

# Magnetism in multiferroics

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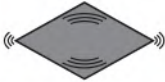
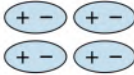
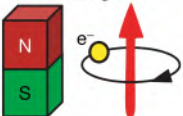
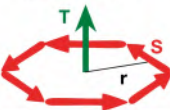
03/07/2025

# Outline

## Multiferroics:

- ▶ Definition
- ▶ Multiferroic types and mechanisms
- ▶ J, DMI, SIA in multiferroic type I (cubic perovskites)
- ▶ Spin driven multiferroics (type II) (cubic perovskites)

# Ferroic orders

| <div>Time</div> <div>Space</div> | Invariant                                                                                               | Change                                                                                                   |
|----------------------------------|---------------------------------------------------------------------------------------------------------|----------------------------------------------------------------------------------------------------------|
| Invariant                        | <p>Ferroelastic</p>   | <p>Ferroelectric</p>  |
| Change                           | <p>Ferromagnetic</p>  | <p>Ferrotoroidic</p>  |

# Multiferroics

Multiferroics:

more than one ferroic order in the same material

(name coined by Hans Schmidt in 1993 but 1st works by Smolenskii et al. 50's who called them ferroelectromagnets)



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... Well, actually hard to find! (FM metals vs insulating FE)

# Multiferroics

**Multiferroics:** more than one ferroic order in the same material ...

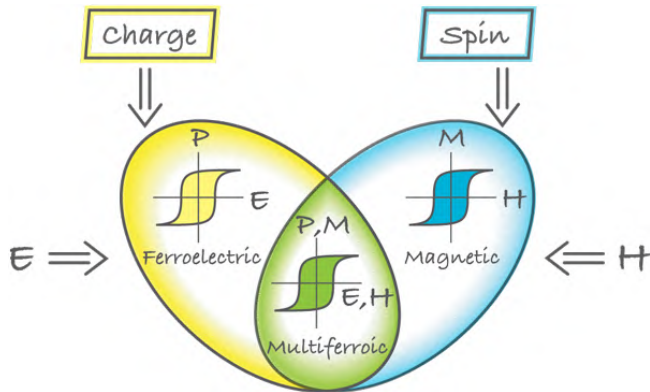
Lets do a hack!



**Multiferroics:** Usual definition plus ... Ferroelectricity + whatever magnetic order!

# Multiferroics

**Multiferroics:** more than one ferroic order in the same material!



# Multiferroics

**Multiferroics:** Usual definition plus ... Ferroelectricity + whatever magnetic order!

But ... still not very common?



Hack further: Extension to multi-antiferroics!

# Multiferroics

The  $d^0$ -ness problem (N. Spaldin 2000)

FE conditions ( $\text{BaTiO}_3$ -type):

- ▶ Displacive FE transition (soft polar mode)
- ▶ Driven by charge transfer through O- $p$ /Ti- $d^0$  hybridization
- ▶  $d^0$  is key  $\longrightarrow$  in contradiction with magnetic systems that need  $d^{n \neq 0}$

Solution: The  $\text{BaTiO}_3$ -type mechanism for FE is actually not the most common:

- ▶ Lone pair mechanism ( $\text{Pb}^{2+}$ ,  $\text{Bi}^{3+}$ , etc)
- ▶ Geometric FE: P is not the primary order parameter (improper, triggered, etc)
- ▶ Geometric FE: steric effects (as in “polar metals”)
- ▶ Spin-driven FE: magnetic order induces FE (P is not the primary OP)

# Multiferroics: Type I vs Type II classification

Tentative to classify multiferroics (Khomsikii 2009)

## Type I multiferroics:

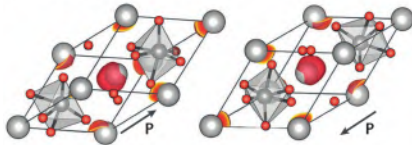
- ▶ Ferroelectric and magnetic orders appear independently ( $T_C^{FE} \neq T_C^{FM}, T_N$ )
- ▶ Polarization can be large
- ▶ Weak coupling between FE and magnetic properties

