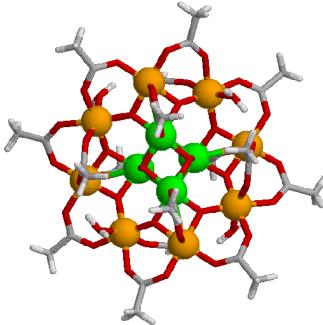
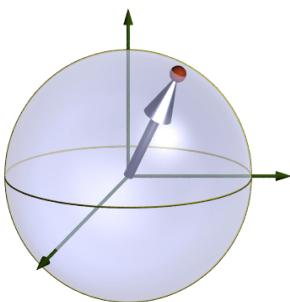
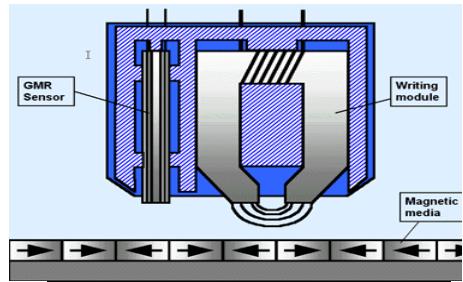
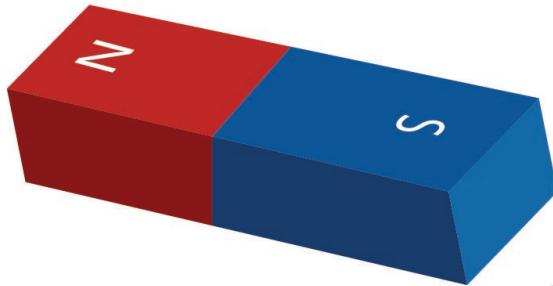


Molecular magnets: physics and applications

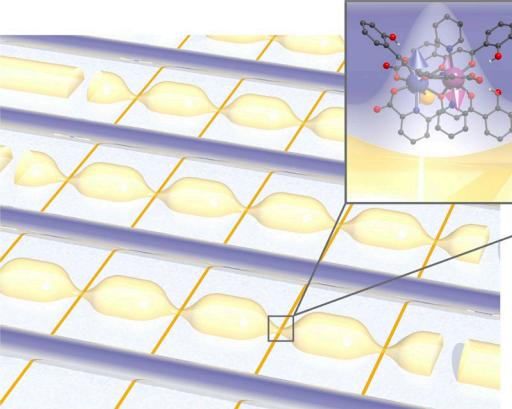


Fernando LUIS

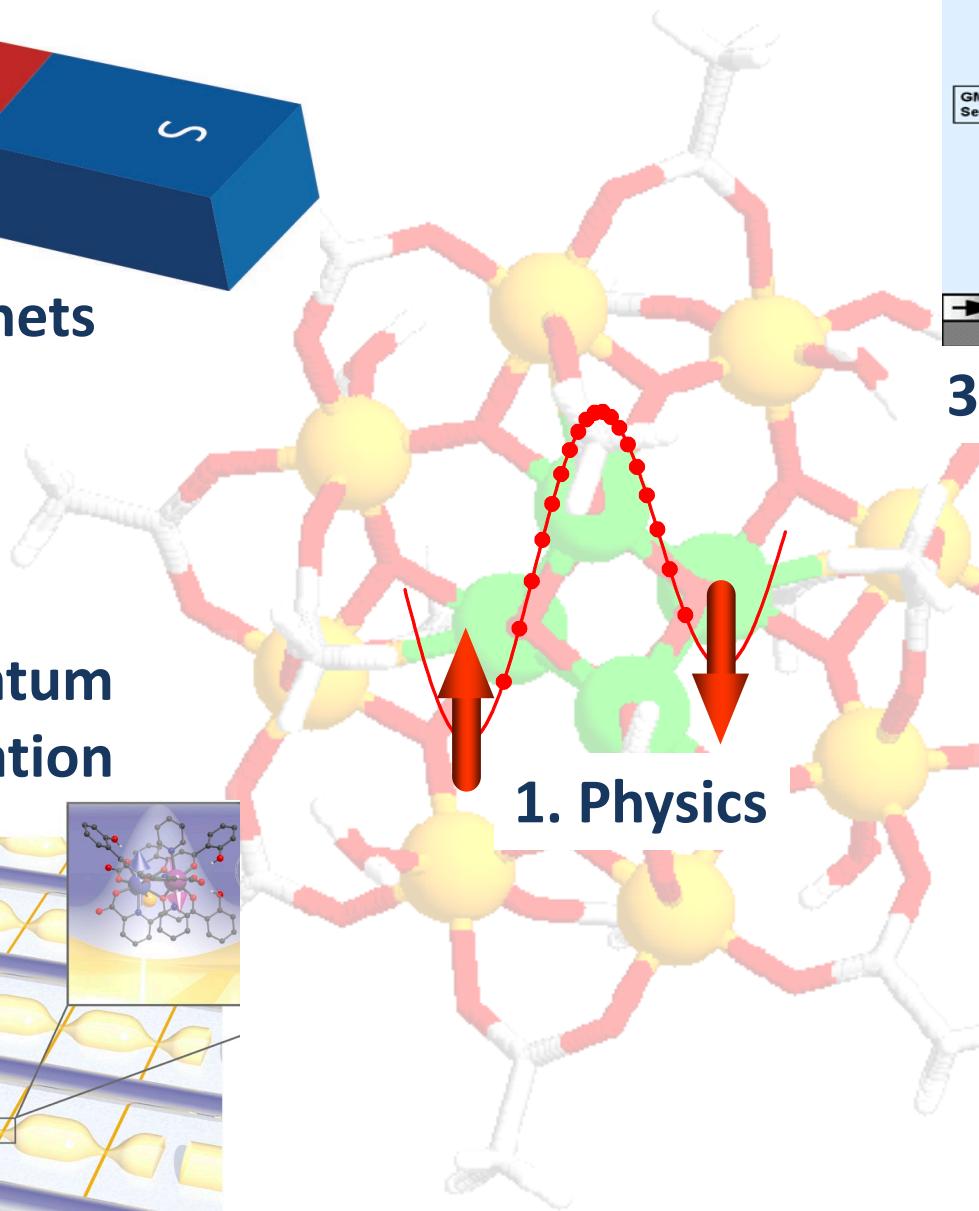
*Instituto de Nanociencia y
Materiales de Aragón*



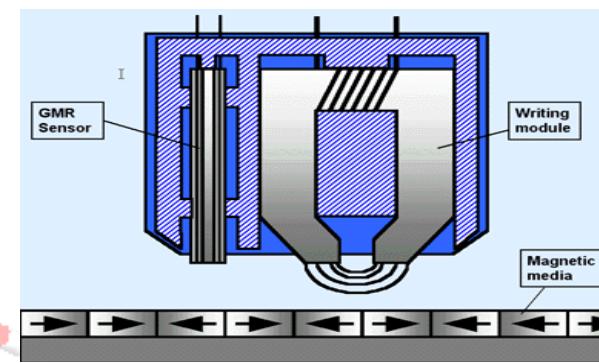
2. Magnets



4. Quantum information



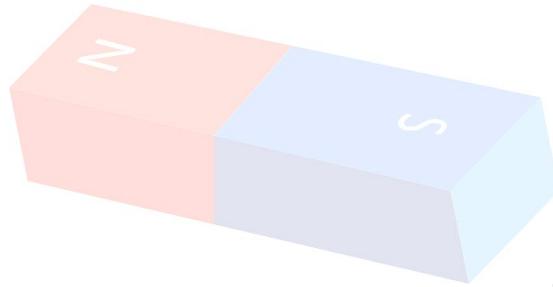
1. Physics



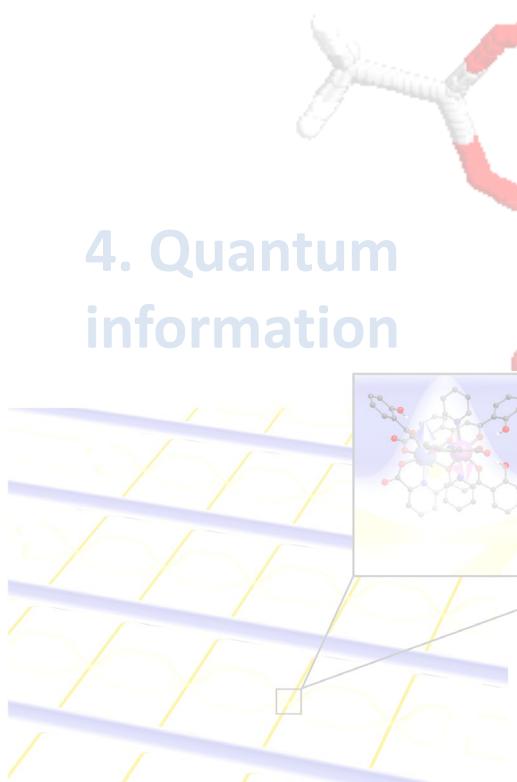
3. Magnetic recording

5. Magnetic refrigeration

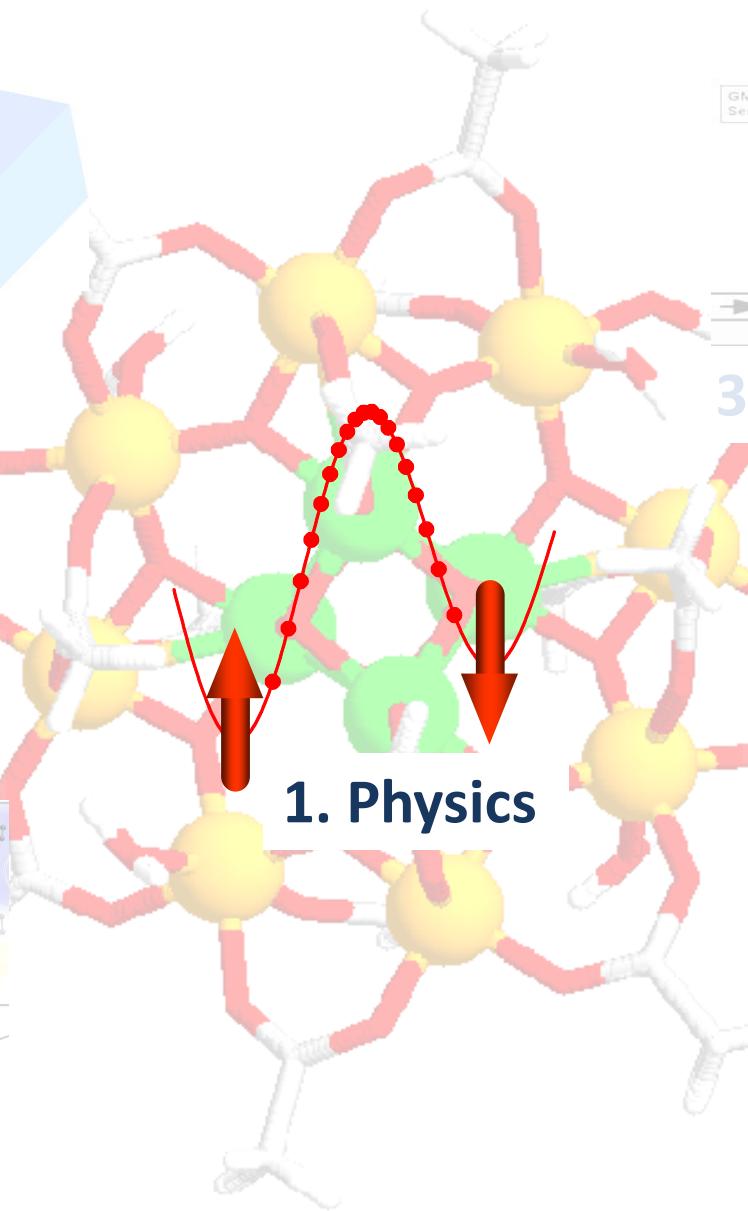




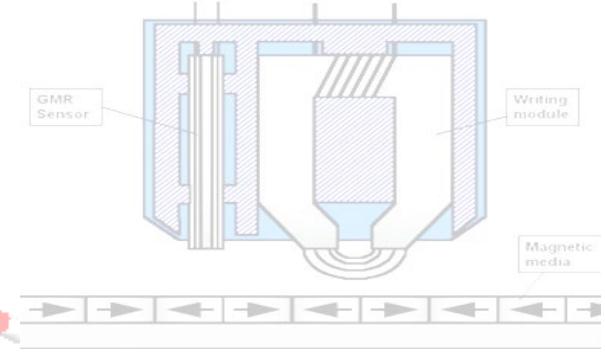
2. Magnets



4. Quantum information



1. Physics



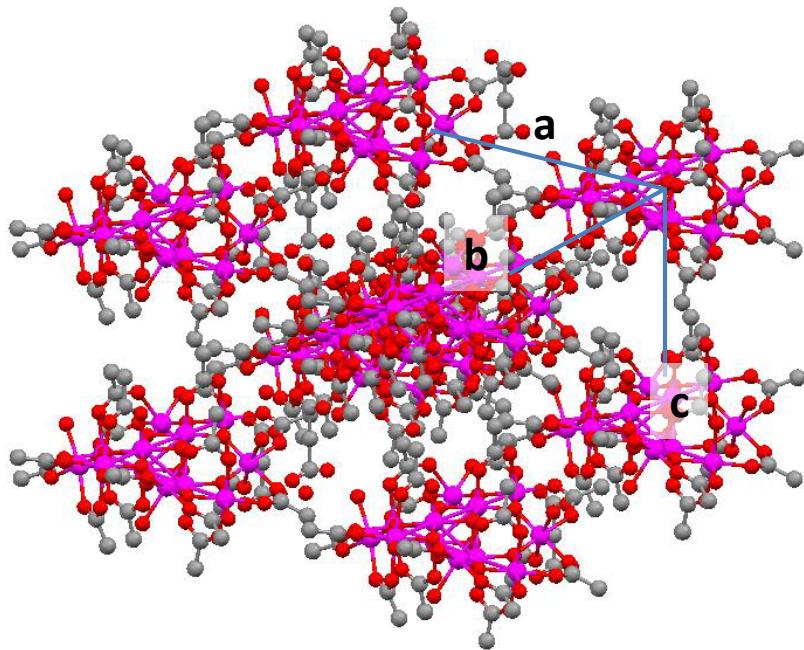
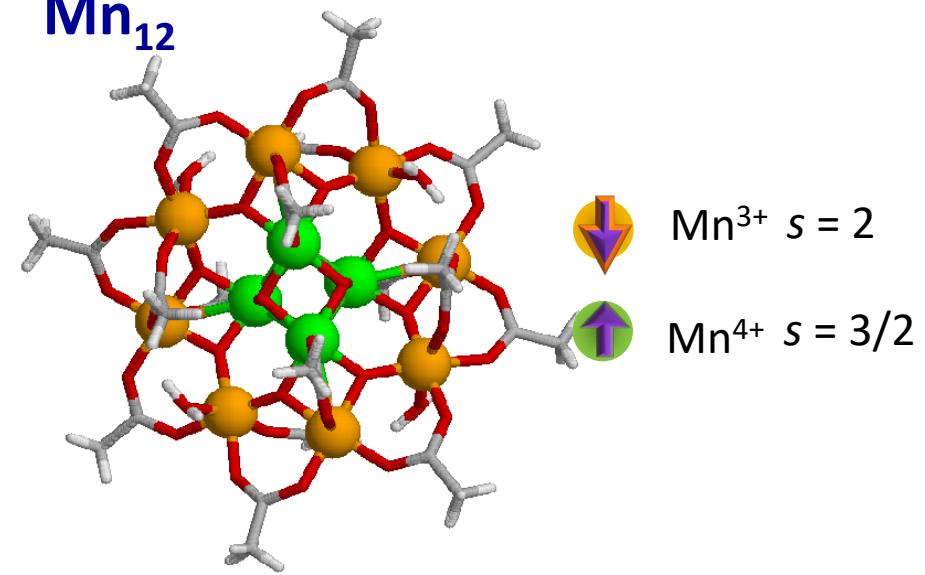
3. Magnetic recording



5. Magnetic refrigeration

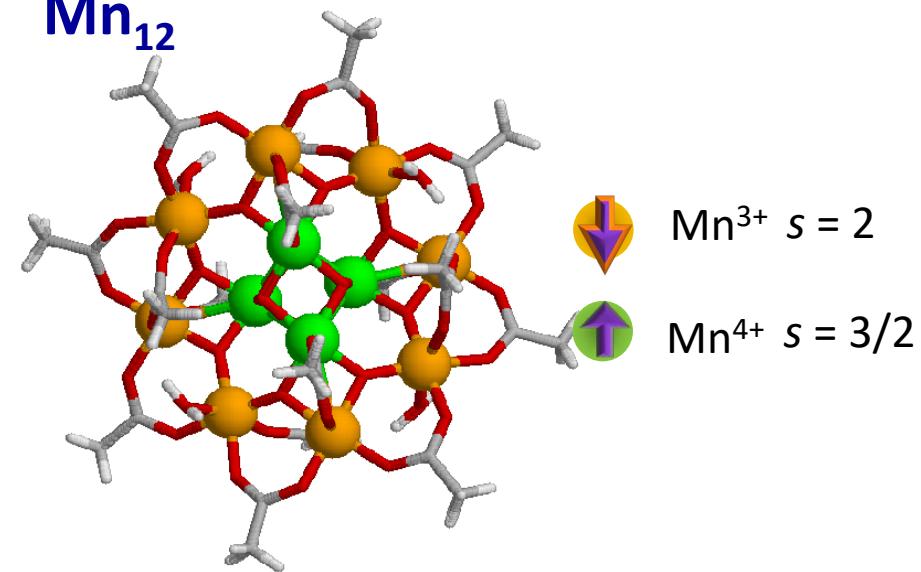
T. Lis, Acta Crystallogr. Sect. B 36, 2042 (1980)

Mn₁₂

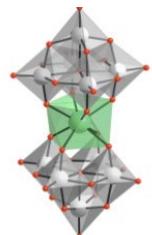


T. Lis, Acta Crystallogr. Sect. B 36, 2042 (1980)

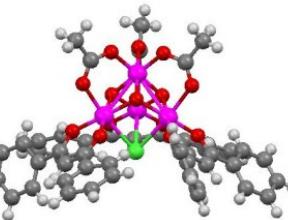
Mn₁₂



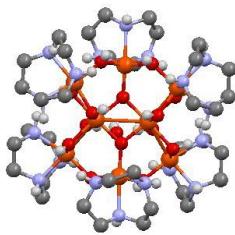
ErW₁₀



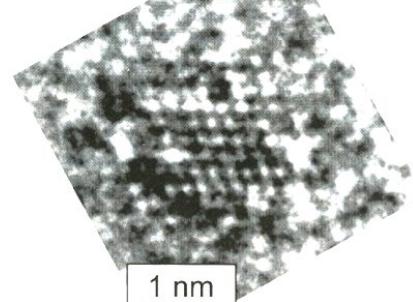
Mn₄Cl



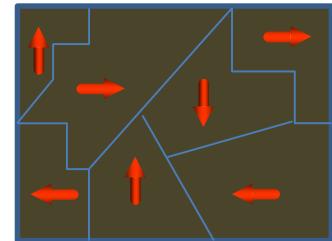
Fe₈



Co nanoparticle



Magnet



0.1 nm

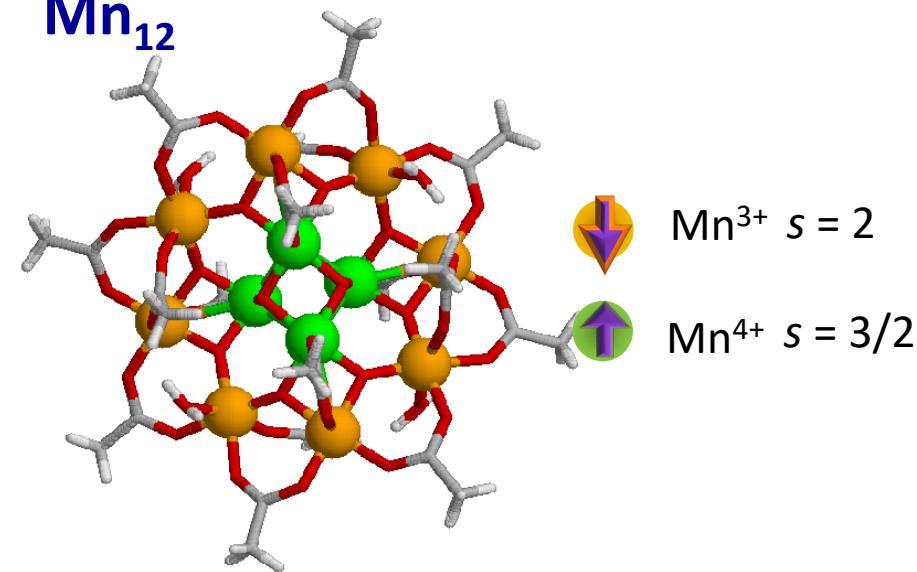
1 nm

10 nm

> 100 nm

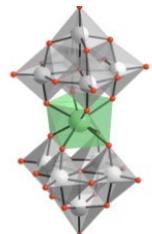
T. Lis, Acta Crystallogr. Sect. B 36, 2042 (1980)

Mn₁₂

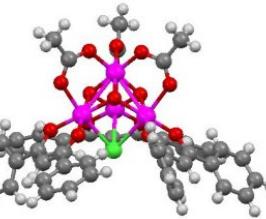


- Mesoscopic size
- Monodisperse
- Chemical design

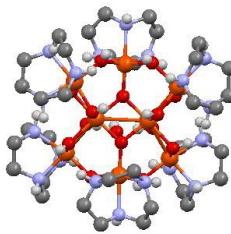
ErW₁₀



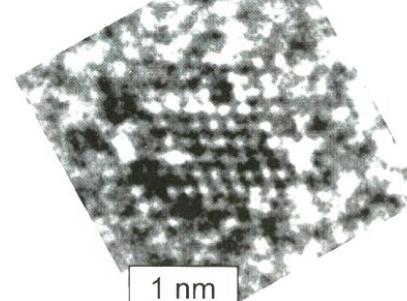
Mn₄Cl



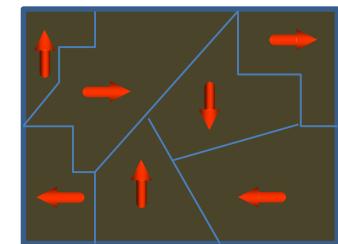
Fe₈



Co nanoparticle



Magnet

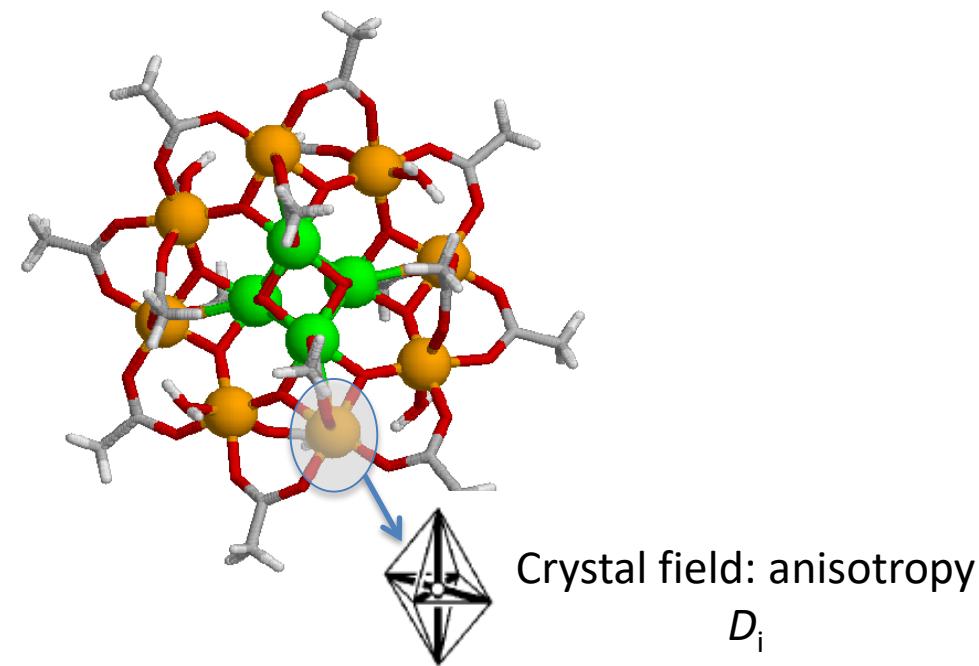


0.1 nm

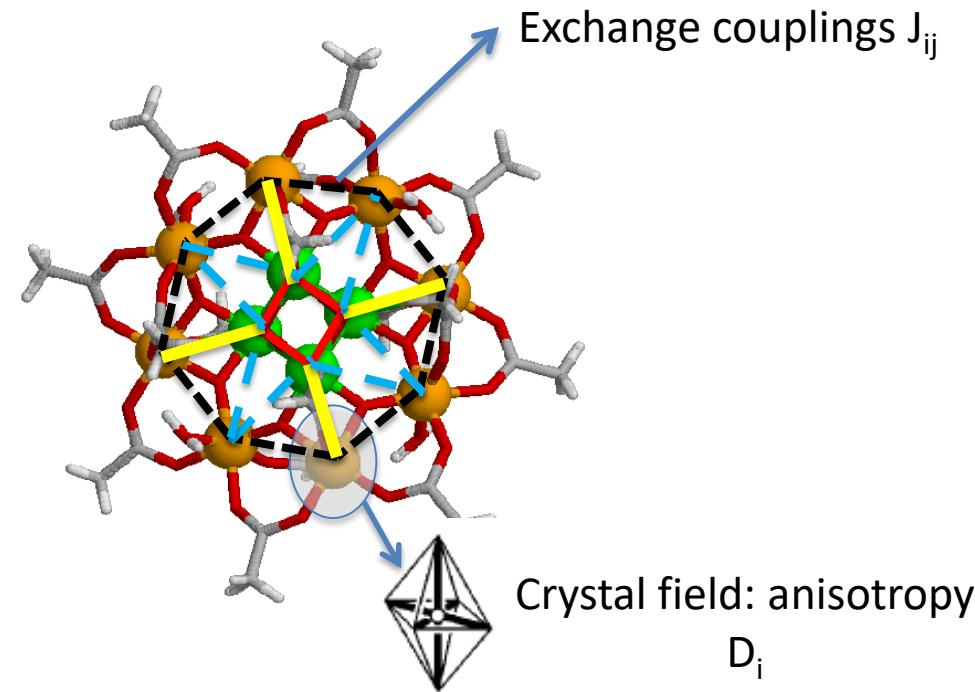
1 nm

10 nm

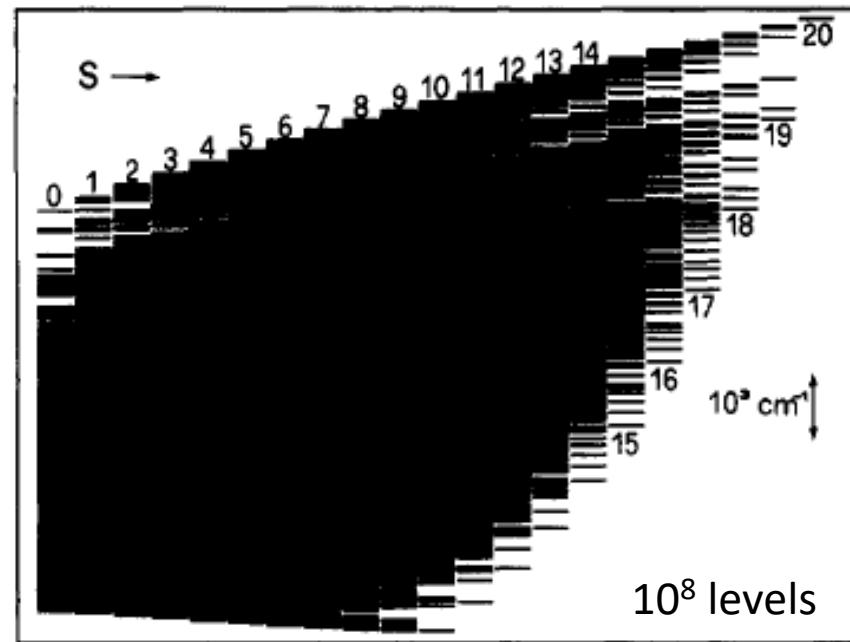
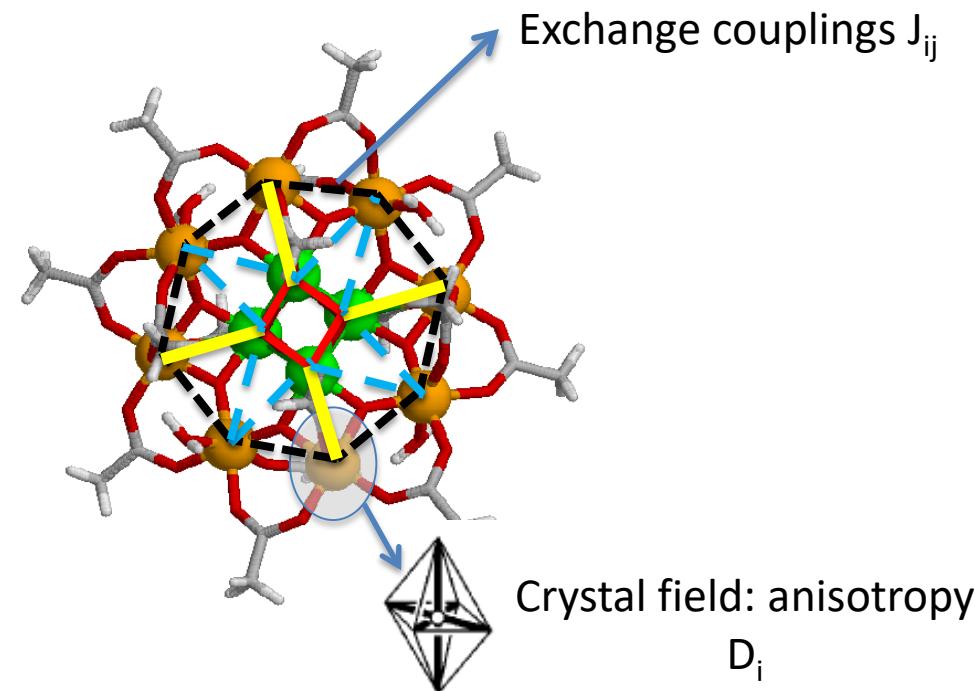
> 100 nm



$$\mathcal{H} = \sum_{i=1}^n \vec{s}_i \widehat{D_i} \vec{s}_i$$



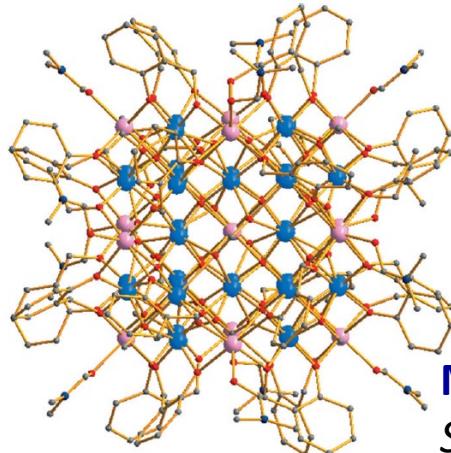
$$\mathcal{H} = \sum_{i=1}^n \widehat{\vec{s}_i D_i \vec{s}_i} + \sum_{i \neq j}^n \widehat{\vec{s}_i J_{ij} \vec{s}_j}$$



