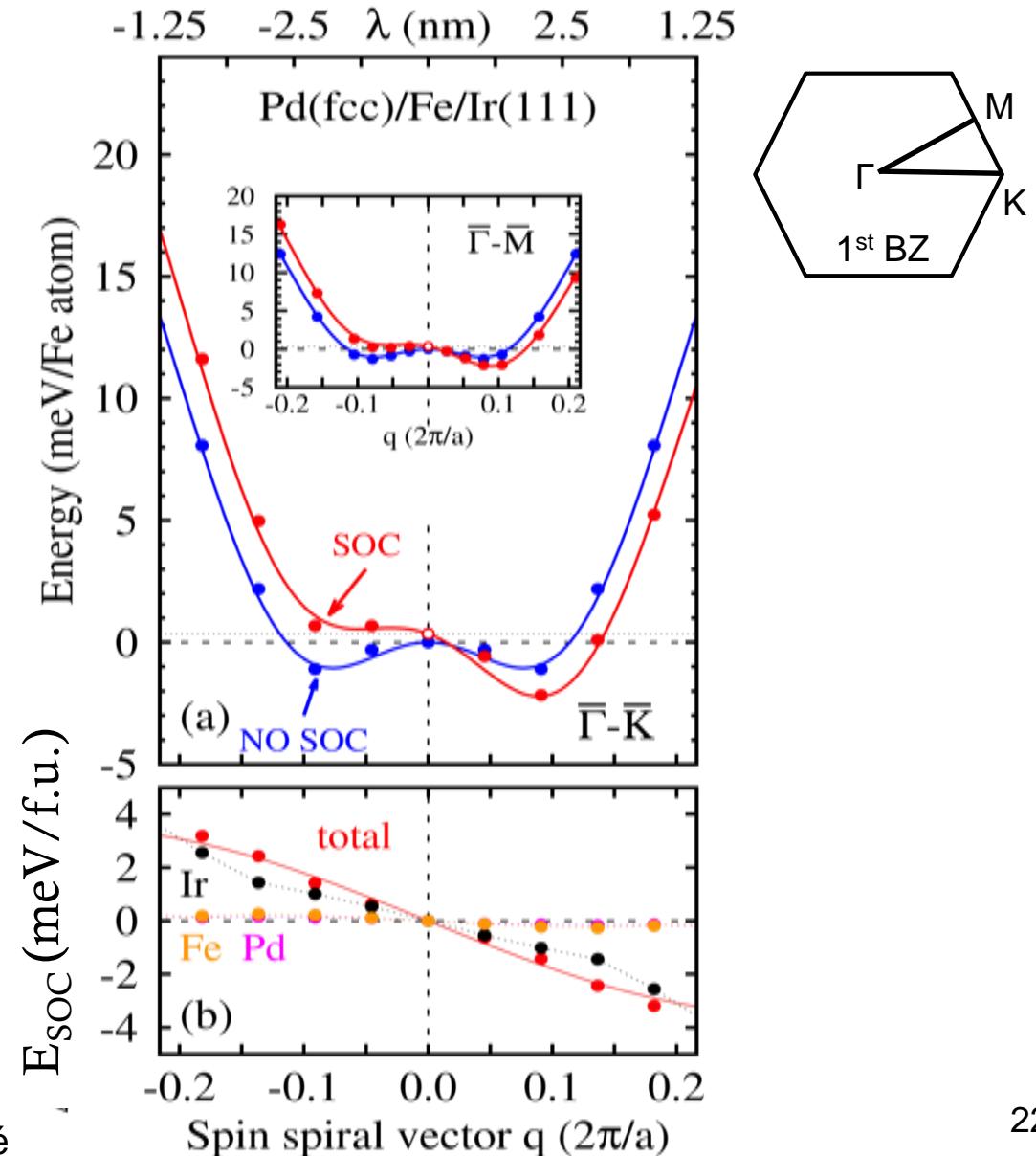
$$H = - \sum_{i,j} \mathbf{M}_i \textcolor{teal}{J}_{ij} \mathbf{M}_j$$

$$- \sum_i \textcolor{red}{K} M_z^2$$

$$- \sum_{i,j} \mathbf{D}_{ij} \cdot (\mathbf{M}_i \times \mathbf{M}_j)$$

$$- \sum_i \mathbf{M}_i \mathbf{B}$$

$$- \sum_{i,j} B_{ij} (\mathbf{M}_i \cdot \mathbf{M}_j)^2 + 4\text{spin}$$

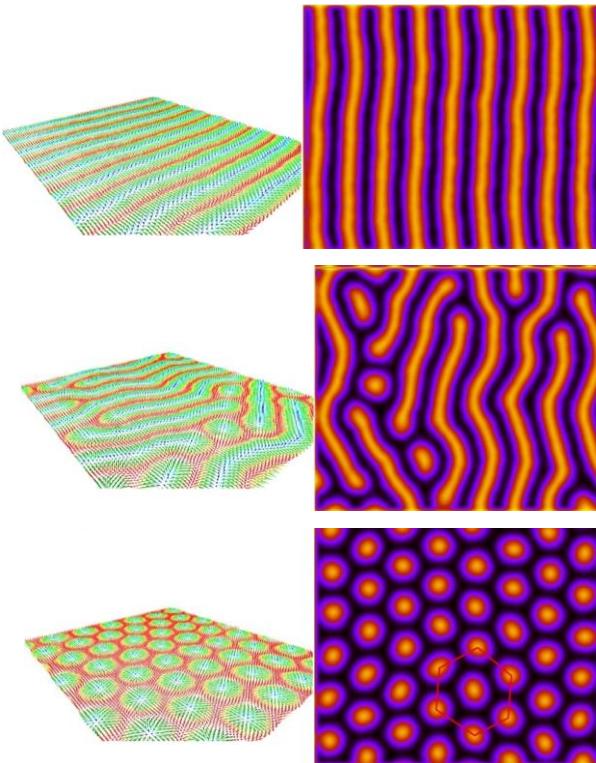


Phase diagram of Pd/Fe(fcc)/Ir(111) at 0K

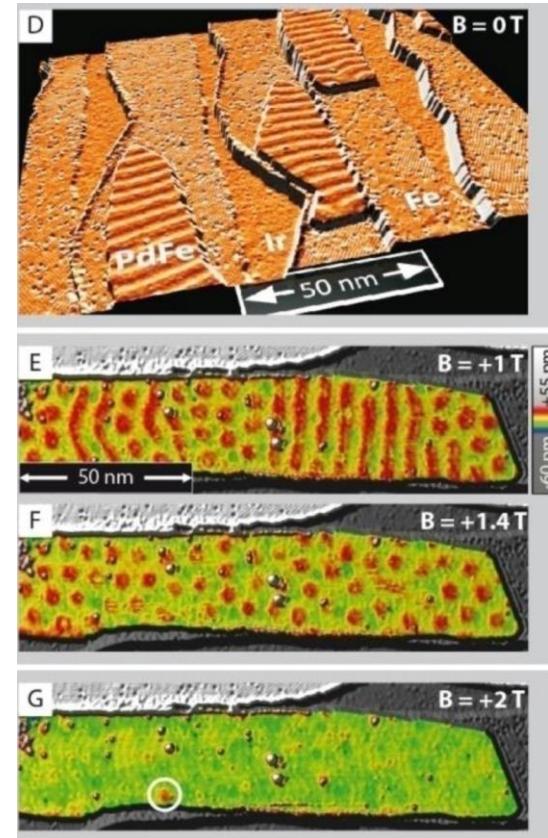
Spin spiral pitch from Monte Carlo: 5.4nm

Monte-Carlo
Simulation

B



Experiments

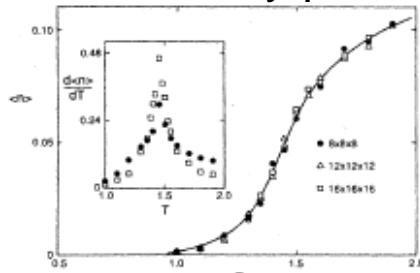


B. Dupé *et al* Nature Commun. **5**, 4030 (2014)
E. Simon *et al* Phys. Rev. B **90**, 094410 (2014)

N. Romming *et al* Science **341**, 636 (2013)
N. Romming *et al* Phys. Rev. Lett. **114**,
177203 (2015)

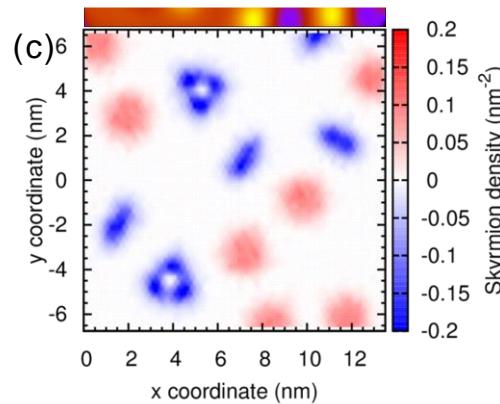
Phase diagram of Pd/Fe(fcc)/Ir(111)

Creation of skyrmion/antiskyrmion density pairs



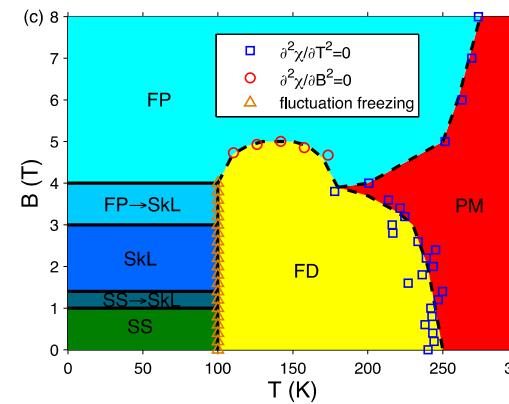
M. Lau *et al.*, Phys Rev B **39**, 7212 (1989)
Y. Nahas *et al.*, Phys. Rev. Lett. **119**, 117601 (2017)

Integrated skyrmion density is no order parameter



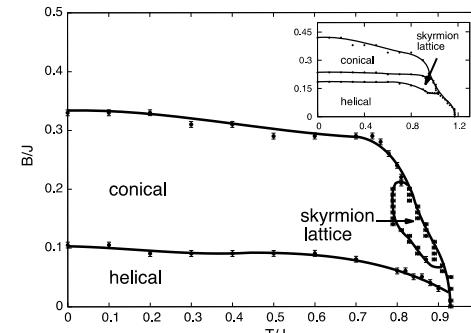
B. Dupé *et al.*, New J. Phys **18**, 055015 (2016)

Pd/Fe/Ir(111)



L. Rosza *et al.*, PRB **93**, 024417 (2016)

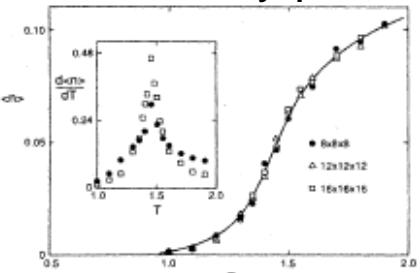
MnSi



S. Bürhanndt *et al.*, PRB **88**, 195137 (2013)

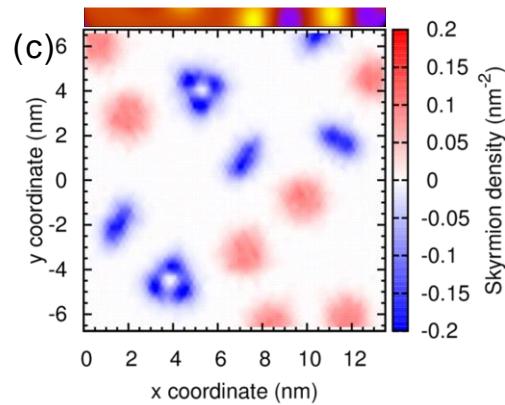
Phase diagram of Pd/Fe(fcc)/Ir(111)

Creation of skyrmion/antiskyrmion density pairs



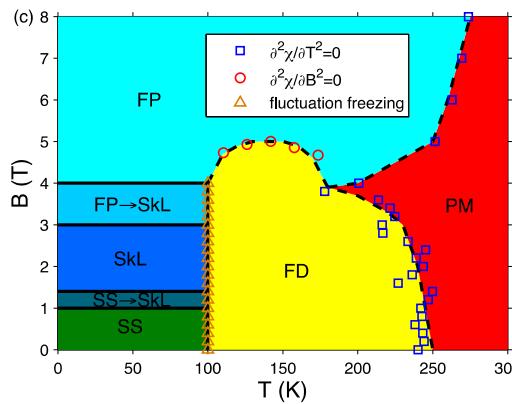
M. Lau et al., Phys Rev B 39, 7212 (1989)
Y. Nahas et al., Phys. Rev. Lett. 119, 117601 (2017)

Integrated skyrmion density is no order parameter



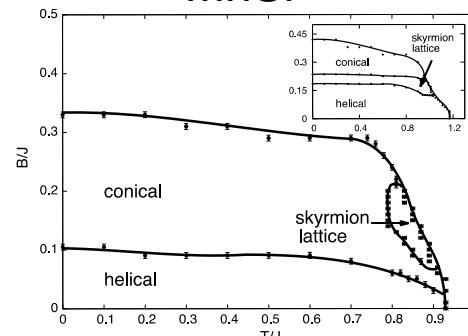
B. Dupé et al., New J. Phys 18, 055015 (2016)

Pd/Fe/Ir(111)



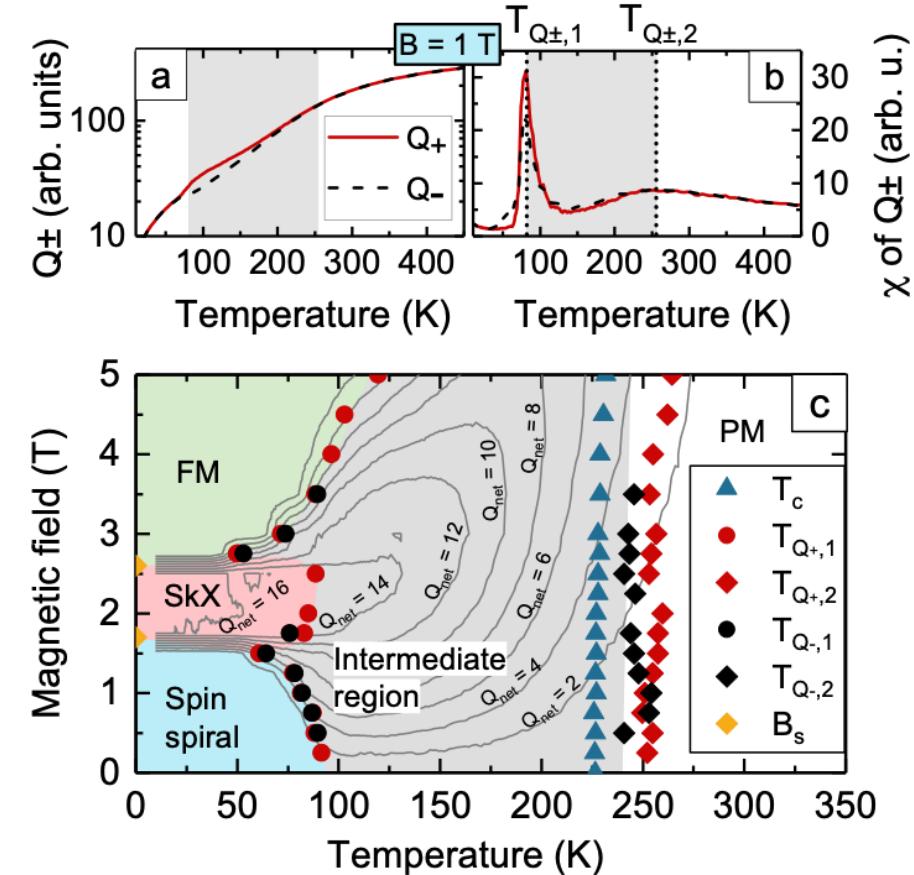
L. Rosza et al., PRB 93, 024417 (2016)