## Type II multiferroics:

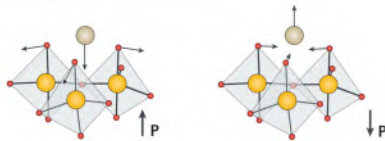
- ▶ Magnetism causes ferroelectricity ( $T_C^{FE} = T_C^{FM}, T_N$ )
- ▶ Polarization is small
- ▶ Strong coupling between polarization and magnetic properties

# Multiferroic Type I mechanisms

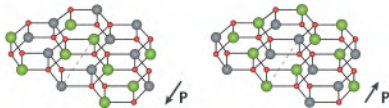
**a** Lone-pair mechanism



**b** Geometric ferroelectricity



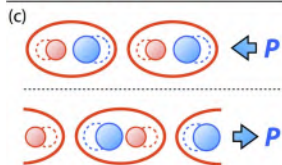
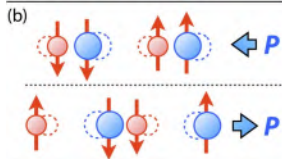
**c** Charge ordering



# Multiferroic Type II mechanisms

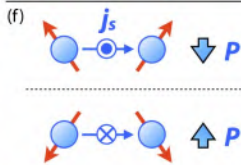
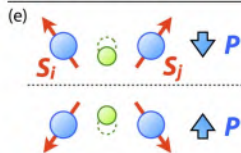
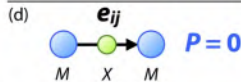
**Exchange striction model**

$$P_{ij} \propto \Pi_{ij}(S_i \cdot S_j)$$



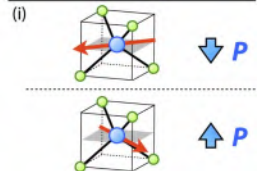
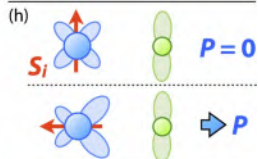
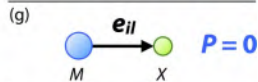
**Inverse DM model  
(Spin current model)**

$$P_{ij} \propto e_{ij} \times (S_i \times S_j)$$

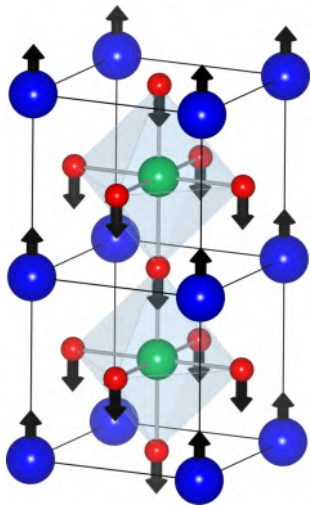


**Spin-dependent  
p-d hybridization model**

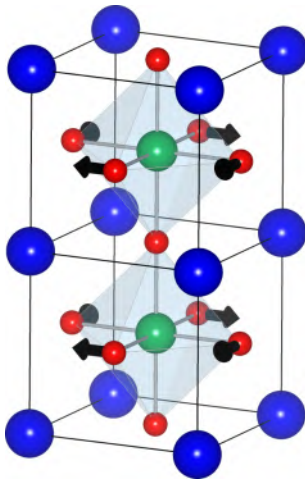
$$P_{il} \propto (S_i \cdot e_{il})^2 e_{il}$$



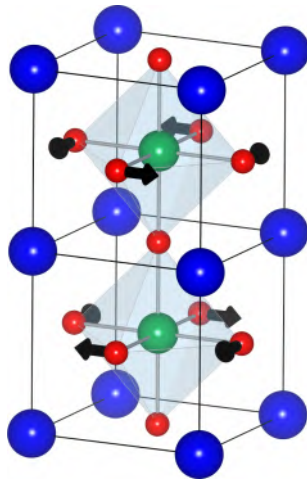
# Multiferroic Type I: Focus on cubic perovskites $\text{ABO}_3$



FE distortion



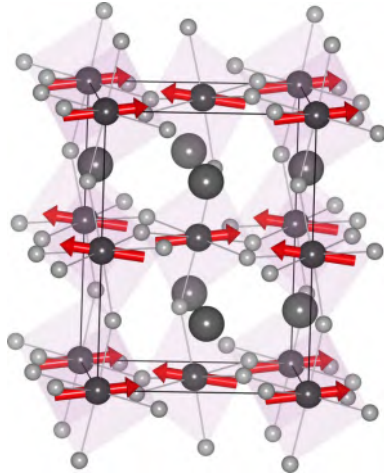
Octahedra rotation  
 $a^0 a^0 a^+$



Octahedra rotation  
 $a^0 a^0 a^-$

# Multiferroic Type I: Focus on cubic perovskites $\text{ABO}_3$

Complex pattern of distortions: how magnetism behaves?