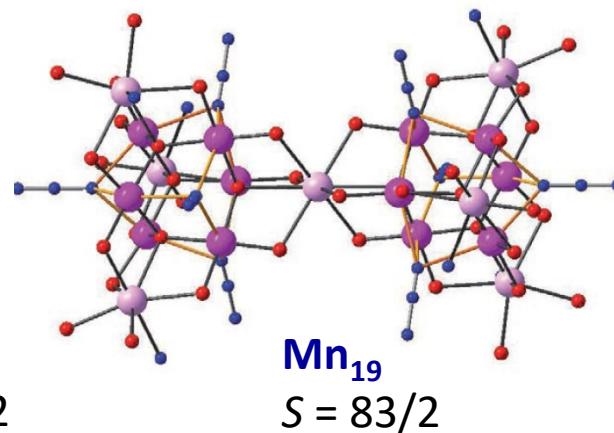
$$\mathcal{H} = \sum_{i=1}^n \vec{s}_i \widehat{D_i} \vec{s}_i + \sum_{i \neq j}^n \vec{s}_i \widehat{J_{ij}} \vec{s}_j$$

- R. Sessoli, H.-L. Tsai, A.R. Shake, S. Wang, J.B. Vincent, K. Folting, D. Gatteschi, G. Christou, D.N. Hendrickson, *J. Am. Chem. Soc.* **115**, 1804 (1993).
- M.I. Katsnelson, V.V. Dobrovitski, B.N. Harmon, *Phys. Rev. B* **59**, 6919 (1999).
- V. V. Mazurenko, Y. O. Kvashnin, Fengping Jin, H. A. De Raedt, A. I. Lichtenstein, and M. I. Katsnelson, *Phys. Rev. B* **89**, 214422 (2014)
- O. Hanebaum and J. Schnack, *Phys. Rev. B* **92**, 064424 (2015)

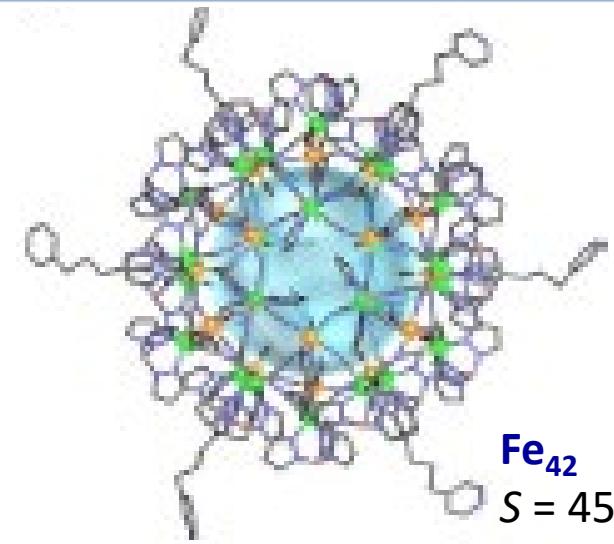
Record spin values



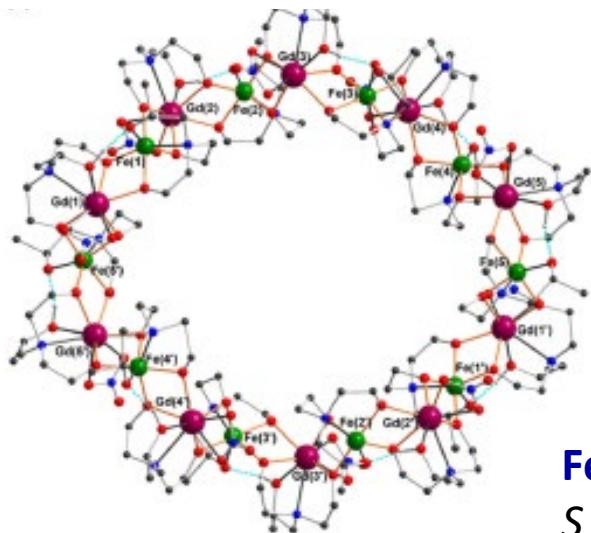
M. Manoli et al, Angew. Chem. **55**, 679 (2016)



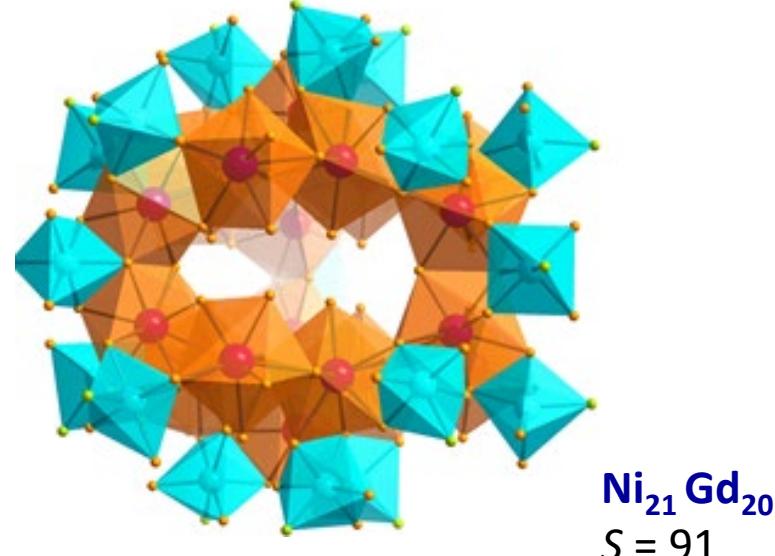
A. M. Ako et al, Angew. Chem. **45**, 4926 (2006)



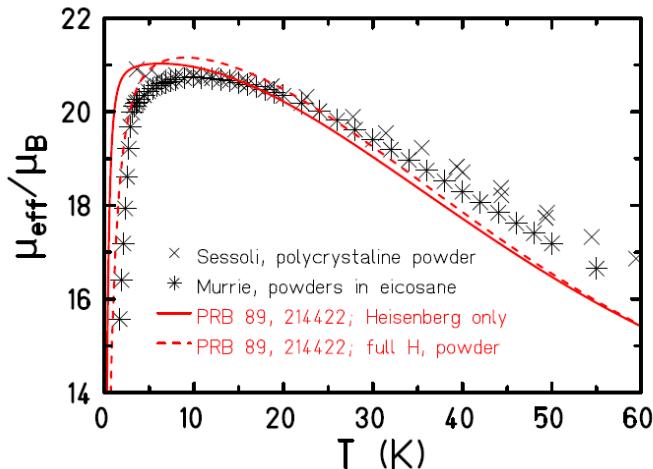
A. M. Ako et al, Nat. Commun. **6**, 5955 (2015)



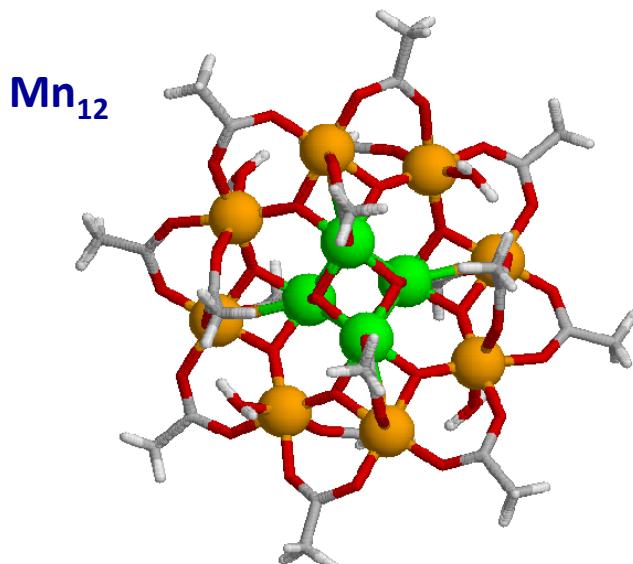
A. Baniodeh et al, npj Quant. Mater. **3**, 10 (2018)



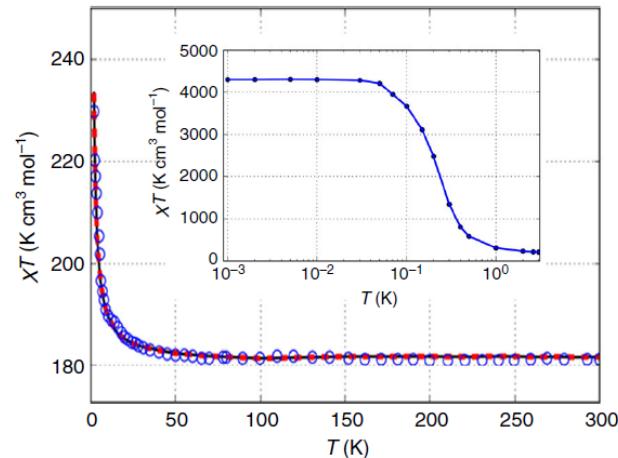
W. P. Chen et al, Nat. Commun. **9**, 2107 (2018)



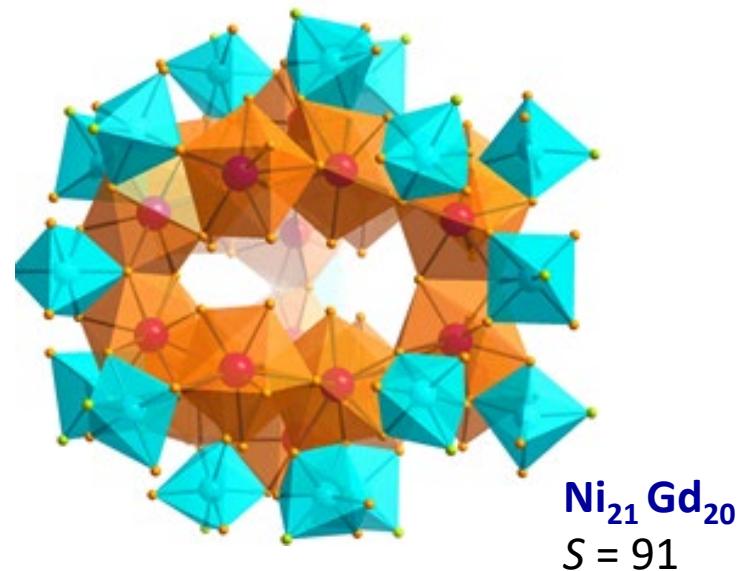
Lanczos approximate diagonalization method



O. Hanebaum and J. Schnack, Phys. Rev. B **92**, 064424 (2015)

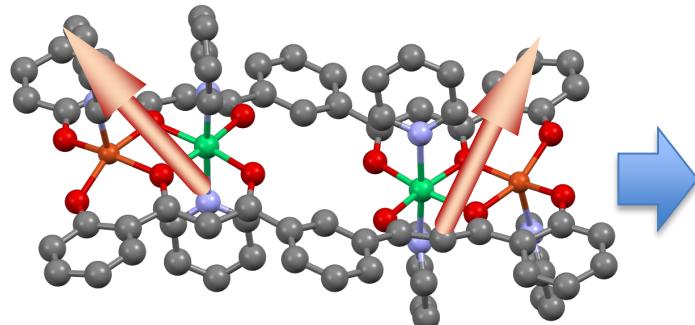


Quantum Monte Carlo simulations

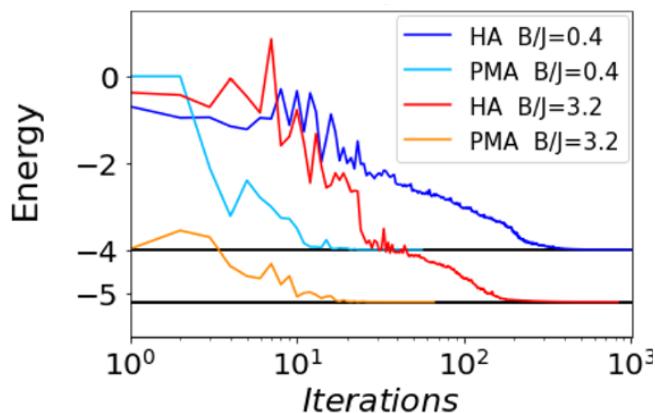


W. P. Chen et al, Nat. Commun. **9**, 2107 (2018)

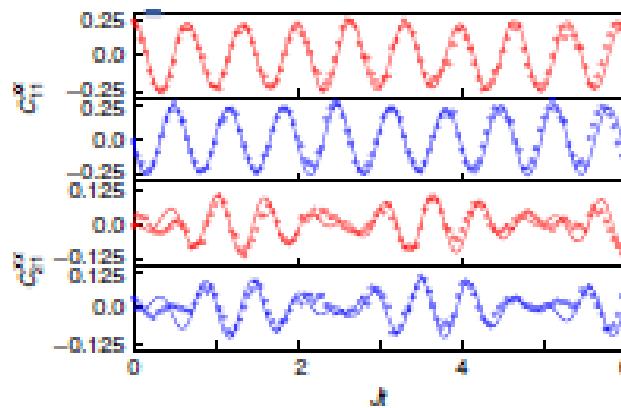
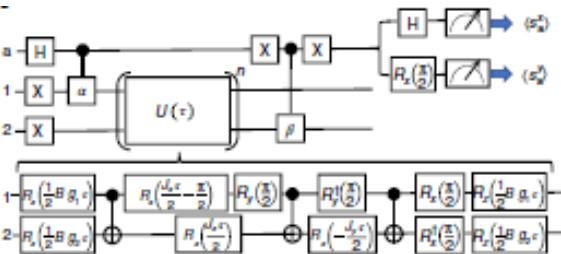
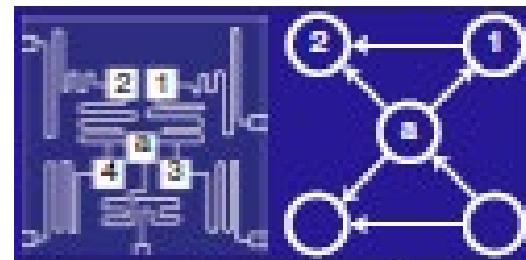
Molecular dimer of two coupled $S = \frac{1}{2}$ spins



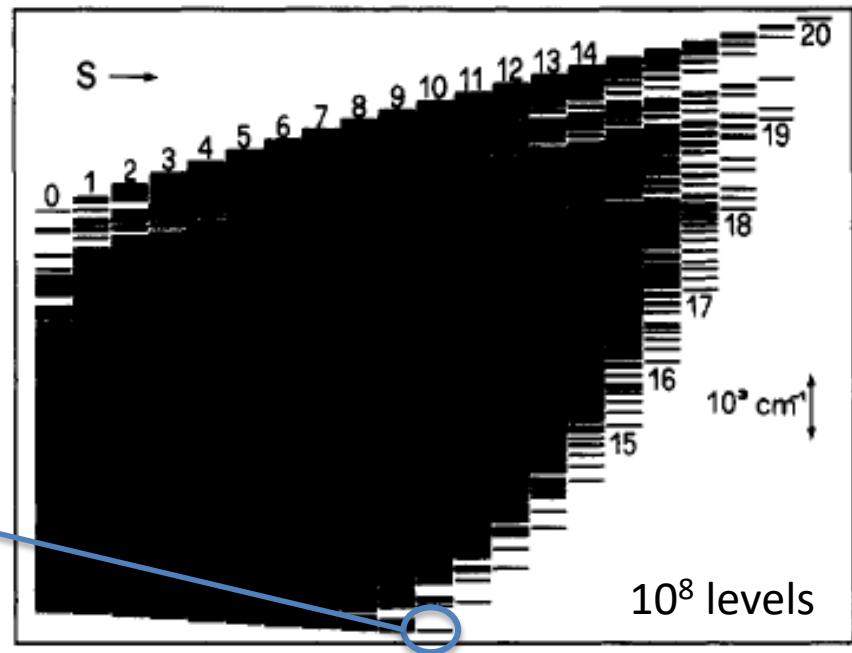
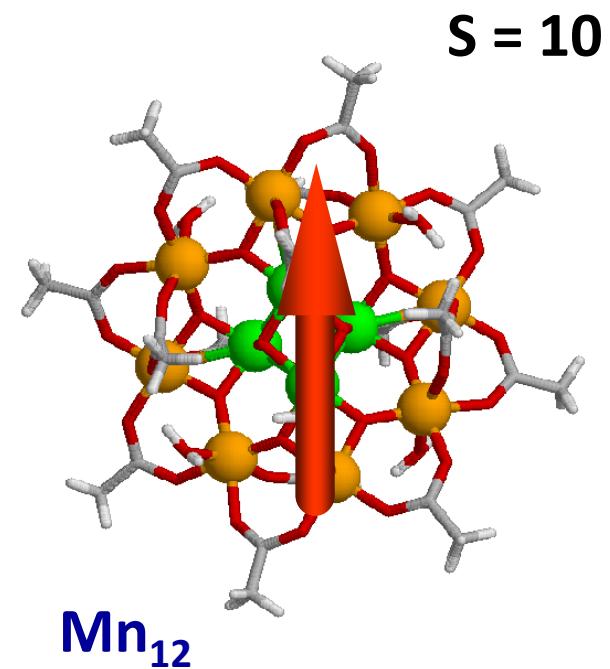
$$\mathcal{H} = \vec{s}_1 \hat{\jmath} \vec{s}_2$$



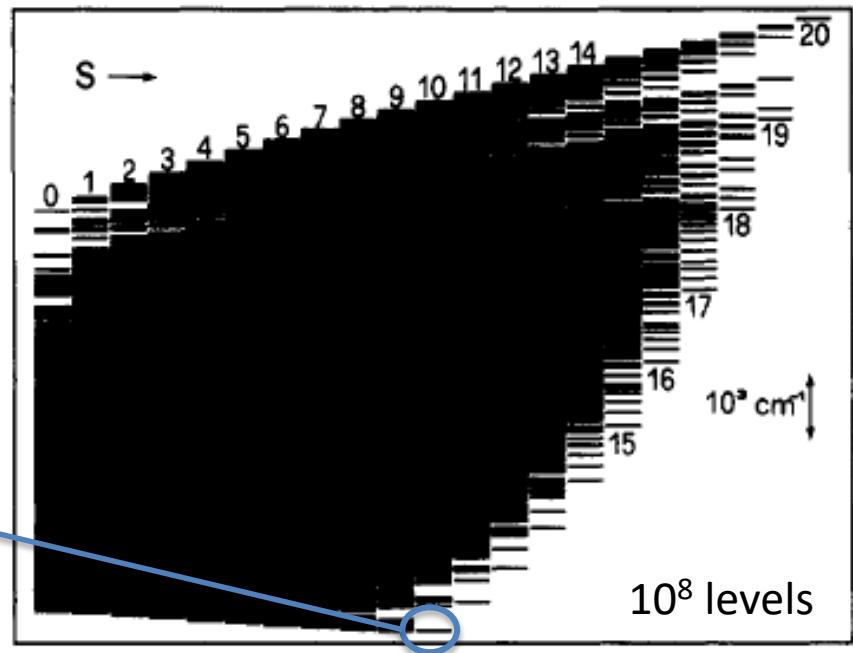
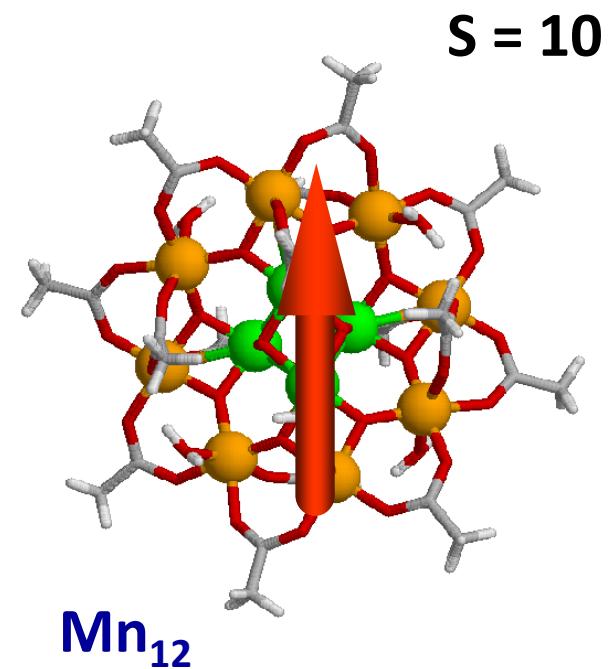
Ibmqx4 processor



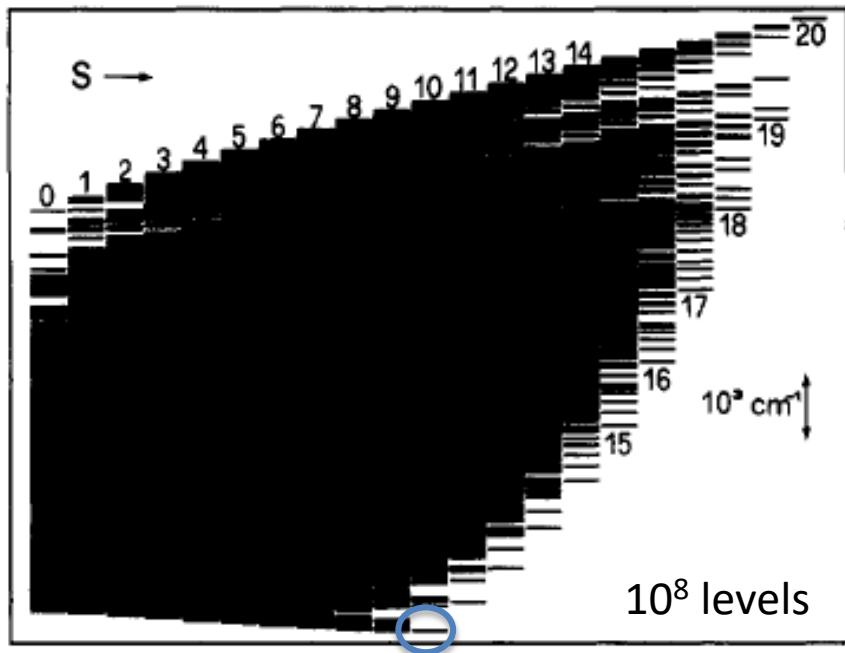
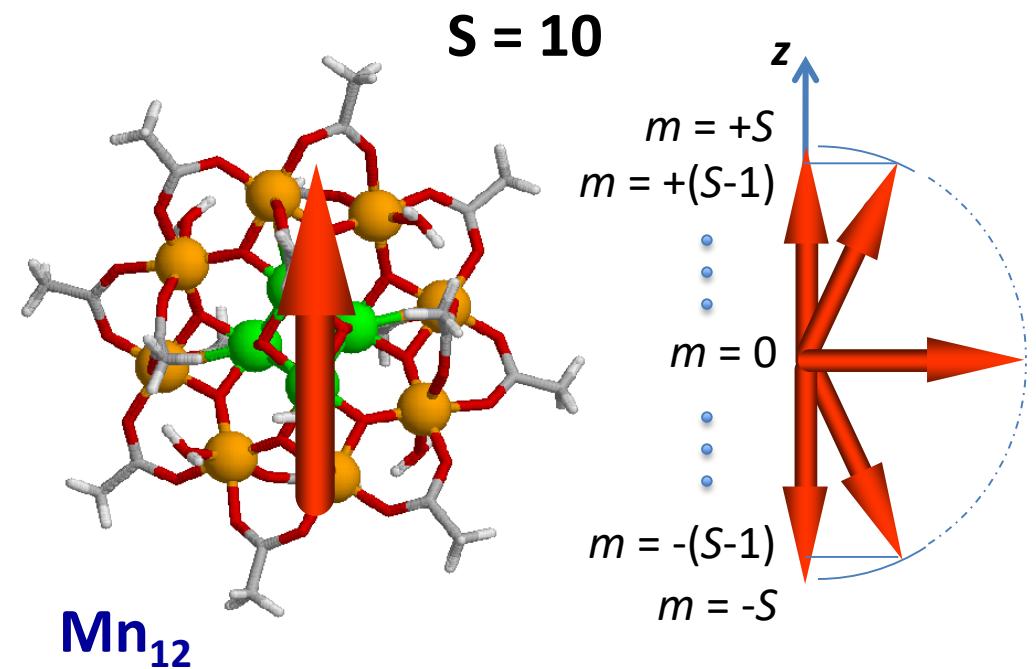
“Giant spin” approximation