MnSi



S. Bürhardt et al., PRB 88, 195137 (2013)

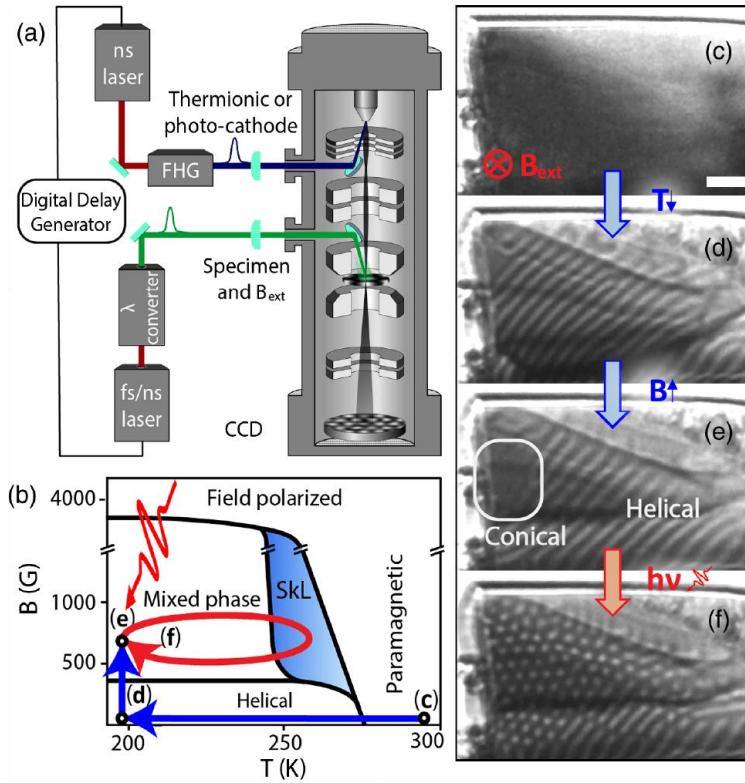
Parallel tempering Monte Carlo



M. Böttcher et al., New Journ. Phys. 20, 103014 (2018)

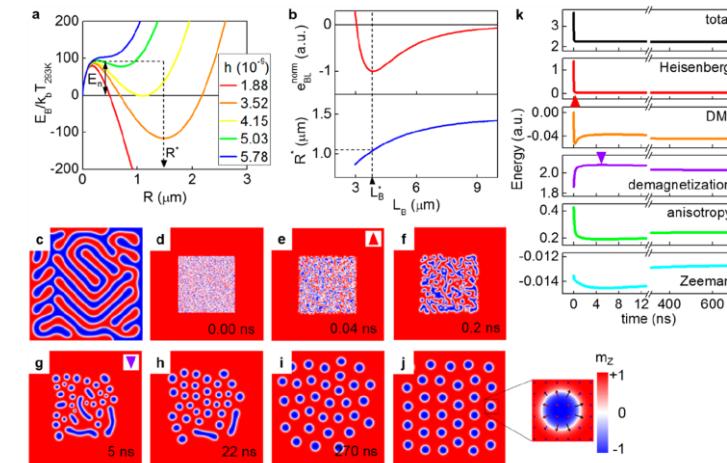
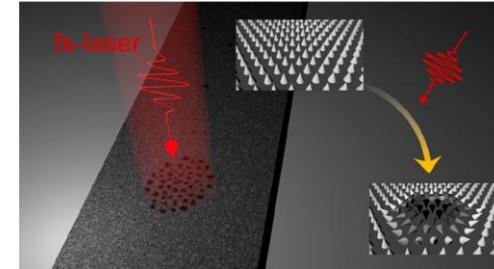
Temperature skyrmion-antiskyrmion generation

FeGe



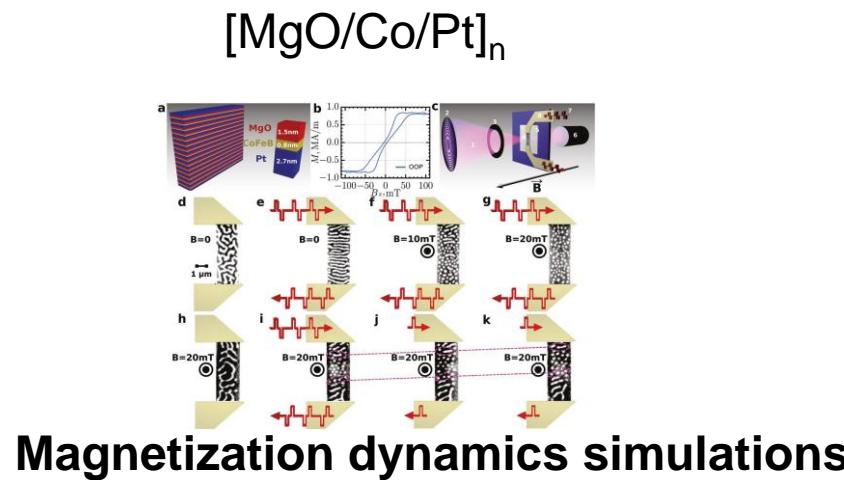
G. Berruto *et al.* Phys. Rev. Lett. **120**, 117201 (2018)

TaO_x/CoFeB/Ta

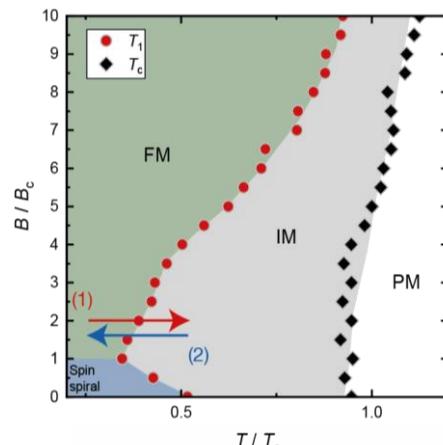


S.-G. Je *et al.* NanoLetters **18**, 7362 (2018)

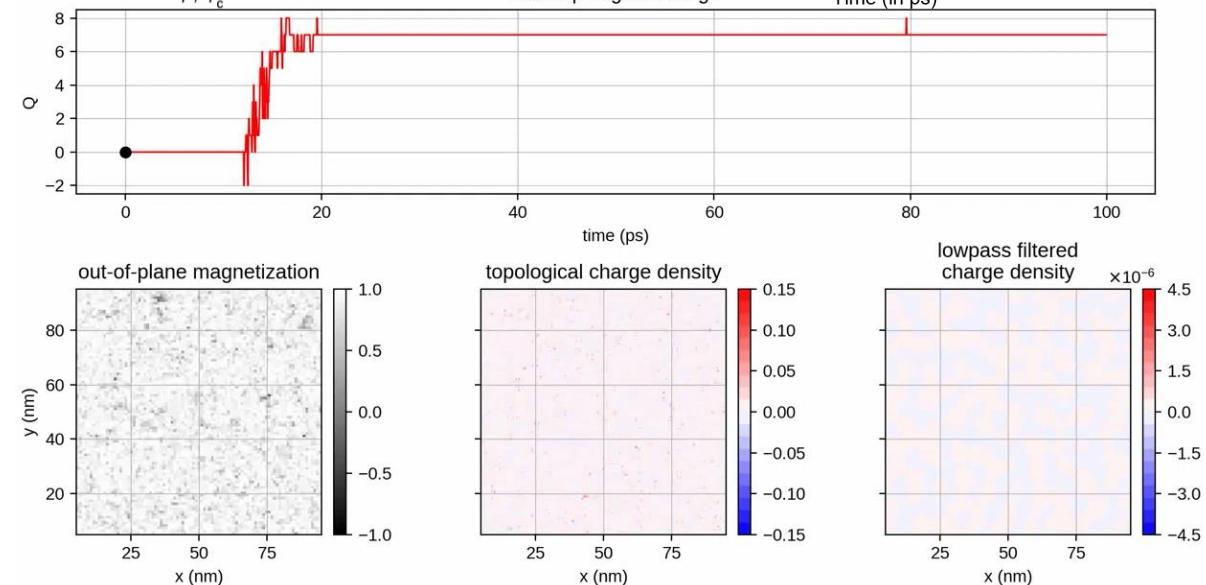
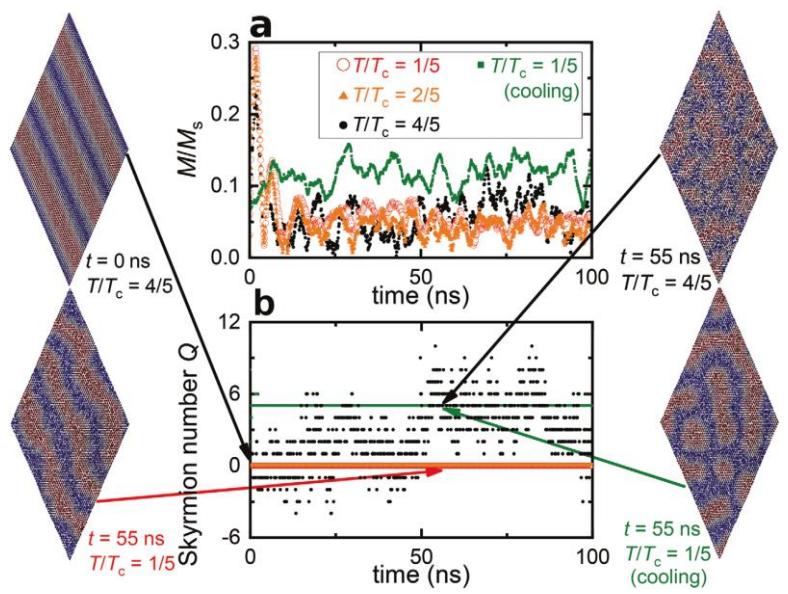
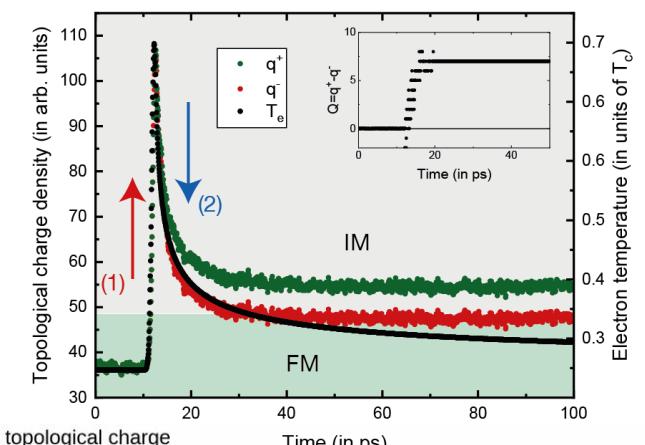
Temperature skyrmion-antiskyrmion generation



Phase diagram of $[\text{MgO}/\text{Co}/\text{Pt}]_n$



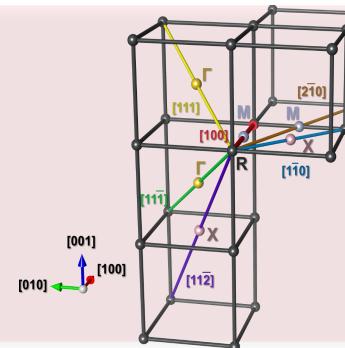
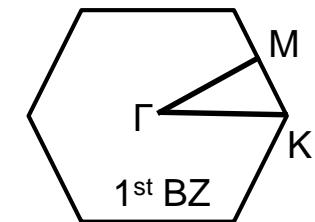
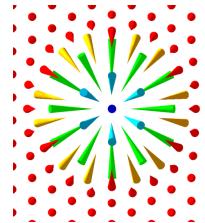
electron temperature



I. Lemesh, BD et al., Advanced Materials **30**, 1805461 (2018)
F. Büttner et al., Nature Mater. **20**, 30 (2021)

Outline

- Introduction on magnetic skyrmions
 - The discovery
 - The racetrack memory
 - Topology and stability
- The different magnetic interactions
 - Origin of the DM interaction
 - Obtaining magnetic interactions from density functional theory
 - Some examples of use
- Isolated skyrmions in Multiferroics
 - BiFeO₃ (BFO) as a good playground
 - Determining the magnetic interactions in BFO
 - Using strain to tune the interactions in BFO



Order parameters of BiFeO₃

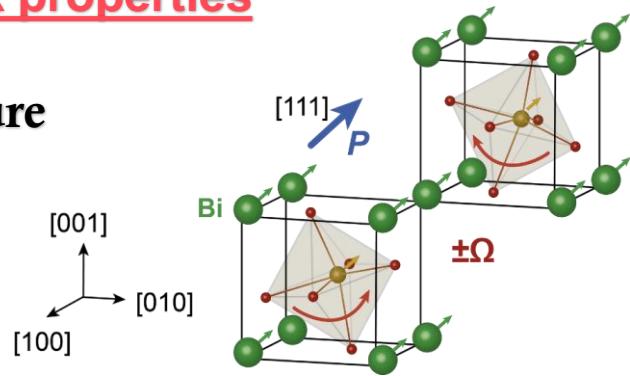
Bulk properties

1. Perovskite structure

Bi Cations

Fe Cations

O Anions



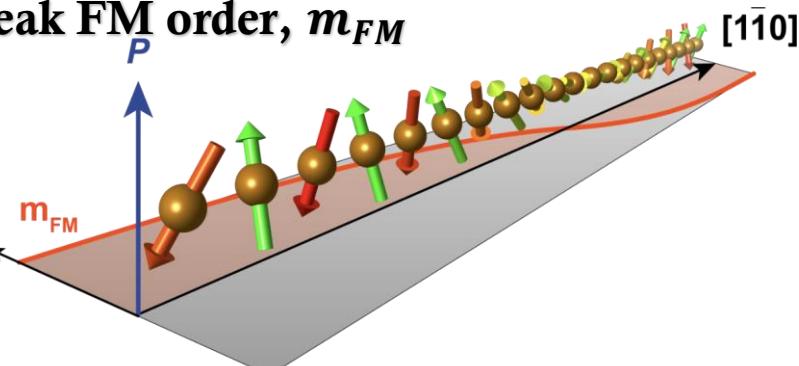
2. Fe-Bi displacement

Polarization along [111] direction

$$P \approx \frac{90 \mu\text{C}}{\text{cm}^2}, T_c = 1123 \text{ K}$$

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4. Local antiferromagnetic order with long-ranged spin cycloid, $\lambda \approx 62 \text{ nm}$ + weak FM order, m_{FM}



Order parameters of BiFeO₃

Bulk properties

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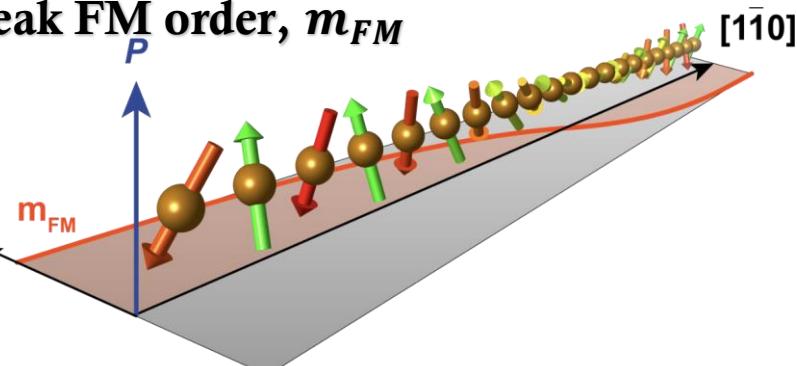


2. Fe-Pol

Investigation of different spin cycloids

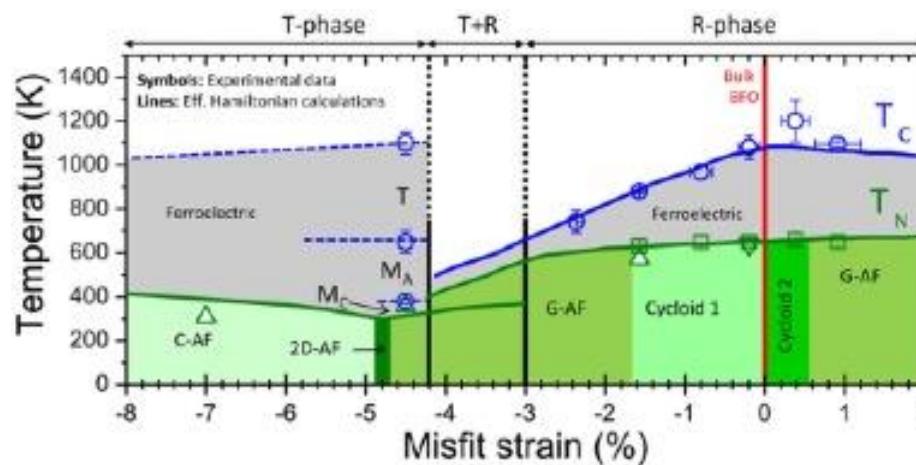
3. Oxygen tilt in antiphase $\pm\Omega$

4. Local antiferromagnetic order with long-ranged spin cycloid, $\lambda \approx 62$ nm + weak FM order, m_{FM}



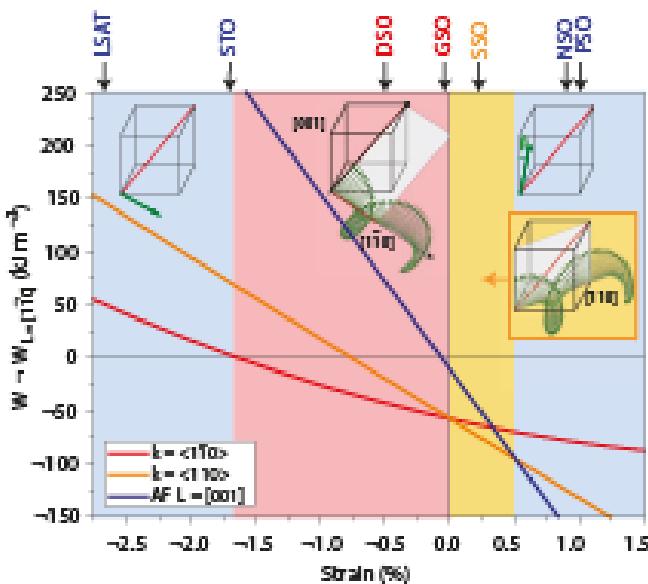
Magnetic properties and orders in BFO

Computed phase diagram from effective Hamiltonian



D.Sando. et al., J. Phys.: Condens. Matter **26**, 473201 (2014)