# Magnetic interactions in cubic perovskites

Can be decomposed into 3 parts:

$$S_i \Phi_{ij} S_j = J_{ij} S_i \cdot S_j + D_{ij} (S_i \times S_j) + S_i A_{ij} S_j$$

- ▶ Exchange:  $J$
- ▶ DM:  $D$
- ▶ The rest:  $A \rightarrow$  SIA

Evaluation of  $J$ ,  $D$  and  $A$  vs distortions: DFT analysis in  $\text{AFeO}_3$

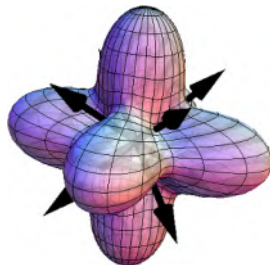
From [PRB 86, 094413 \(2012\)](#), see also [PRB 99, 104420 \(2019\)](#)

# Effect of distortions on SIA

Cubic structure: small anisotropy (4th and 6th order)

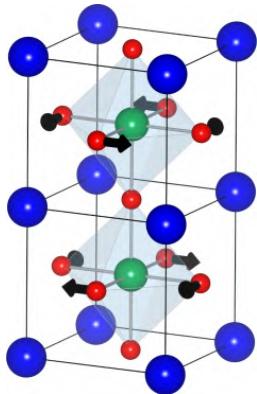
$$E_{SIA} = K_1(S_x^2 S_y^2 + S_y^2 S_z^2 + S_z^2 S_x^2) + K_2(S_x^2 S_y^2 S_z^2)$$

| ( $\mu\text{eV}$ ) | $K_1$ | $K_2$ |
|--------------------|-------|-------|
| BiFeO <sub>3</sub> | -3.66 | 0.06  |

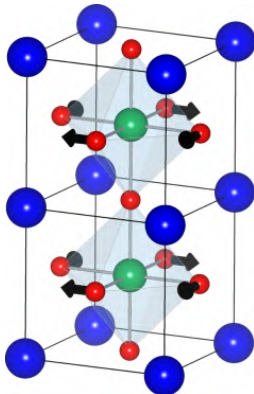


# Effect of distortions on SIA

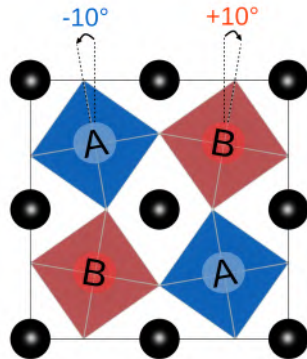
Octahedra rotation:  $a^0 a^0 c^{+/-}$



$a^0 a^0 a^-$



$a^0 a^0 a^+$



top view

# Effect of distortions on SIA

$a^0 a^0 c^{+/-}$  structures: 2<sup>nd</sup> and 4<sup>th</sup> orders

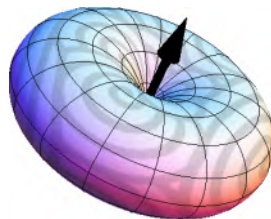
$$E_{SIA}(\theta, \phi) = K_1 \sin^2(\theta) + K'_1 \sin^2(\theta) \cos(2\phi) \\ + K_2 \sin^4(\theta) + K''_2 \sin^4(\theta) \cos(4\phi)$$

# Effect of distortions on SIA

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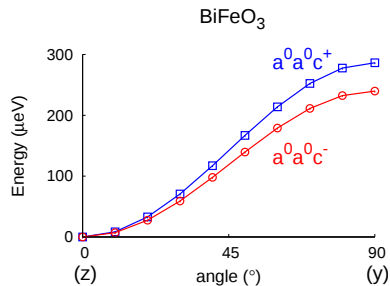
| BiFeO <sub>3</sub>                            | ( $\mu\text{eV}$ ) | $K_1$ | $K'_1$ | $K_2$ | $K''_2$ |
|-----------------------------------------------|--------------------|-------|--------|-------|---------|
| 0 <sup>0</sup> 0 <sup>0</sup> 10 <sup>+</sup> |                    | 264.0 | 0      | 3.5   | 0.7     |
| 0 <sup>0</sup> 0 <sup>0</sup> 10 <sup>-</sup> |                    | 235.3 | 0      | 4.3   | 0.8     |