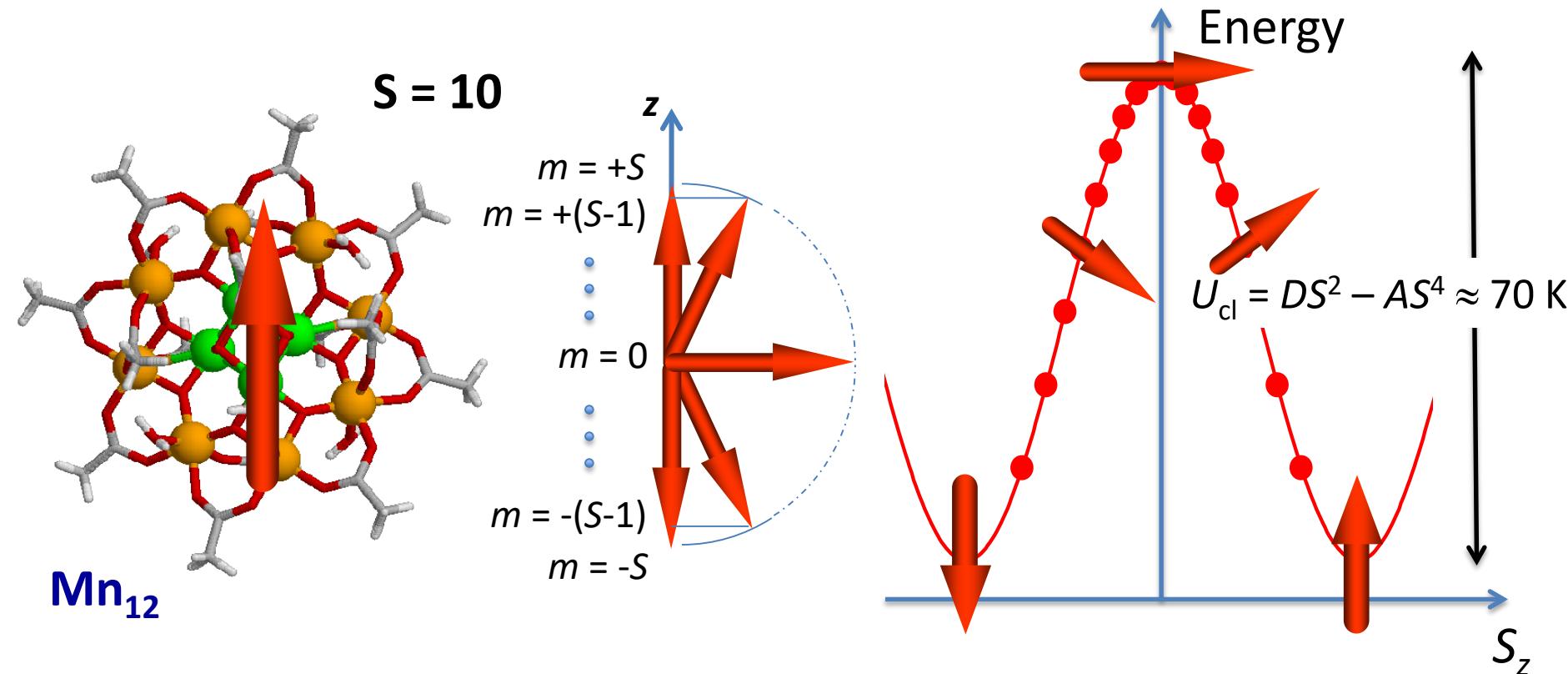
$$\mathcal{H} = \sum_{i=1}^n \vec{s}_i \widehat{D_i} \vec{s}_i + \sum_{i \neq j}^n \vec{s}_i \times \vec{s}_j$$



$$\mathcal{H} \approx -DS_z^2 + AS_z^4 + C(S_x^4 + S_y^4)$$

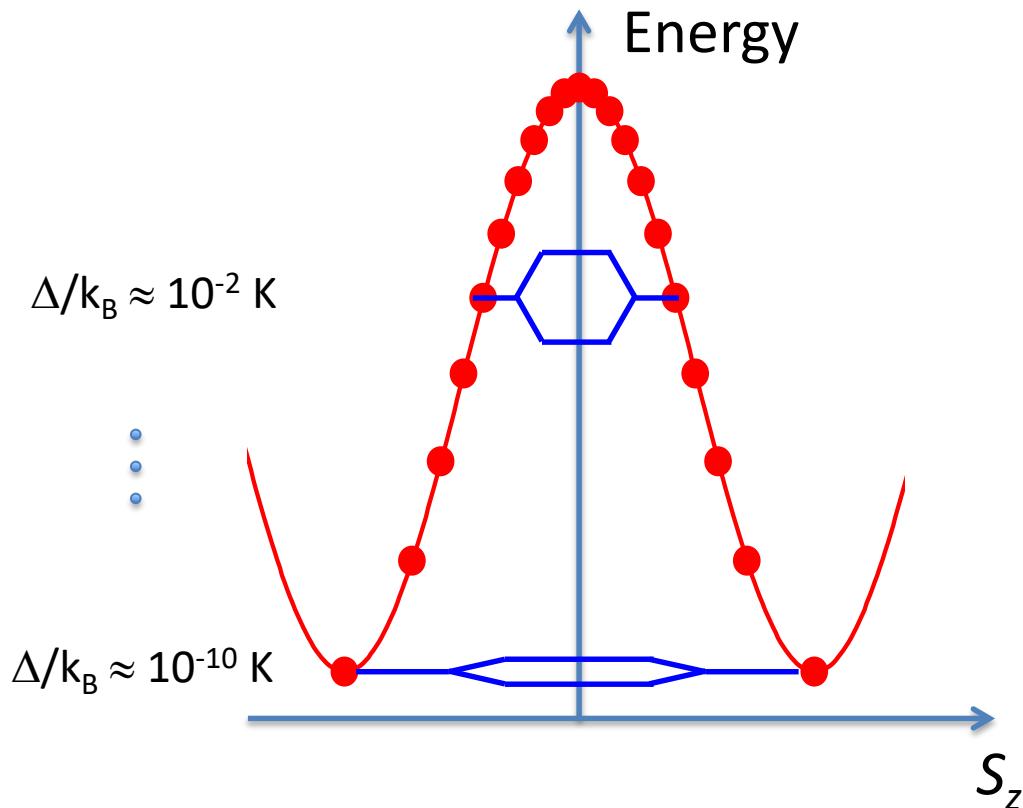
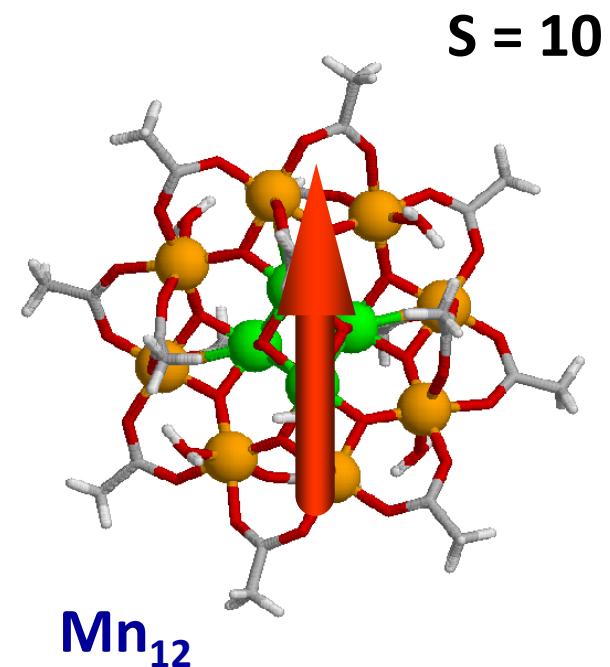


$$\mathcal{H} \approx -DS_z^2 + AS_z^4 + C(S_x^4 + S_y^4)$$



$$\mathcal{H} \approx -DS_z^2 + AS_z^4 + C(S_x^4 + S_y^4)$$

R. Sessoli, D. Gatteschi, A. Caneschi and M. A. Novak, Nature **365**, 141 (1993); F. Hartmann-Boutron, P. Politi and J. Villain, Int- J. Mod. Phys. **10**, 2577 (1996).

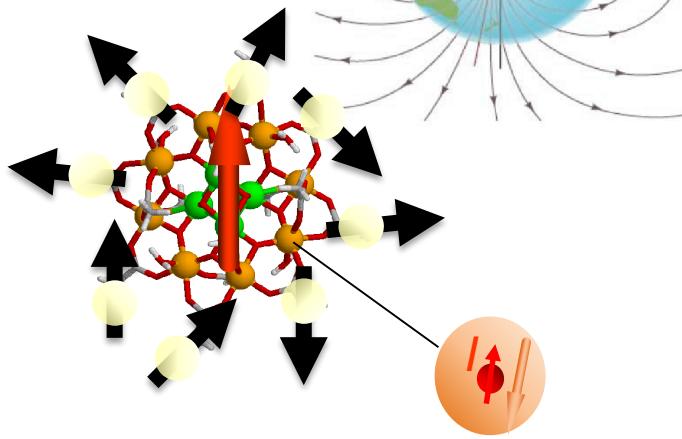


$$\mathcal{H} \approx -DS_z^2 + AS_z^4 + C(S_x^4 + S_y^4)$$

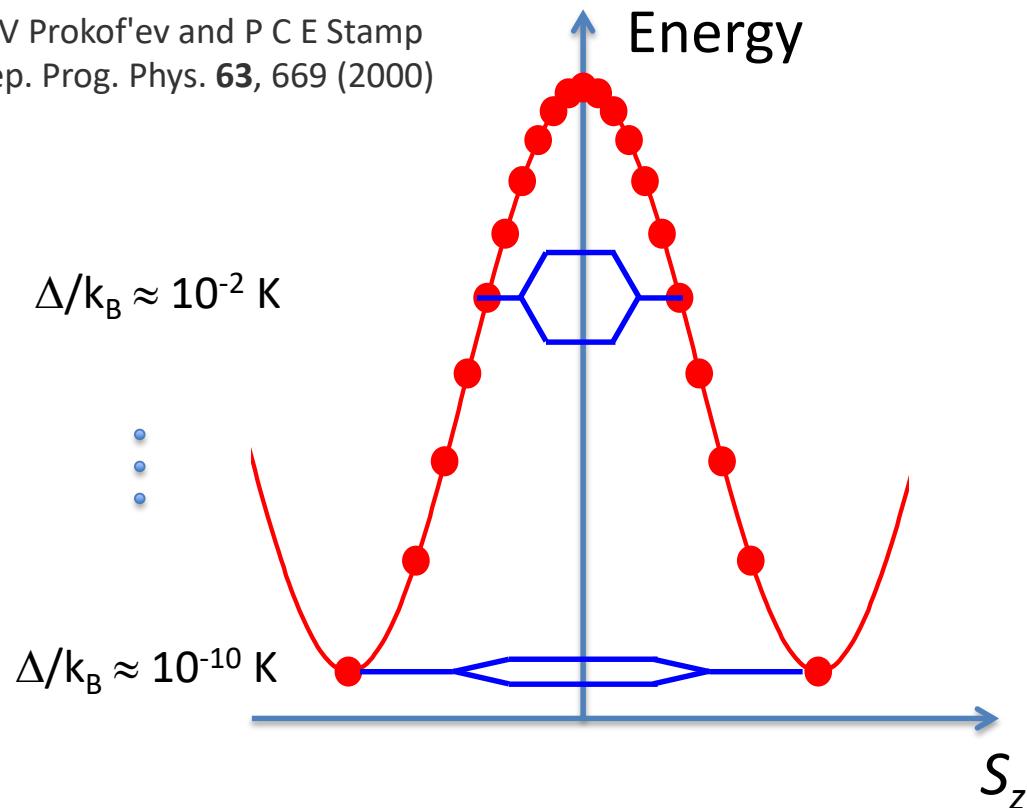
R. Sessoli, D. Gatteschi, A. Caneschi and M. A. Novak, Nature **365**, 141 (1993); F. Hartmann-Boutron, P. Politi and J. Villain, Int- J. Mod. Phys. **10**, 2577 (1996).

Magnetic anisotropy: off-diagonal terms

Environmental fields

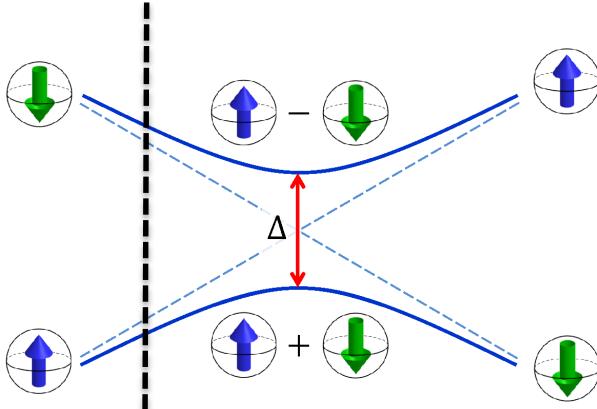
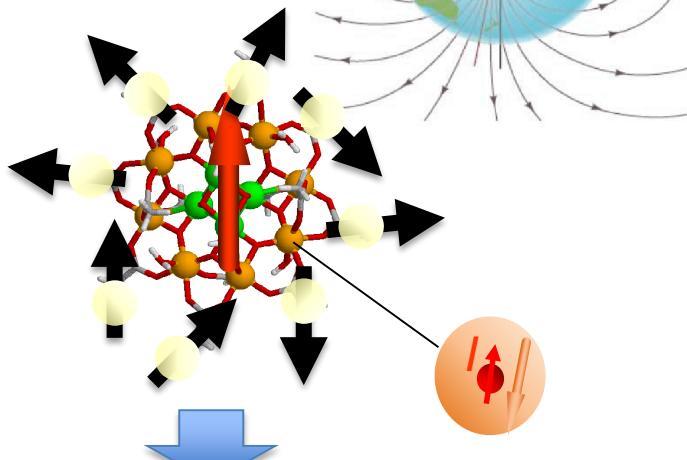
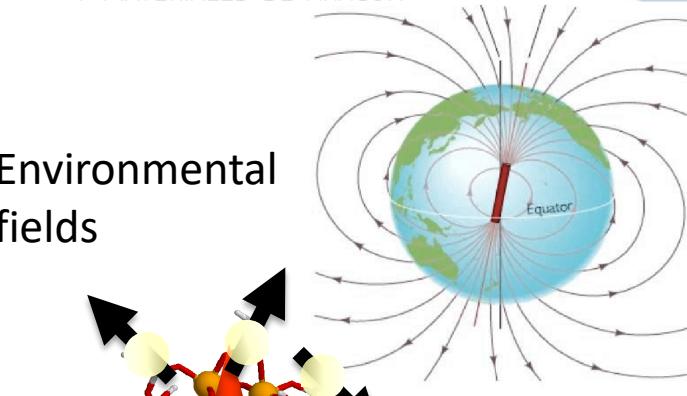


N V Prokof'ev and P C E Stamp
Rep. Prog. Phys. **63**, 669 (2000)

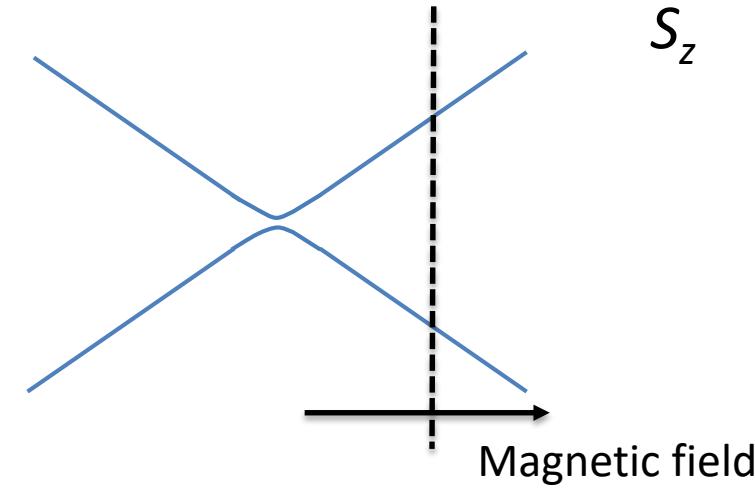
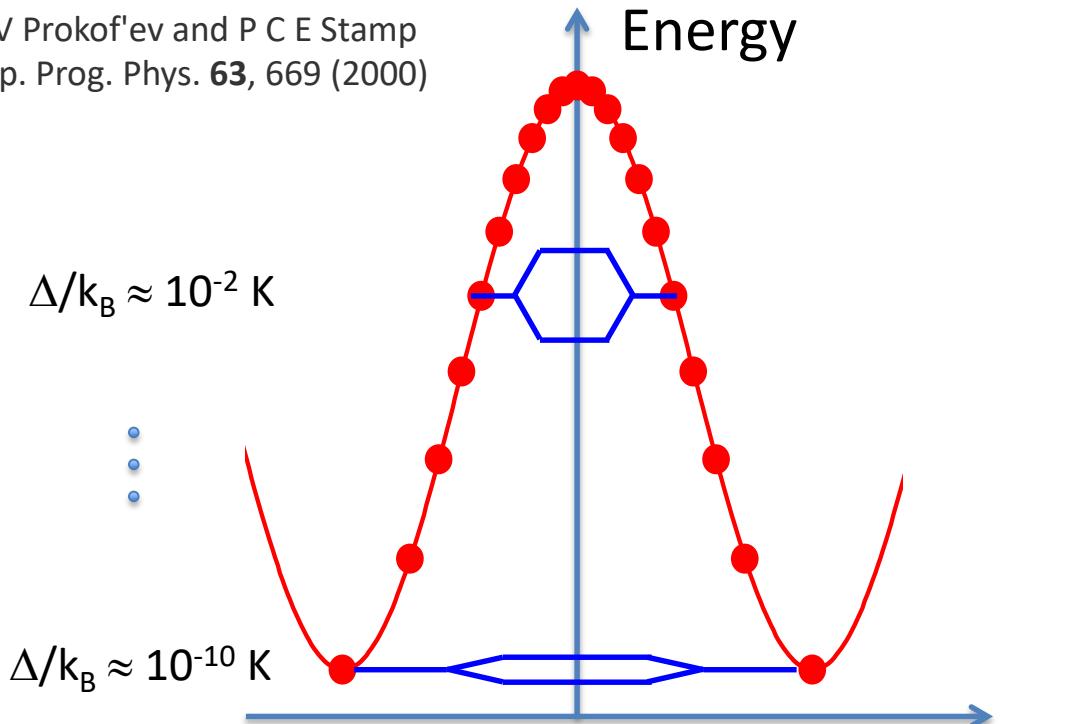


Magnetic anisotropy:
off-diagonal terms

Environmental fields

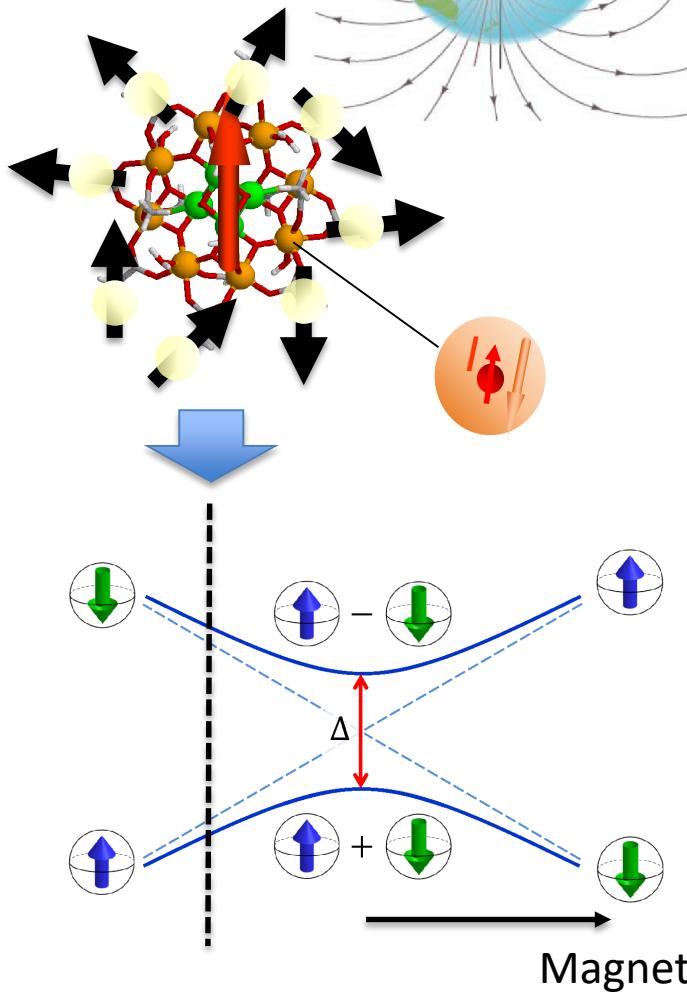


Magnetic field

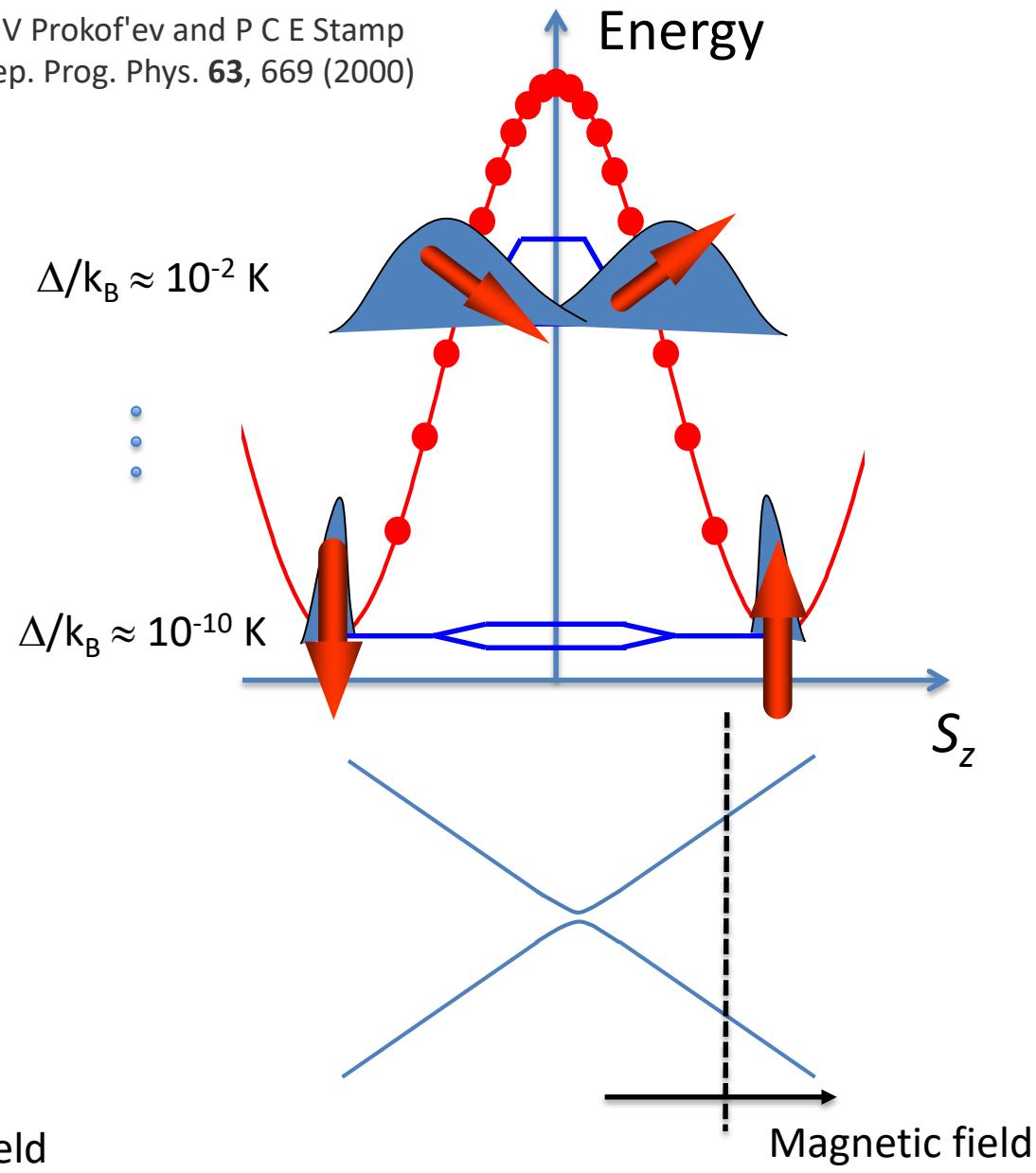
N V Prokof'ev and P C E Stamp
Rep. Prog. Phys. **63**, 669 (2000)

Magnetic field

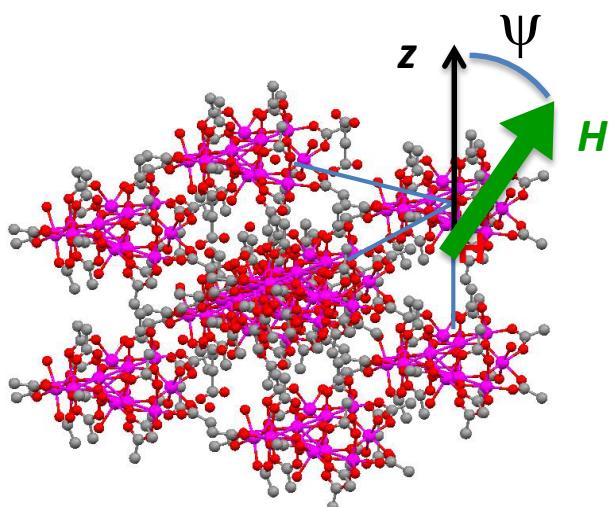
Environmental fields

Magnetic anisotropy:
off-diagonal terms

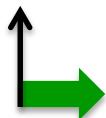
N V Prokof'ev and P C E Stamp
Rep. Prog. Phys. **63**, 669 (2000)