Spin spirals from experiments



D. Sando, et al., Nature Mater. **12**, 641-646 (2013)

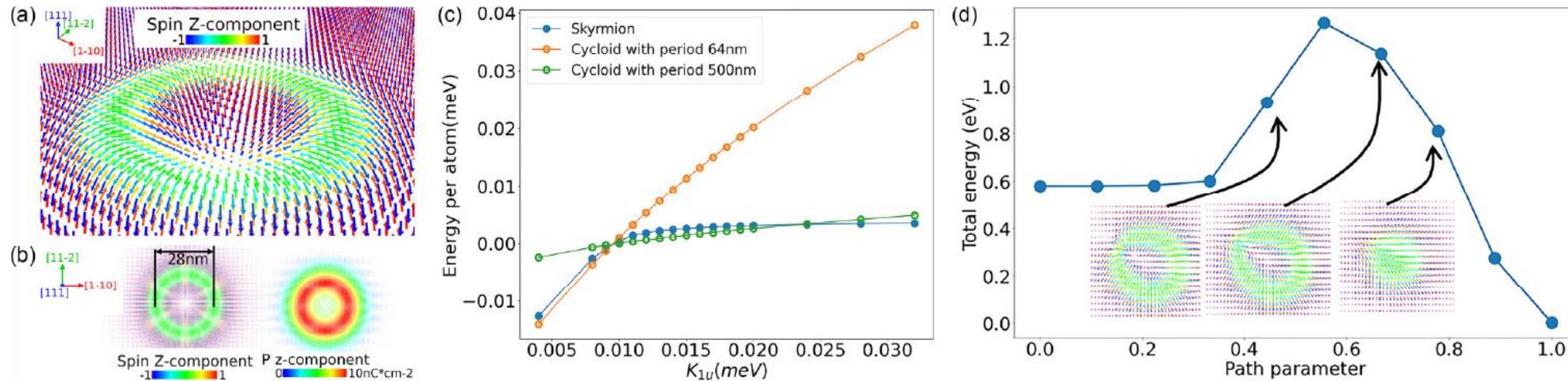
Experimental based Hamiltonian

Heisenberg Hamiltonian obtained from Neutron diffraction
Easy axis anisotropy

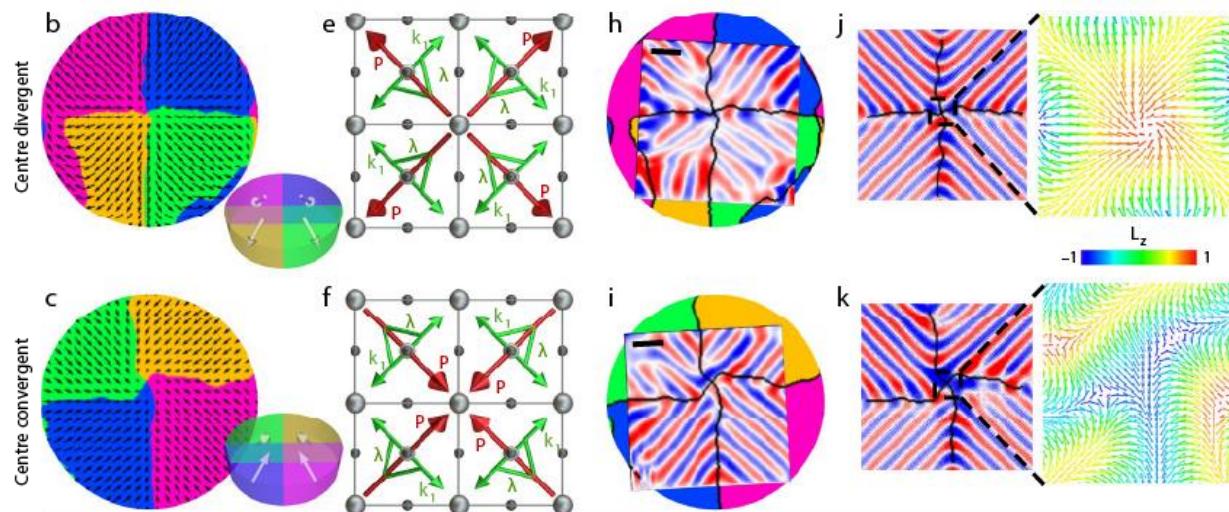
C. Weingart, et al., Phys. Rev. B **86**, 094413 (2012)
R. Fishman, Phys. Rev. B **87**, 134416 (2013)

Topological textures in BFO

Stable Skyrmion in BFO with imposed out-of-plane anisotropy



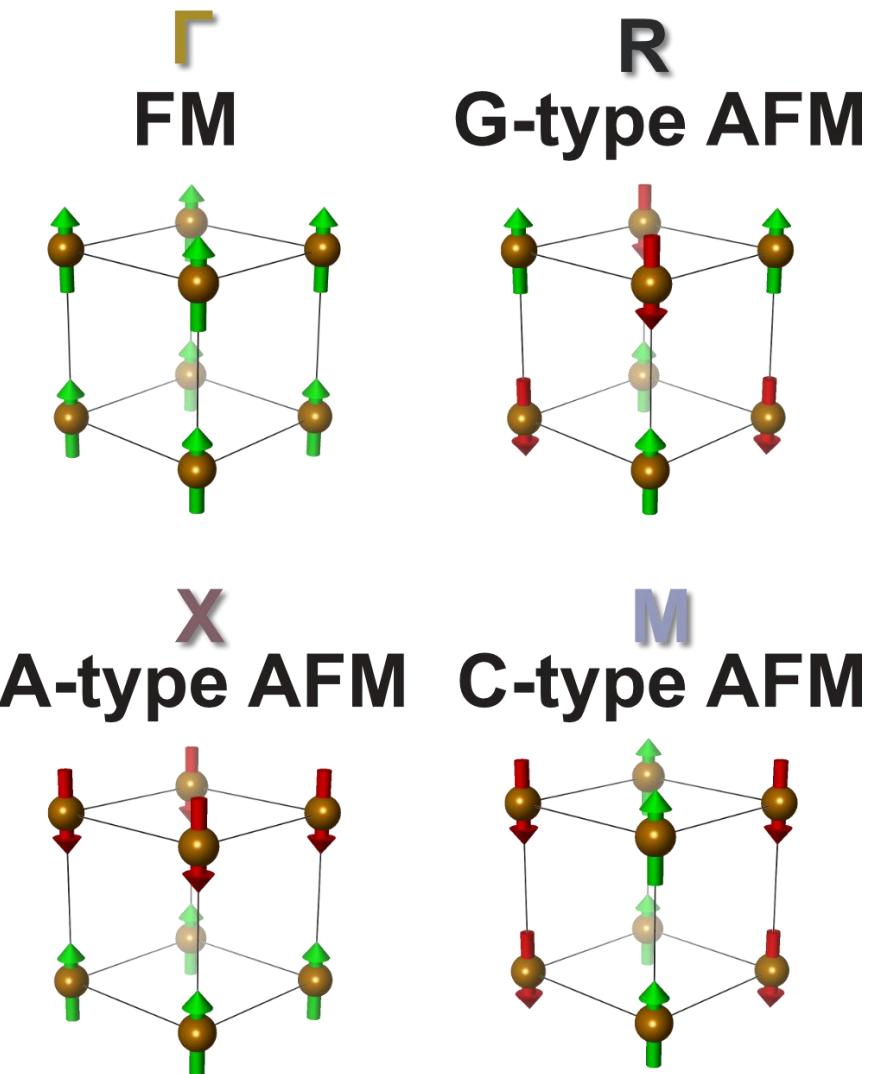
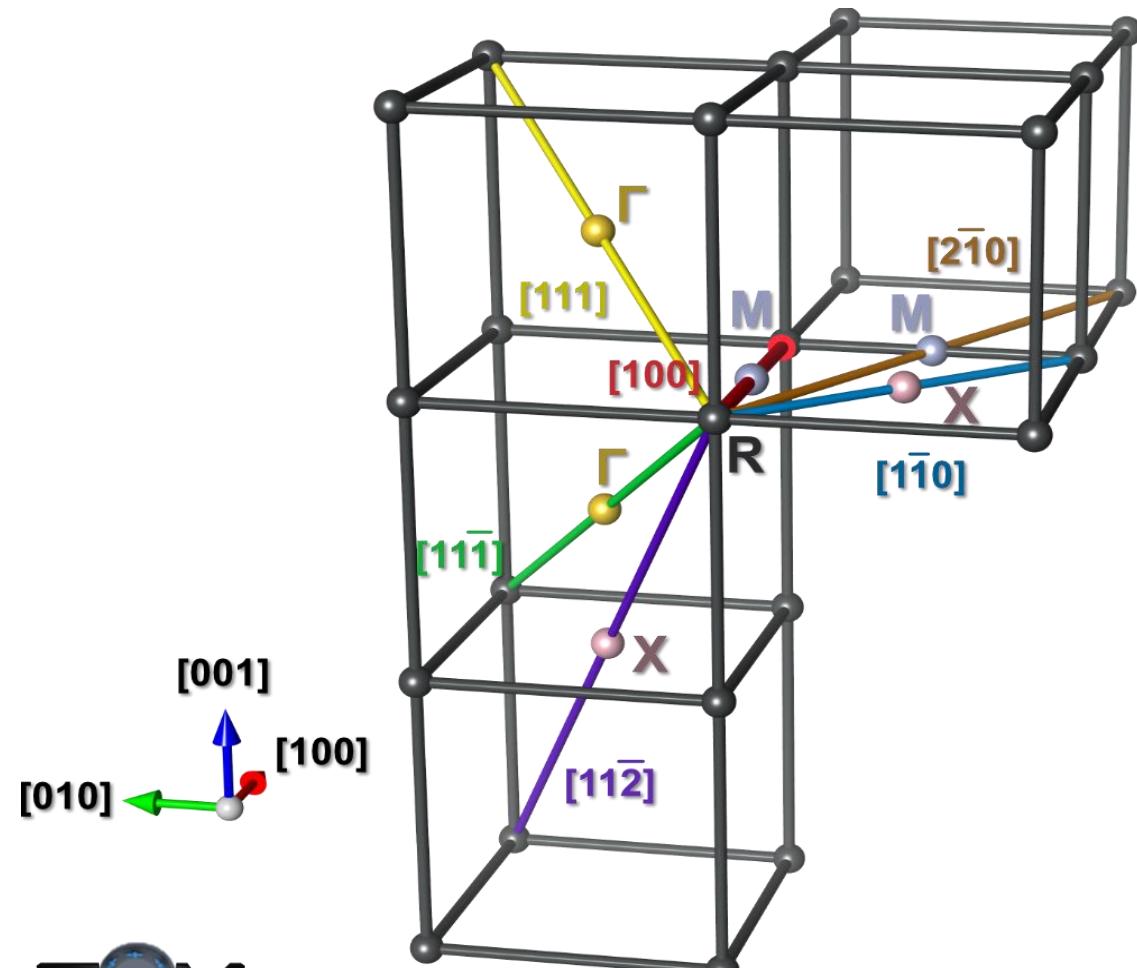
Experimental observation of a skyrmion embedded in a spin spiral ground state



Z. Li, et al., Phys. Rev. Research 5, 043109 (2023)
A. Chaudron et al., Nat. Matter 23, 905-911 (2024)

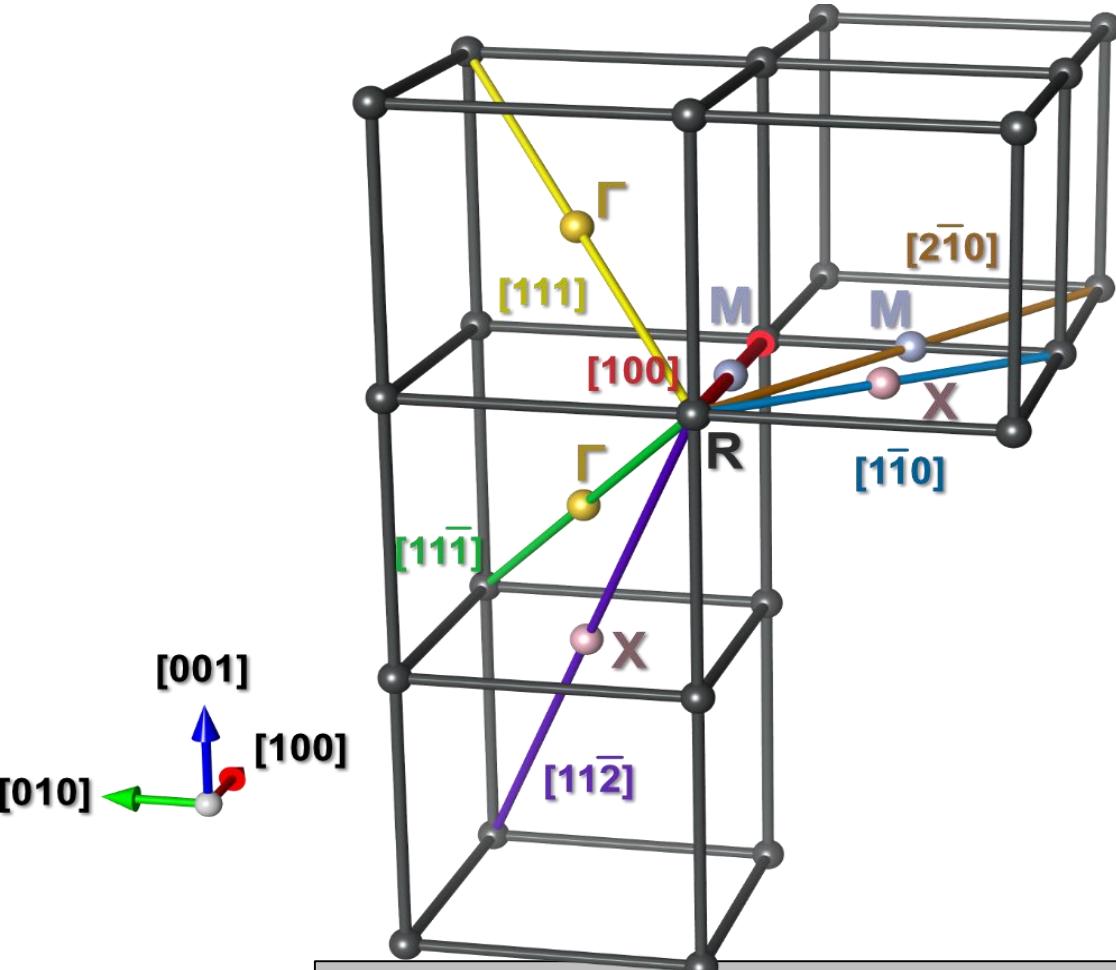
Brillouin zone and high symmetry points of BFO

Detailed path of the q-vector



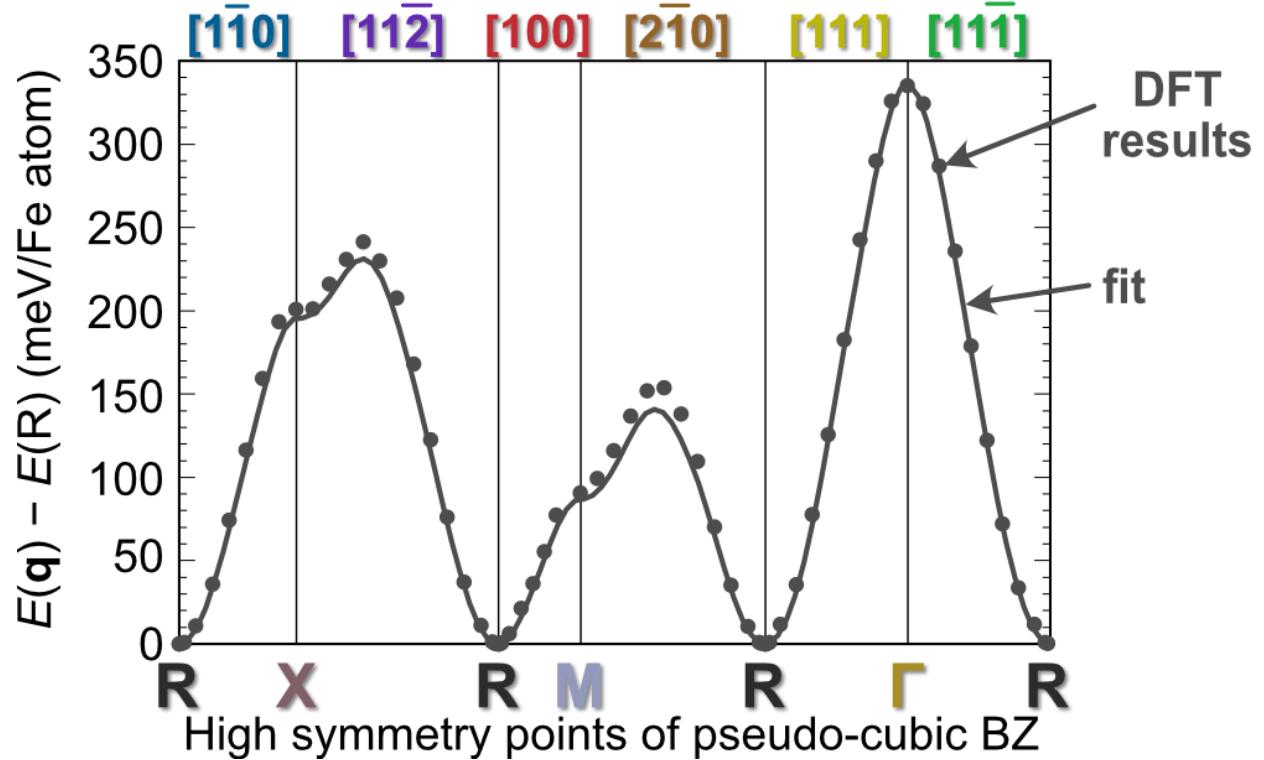
Spin spiral energy calculation in BFO

Detailed path of the q-vector



B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
S. Meyer, et al., Phys. Rev. B **108**, 024403 (2023)