$K_1 > 0 \implies$  easy axis shape

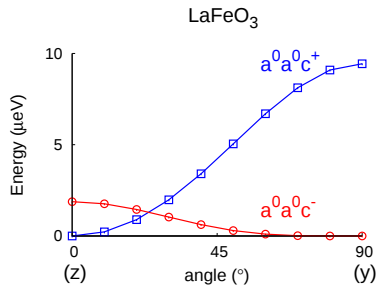
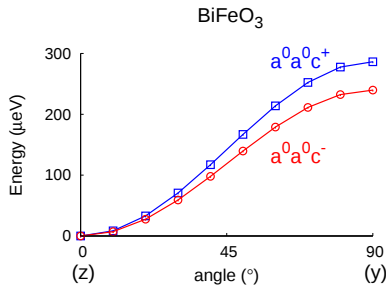
# Effect of distortions on SIA

$a^0a^0c^{+/-}$  structures: SIA shape and amplitude



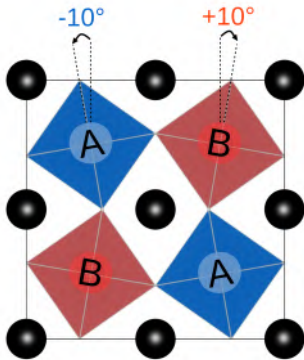
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$a^0a^0c^{+/-}$  structures: SIA shape and amplitude



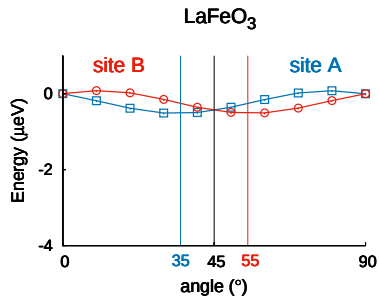
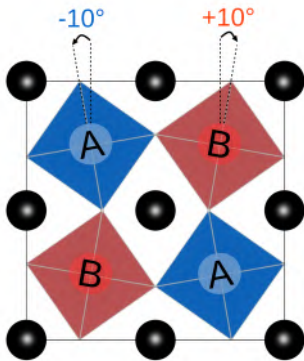
# Effect of distortions on SIA

$a^0a^0c^{+/-}$  structures: SIA shape and amplitude



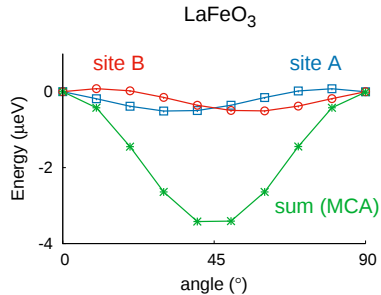
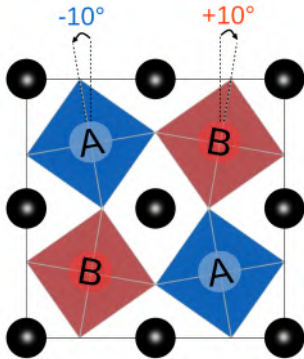
# Effect of distortions on SIA

$a^0a^0c^{+/-}$  structures: SIA shape and amplitude



# Effect of distortions on SIA

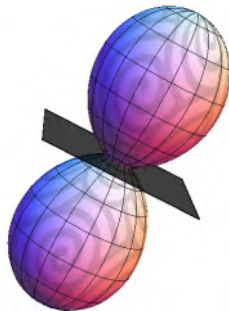
$a^0a^0c^{+/-}$  structures: SIA shape and amplitude