Angle-dependent response

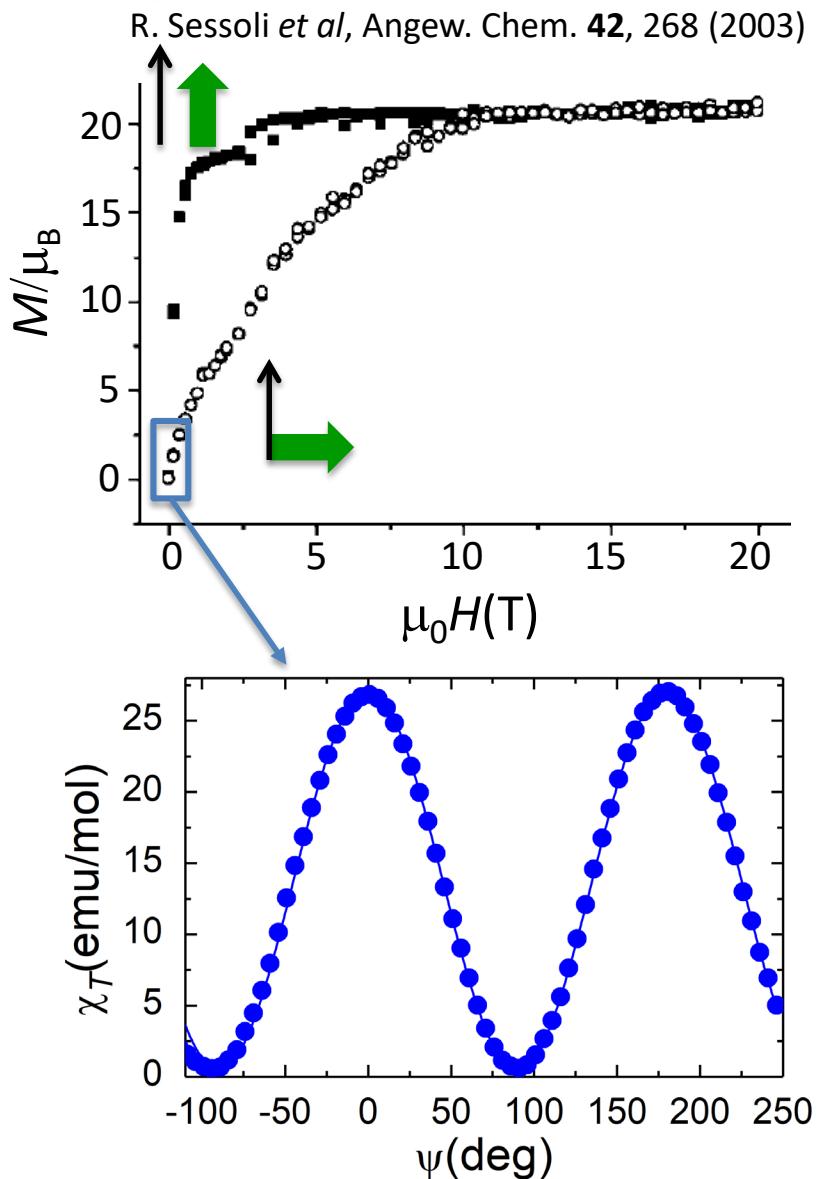


$$\mathcal{H} \approx \mathcal{H}_{\text{anis}} - g\mu_B \vec{H} \vec{S}$$

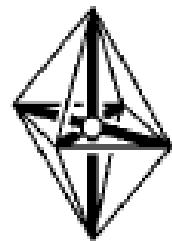
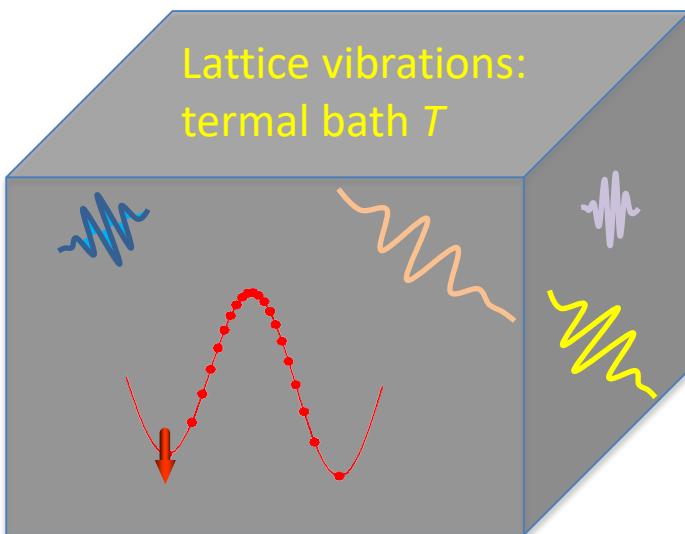


$$\chi_{\perp} \simeq \frac{Ng\mu_B S}{H_k}$$

$$\chi_{zz} \simeq \frac{N(g\mu_B S)^2}{k_B T}$$



Magnetic relaxation



Modulation of the magnetic anisotropy



Spin-phonon interaction

Master equation for spin level populations P_i

$$\frac{dP_i}{dt} = \sum_{j \neq i}^{2S+1} \Gamma_{i \leftarrow j} P_j - \sum_{j \neq i}^{2S+1} \Gamma_{j \leftarrow i} P_i$$



$$M \simeq M_0 + (M_T - M_0)(1 - e^{-t_{exp}/\tau})$$

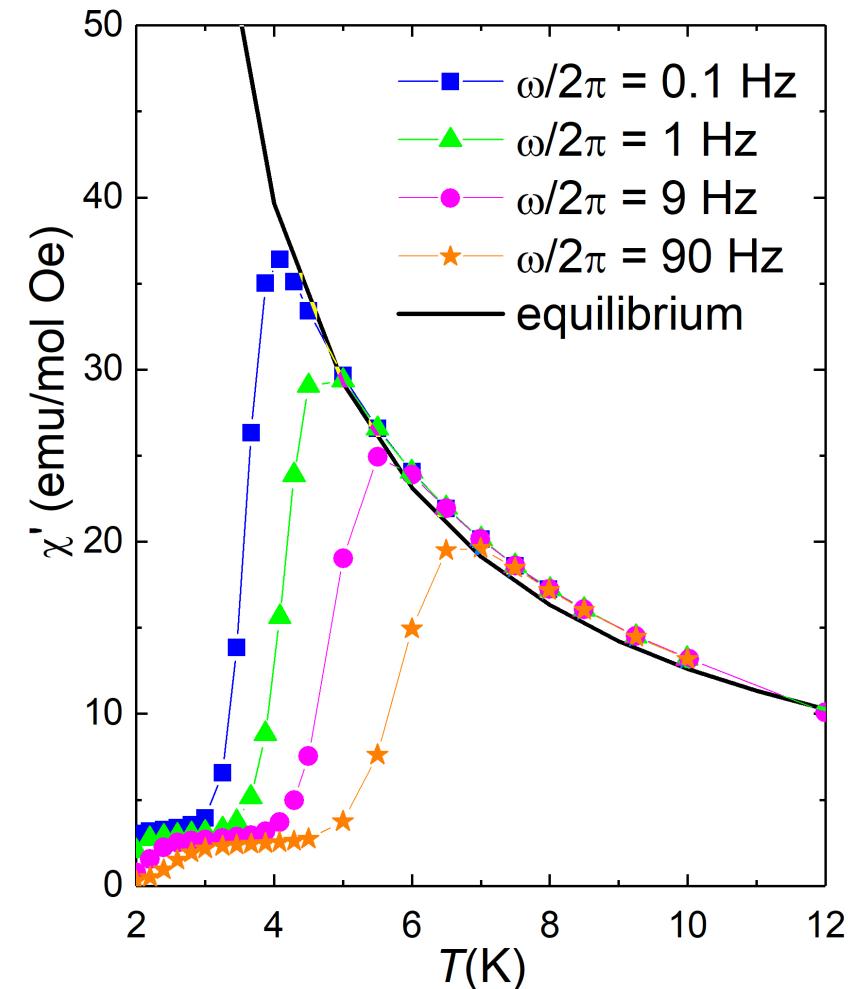
Characteristic time scale $\tau(T, H)$



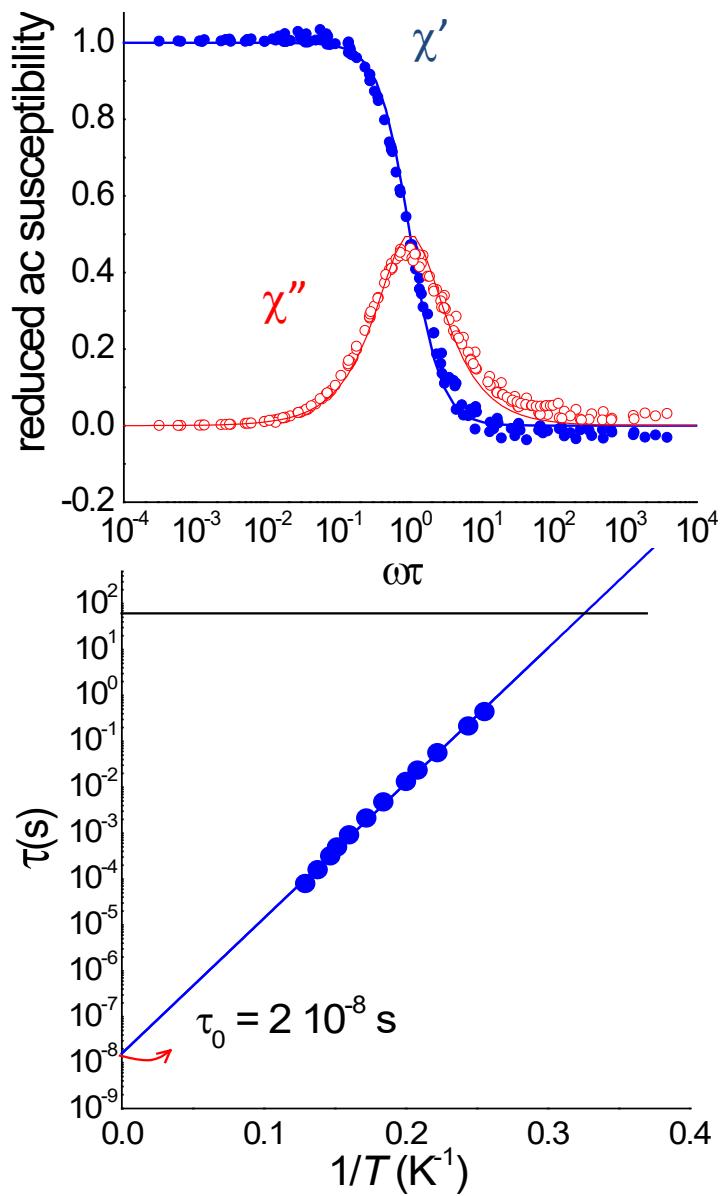
Off-equilibrium for $\tau > t_{exp}$

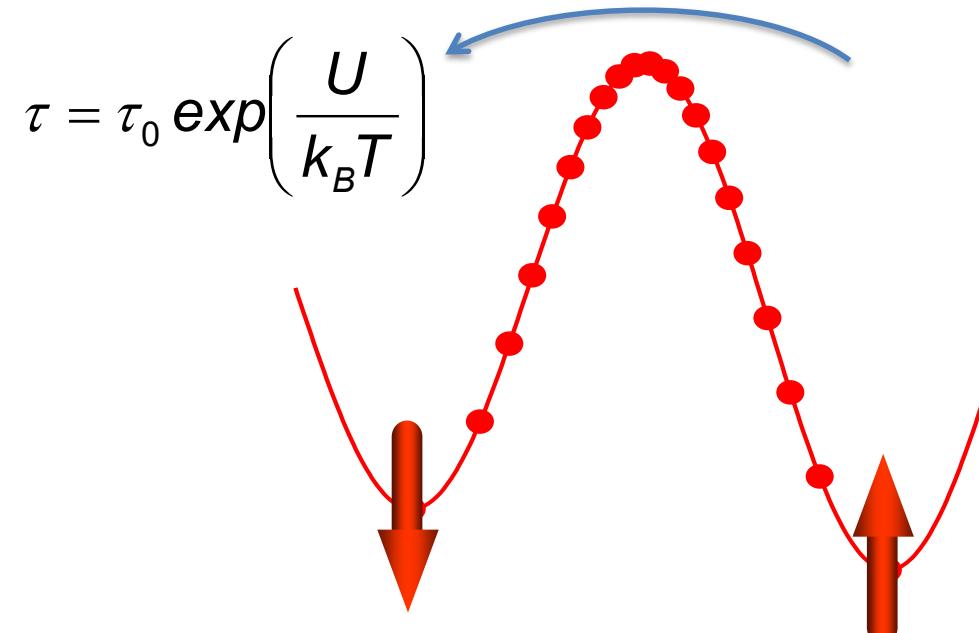
- P. Ehrenfest, Leiden Commun. Suppl. **4b** (1919)
- H. A. Kramers, Physica **7**, 284 (1940)
- J. Villain, F. Hartman-Boutron, R. Sessoli and A. Rettori, EPL **27**, 159 (1994)
- F. Luis, J. Bartolomé and J. F. Fernández, Phys. Rev. B **57**, 505 (1998)

R. Sessoli et al, Nature **365**, 141 (1993)



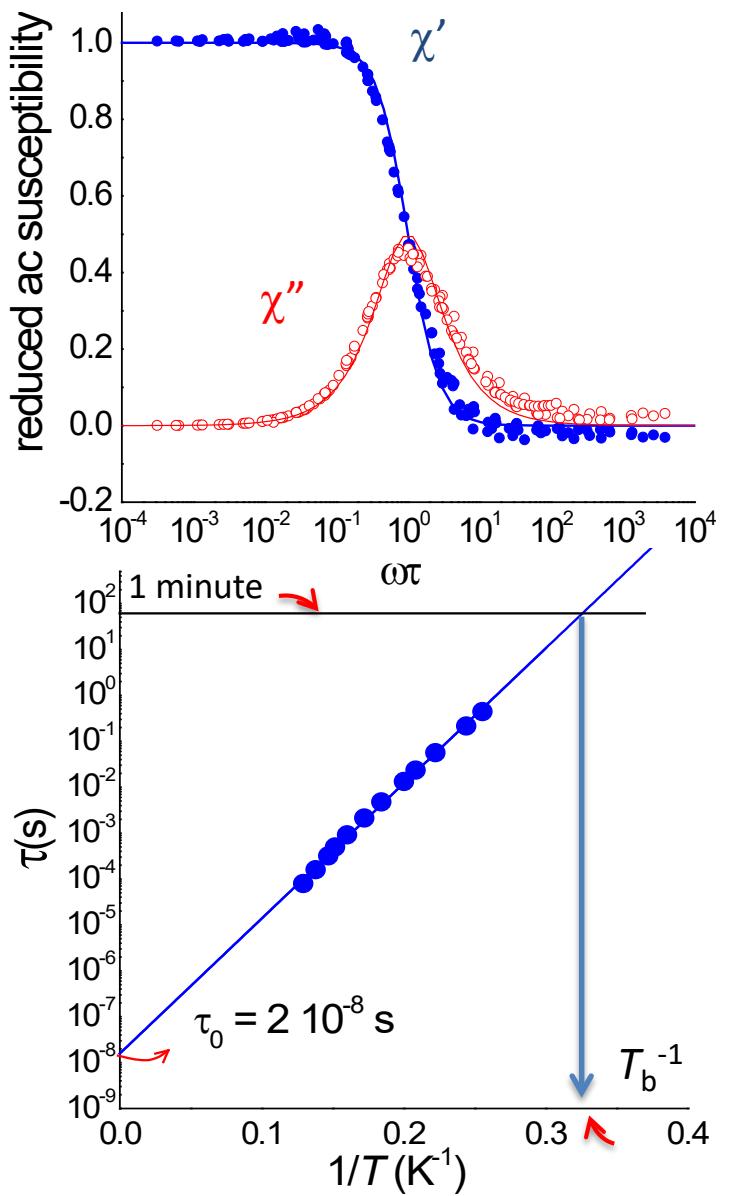
$$\chi_{zz} \equiv \chi'_{zz} - i\chi''_{zz} \approx \frac{\chi_T}{1 + i\omega\tau}$$

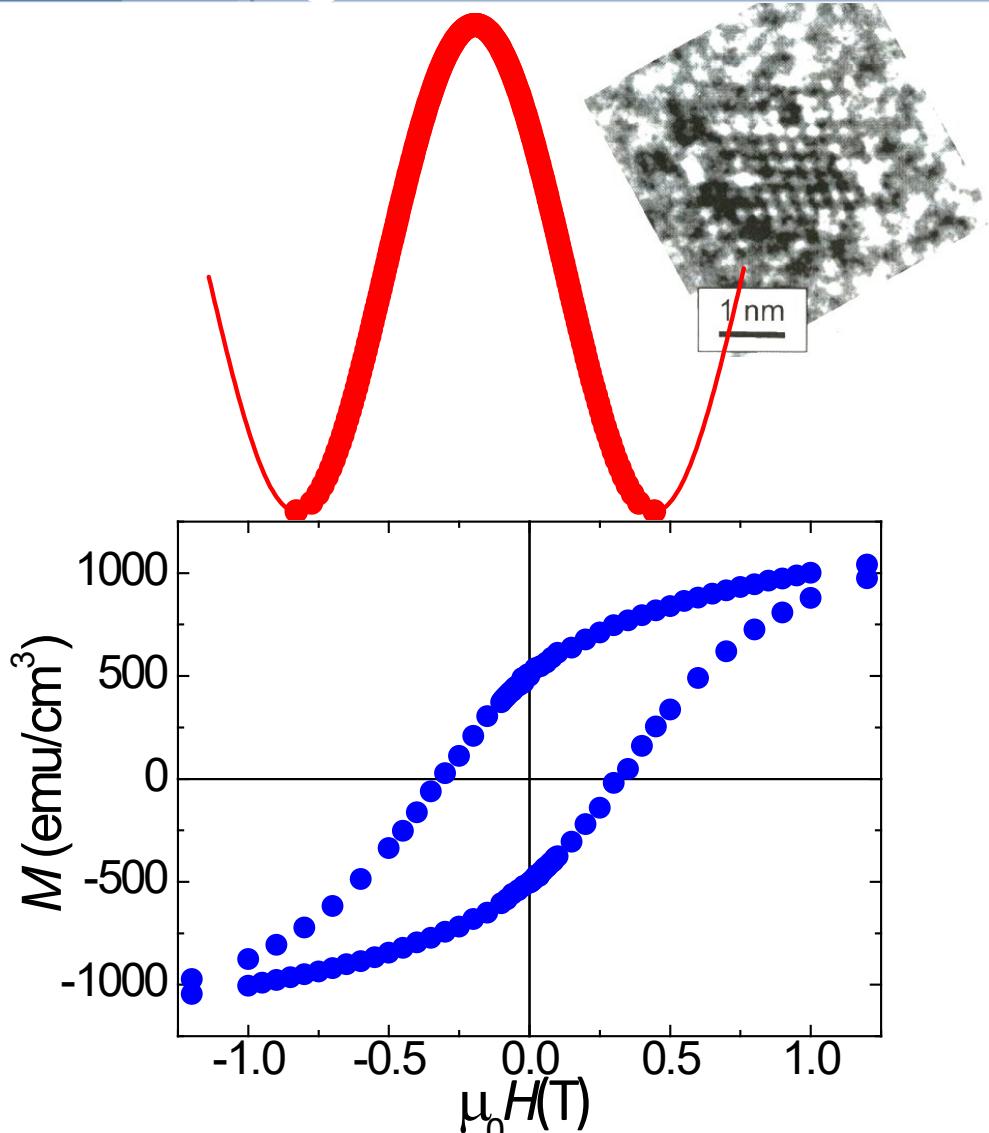
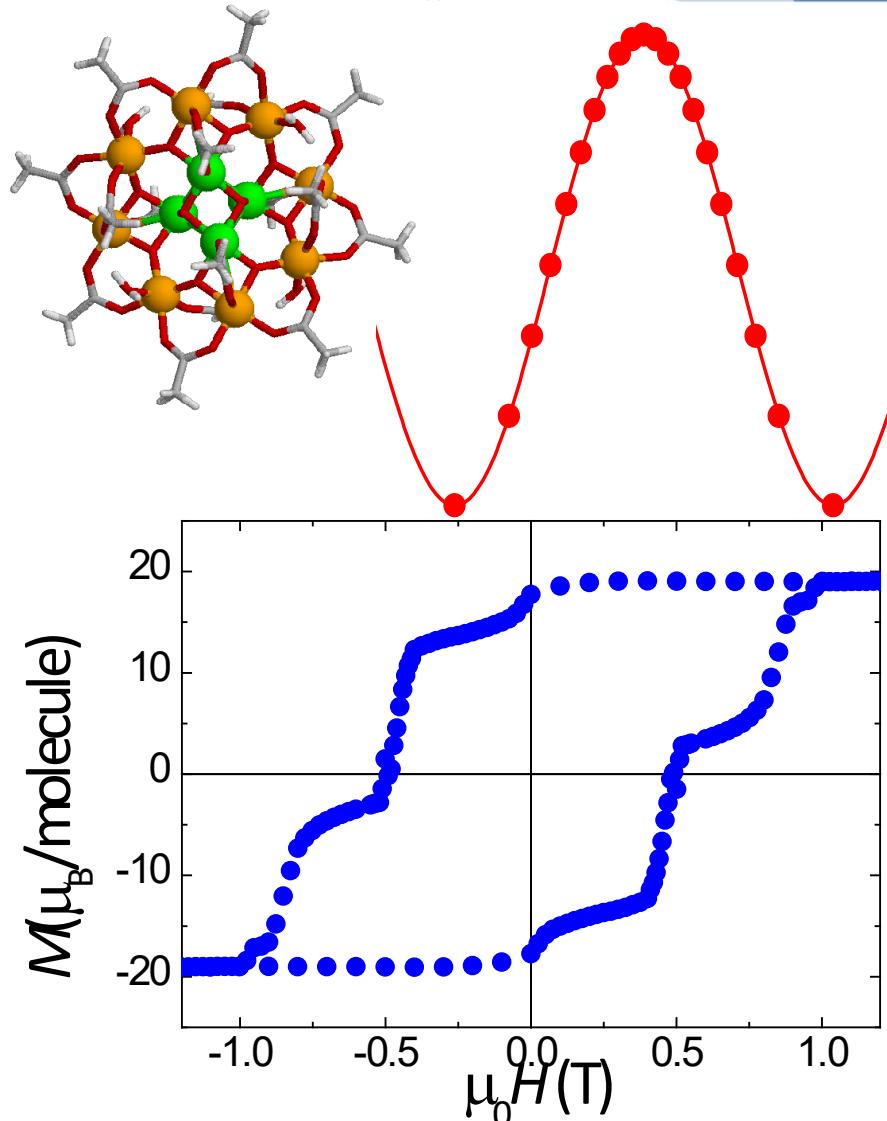




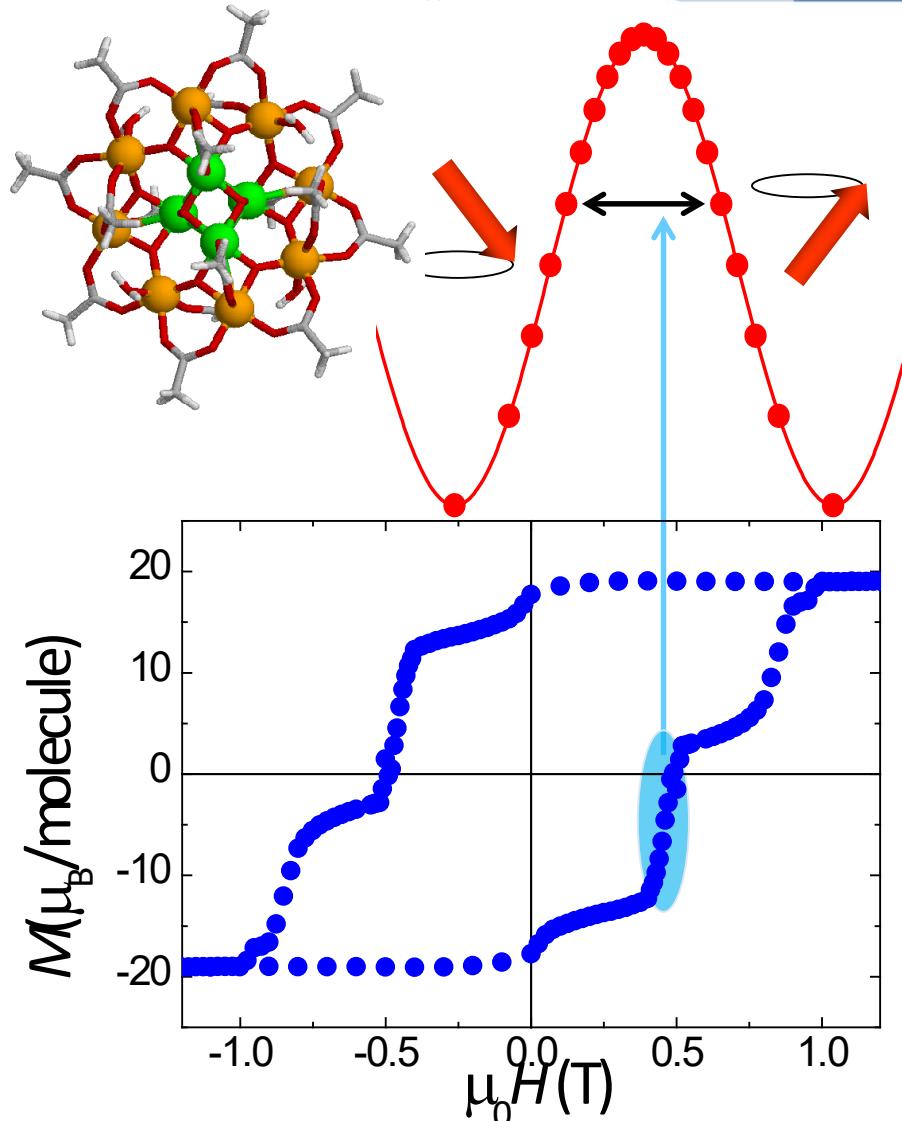
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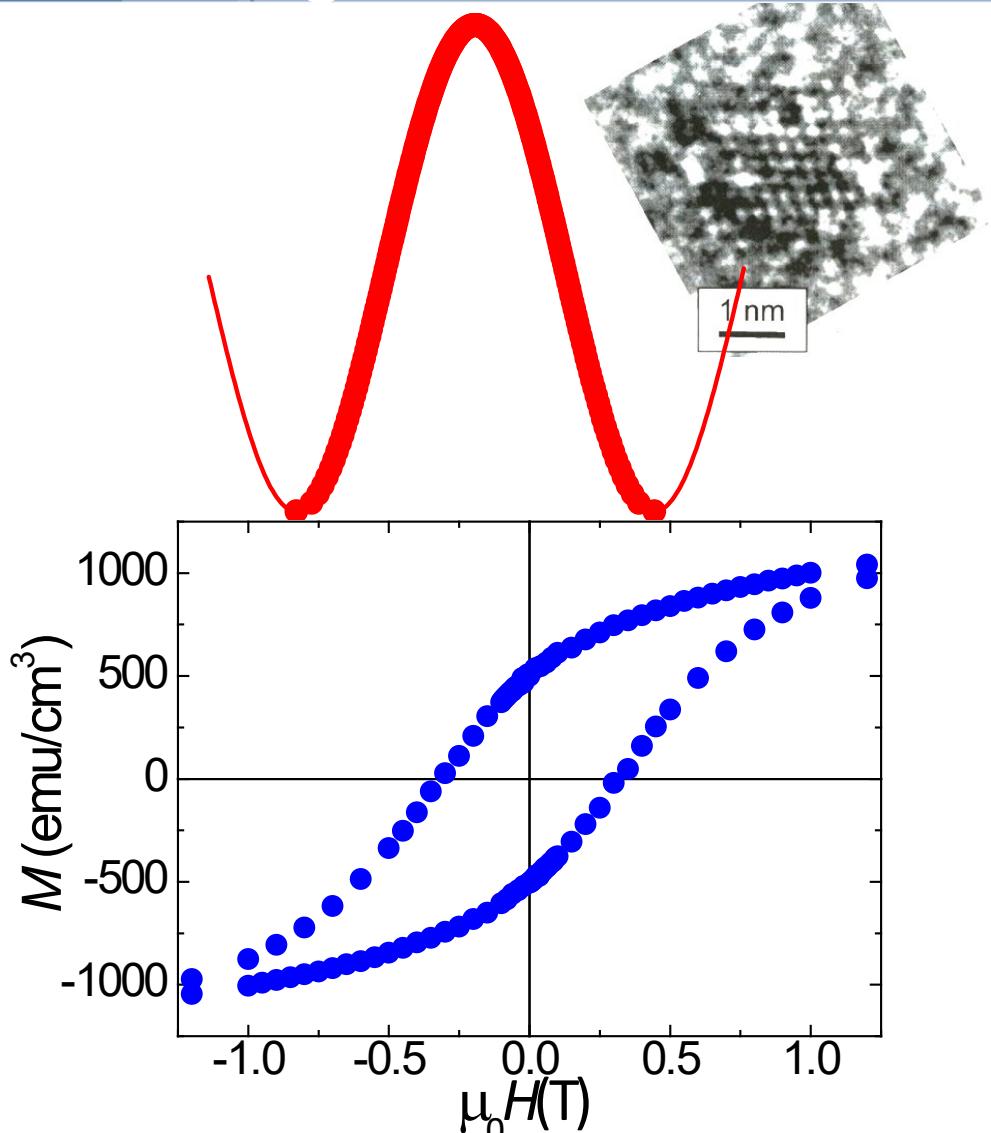