Directions within the pseudo-cubic BZ



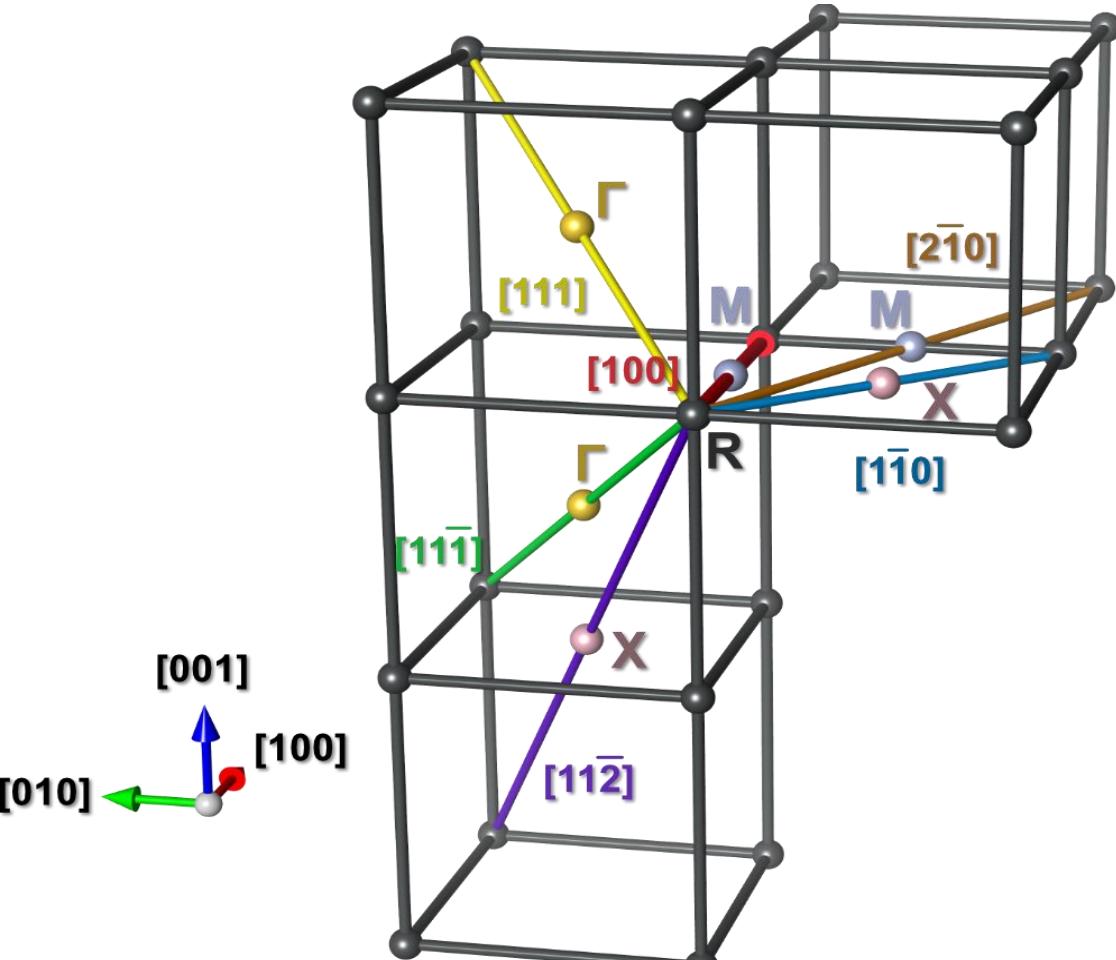
High symmetry points of pseudo-cubic BZ

Conclusions

Dominant NN exchange J_1
Exchange fully isotropic in 3D BZ

Spin spiral energy calculation in BFO

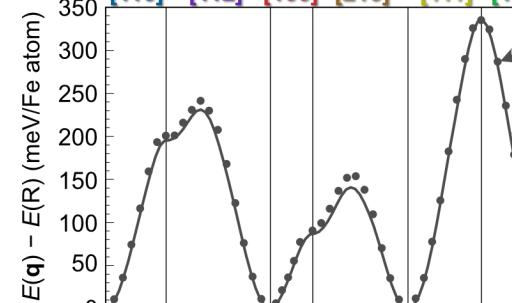
Detailed path of the q-vector



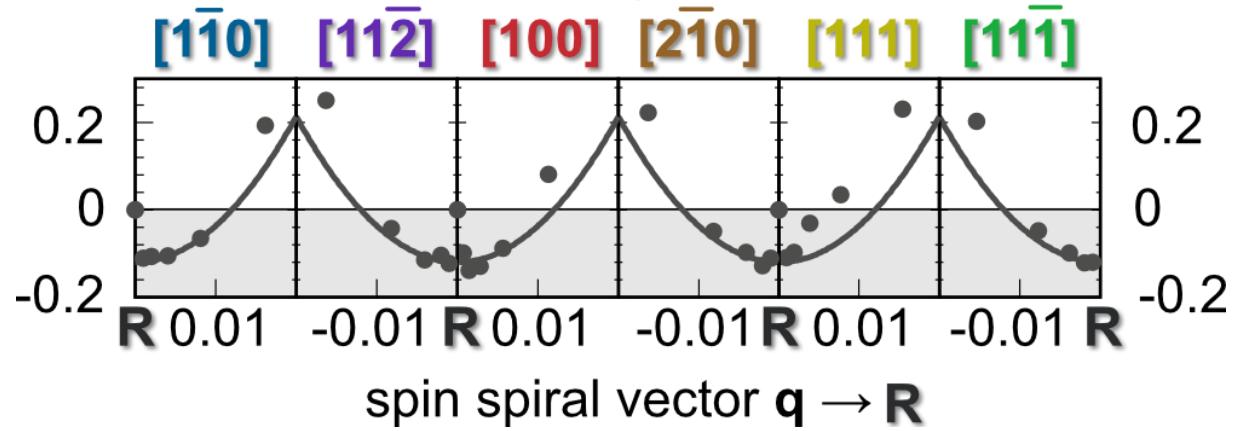
B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
S. Meyer, et al., Phys. Rev. B **108**, 024403 (2023)

Directions within the pseudo-cubic BZ

[$\bar{1}\bar{1}0$] [$\bar{1}1\bar{2}$] [100] [$2\bar{1}0$] [111] [$1\bar{1}\bar{1}$]



Zoom around ground state



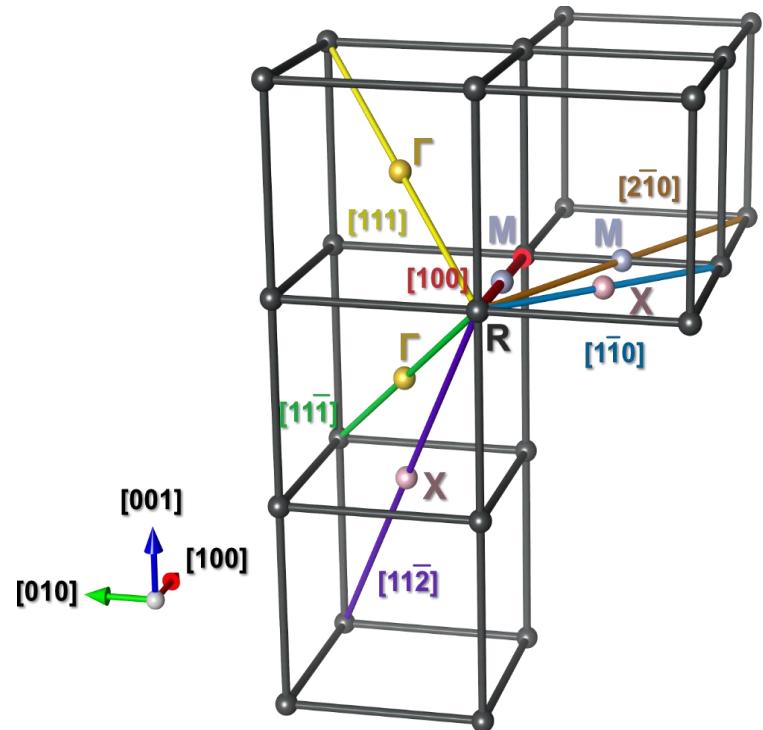
spin spiral vector $\mathbf{q} \rightarrow \mathbf{R}$

Conclusions

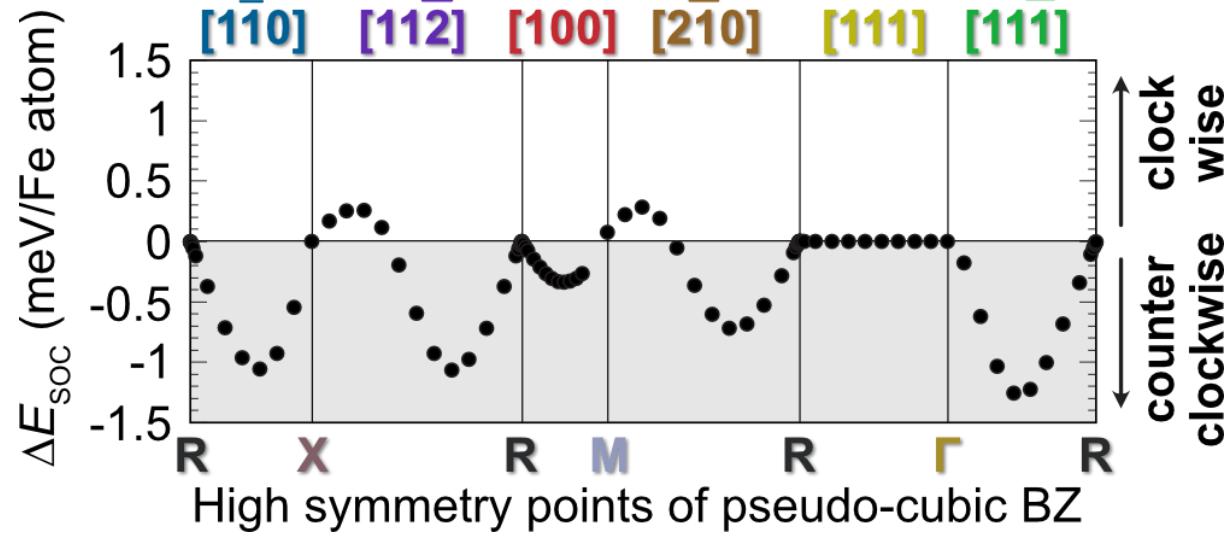
Dominant NN exchange J_1
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DM interaction energy calculation in BFO

Detailed path of the \mathbf{q} -vector



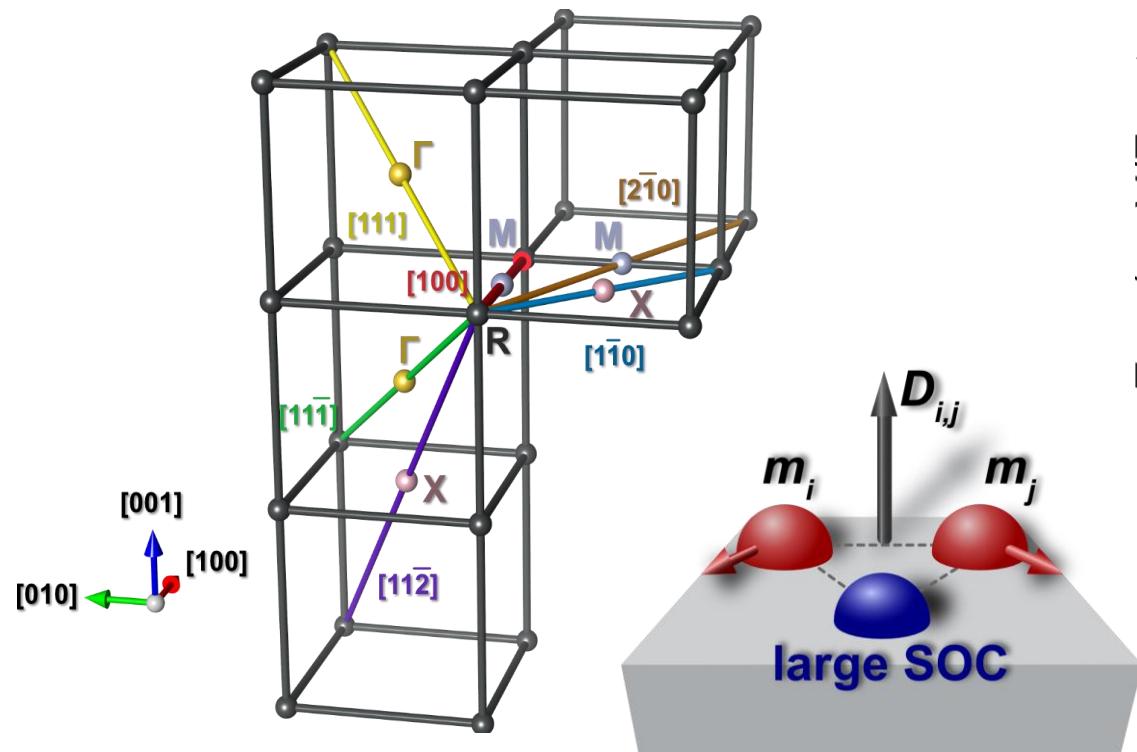
Directions within the pseudo-cubic BZ



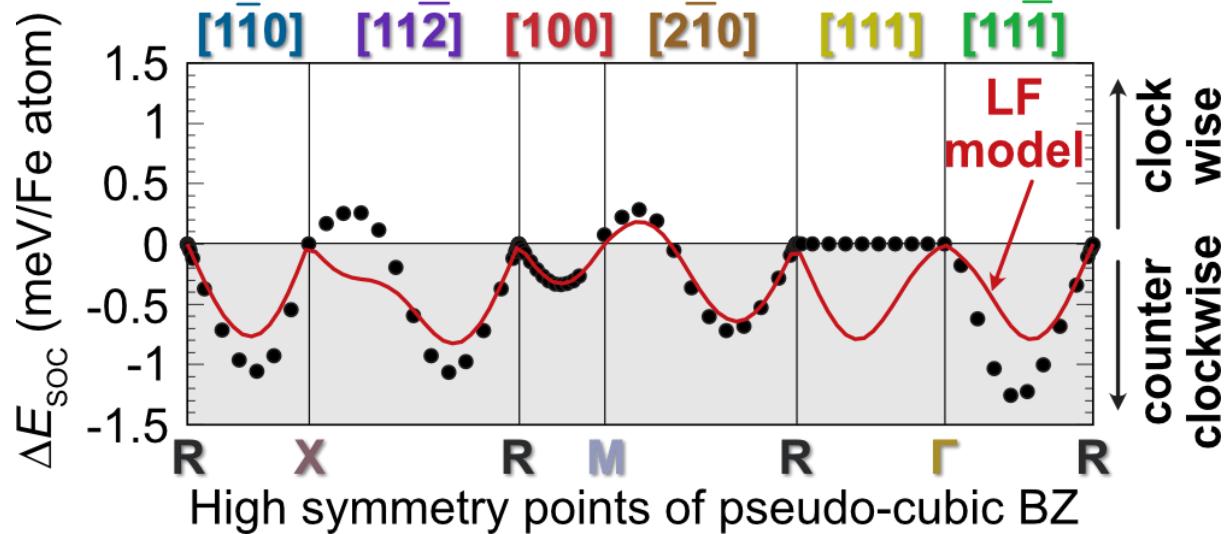
B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
S. Meyer, et al., Phys. Rev. B **108**, 024403 (2023)

DM interaction energy calculation in BFO

Detailed path of the \mathbf{q} -vector



Directions within the pseudo-cubic BZ



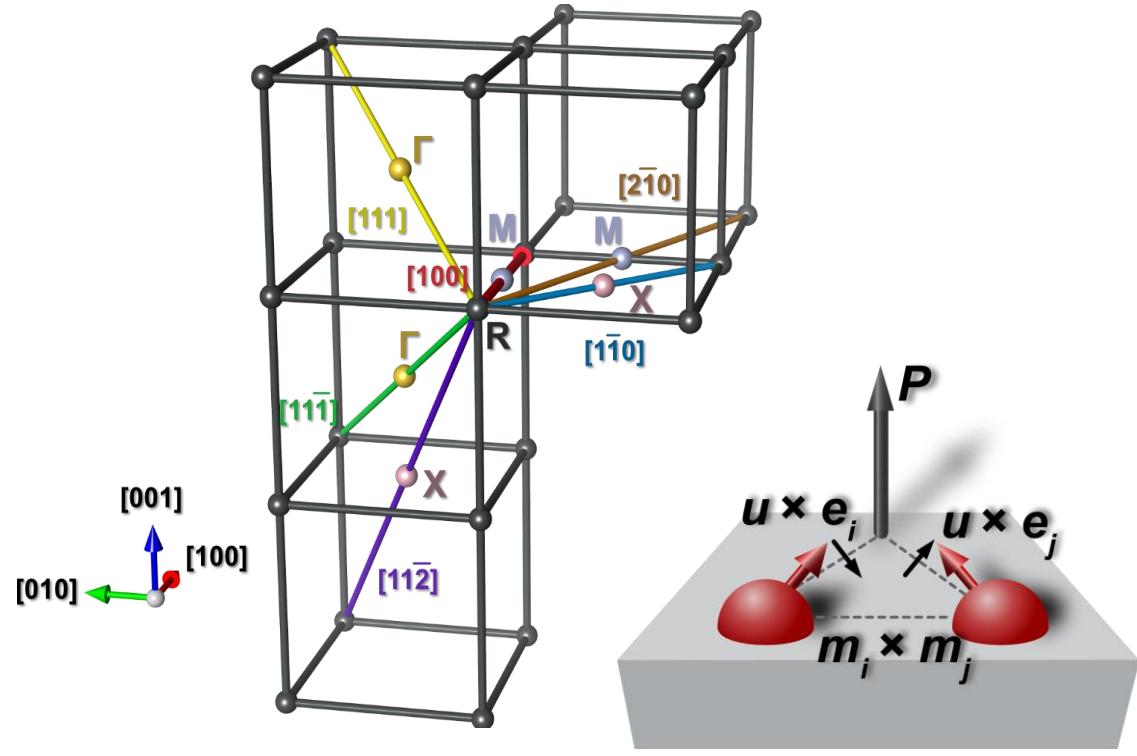
\mathbf{D}_{ij} from Fe-O-Fe bonds

$$\mathcal{H}_{DMI}^{LF} = - \sum_{i,j} \mathbf{D}_{ij} (\mathbf{m}_i \times \mathbf{m}_j)$$