# Effect of distortions on SIA

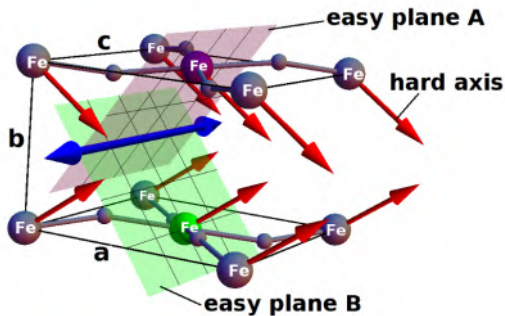
$a^-b^+a^-$  ( $Pnma$ ) and  $a^-a^-a^-$  ( $R\bar{3}c$ ) structures: easy-plane

| BiFeO <sub>3</sub>          | $K_1$ ( $\mu\text{eV}$ ) |
|-----------------------------|--------------------------|
| $Pnma$ ( $7^-8^+7^-$ )      | -402                     |
| $R\bar{3}c$ ( $9^-9^-9^-$ ) | -400                     |



# Effect of distortions on SIA

$a^- b^+ a^-$  ( $Pnma$ ) structure:



Two different easy planes locally but a global easy axis!

# Effect of FE distortions on SIA

|             |     | $K_1$ ( $\mu\text{eV}$ ) |
|-------------|-----|--------------------------|
| $9^-9^-9^-$ | BFO | -400                     |

# Effect of FE distortions on SIA

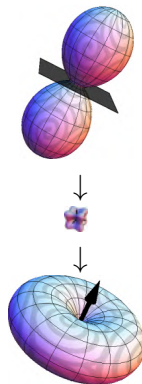
| $K_1$ ( $\mu\text{eV}$ ) |     |      |
|--------------------------|-----|------|
| $9^-9^-9^-$              | BFO | -400 |
| $9^-9^-9^-+0.5\text{FE}$ | BFO | -281 |
| $9^-9^-9^-+1.0\text{FE}$ | BFO | -1.3 |
| $9^-9^-9^-+1.5\text{FE}$ | BFO | 139  |

# Effect of FE distortions on SIA

| $K_1$ ( $\mu\text{eV}$ ) |     |      |
|--------------------------|-----|------|
| $9^-9^-9^-$              | BFO | -400 |
| $9^-9^-9^-+0.5\text{FE}$ | BFO | -281 |
| $9^-9^-9^-+1.0\text{FE}$ | BFO | -1.3 |
| $9^-9^-9^-+1.5\text{FE}$ | BFO | 139  |
| 1.0 FE                   | BFO | 217  |
| 1.5 FE                   | BFO | 349  |

# Effect of FE distortions on SIA

|                          |     | $K_1$ ( $\mu\text{eV}$ ) |
|--------------------------|-----|--------------------------|
| $9^-9^-9^-$              | BFO | -400                     |
| $9^-9^-9^-+0.5\text{FE}$ | BFO | -281                     |
| $9^-9^-9^-+1.0\text{FE}$ | BFO | -1.3                     |
| $9^-9^-9^-+1.5\text{FE}$ | BFO | 139                      |
| 1.0 FE                   | BFO | 217                      |
| 1.5 FE                   | BFO | 349                      |



Competition between FE and OR's SIA!

# Effects on $J$

|                    |                               |                                                     | $J_{ac}$ | $J_b$ | (meV) |
|--------------------|-------------------------------|-----------------------------------------------------|----------|-------|-------|
| BiFeO <sub>3</sub> | cubic                         | (0 <sup>0</sup> 0 <sup>0</sup> 0 <sup>0</sup> )     | 7.36     | –     |       |
|                    | <i>Pnma</i>                   | (7 <sup>-</sup> 8 <sup>+</sup> 7 <sup>-</sup> )     | 6.52     | 6.68  |       |
|                    | <i>R<math>\bar{3}c</math></i> | (9 <sup>-</sup> 9 <sup>-</sup> 9 <sup>-</sup> )     | 5.96     | –     |       |
|                    | <i>R3c</i>                    | (9 <sup>-</sup> 9 <sup>-</sup> 9 <sup>-</sup> + FE) | 5.36     | –     |       |