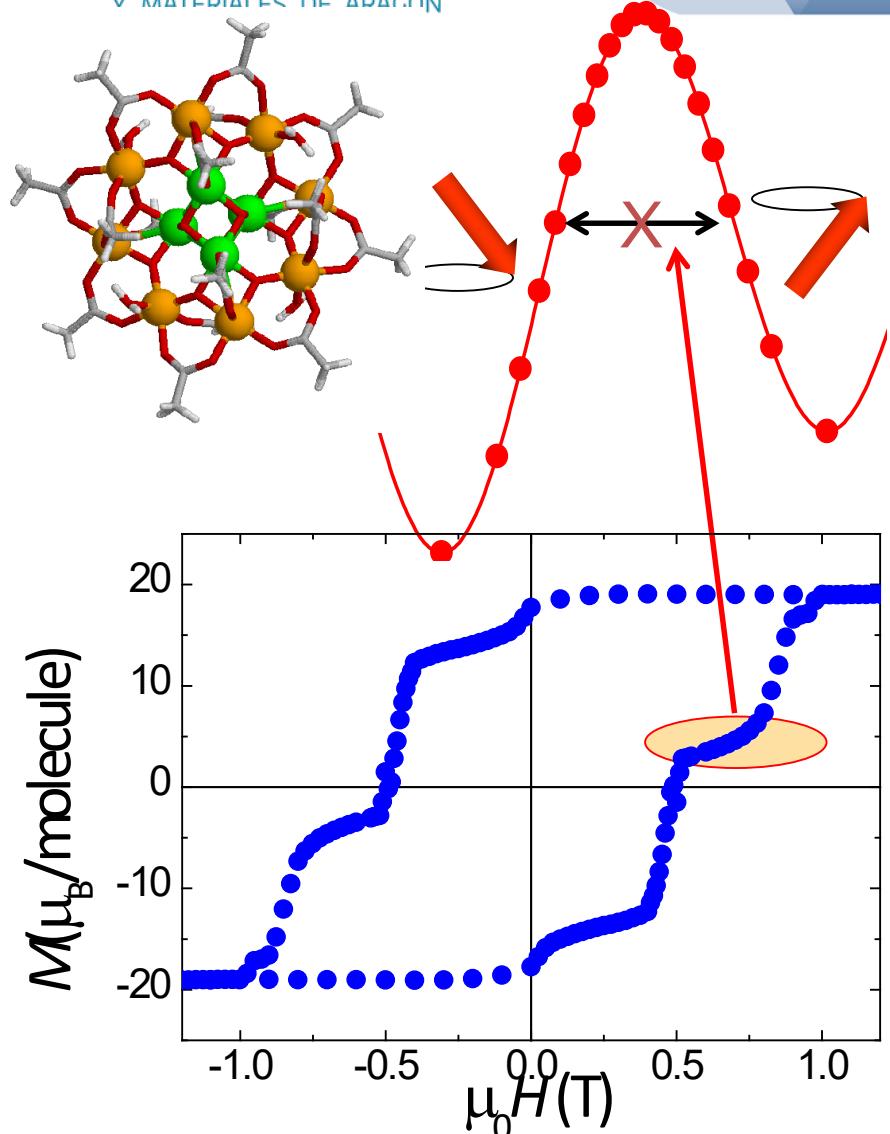


J. R. Friedman, M. P. Sarachik, J. Tejada and R. Ziolo, Phys. Rev. Lett. **76**, 3830 (1996); J. M. Hernández, X. X. Zhang, F. Luis, J. Bartolomé, J. Tejada and R. Ziolo, Europhys. Lett. **35**, 301 (1996); L. Thomas, F. Lionti, R. Ballou, D. Gatteschi, R. Sessoli and B. Barbara, Nature **383**, 145 (1996)

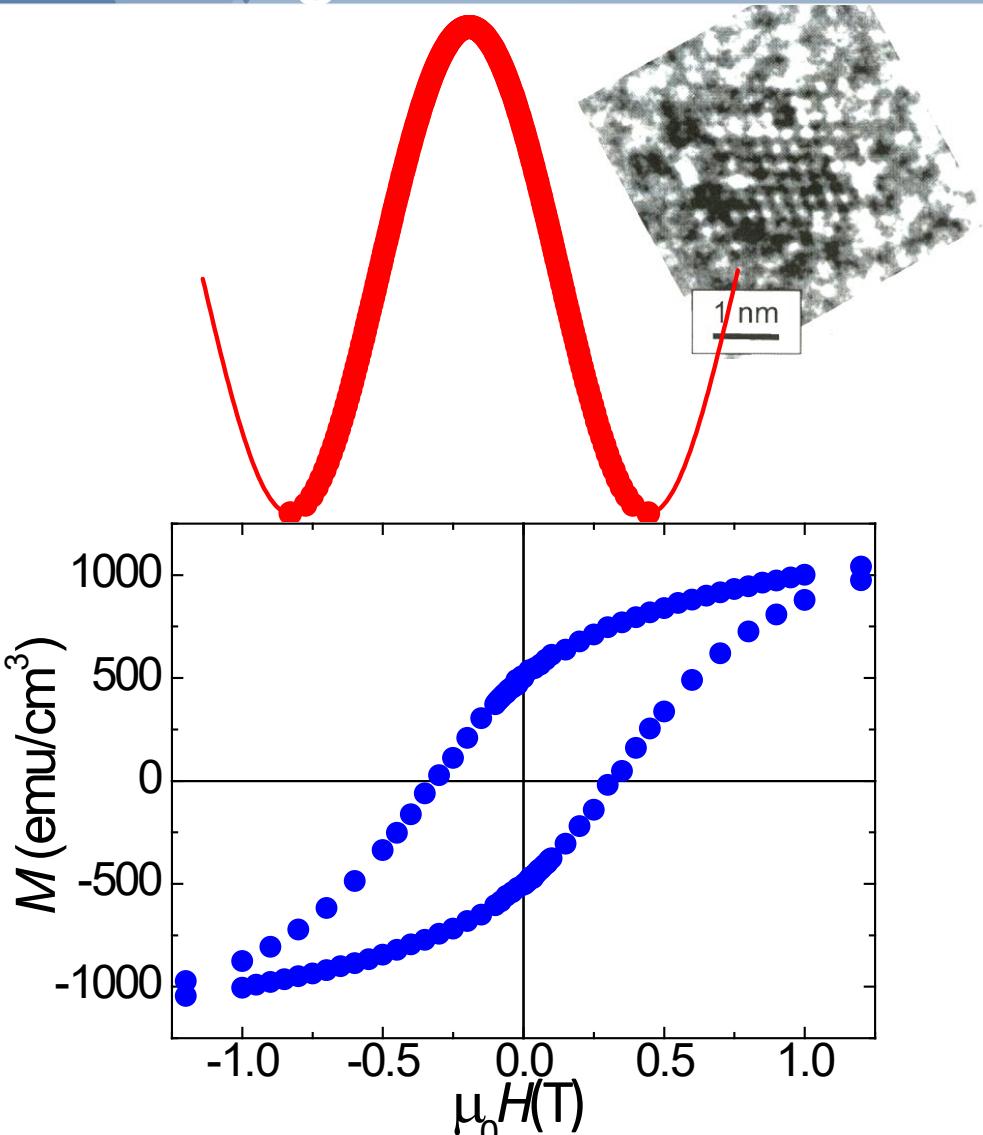


J. R. Friedman, M. P. Sarachik, J. Tejada and R. Ziolo, Phys. Rev. Lett. **76**, 3830 (1996); J. M. Hernández, X. X. Zhang, F. Luis, J. Bartolomé, J. Tejada and R. Ziolo, Europhys. Lett. **35**, 301 (1996); L. Thomas, F. Lionti, R. Ballou, D. Gatteschi, R. Sessoli and B. Barbara, Nature **383**, 145 (1996)

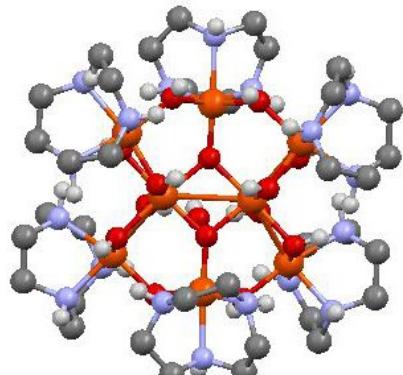




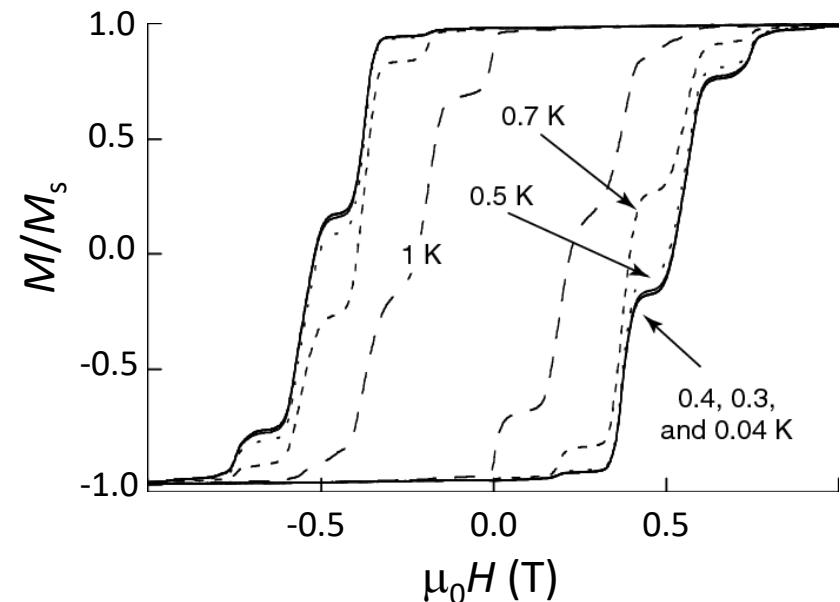
J. R. Friedman, M. P. Sarachik, J. Tejada and R. Ziolo, Phys. Rev. Lett. **76**, 3830 (1996); J. M. Hernández, X. X. Zhang, F. Luis, J. Bartolomé, J. Tejada and R. Ziolo, Europhys. Lett. **35**, 301 (1996); L. Thomas, F. Lionti, R. Ballou, D. Gatteschi, R. Sessoli and B. Barbara, Nature **383**, 145 (1996)



Ground state tunneling Landau-Zener experiments

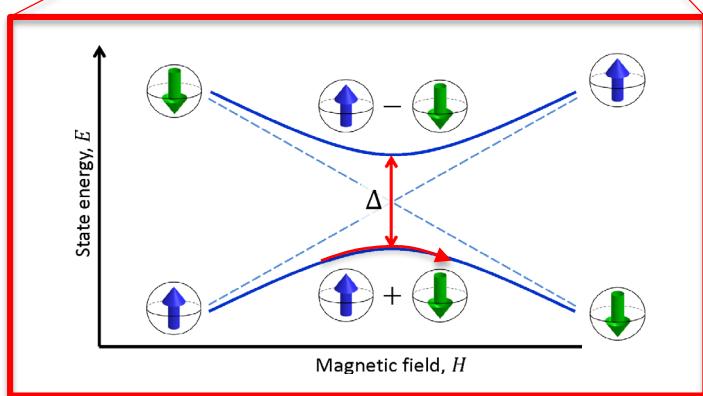
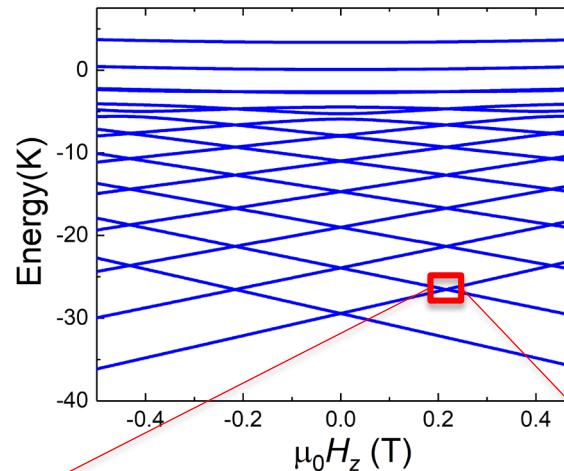


Fe₈
S = 10



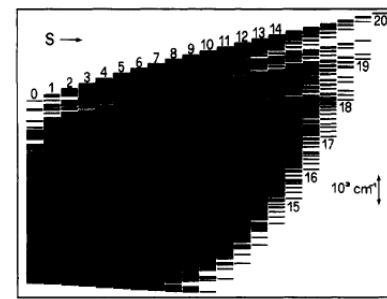
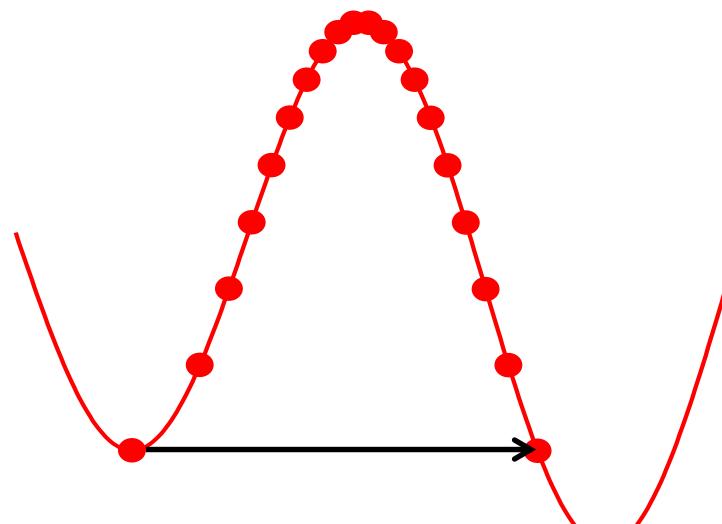
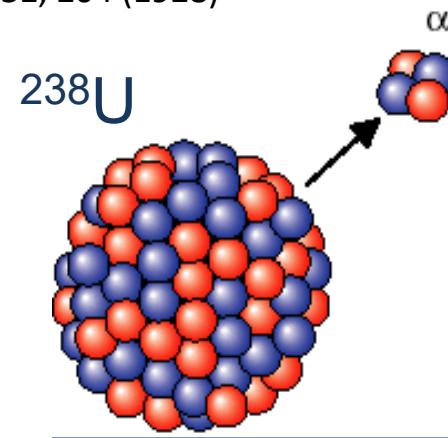
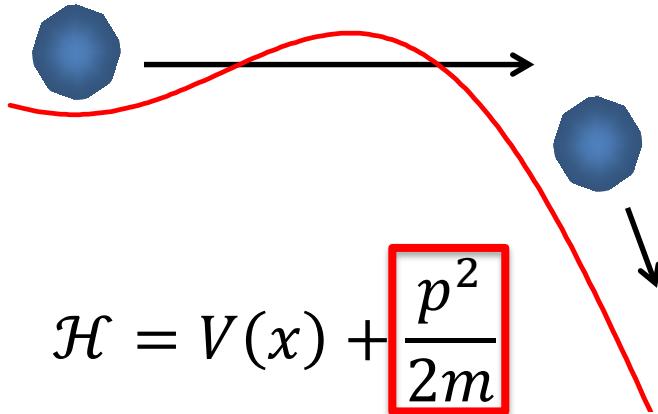
Sangregorio C., Ohm T., Paulsen C., Sessoli R. and Gatteschi D., *Phys. Rev. Lett.*, **78**, 4645 (1997); W. Wernsdorfer *et al*, *Europhys. Lett.* **50** (4), 552 (2000)

$$\mathcal{H} \approx -DS_z^2 + E(S_x^2 - S_y^2) - g\mu_B \vec{H} \cdot \vec{S}$$

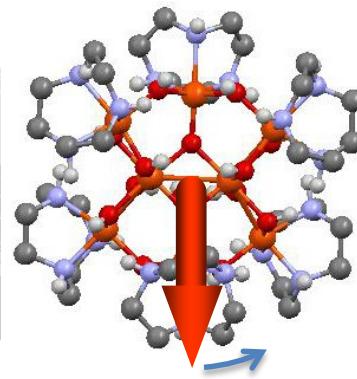


$$P_{LZ} = 1 - \exp\left(-\frac{\pi\Delta^2}{4\hbar g\mu_B} \frac{dH}{dt}\right)$$

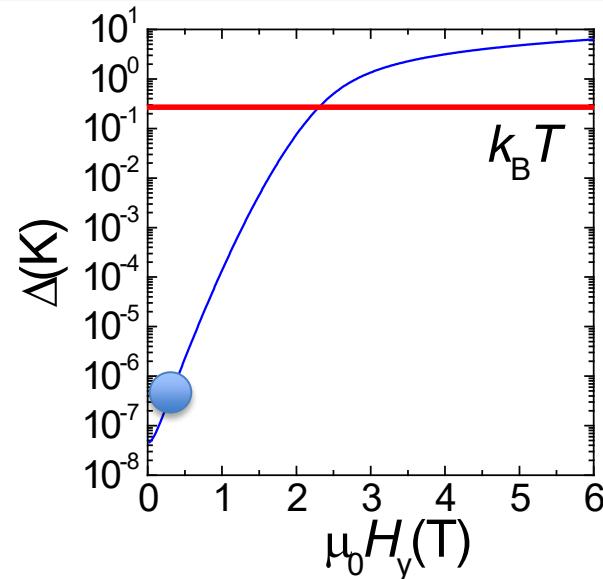
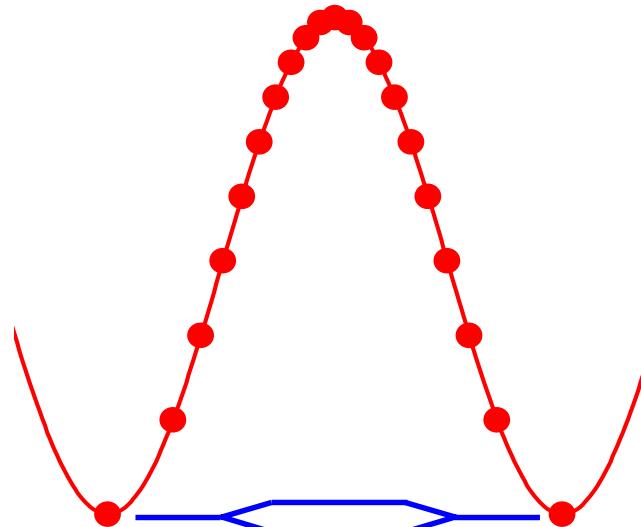
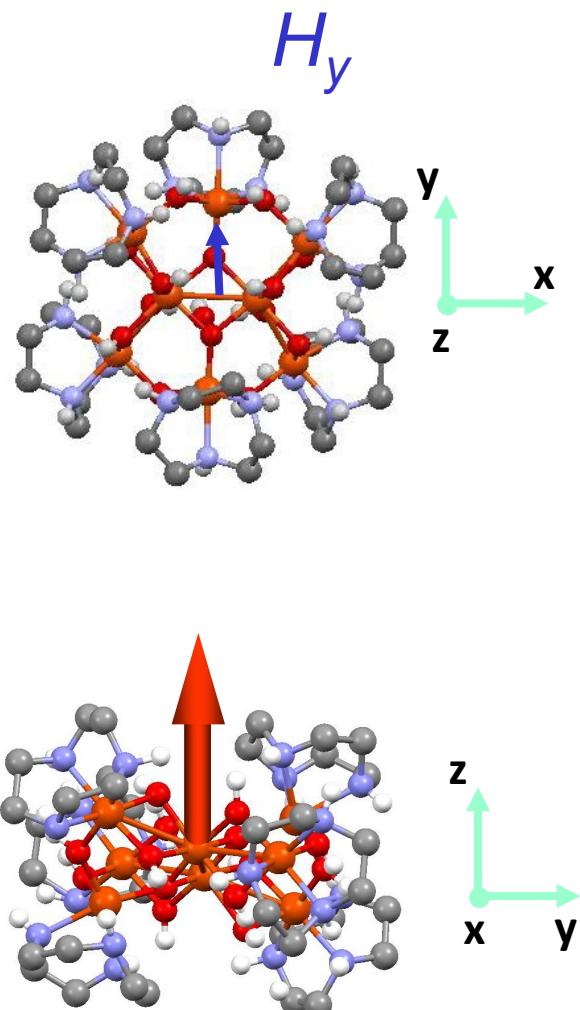
G. Gamow, Z. Physik **51**, 204 (1928)



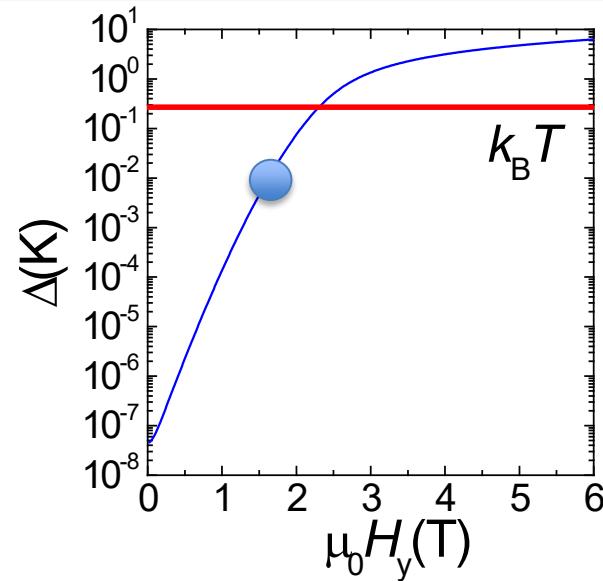
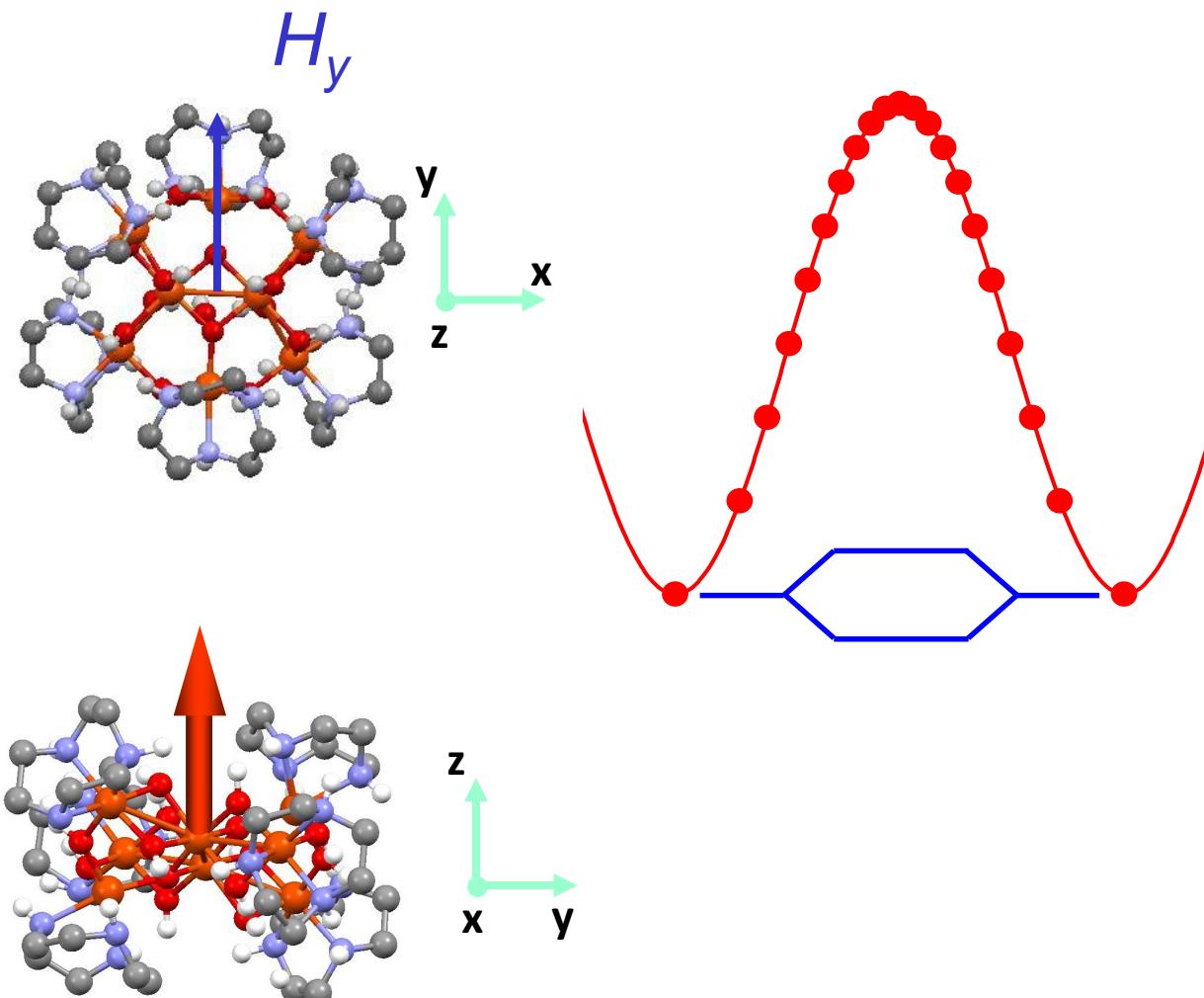
$$\mathcal{H} = -DS_z^2 + E(S_x^2 - S_y^2) - g\mu_B(H_xS_x + H_yS_y)$$



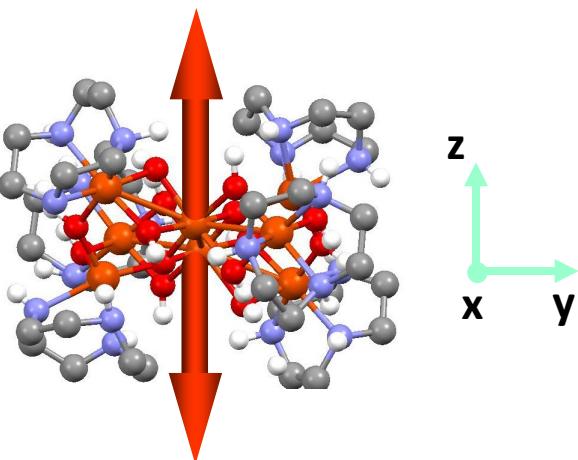
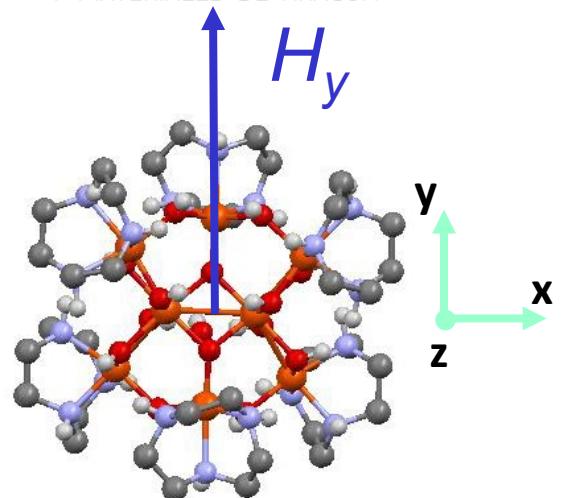
A magnetic Schrödinger cat



A magnetic Schrödinger cat

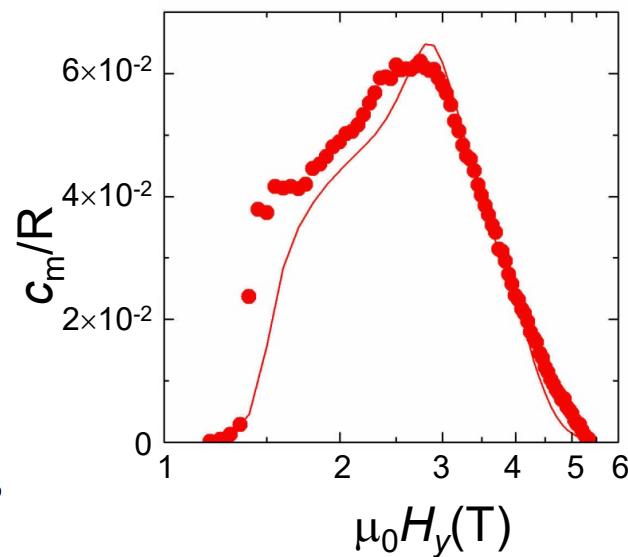
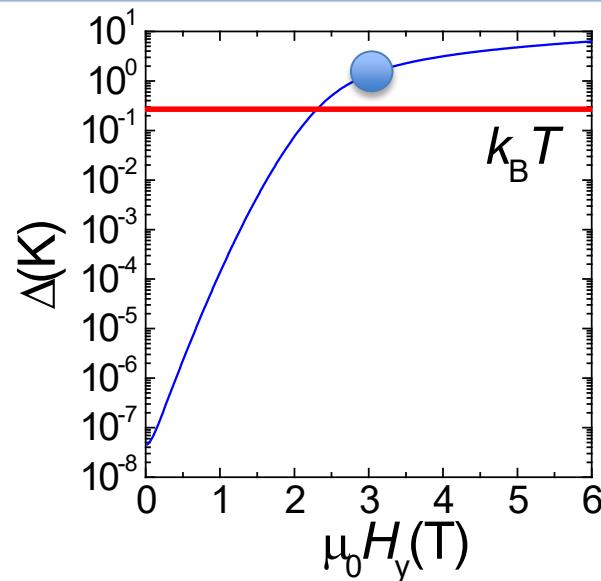