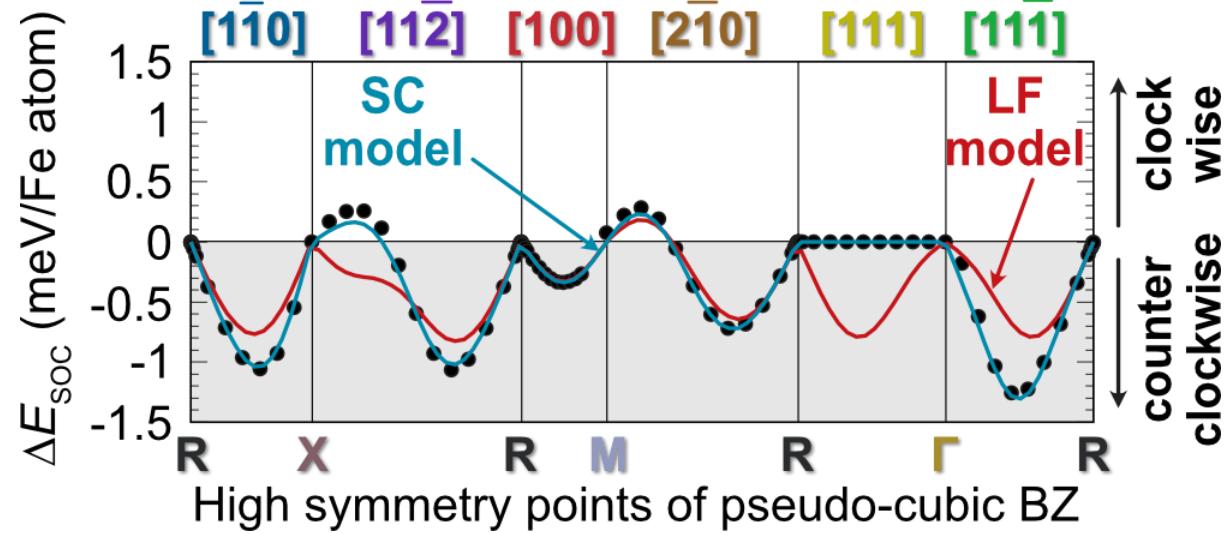
B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
S. Meyer, et al., Phys. Rev. B **108**, 024403 (2023)

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Directions within the pseudo-cubic BZ

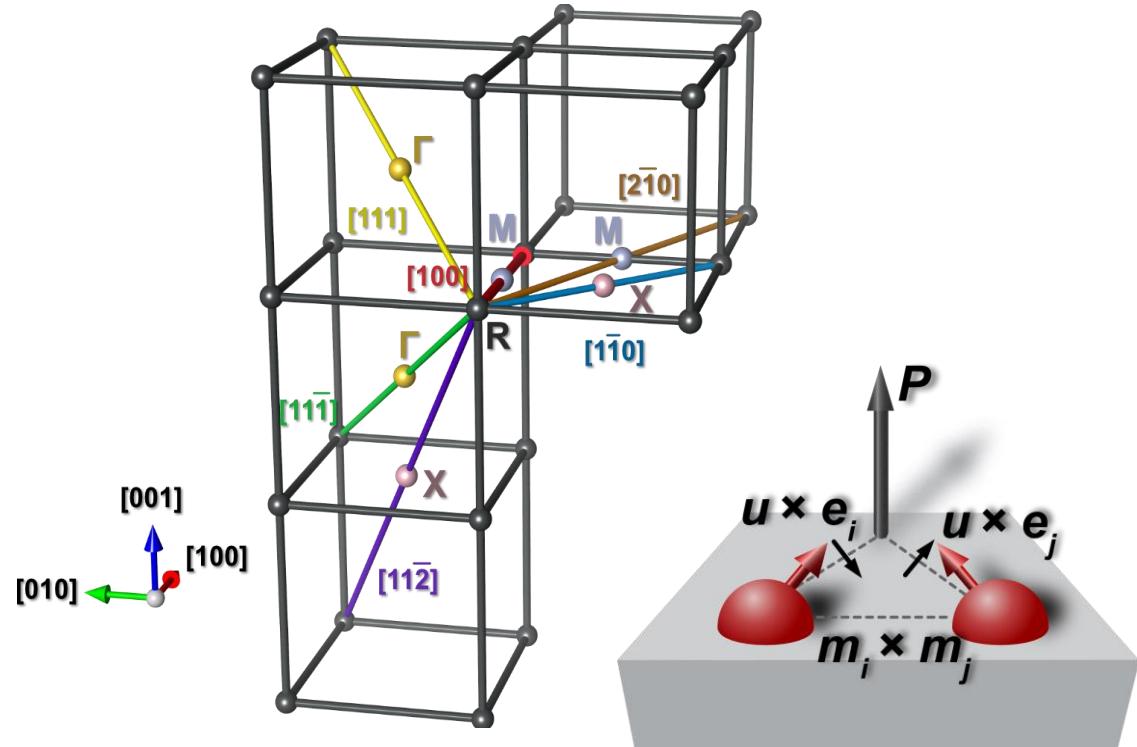


$$\mathcal{H}_{DMI}^{SC} = - \sum_{i,j} C_{ij} (\mathbf{u}_i \times \mathbf{e}_{ij}) (\mathbf{m}_i \times \mathbf{m}_j)$$

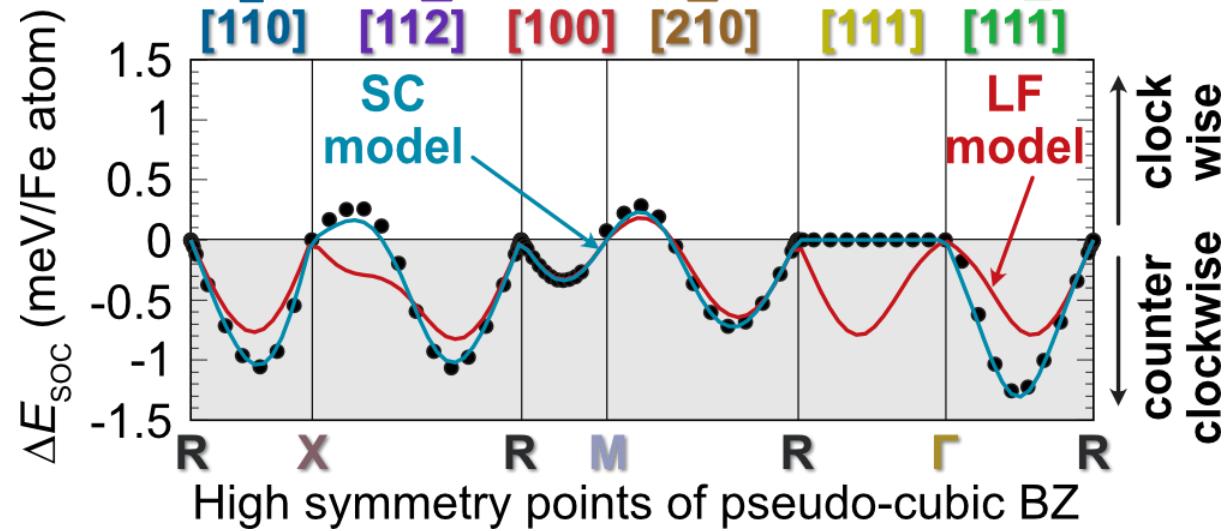
B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
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DM interaction energy calculation in BFO

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Directions within the pseudo-cubic BZ



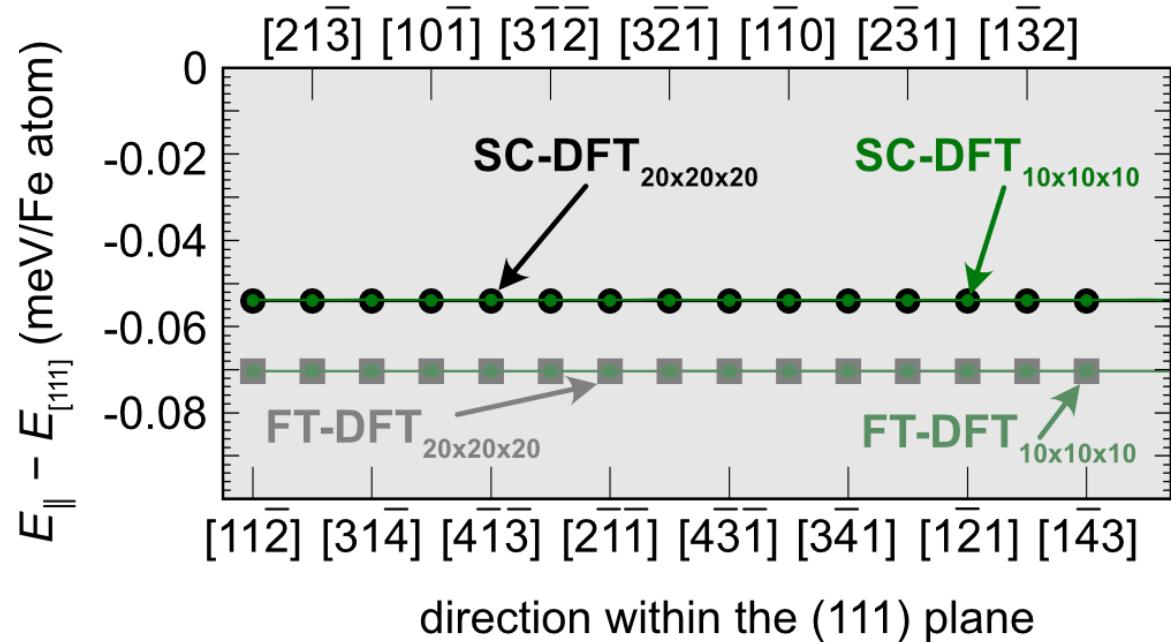
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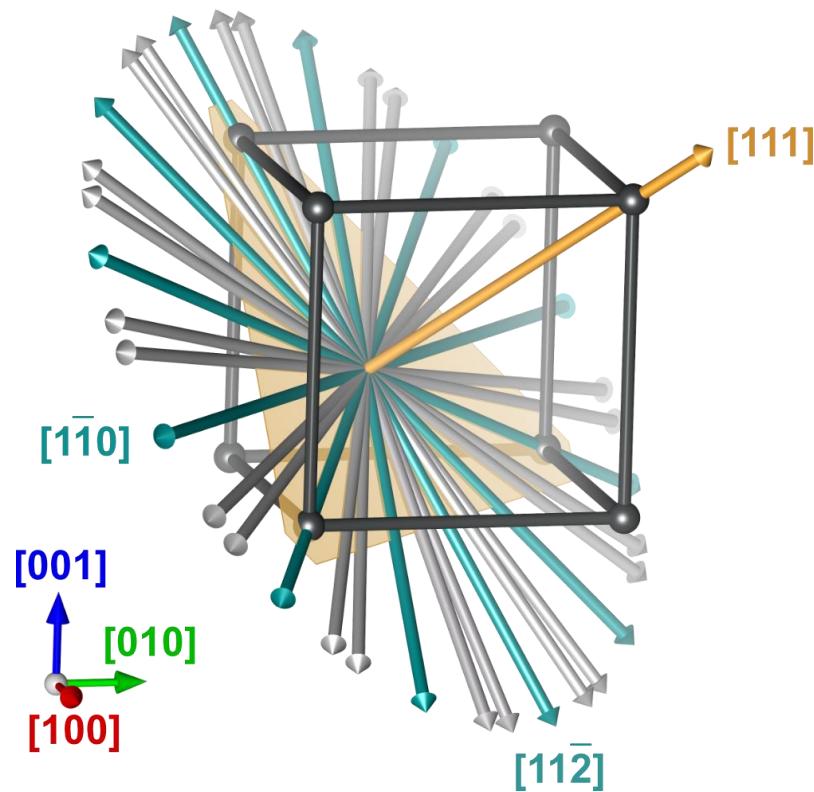
No SOC contribution in [111] direction
Disagreement with LF model
Spin-current model in agreement with data

B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
S. Meyer, et al., Phys. Rev. B **108**, 024403 (2023)

Magnetocrystalline anisotropy in BFO

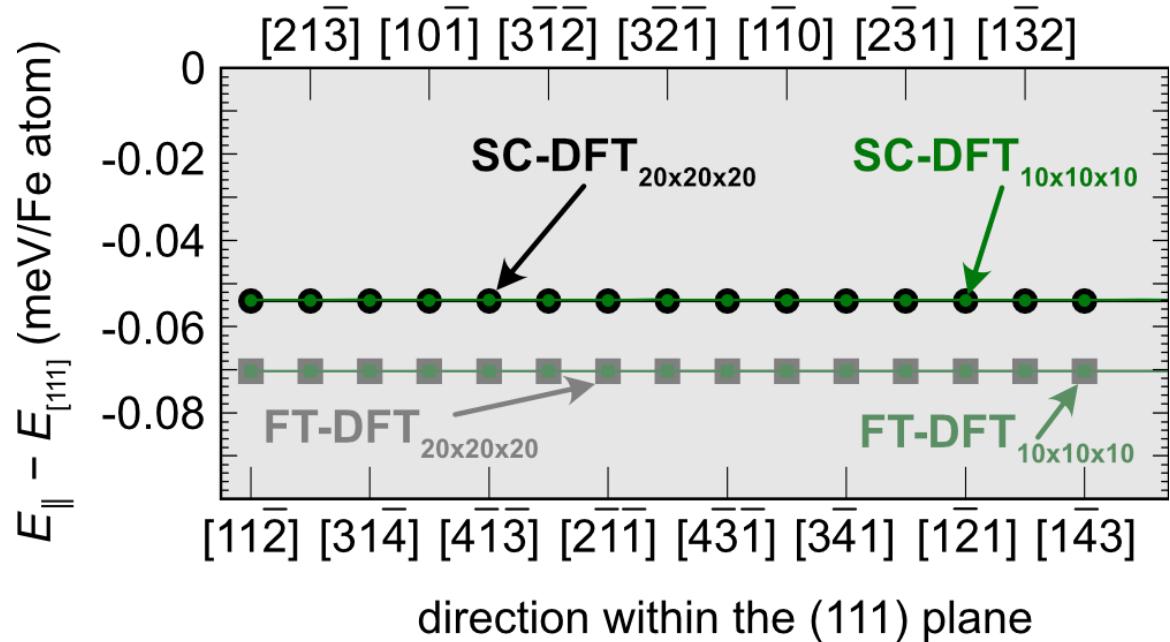


Calculations of preferred magnetization direction



B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
S. Meyer, et al., Phys. Rev. B **108**, 024403 (2023)