$J$  decreases with OR distortions because Fe–O–Fe bond angle  $< 180^\circ$

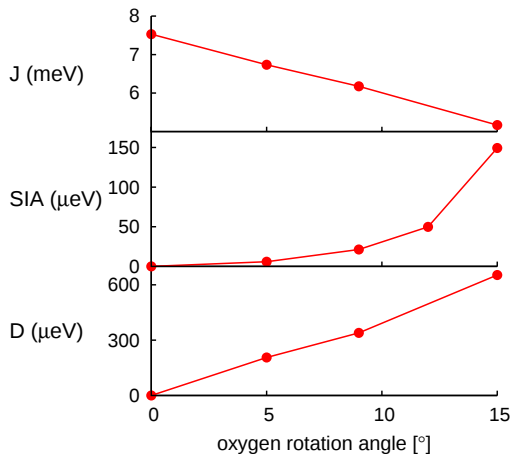
# Effects on DM

|                    |                               |                                                   | $D_x$ | $D_y$ | $D_z$ | ( $\mu\text{eV}$ ) |
|--------------------|-------------------------------|---------------------------------------------------|-------|-------|-------|--------------------|
| BiFeO <sub>3</sub> | cubic                         | (0 <sup>0</sup> 0 <sup>0</sup> 0 <sup>0</sup> )   | 0     | 0     | 0     |                    |
|                    | <i>Pnma</i>                   | (7 <sup>-</sup> 8 <sup>+</sup> 7 <sup>-</sup> )   | 454   | 208   | 124   |                    |
|                    | <i>R<math>\bar{3}c</math></i> | (9 <sup>-</sup> 9 <sup>-</sup> 9 <sup>-</sup> )   | 170   | 170   | 170   |                    |
|                    | <i>R3c</i>                    | (9 <sup>-</sup> 9 <sup>-</sup> 9 <sup>-</sup> FE) | 146   | 146   | 146   |                    |

DMI increases with OR distortions because Fe–O–Fe bond angle goes away from 180°

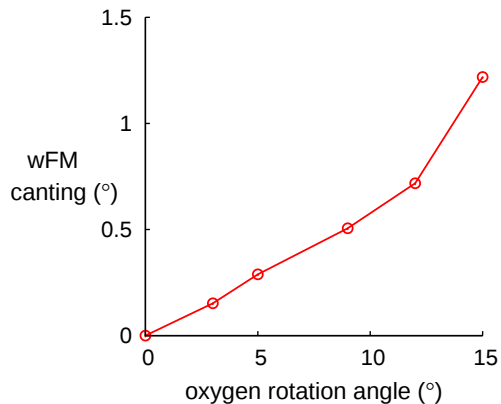
# Effect of distortions on wFM

$J$ , DM and SIA vs OR amplitude in  $R\bar{3}c$ :



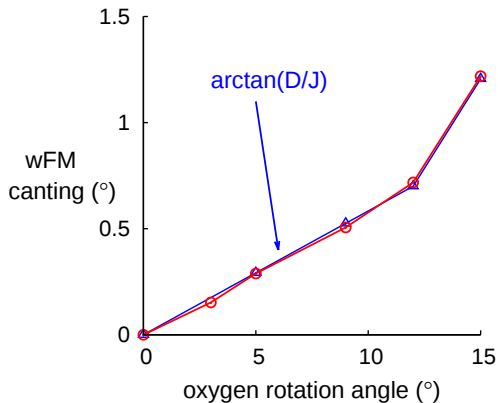
# Effect of distortions on wFM

wFM vs AFD amplitude in  $R\bar{3}c$ :



# Effect of distortions on wFM

wFM vs AFD amplitude in  $R\bar{3}c$ :



$$\text{wFM} = \arctan(D/J)$$

# Effect of distortions on wFM

Microscopic model: PRL 109, 037207 (2012)

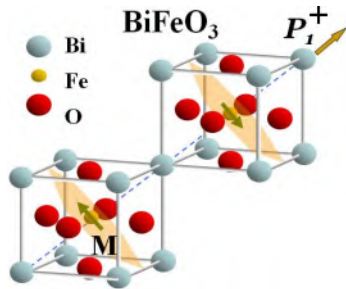
Coupling with the octahedra rotations  $\omega$ :

$$D_{wFM} \propto (\omega_i - \omega_j) \cdot (\mathbf{S}_i \times \mathbf{S}_j)$$