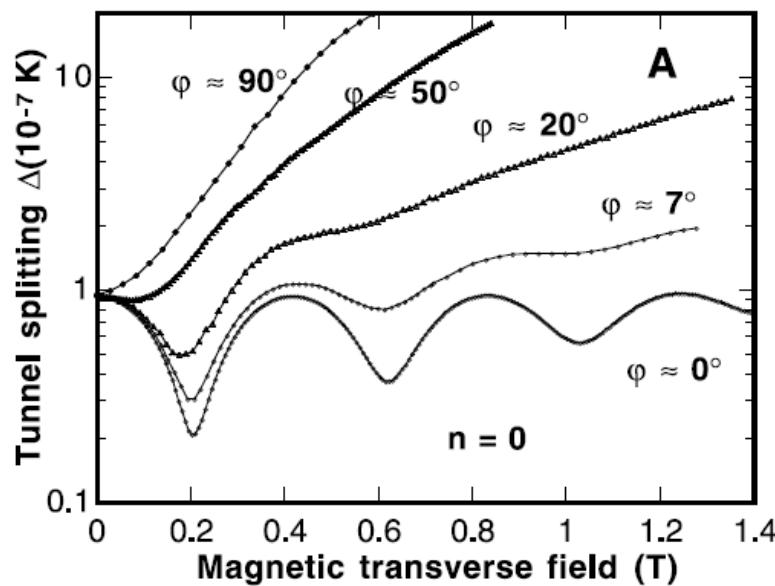
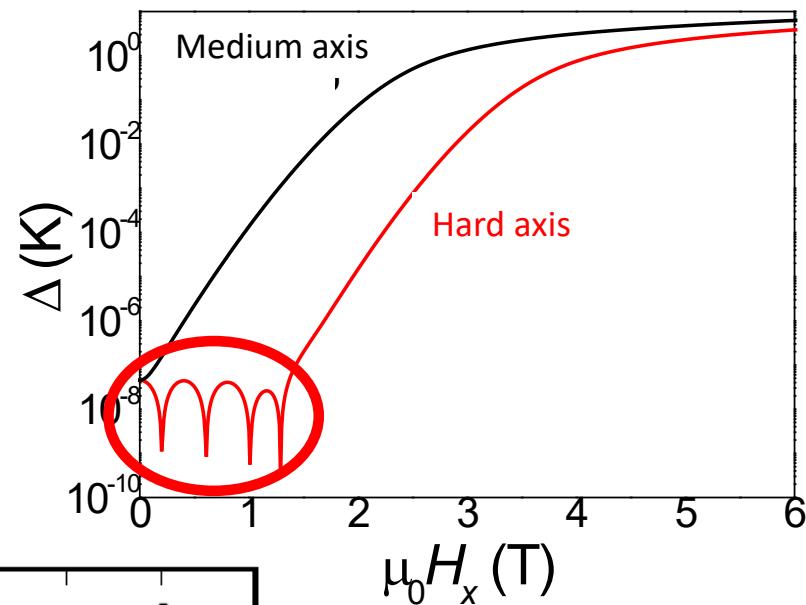
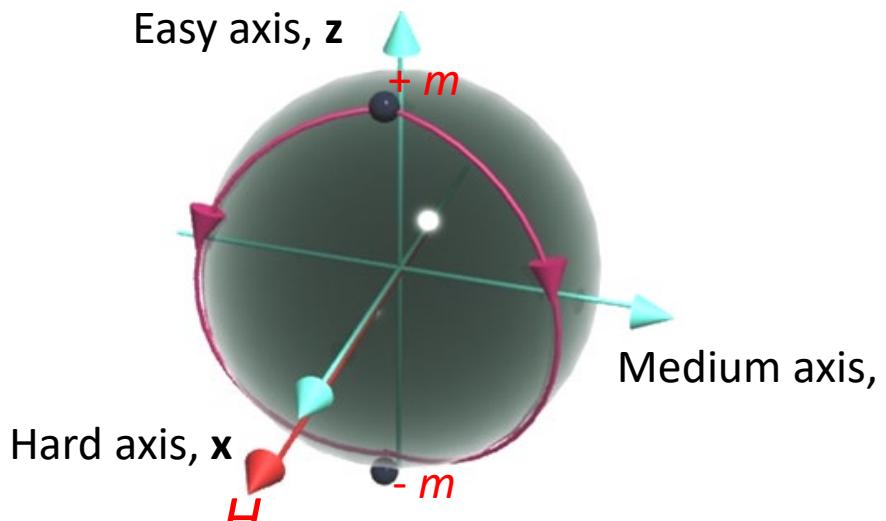
A magnetic Schrödinger cat

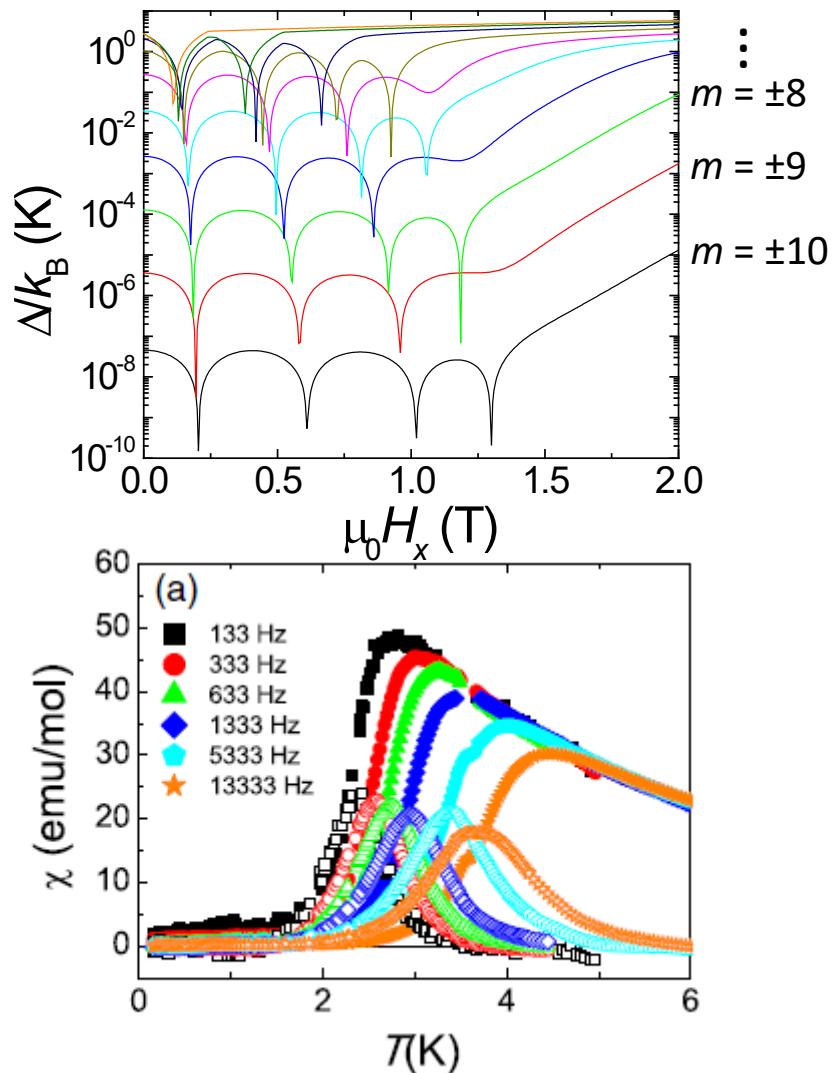


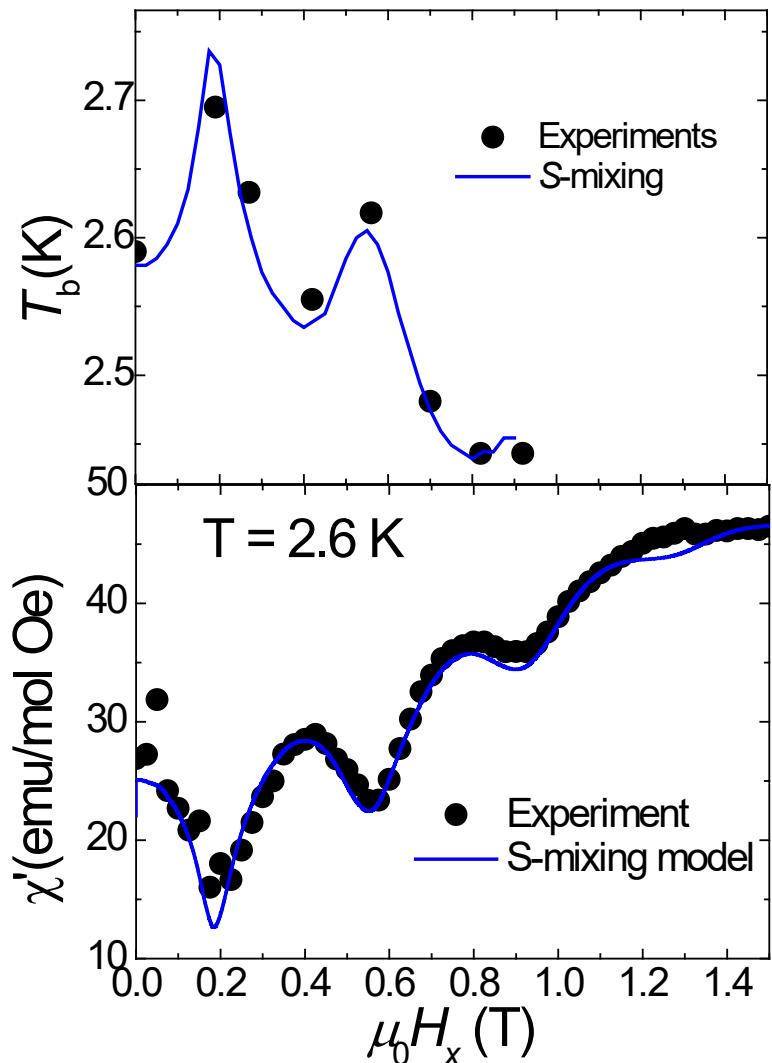
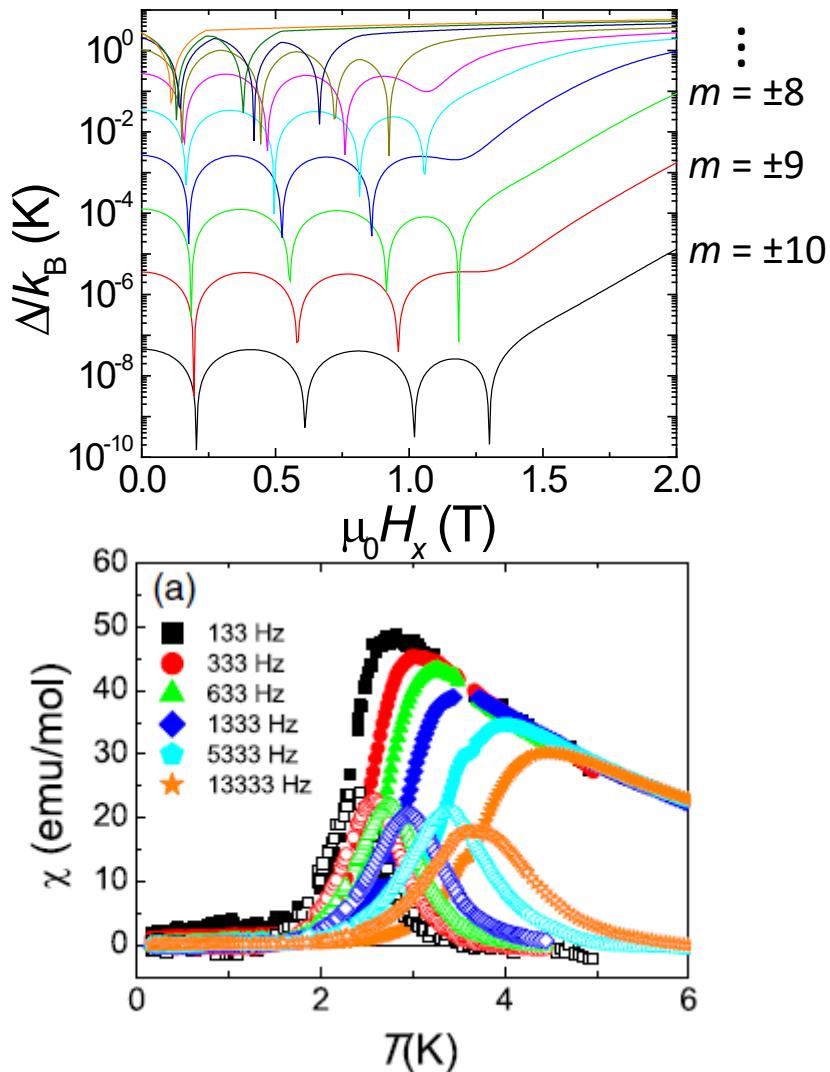
$$\frac{c_m}{R} = \left(\frac{\Delta/k_B T}{e^{\Delta/2k_B T} + e^{-\Delta/2k_B T}} \right)^2$$

Robust superposition states

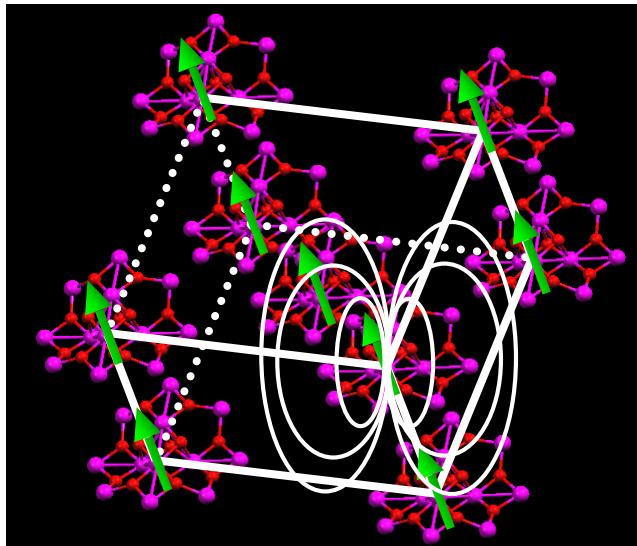








Pure dipolar magnetic order

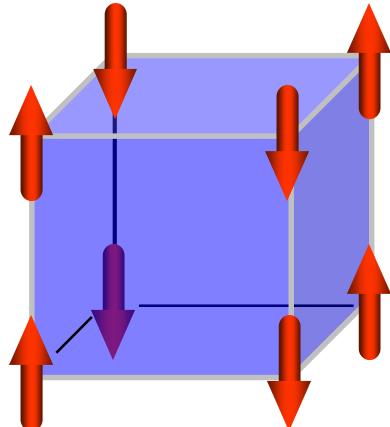


$$\overrightarrow{B}_{dip}(\vec{r}) = \frac{\vec{\mu}}{r^3} - \frac{3(\vec{\mu}\vec{r})}{r^5}$$

Ground state can be predicted from symmetry considerations

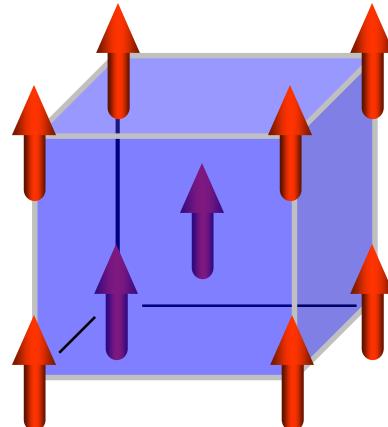
J. M. Luttinger and L. Tisza, Phys. Rev. **70**, 954 (1946)

AF



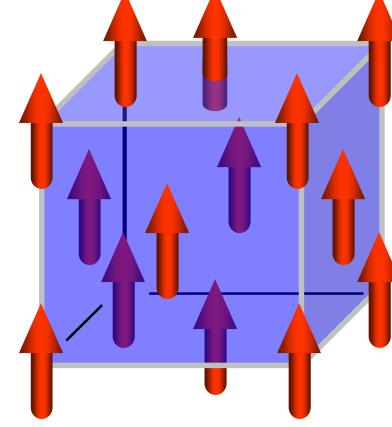
Simple cubic, tetragonal,
hexagonal

F



Body centered lattices

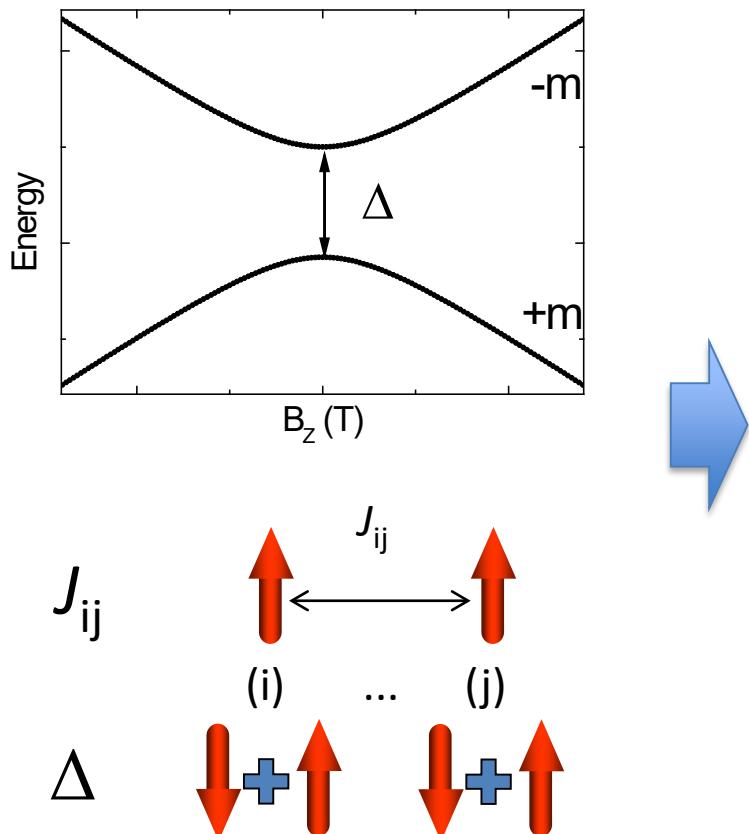
F



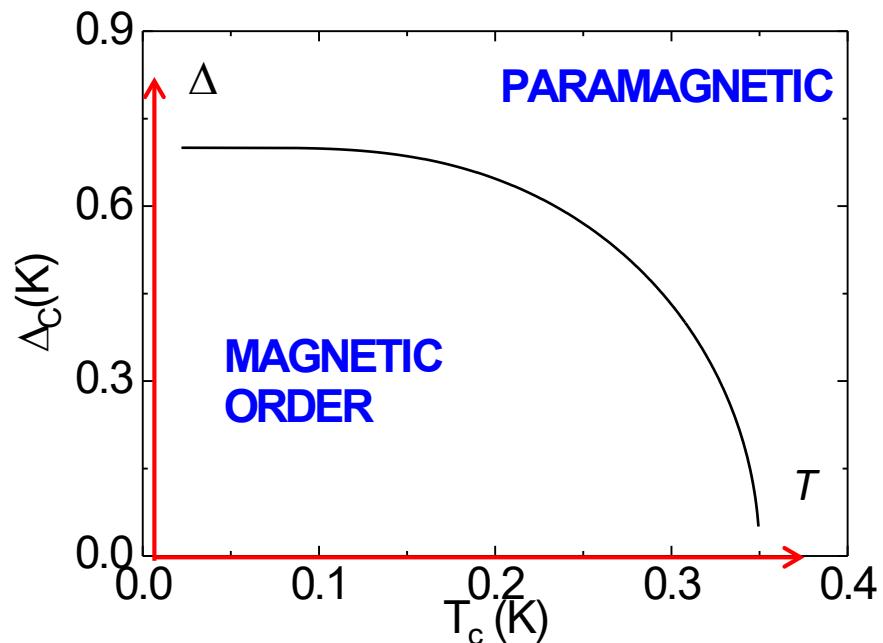
Face centered lattices

Ising model under transverse magnetic field

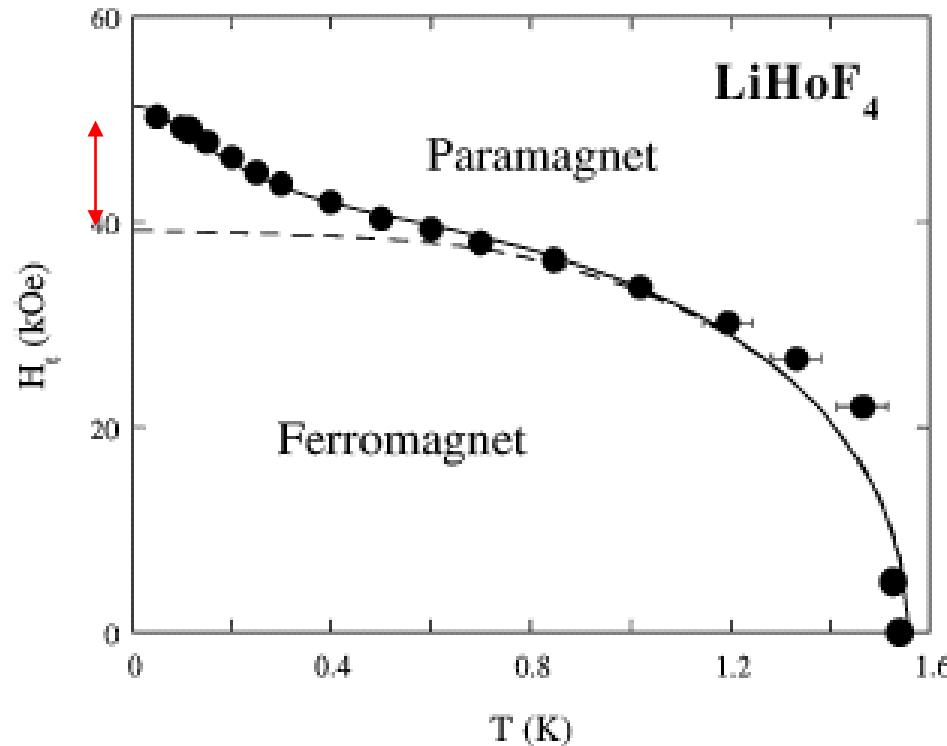
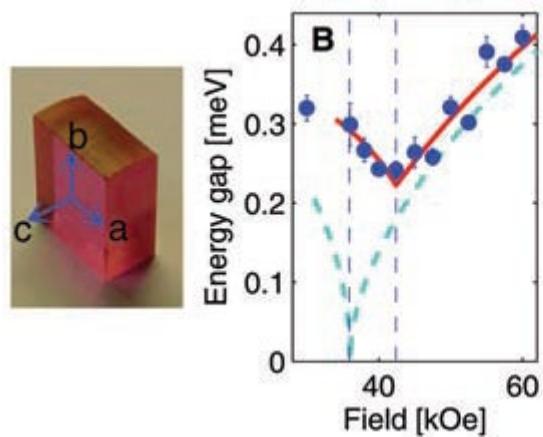
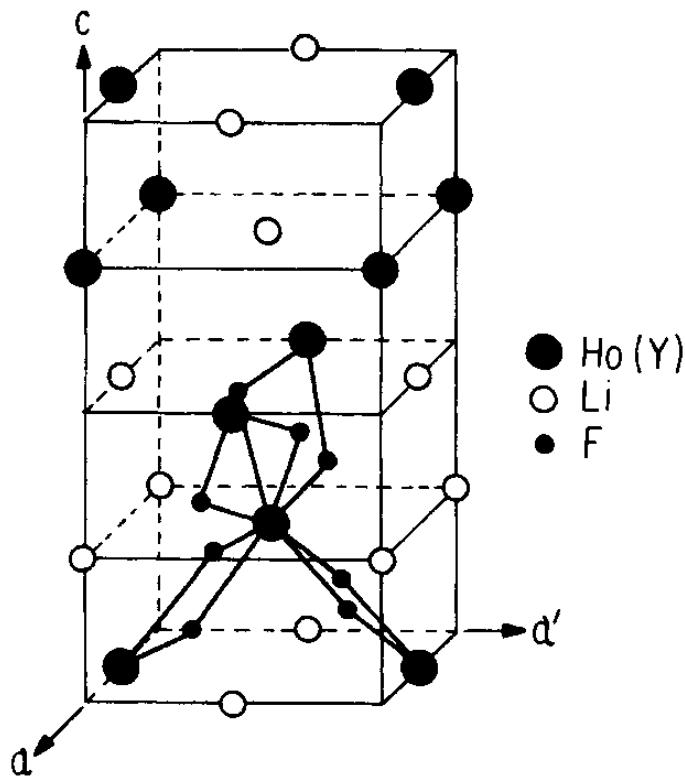
$$\mathcal{H} = 2S^2 \sum_{ij} J_{ij} \sigma_{iz} \sigma_{jz} - \Delta \sum_i \sigma_{ix}$$



$$\coth\left(\frac{\Delta}{2kT_c}\right) = \frac{J}{\Delta}$$



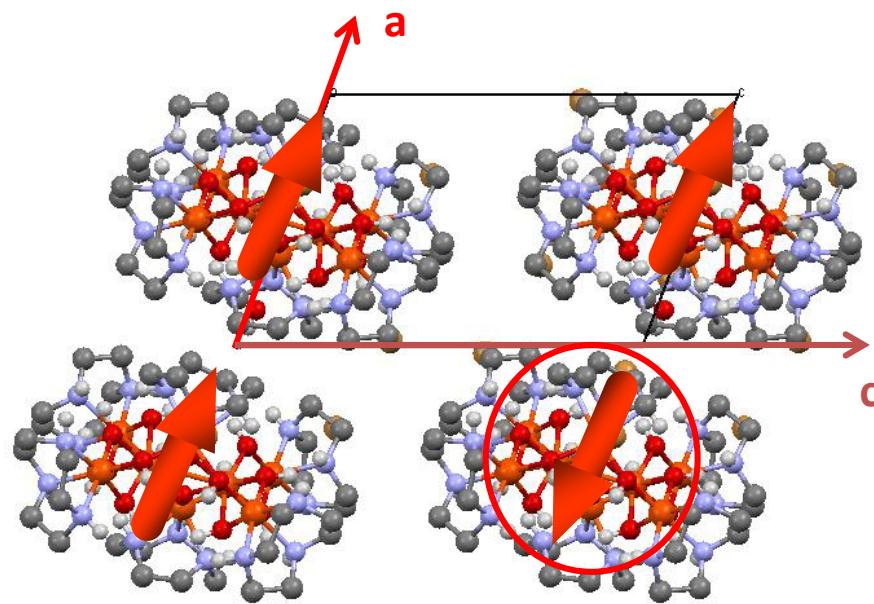
D.Bitko,T.F. Rosenbaum, G. Aeppli, PRL **77**,940 (1996)