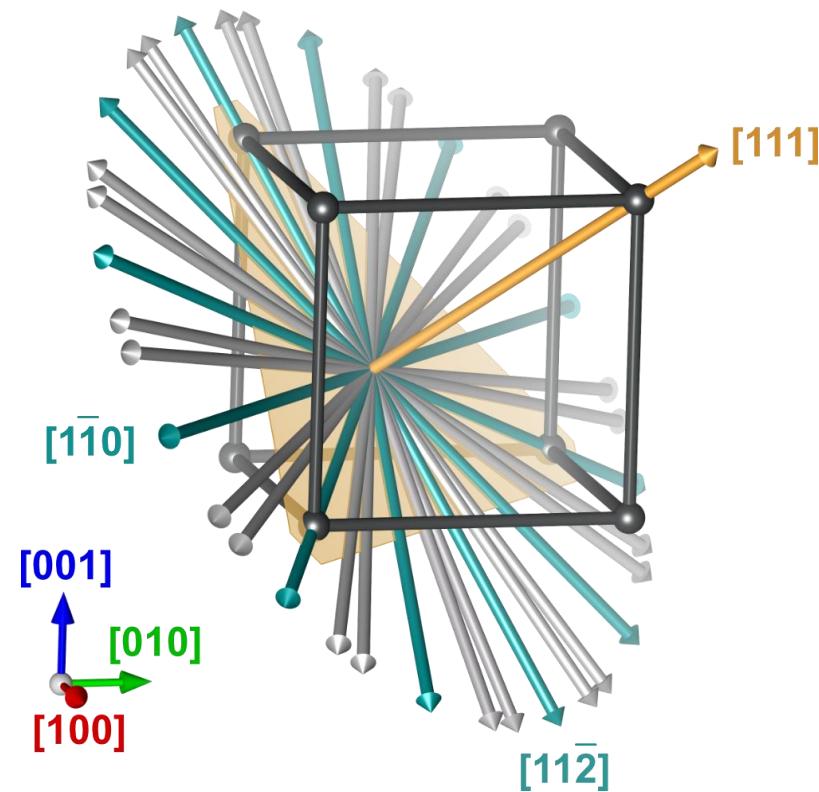
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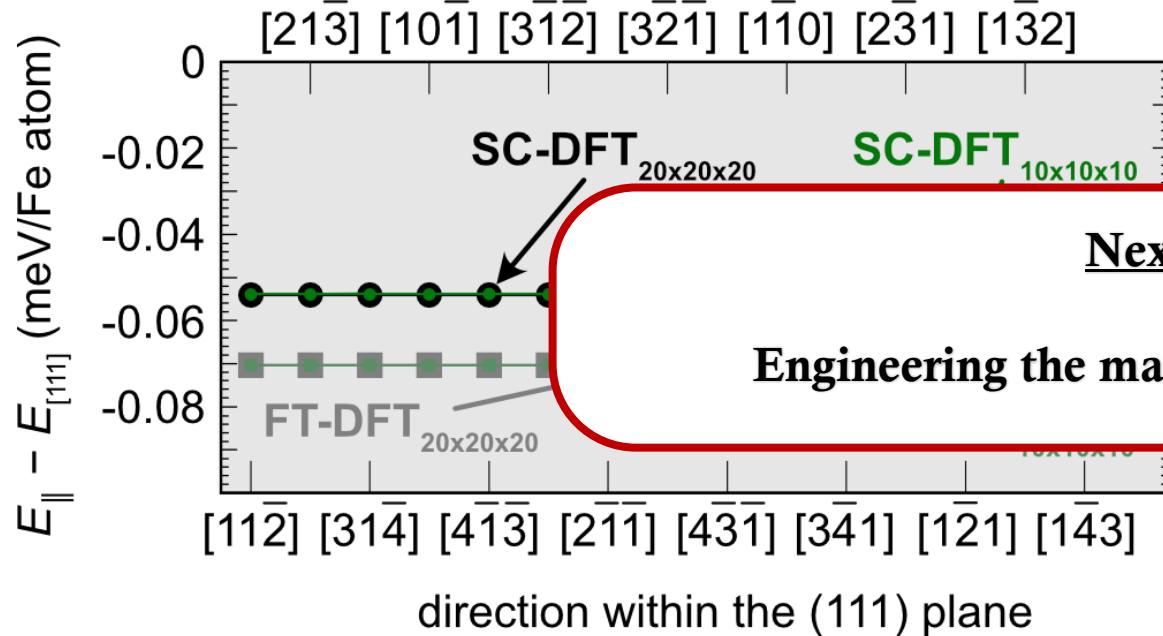
- Extremely small anisotropy
- Hard [111] axis
- Completely easy (111) plane of magnetization

Calculations of preferred magnetization direction

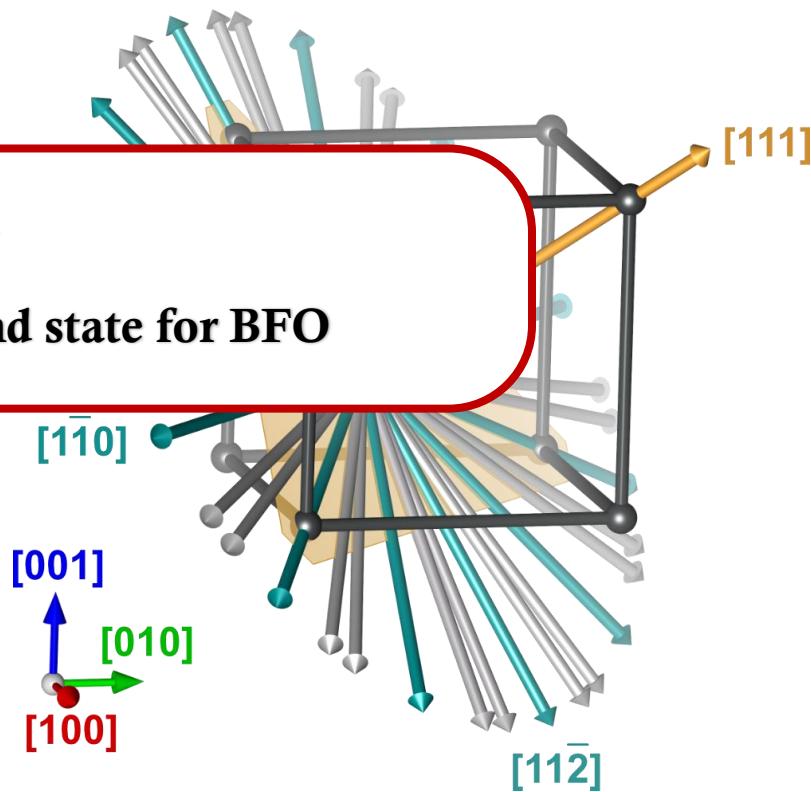


B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
S. Meyer, et al., Phys. Rev. B **108**, 024403 (2023)

Magnetocrystalline anisotropy in BFO



Calculations of preferred magnetization direction



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- Extremely small anisotropy
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B. Xu, et al., Phys. Rev. B **103**, 214423 (2023)
S. Meyer, et al., Phys. Rev. B **108**, 024403 (2023)

Order parameters of BiFeO_3

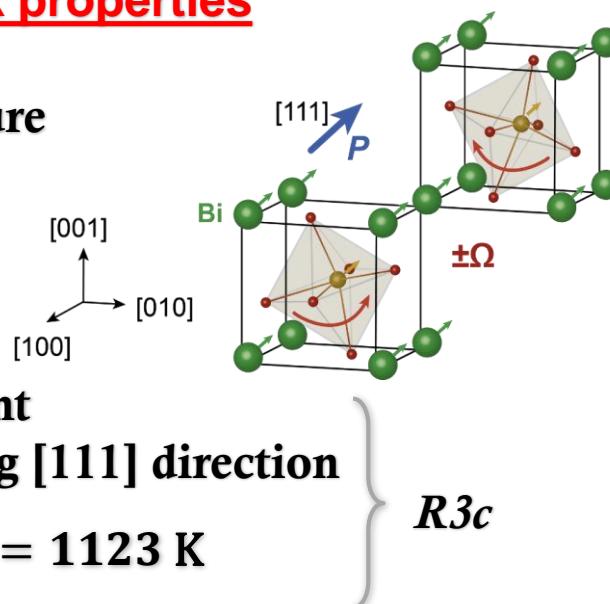
Bulk properties

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Fe Cations

O Anions



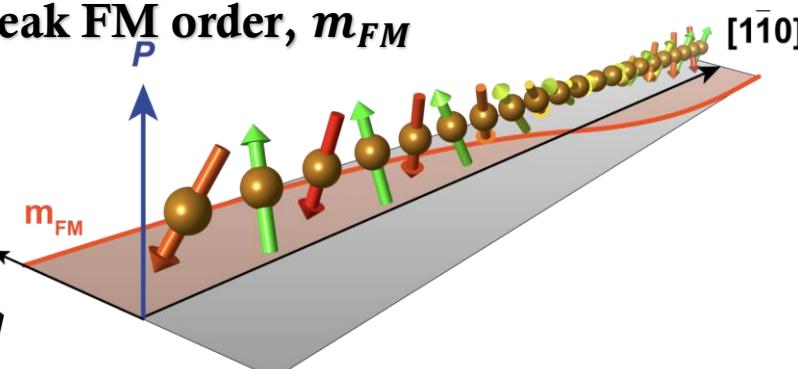
2. Fe-Bi displacement

Polarization along [111] direction

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3. Oxygen tilt in antiphase $\pm\Omega$

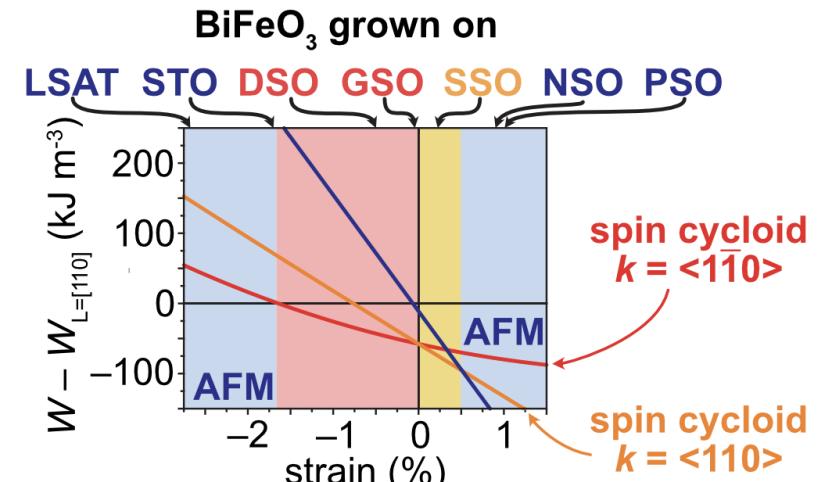
4. Local antiferromagnetic order with long-ranged spin cycloid, $\lambda \approx 62 \text{ nm}$ + weak FM order, m_{FM}



Strain properties

1. Precise modification of material's lattice parameters

2. Modification of multiferroic properties:



D. Sando, et al., Nature Mater. 12, 641 (2013)

3. Collinear AFM state for strain ε $< -0.5\%$ and $\varepsilon > +0.5\%$

4. Large sensitivity of magnetic ground states Different results for equivalent substrates

Order parameters of BiFeO₃

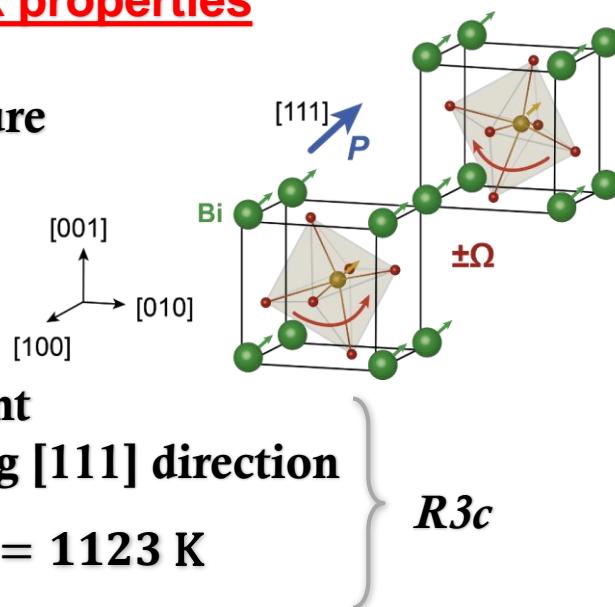
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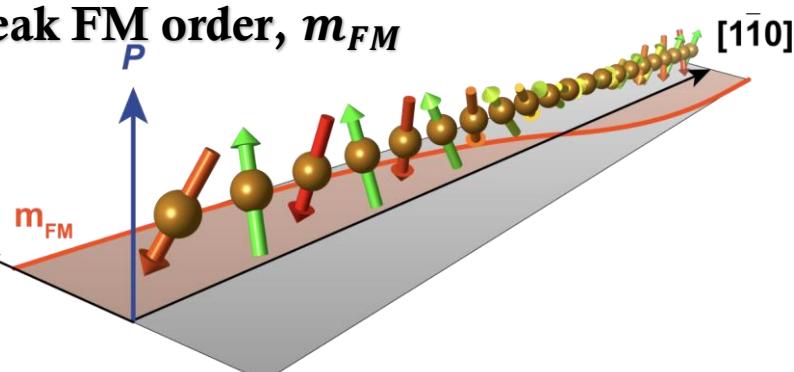
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Strain properties

1. Precise modification of material's lattice parameters
2. Modification of multiferroic properties:

BiFeO₃ grown on

Objective:

Investigation of magnetic energies with epitaxial strain

compressive



$\epsilon < 0\%$



$\epsilon = 0\%$

no strain



$\epsilon > 0\%$



$\epsilon > 0\%$

3. Collinear AFM state for strain ϵ

$< -0.5\%$ and $\epsilon > +0.5\%$

4. Large sensitivity of magnetic ground states

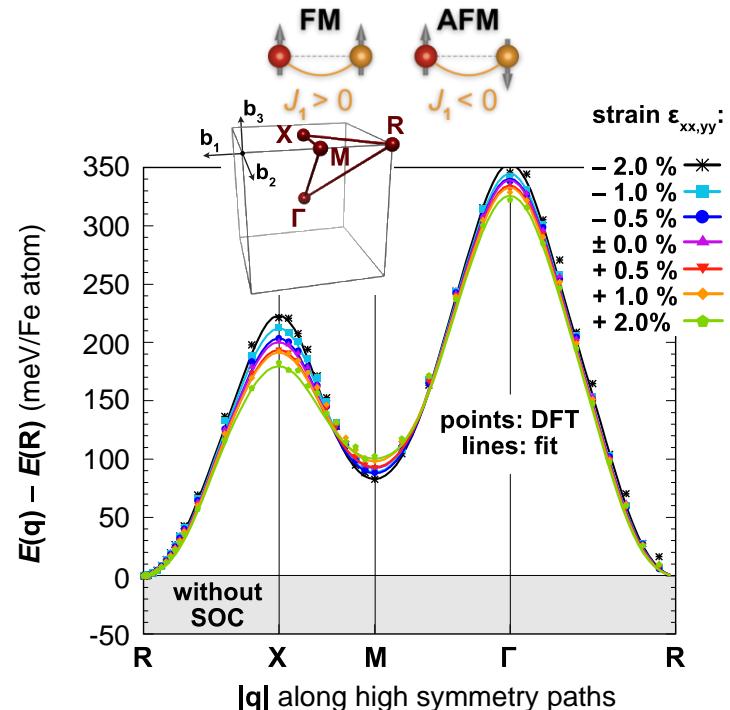
Different results for equivalent substrates

Evolution of magnetic interactions with strain

S. Meyer, et al., Phys. Rev. B 109, 184431

(2024) Exchange interaction

$$\mathcal{H}_{ex} = - \sum_{i,j} J_{ij} (\mathbf{m}_i \cdot \mathbf{m}_j)$$



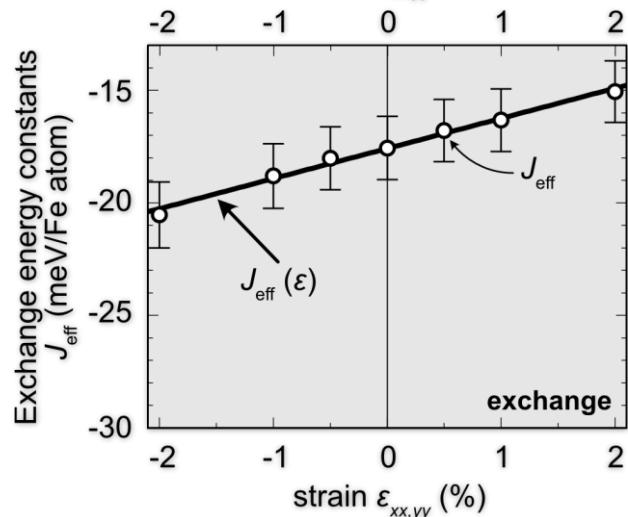
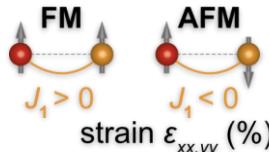
Linearly decreasing strength

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S. Meyer, et al., Phys. Rev. B 109, 184431

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Linearly decreasing
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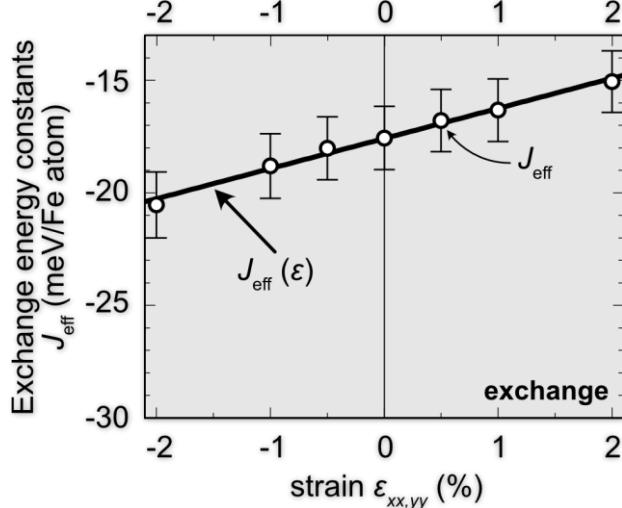
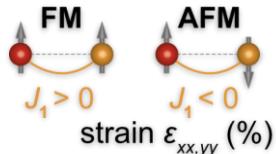
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S. Meyer, et al., Phys. Rev. B 109, 184431

(2024)

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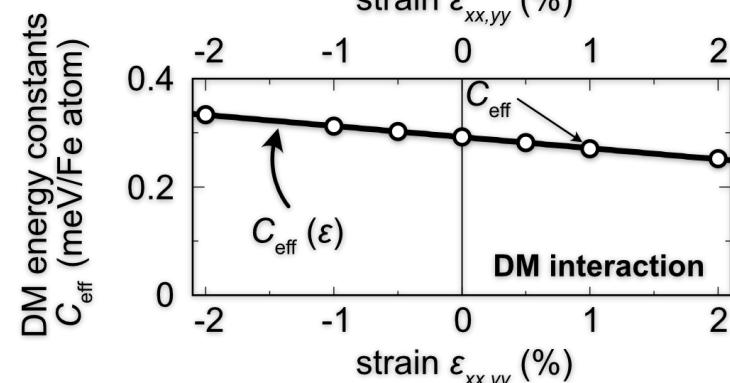
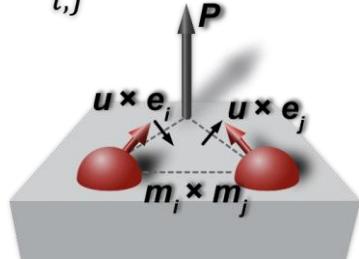
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Linearly decreasing strength