Coupling with the polar distortions  $\mathbf{u}$  (“Spin-Current”):

$$D_{SC} \propto (\mathbf{u}_i - \mathbf{e}_{ij}) \cdot (\mathbf{S}_i \times \mathbf{S}_j)$$

# Multiferroic perovskites: $\text{BiFeO}_3$



$\text{BiFeO}_3$  ( $R3c$ )

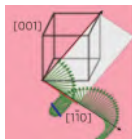
$\text{Fe}^{3+} \rightarrow 3d^5$

G-type AFM + ferroelectricity

$\rightarrow$  multiferroic at room temperature ( $T_{\text{FE}} = 1100 \text{ K}$ ,  $T_N = 640 \text{ K}$ )

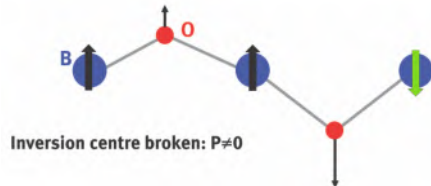
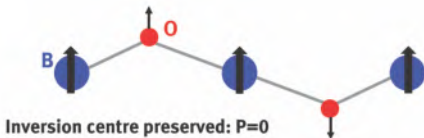
+ Spin cycloid!

from Spin-current driven DMI  
[PRB 108, 024403 \(2023\)](#)

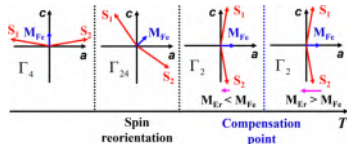
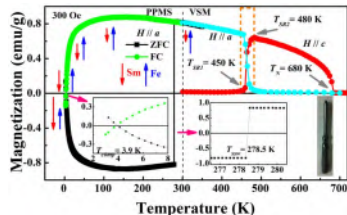
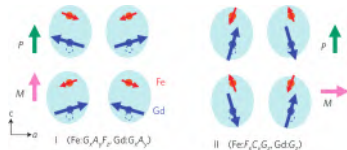


# Multiferroic type II perovskites

From exchange striction



# Rare Earth perovskites: $R\text{FeO}_3$



$R = \text{La, Ce, Pr, Nd, Sm, Eu, Gd, Tb, Dy, Ho, Er, Tm, Yb and Lu}$

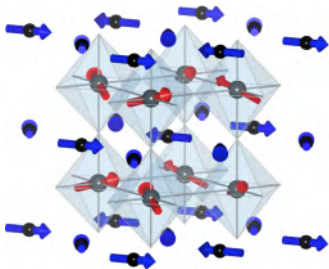
G-type AFM + weak FM of the  $TM$  cation

Interaction between  $R$   $f$  electron spins and  $TM$   $d$  electron spins

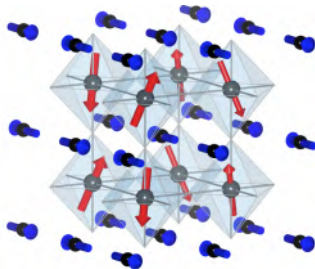
Spin reorientation and compensation point of the wFM

# Rare Earth perovskites: $R\text{FeO}_3$

Multiferroicity due to the presence of both  $R$  and Fe magnetic atoms  
(exchange-striction):



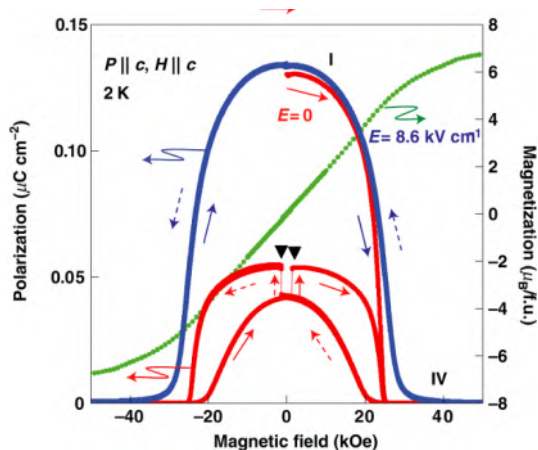
Fe:  $\mathbf{G}_x \mathbf{A}_y \mathbf{F}_z$  ; Gd:  $\mathbf{G}_x \mathbf{A}_y$   
 $\mathbf{M} \parallel \mathbf{z}$  ;  $\mathbf{P} \parallel \mathbf{z}$