- Significant exchange interactions
- High hyperfine interactions

H. M Rønnow et al, Science **308**, 389 (2005)

Dipolar ferromagnetic order in Fe_8



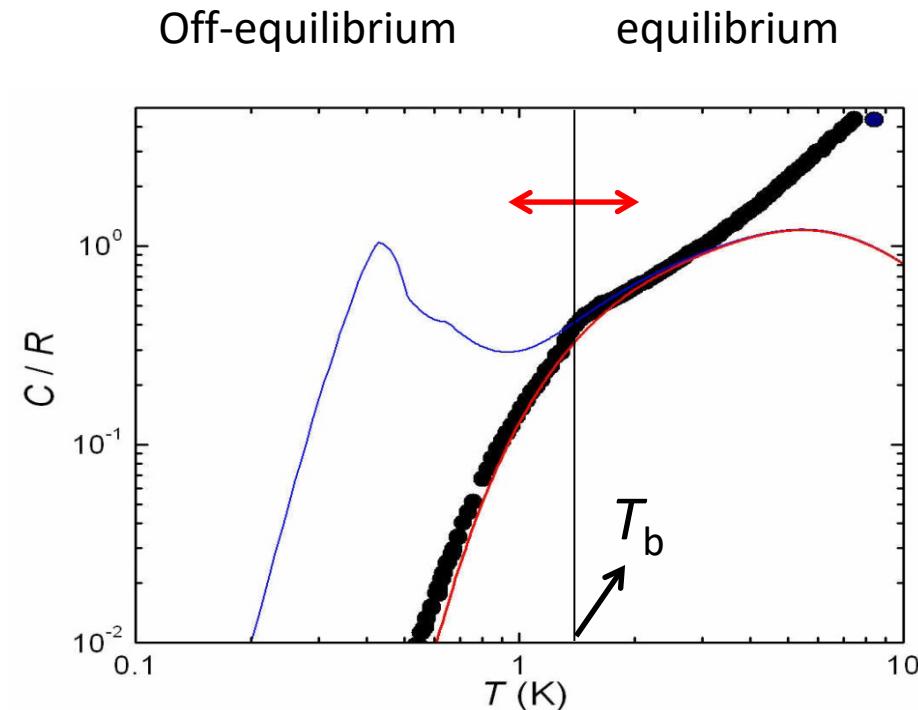
Monte Carlo Simulations



Ferromagnetic ground state

$$T_c \approx 540 \text{ mK}$$

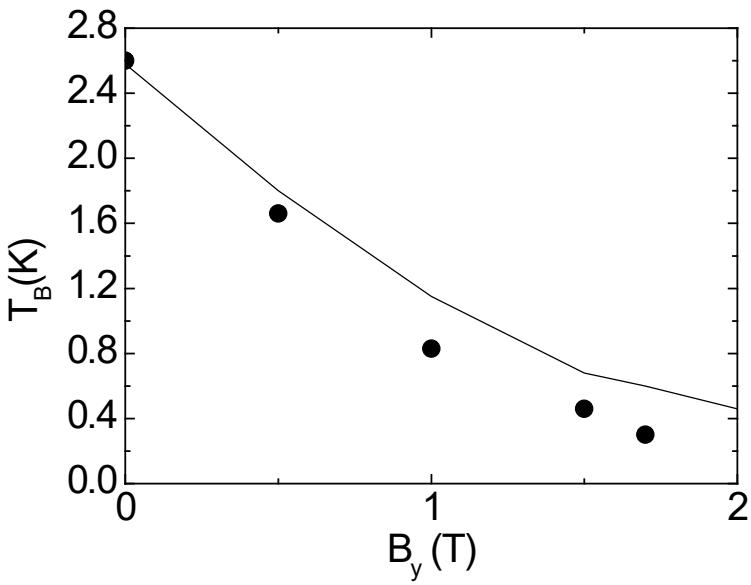
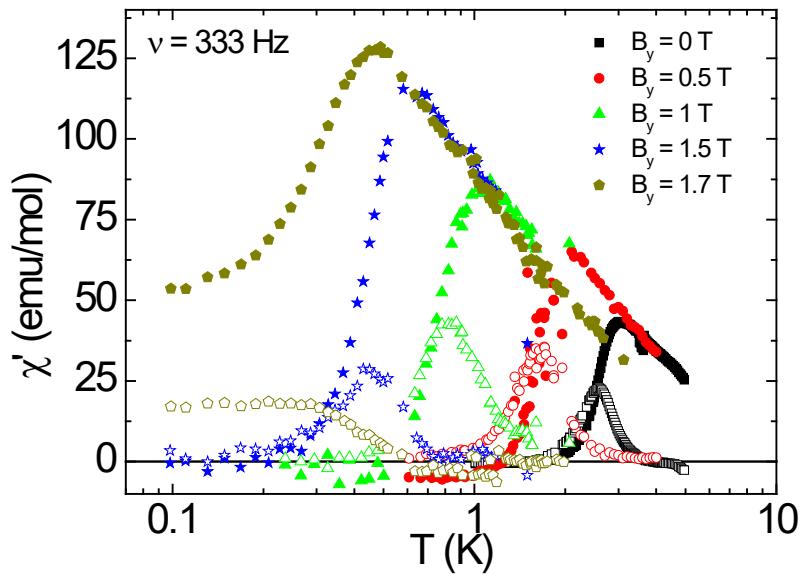
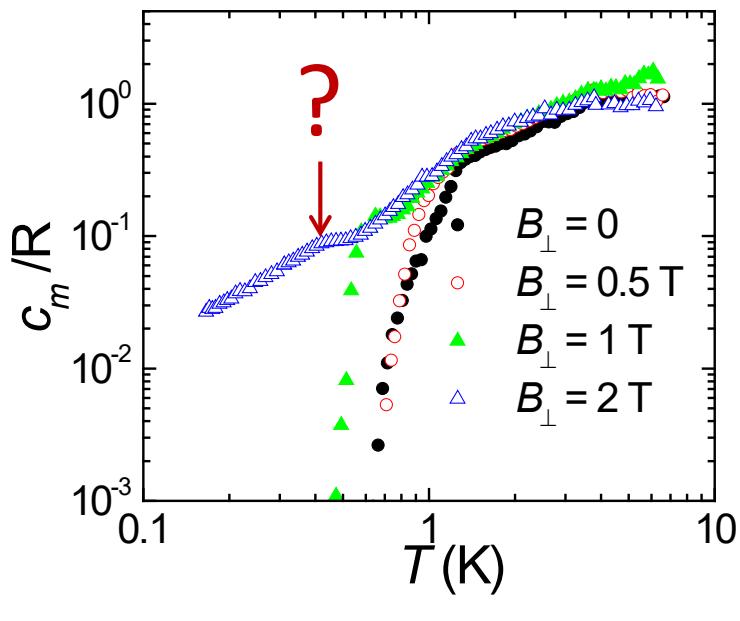
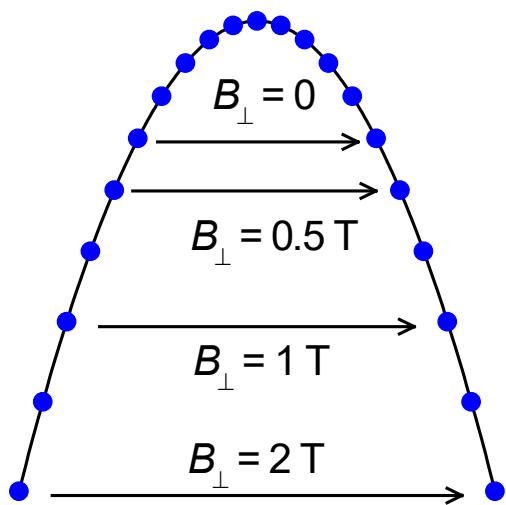
J.F. Fernández et al, PRB **62**, 55 (2000)
 X. Martínez-Hidalgo, E. M. Chudnovsky, and A. Aharony, Europhys. Lett. **55**, 273 (2001)

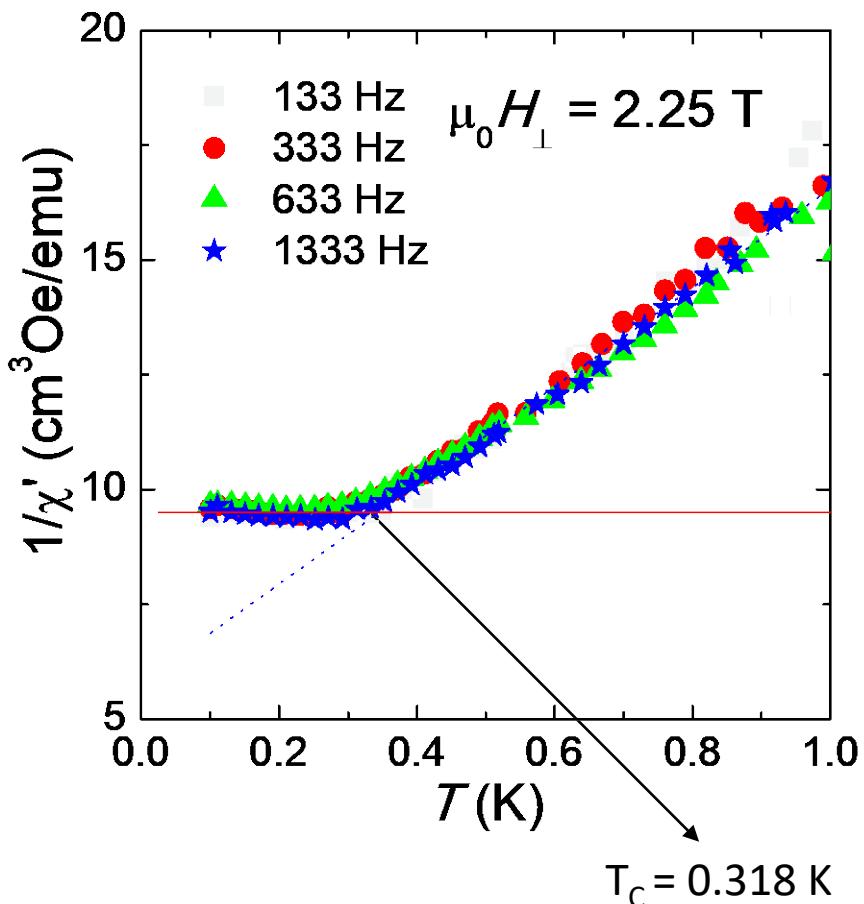


High anisotropy barriers: $U \approx 20 \text{ K}$

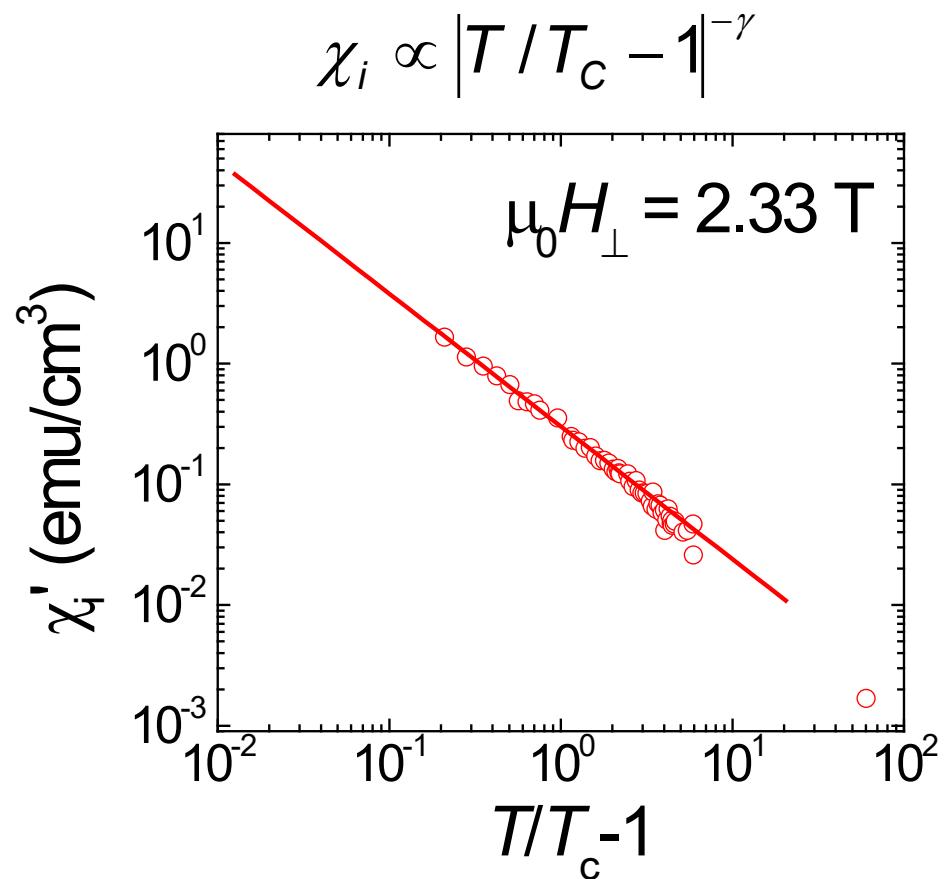


No equilibrium for $T_b \approx U/12 > T_c$



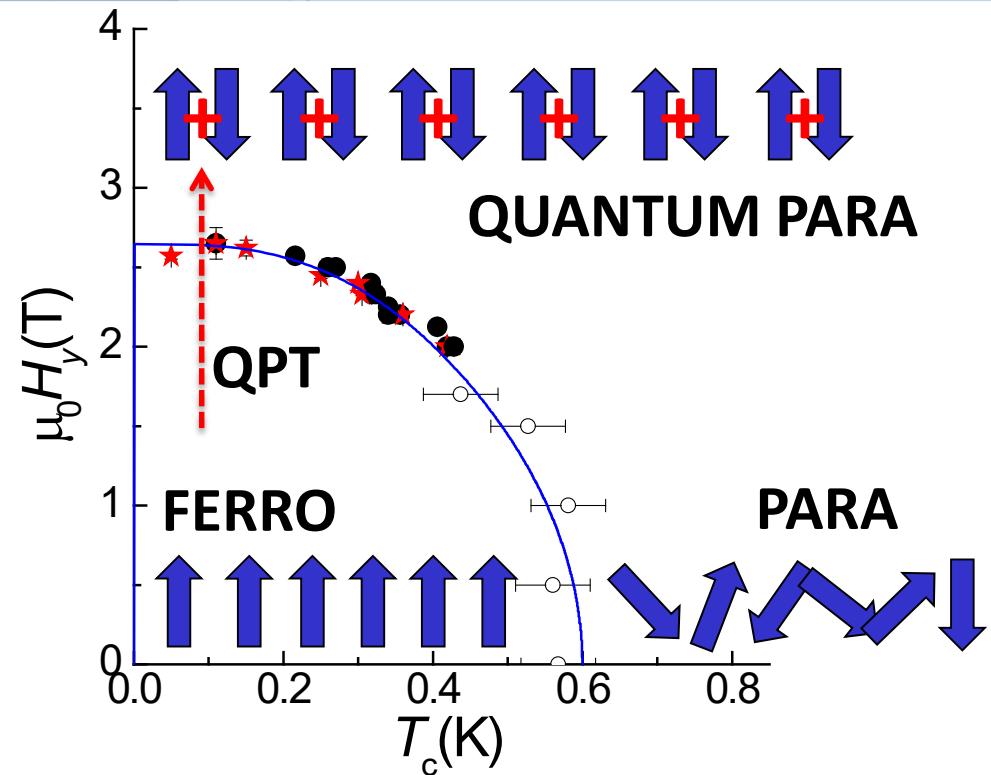
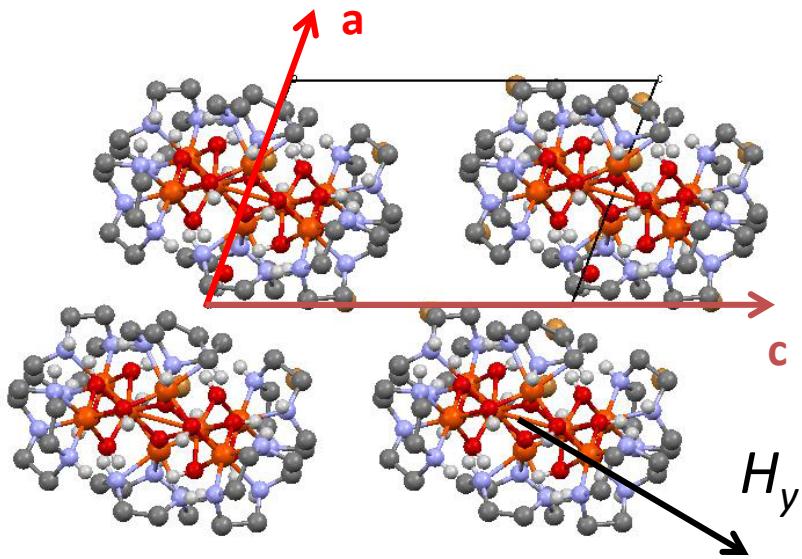


$\frac{1}{\chi_{\max}} \approx N$ **FERRO**



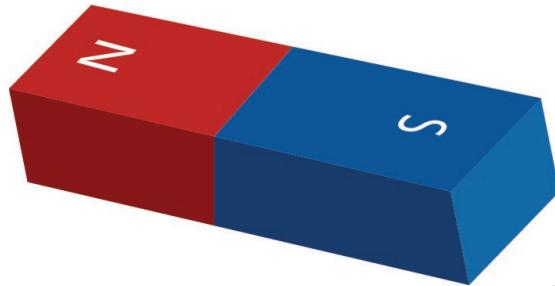
$\gamma \sim 1$ **Mean field dipolar ferromagnet**

Quantum phase transition



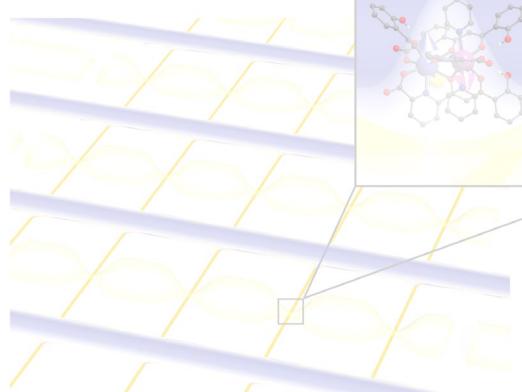
Model realization of the quantum Ising model

$$\mathcal{H} = 2S^2 \sum_{ij} J_{ij} \sigma_{iz} \sigma_{jz} - \Delta \sum_i \sigma_{ix}$$

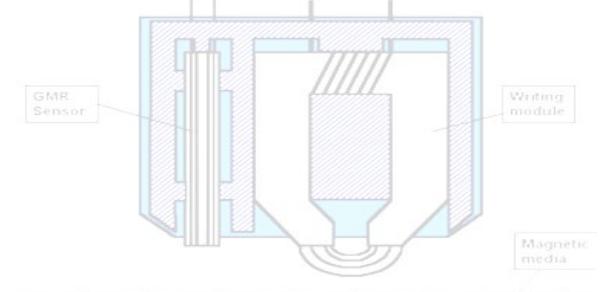
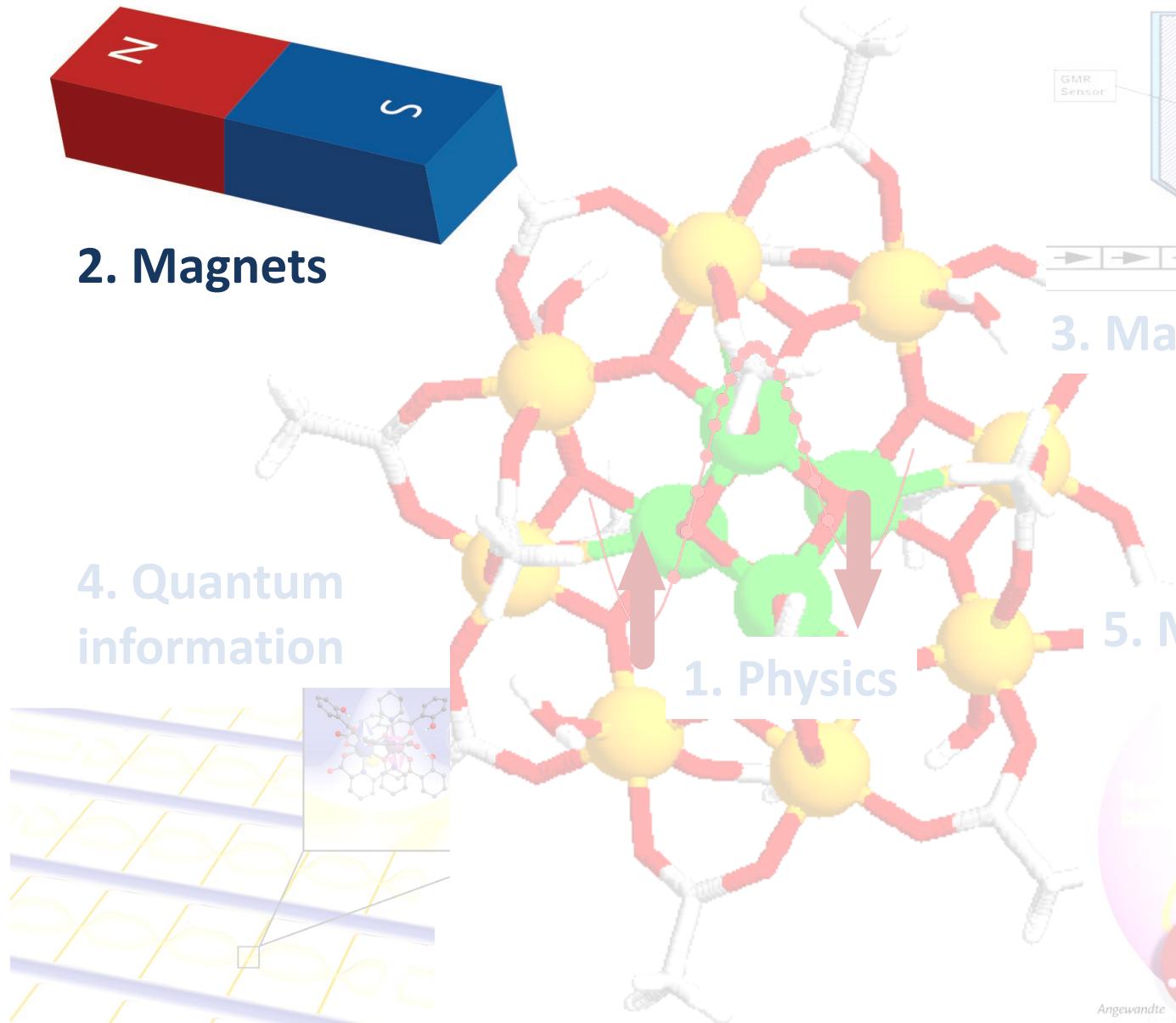


2. Magnets

4. Quantum information



1. Physics

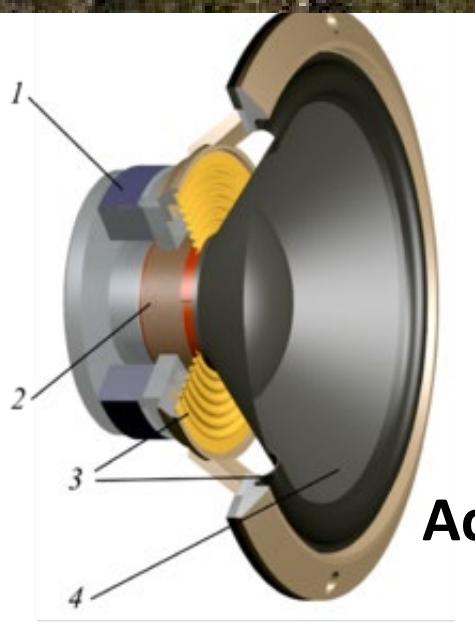
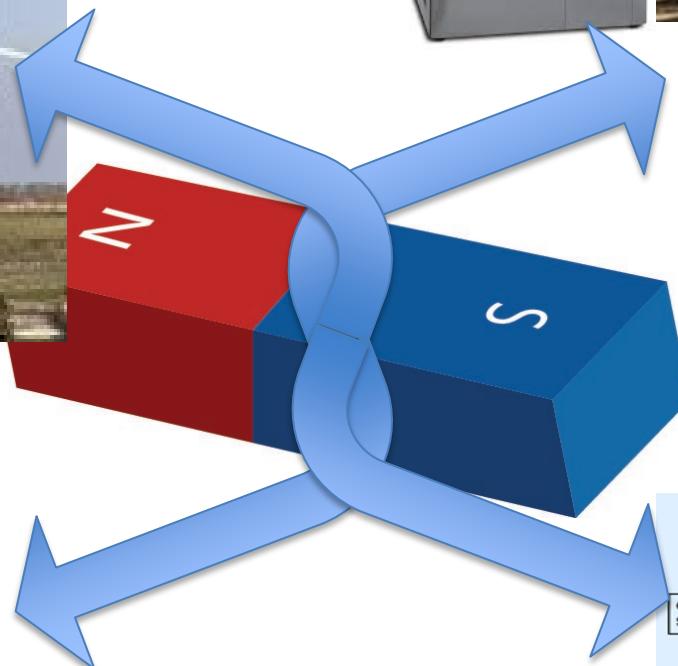


3. Magnetic recording

5. Magnetic coolers



Magnets are everywhere



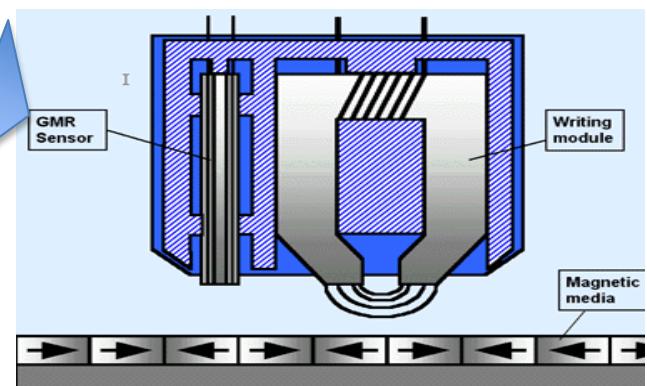
Actuators



Motors



Data storage



1 0 1 0 1 0 0 ...