Dzyaloshinskii-Moriya interaction

$$\mathcal{H}_{DMI}^{SC} = - \sum_{i,j} C_{ij} (\mathbf{u} \times \mathbf{e}_{ij}) (\mathbf{m}_i \times \mathbf{m}_j)$$



Linearly decreasing strength

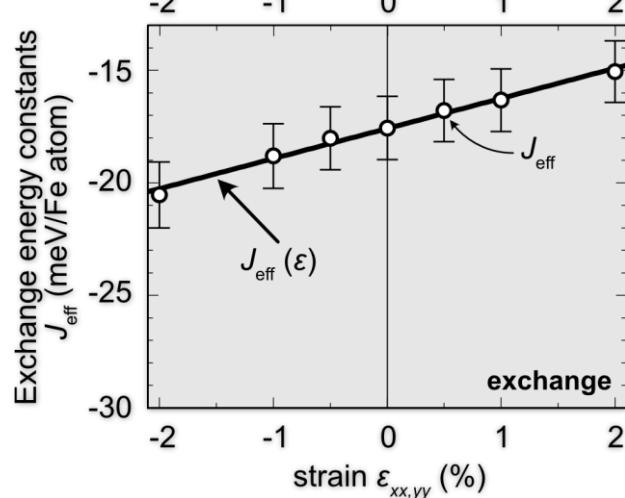
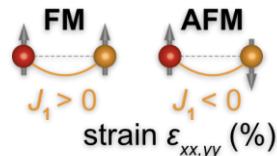
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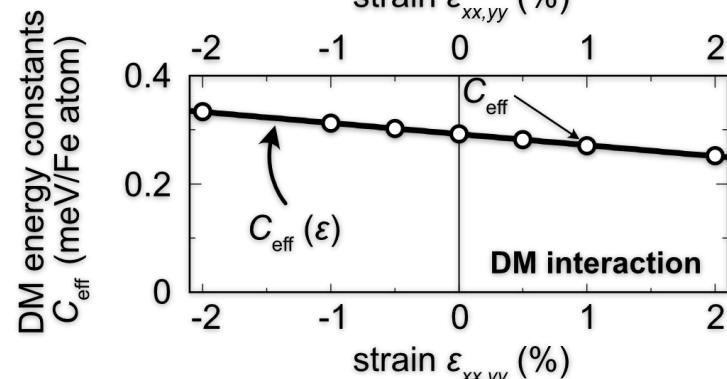
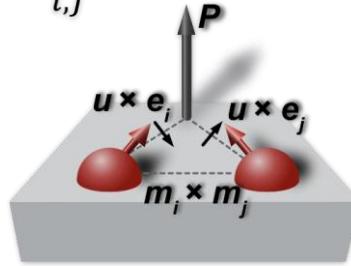


Linearly decreasing strength



Dzyaloshinskii-Moriya interaction

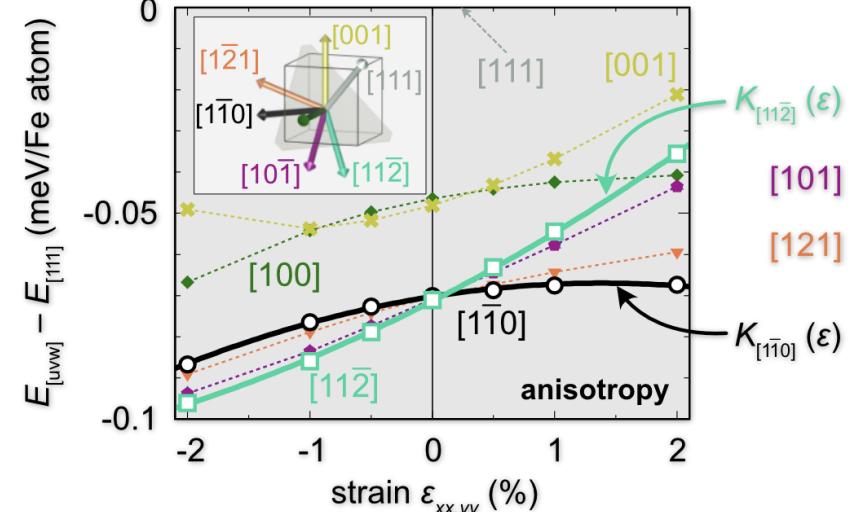
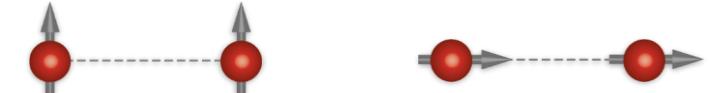
$$\mathcal{H}_{DMI}^{SC} = - \sum_{i,j} C_{ij} (\mathbf{u} \times \mathbf{e}_{ij}) (\mathbf{m}_i \times \mathbf{m}_j)$$



Linearly decreasing strength

Magnetocrystalline anisotropy

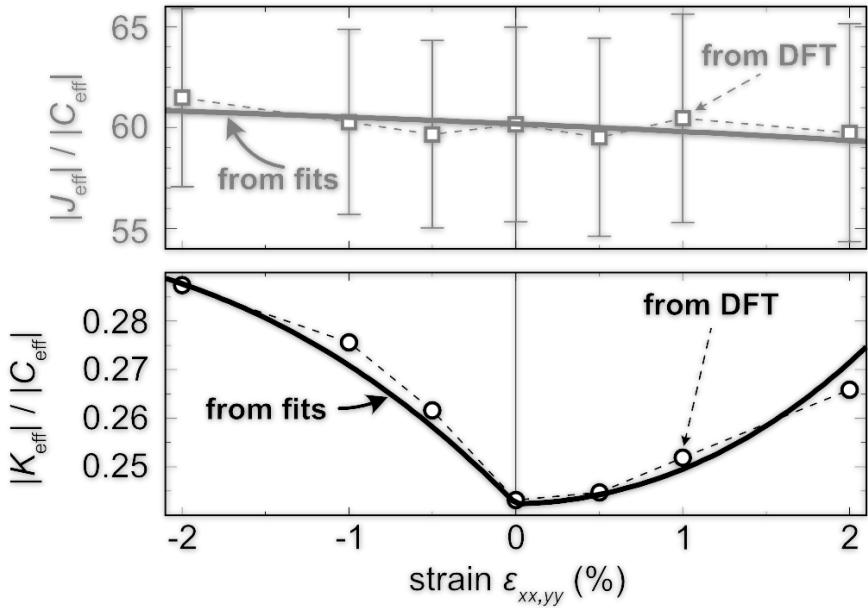
$$\mathcal{H}_{ani} = - \sum_i K \mathbf{m}_{[111]}^2$$



[112] easy axis for $\epsilon < 0$
[1-10] easy axis for $\epsilon > 0$

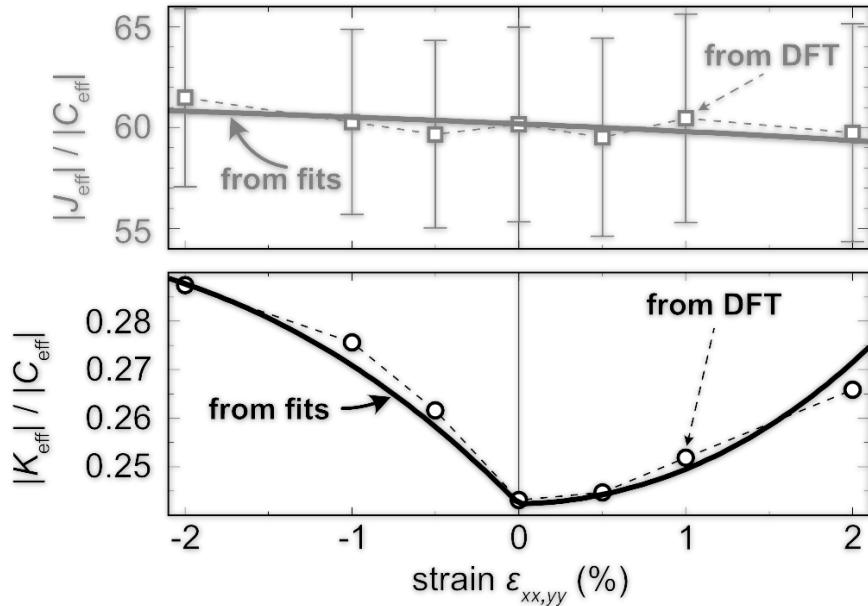
Evolution of the ratio between Exchange, anisotropy and DM

Ratios of magnetic interactions



Evolution of the ratio between Exchange, anisotropy and DM

Ratios of magnetic interactions

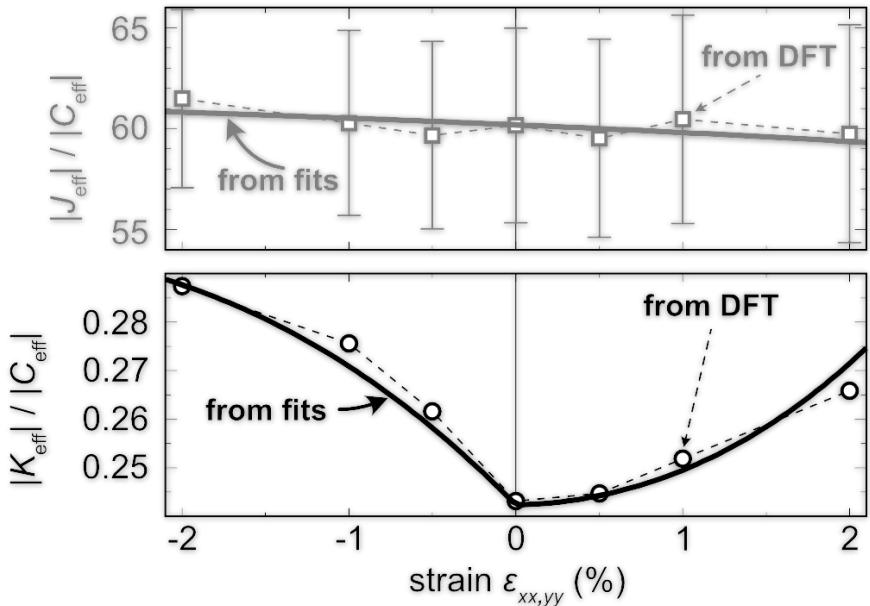


Conclusions

- $\varepsilon < 0$: Preferred collinear order from exchange and anisotropy
- $\varepsilon > 0$: Weaker collinear order from exchange vs. DMI, but Stronger due to MAE

Domain wall energy

Ratios of magnetic interactions



Conclusions

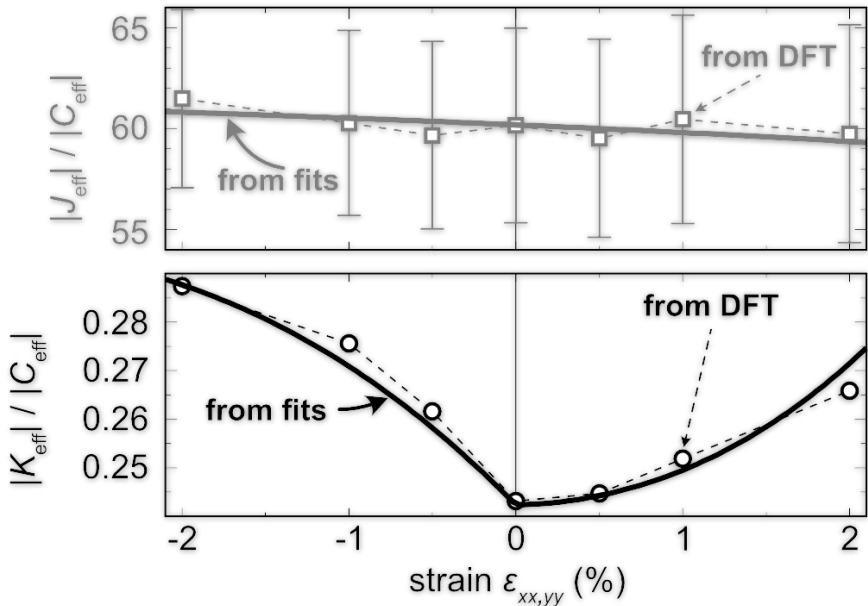
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Magnetic domain wall energies

$$E_{DW}(\varepsilon) = \frac{4}{a^2(\varepsilon)} \sqrt{J_{\text{eff}}(\varepsilon) K_{\text{eff}}(\varepsilon)} - \frac{2\pi}{a^2(\varepsilon)} C_{\text{eff}}(\varepsilon)$$

Domain wall energy

Ratios of magnetic interactions



Conclusions

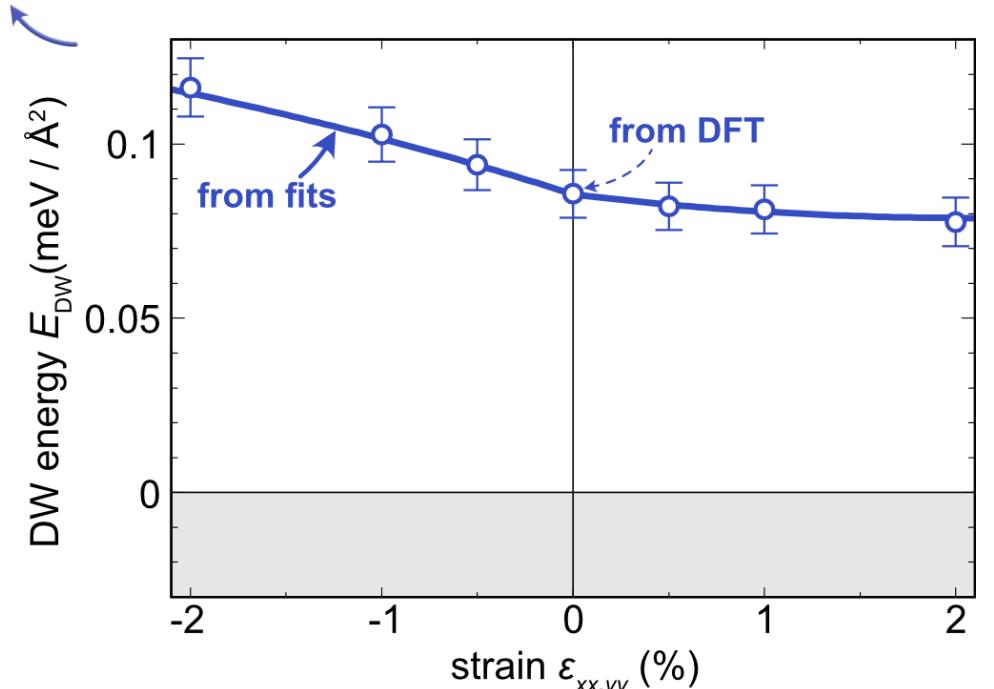
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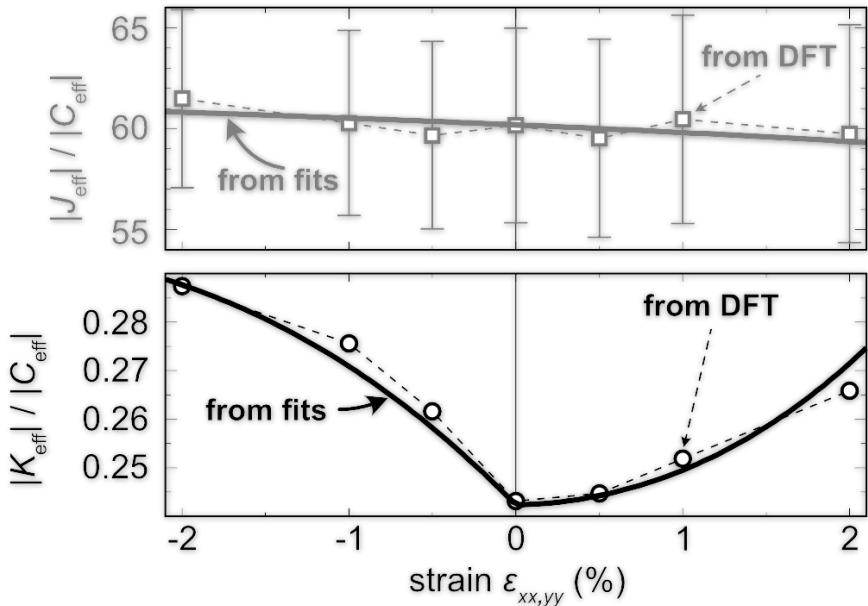
increasing collinear stability
with compressive strain