Fe:  $\mathbf{F}_x \mathbf{C}_y \mathbf{G}_z$  ; Gd:  $\mathbf{G}_z$   
 $\mathbf{M} \parallel \mathbf{x}$  ;  $\mathbf{P} \parallel \mathbf{x}$

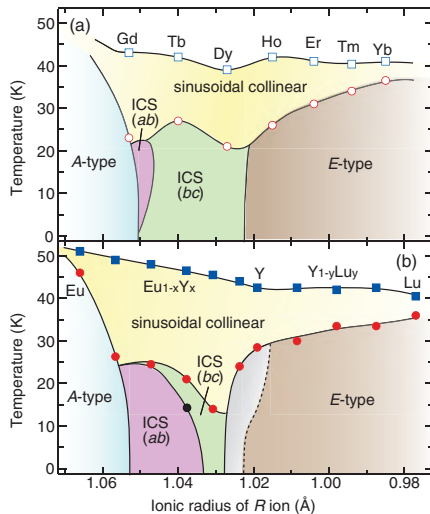
# Rare Earth perovskites: $R\text{FeO}_3$

Strong magnetoelectric coupling ( $\text{GdFeO}_3$ ):



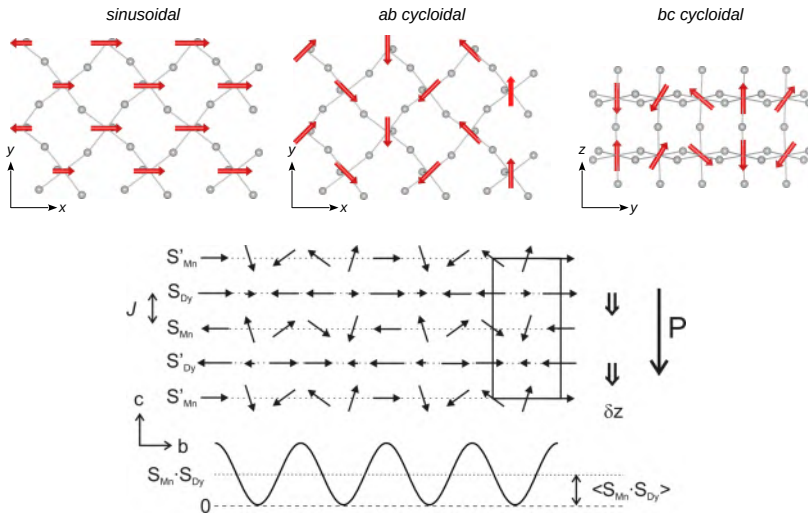
# Rare Earth perovskites: $RMnO_3$

Rich magnetic phase diagram:



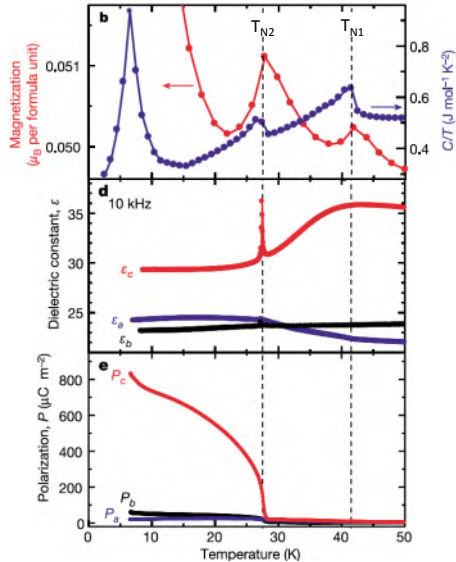
# Rare Earth perovskites: $RMnO_3$

Spiral orders induces ferroelectricity (spin-current & exchange-striction):



# Rare Earth perovskites: $RMnO_3$

$TbMnO_3$ :  
(spin-current model)



# Conclusion

- ▶ Multiferroics, in the extended definition, can exhibit numerous possibilities
- ▶ Magnetoelectric multiferroics

## Going beyond:

- ▶ Strain and interface engineering of new multiferroics
- ▶ Skyrmions (both magnetic and electric)
- ▶ Composites (mixing FE and FM materials)
- ▶ 2D materials
- ▶ Type III Multiferroics?

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