similar ground state
as in bulk for tensile strain,
but more sensitivity



Domain wall energy

Ratios of magnetic interactions



Conclusions

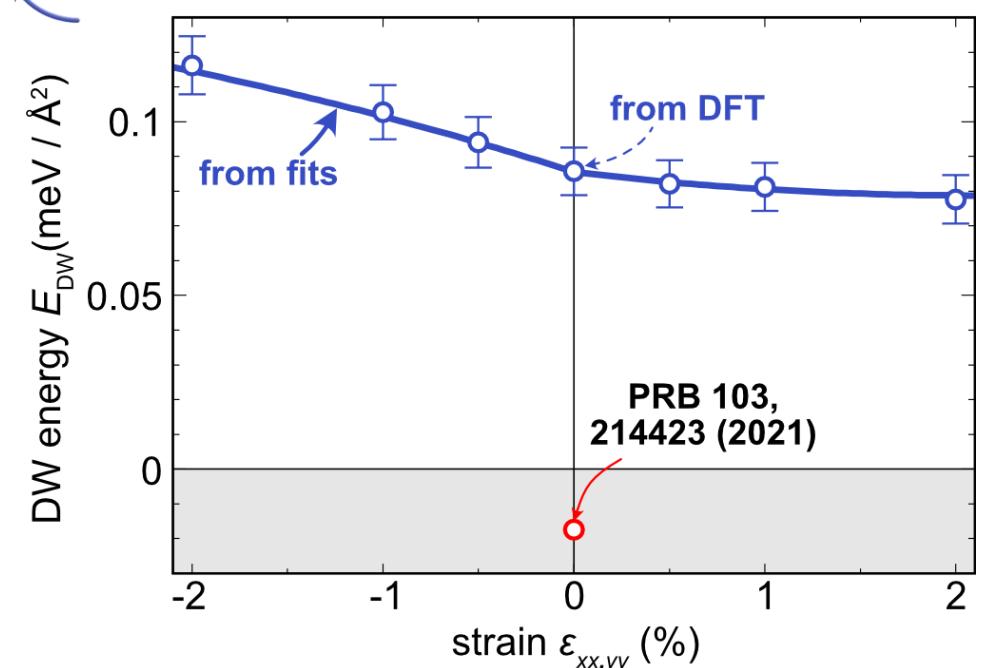
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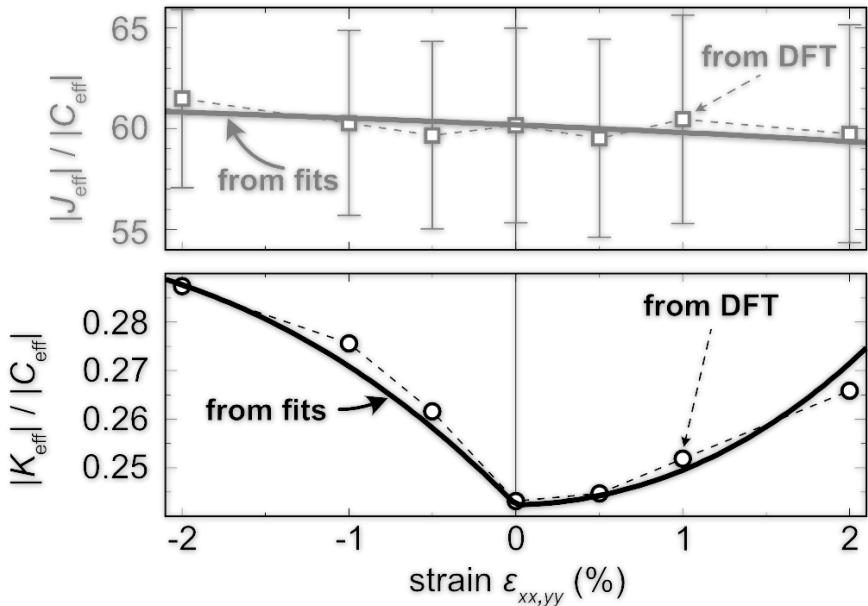
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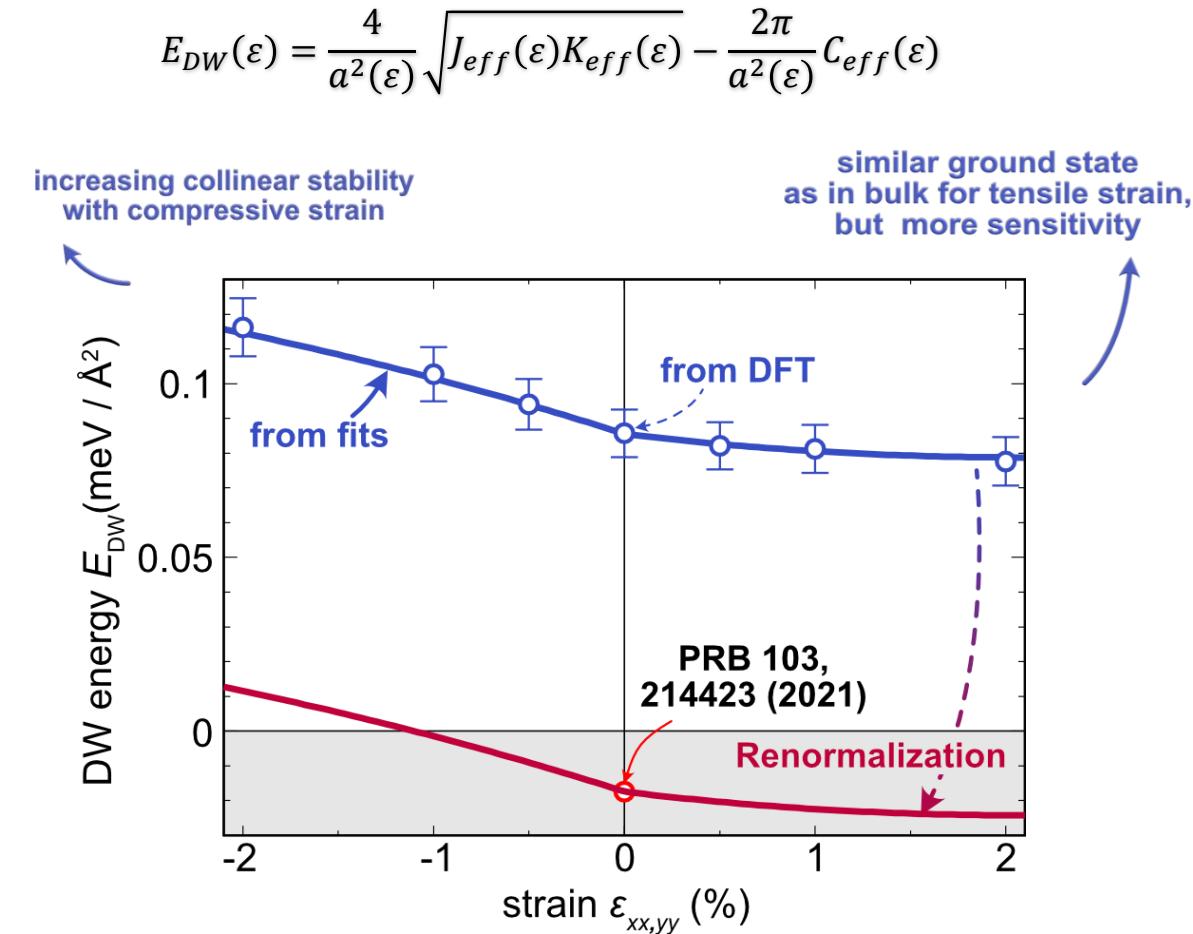
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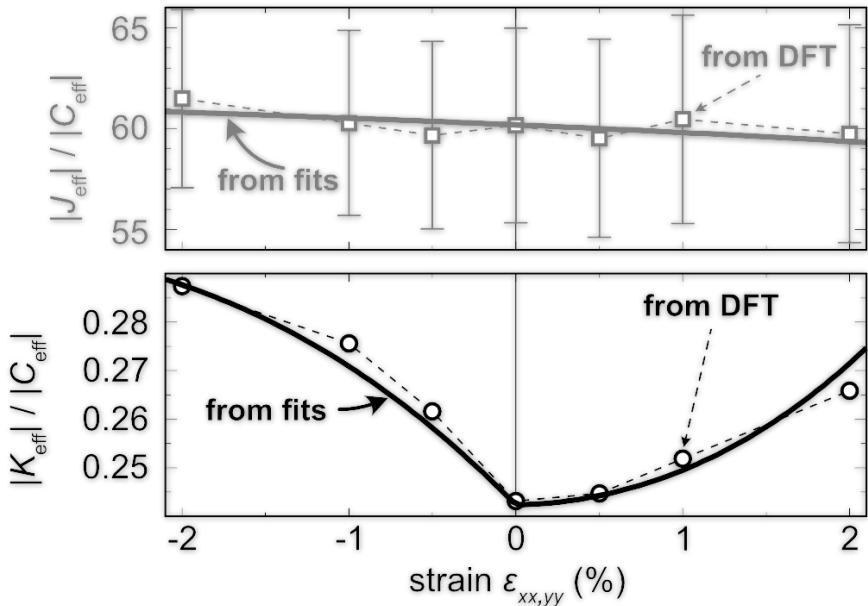
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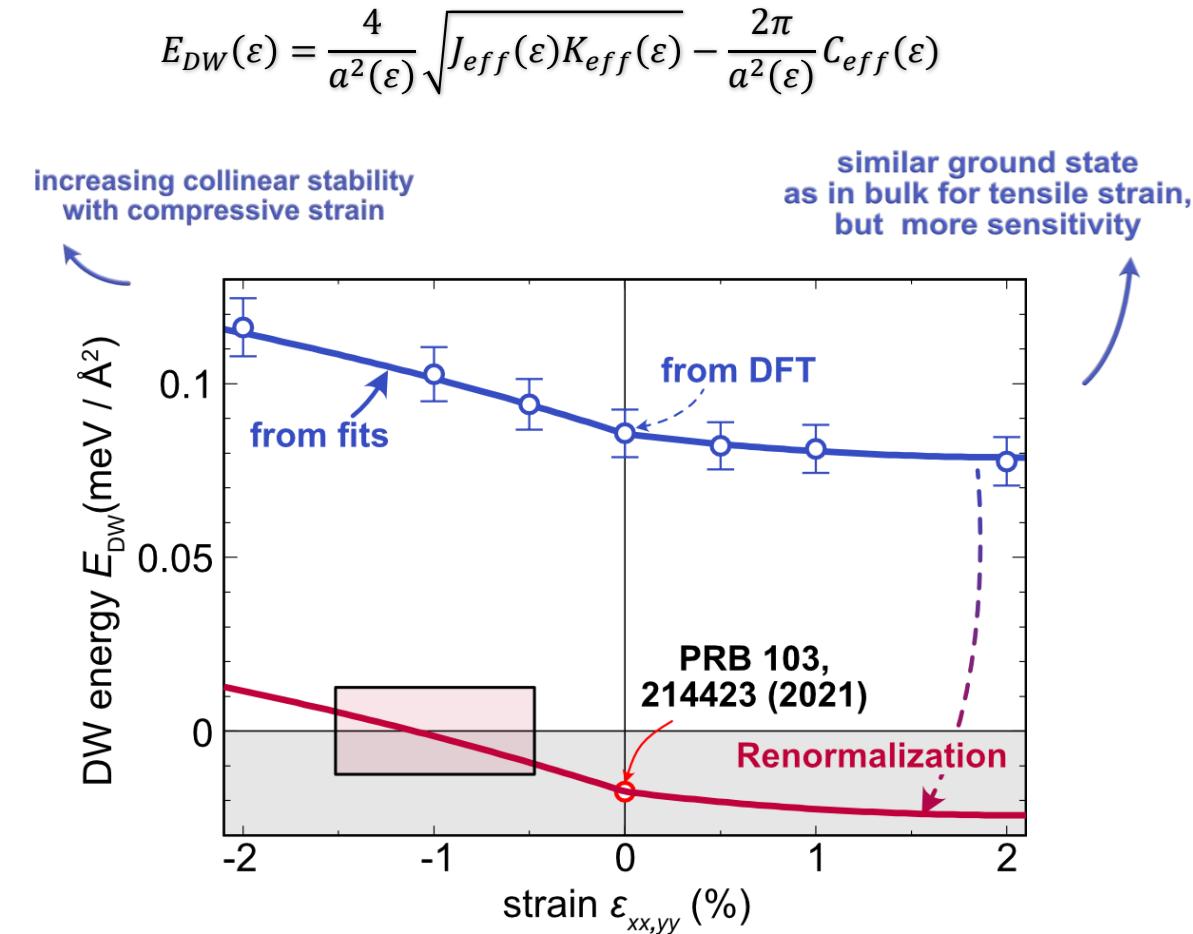
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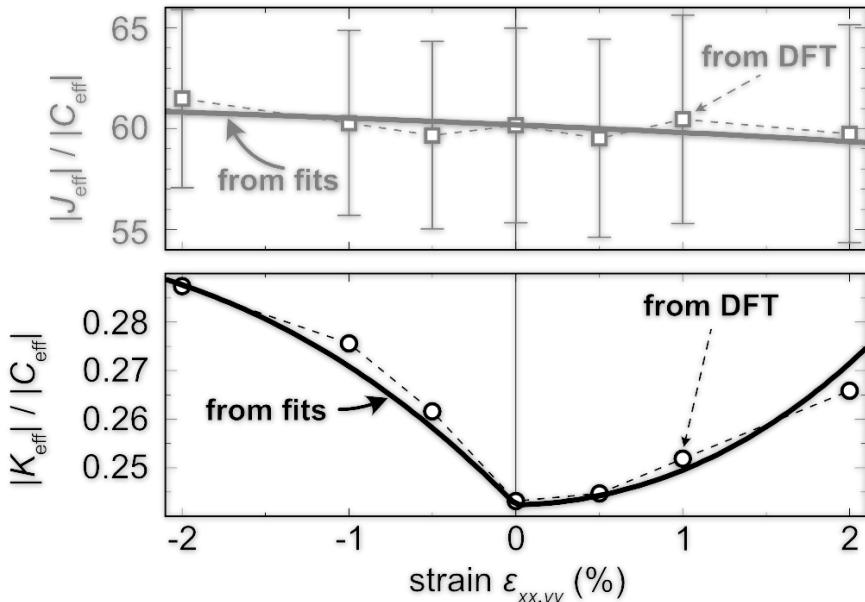
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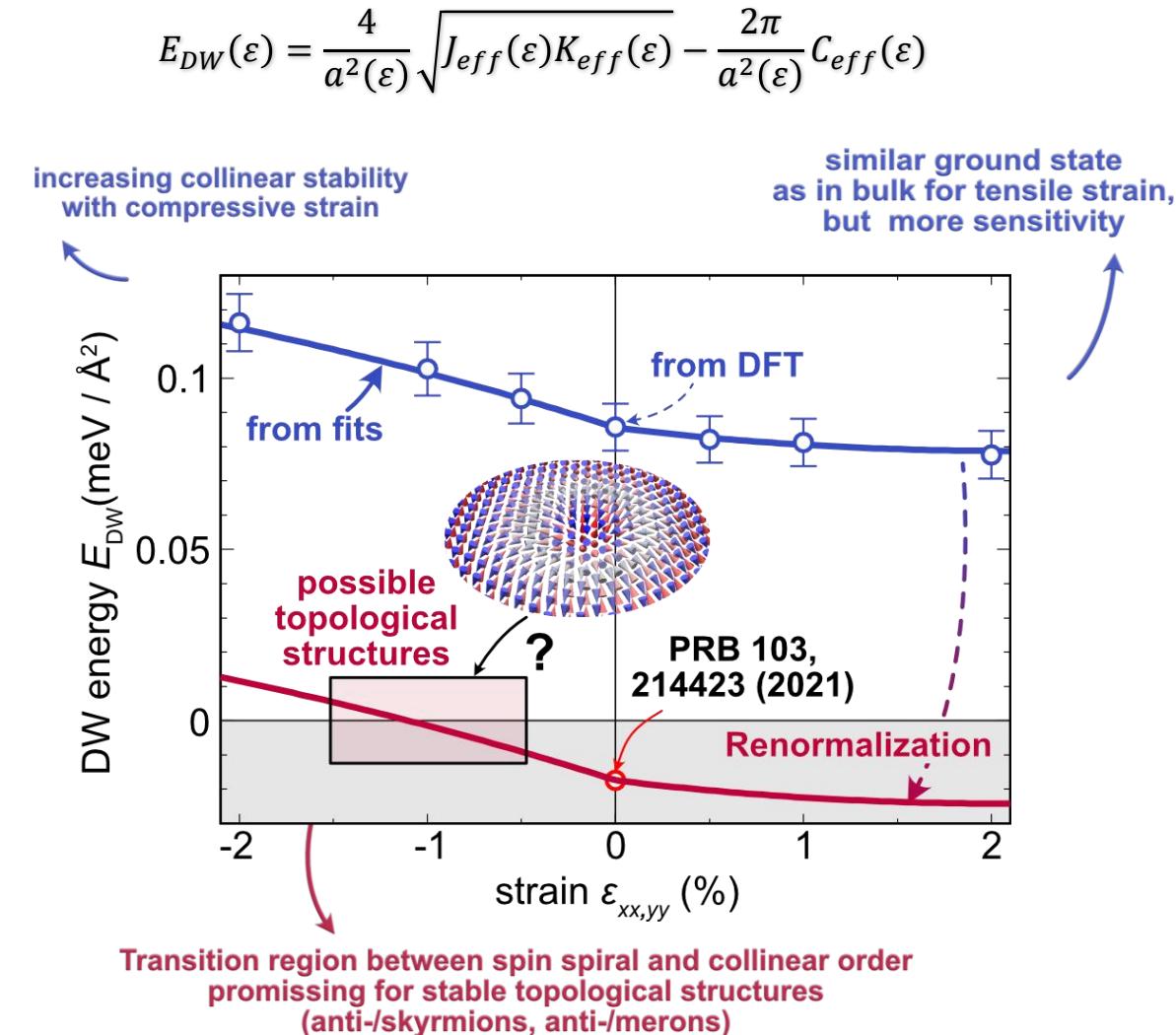
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Magnetic domain wall energies



Conclusion

- Topology is a very rich playground to do physics
- Multiferroics offer an excellent platform to stabilize ferroelectric and magnetic skyrmions
- Skyrmions can be functionalize for
 - neuromorphic computing,
 - Particle physics
 - Quantum computing
- Check our code github.com/bertdupe/Matjes

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