Figure I
Development of Permanent Magnets in the 1900's

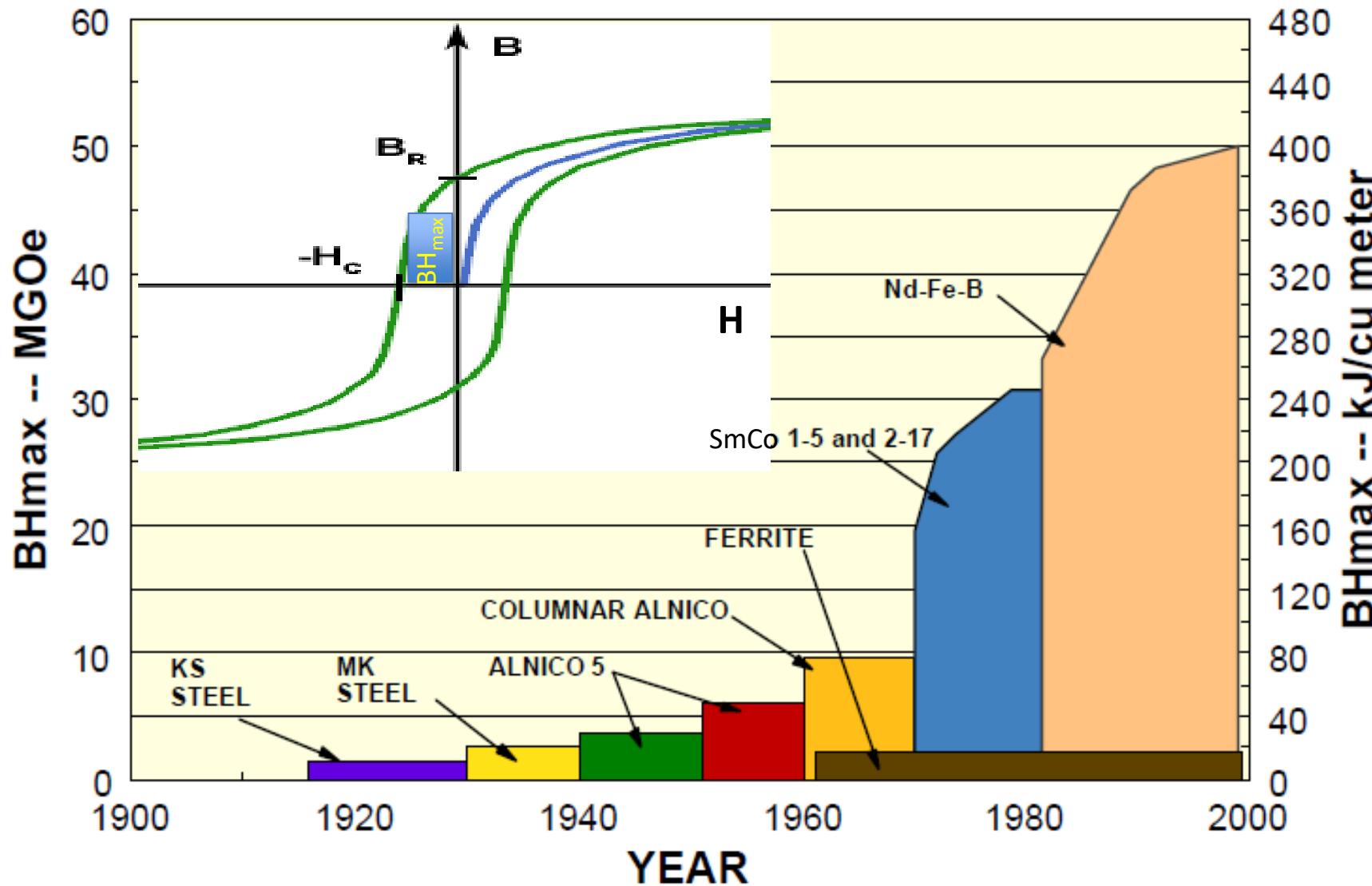
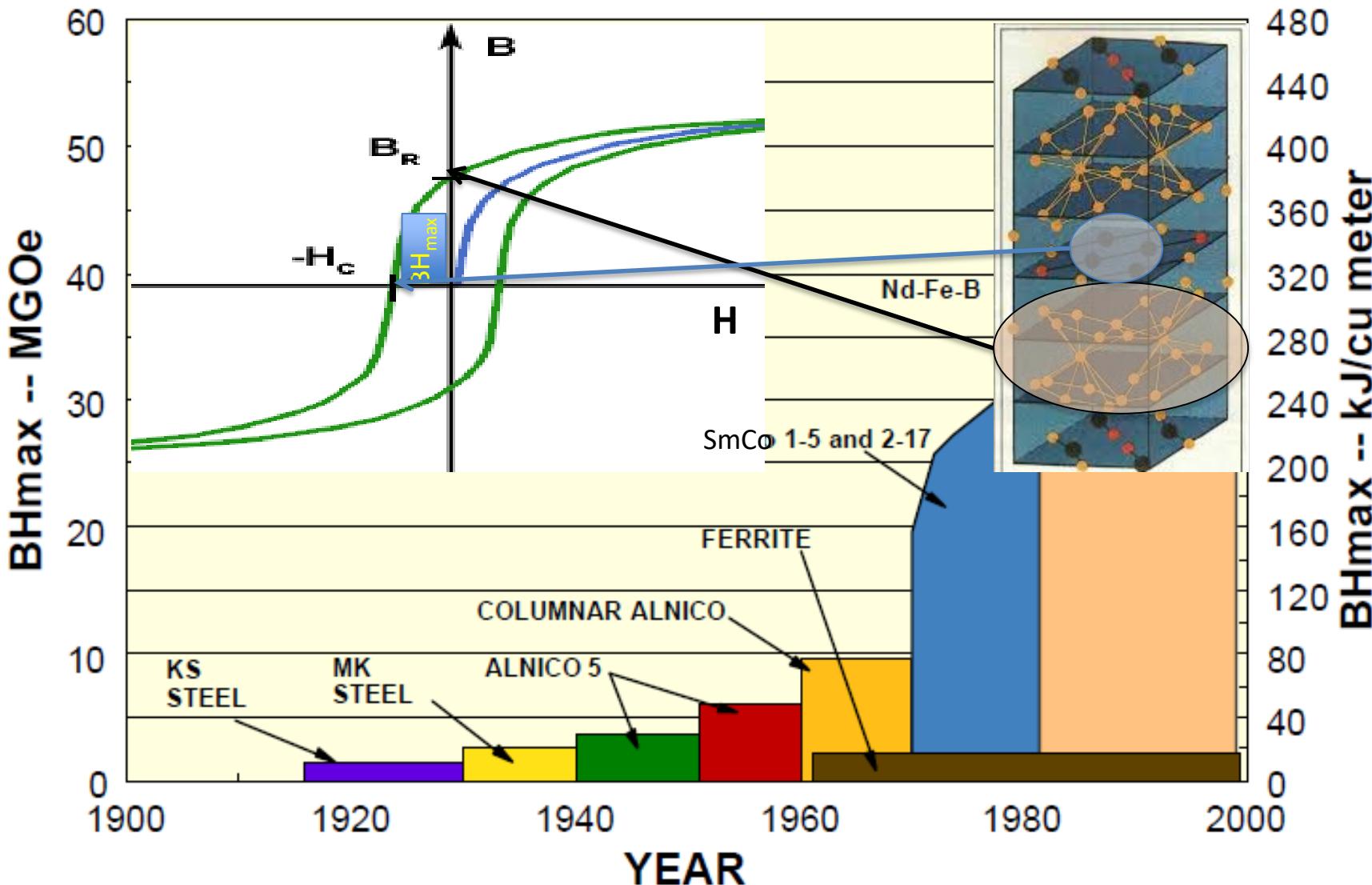
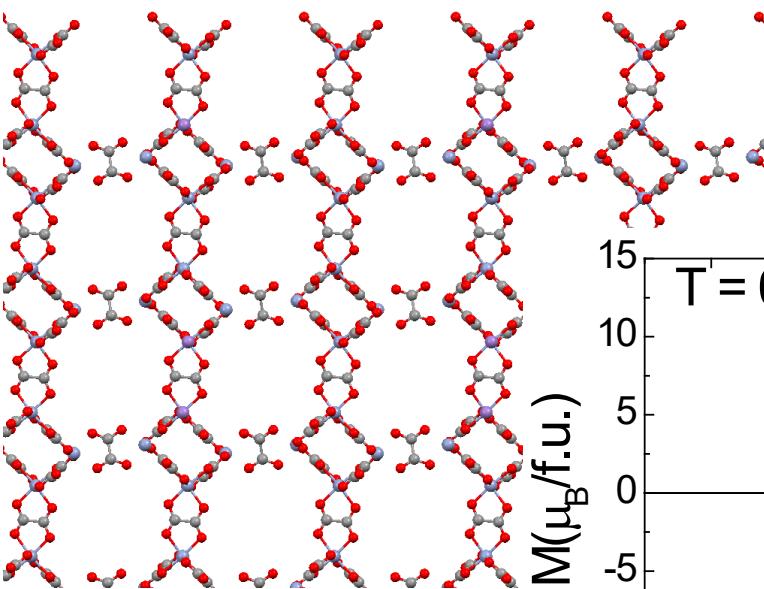


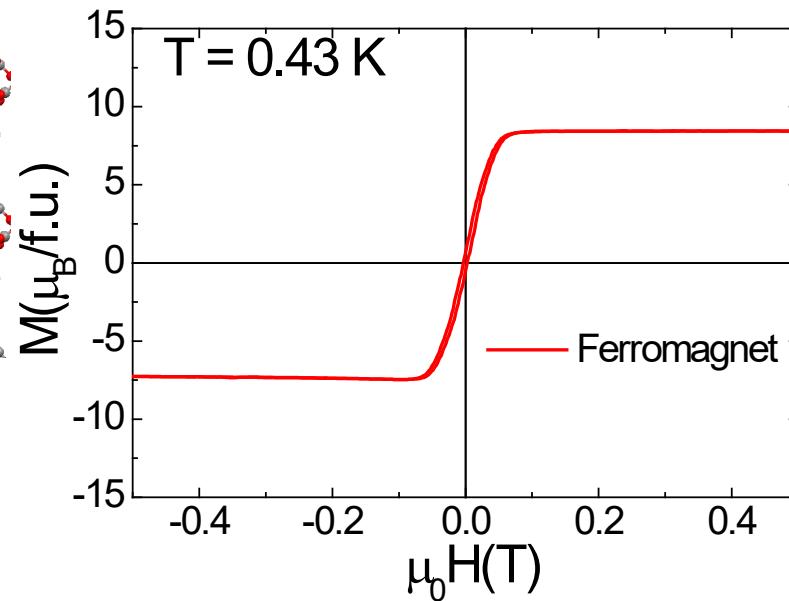
Figure I
Development of Permanent Magnets in the 1900's

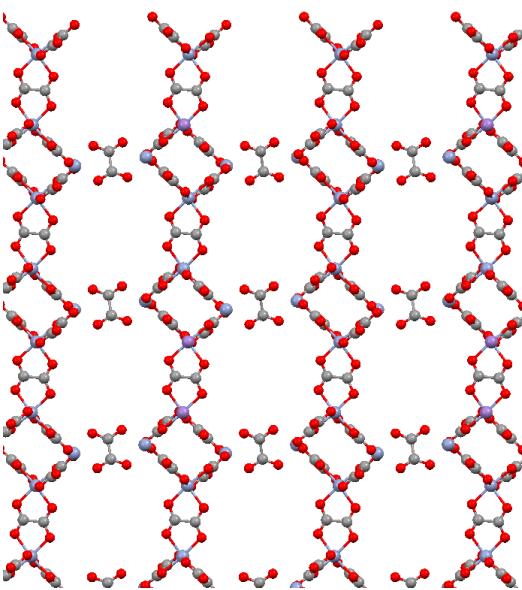




MnCr-oxalate

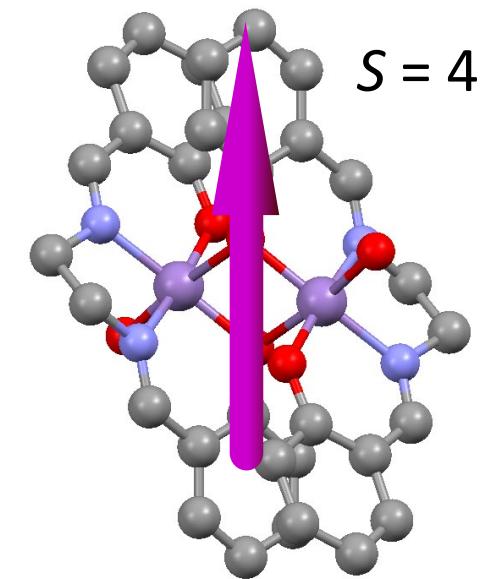
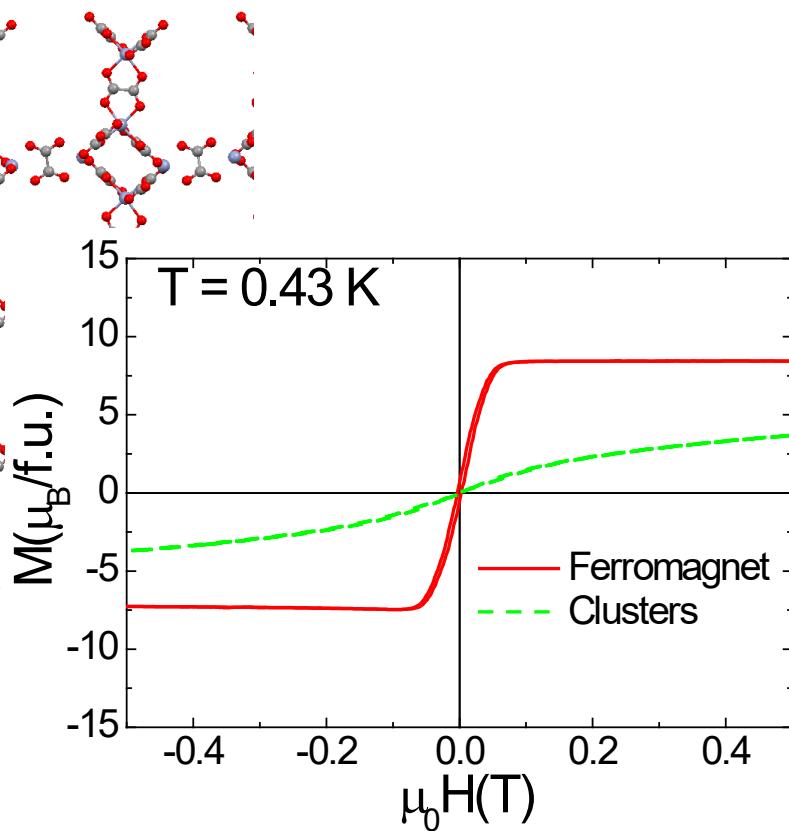
$T_c = 5 \text{ K}$





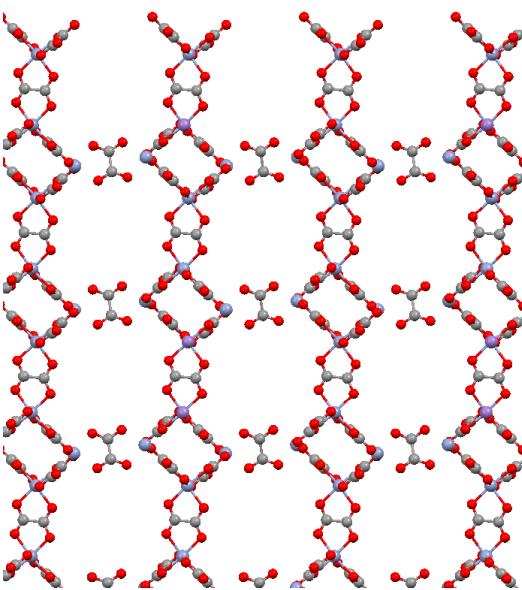
MnCr-oxalate

$T_c = 5 \text{ K}$

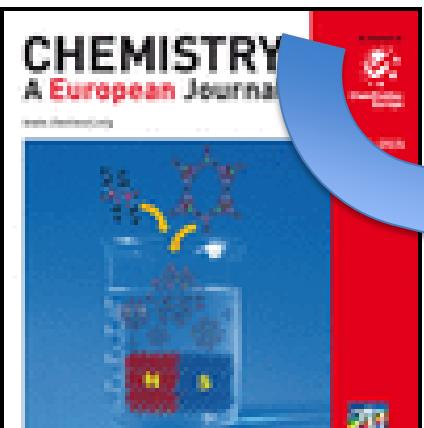
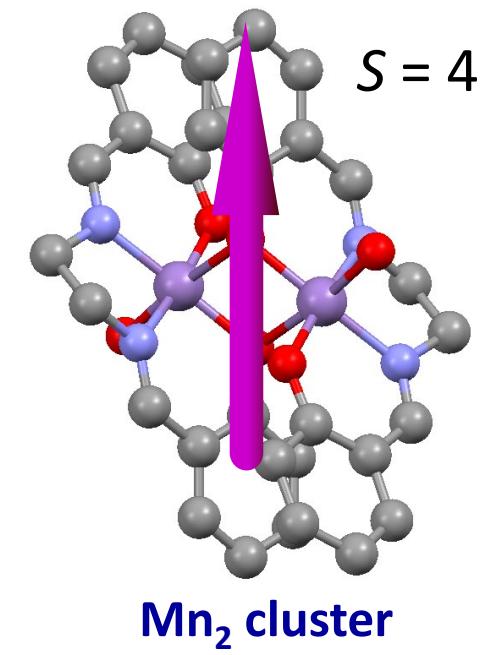
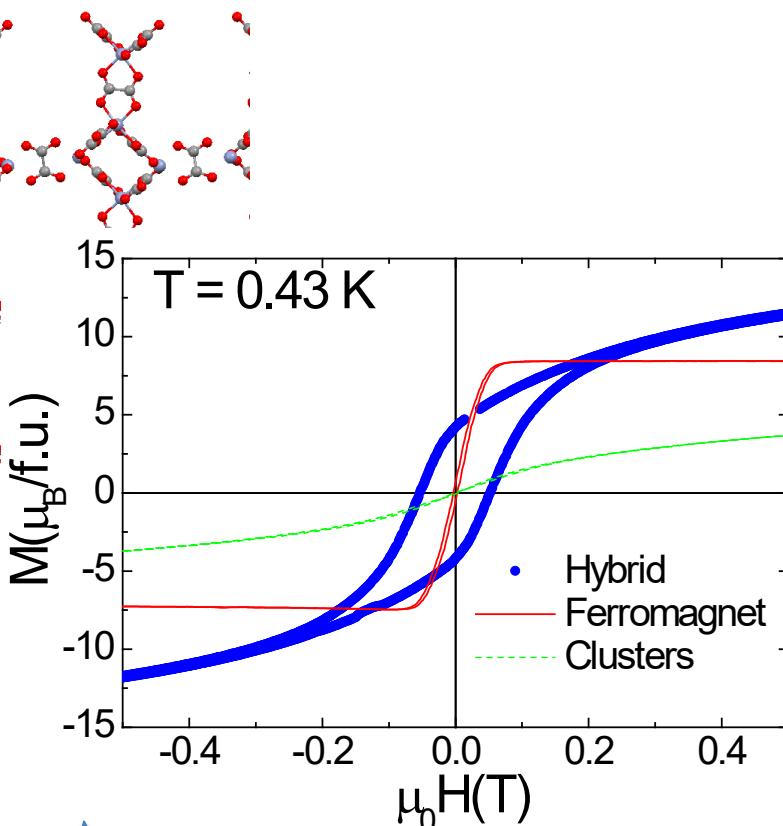


Mn₂ cluster

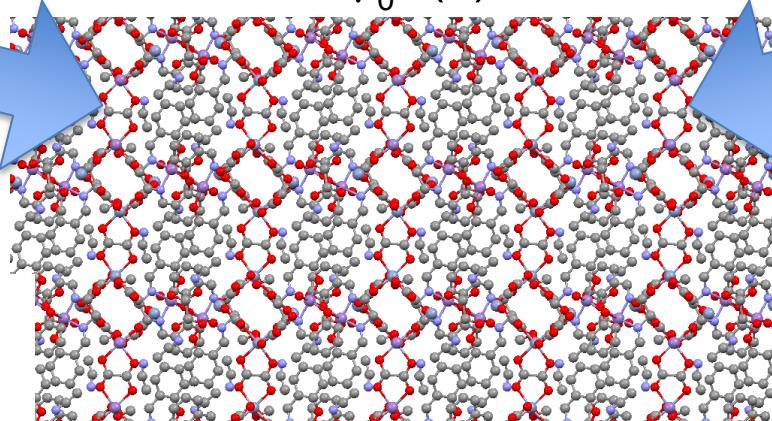
$T_b < 0.4 \text{ K}$



MnCr-oxalate

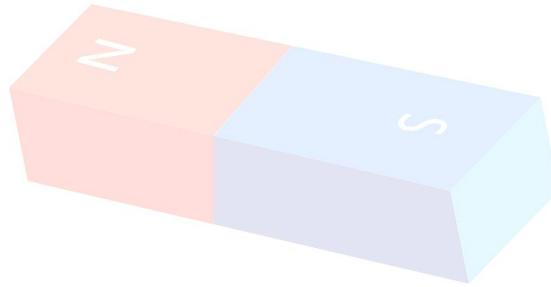


M. Clemente, E. Coronado, C. Gómez, A. Camón, A. Repollés, F. Luis, Chem. A Eur. J. **20**, 1669 (2014)

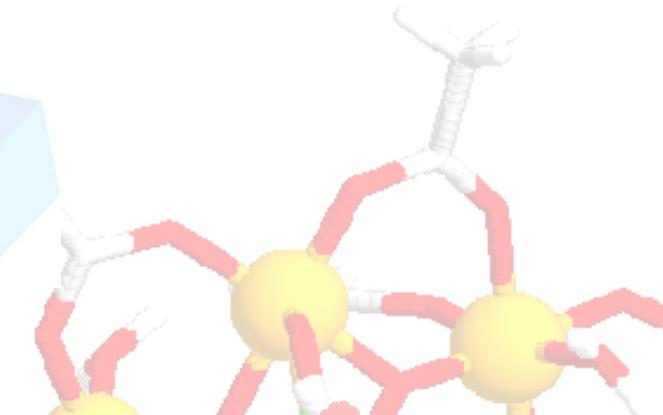


Challenge

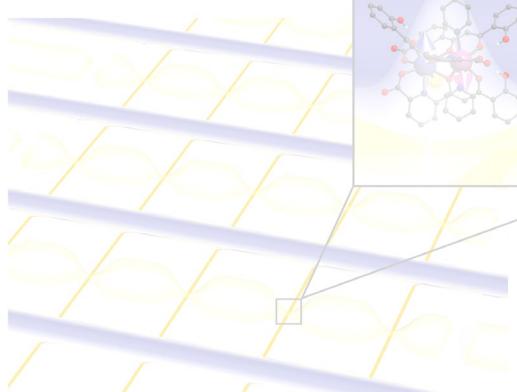
$T_c \approx 5 \text{ K} \rightarrow T_c > 400 \text{ K}$



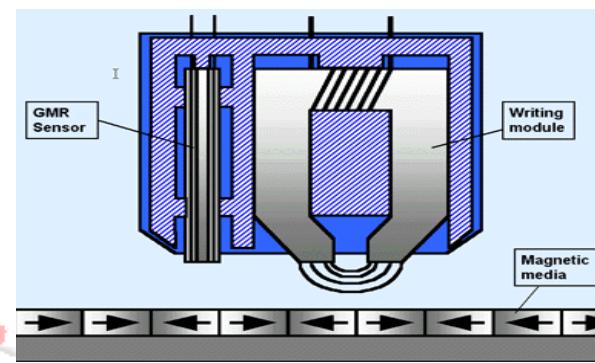
2. Magnets



4. Quantum information



1. Physics



3. Magnetic recording



5. Magnetic coolers



A century of magnetic recording



Telephone
Denmark
1898

RAMAC
IBM
1956



Magnetic hard disk
2021



A century of magnetic recording



Telephone
Denmark
1898

RAMAC
IBM
1956

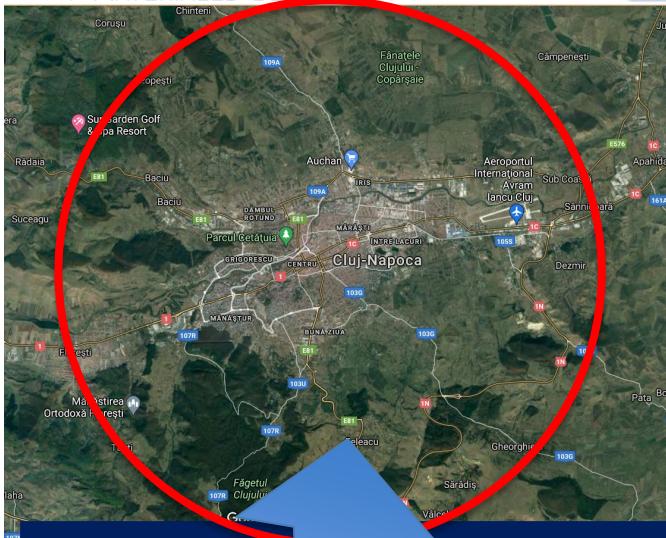


Magnetic hard disk
2021

1 Tbyte



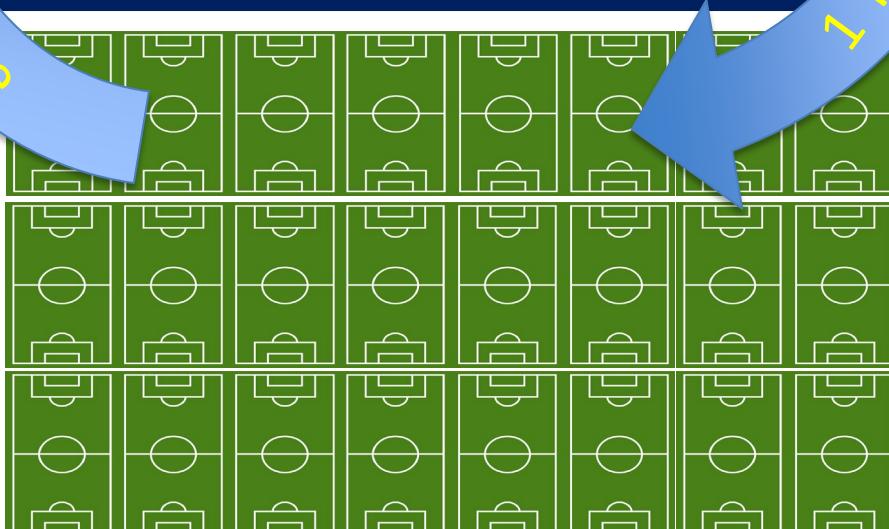
A century of magnetic recording



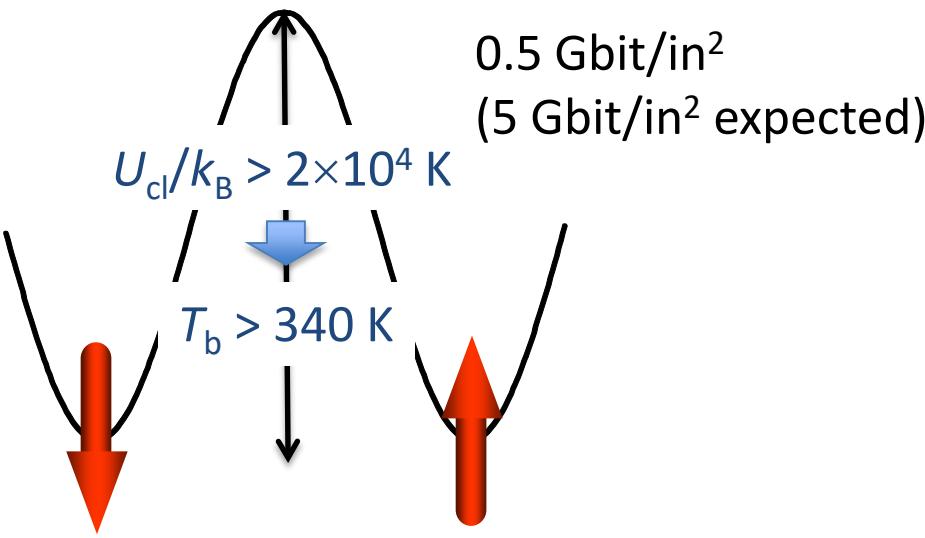
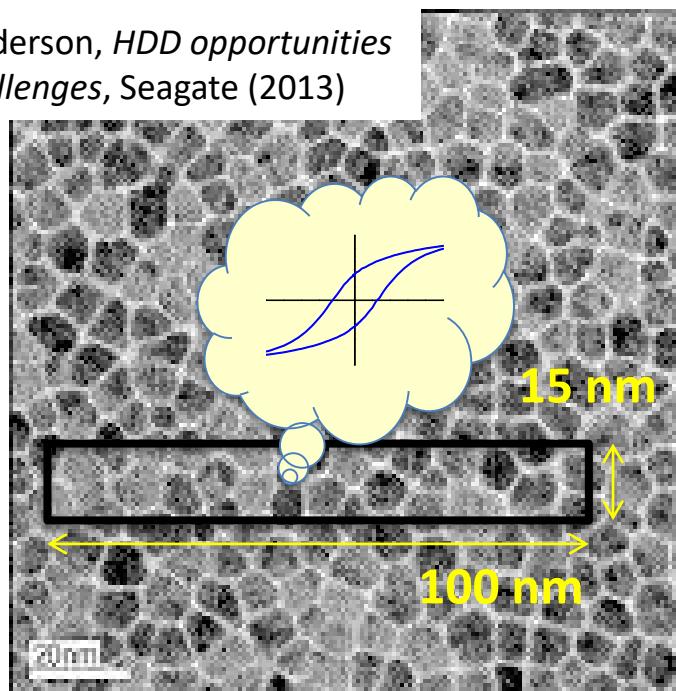
Telegraphor
Denmark
1898

RAMAC
IBM
1956

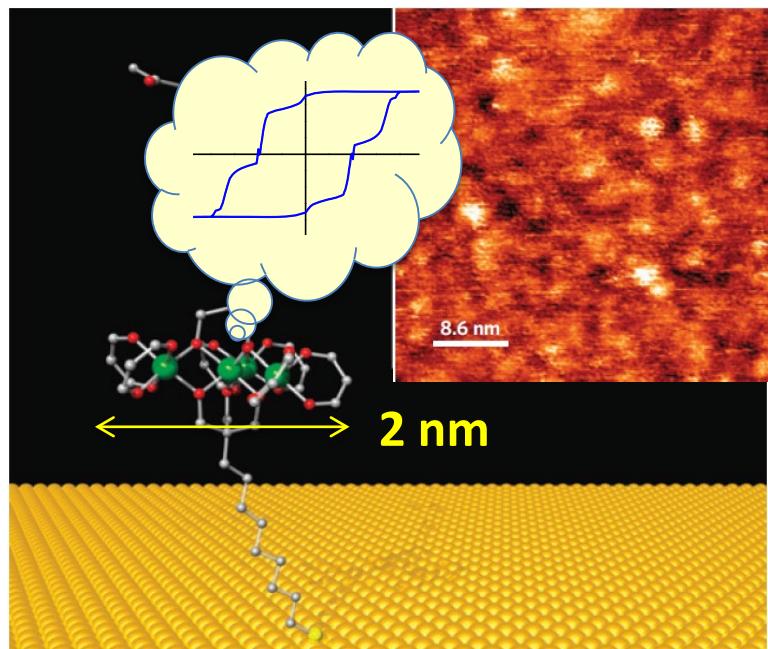
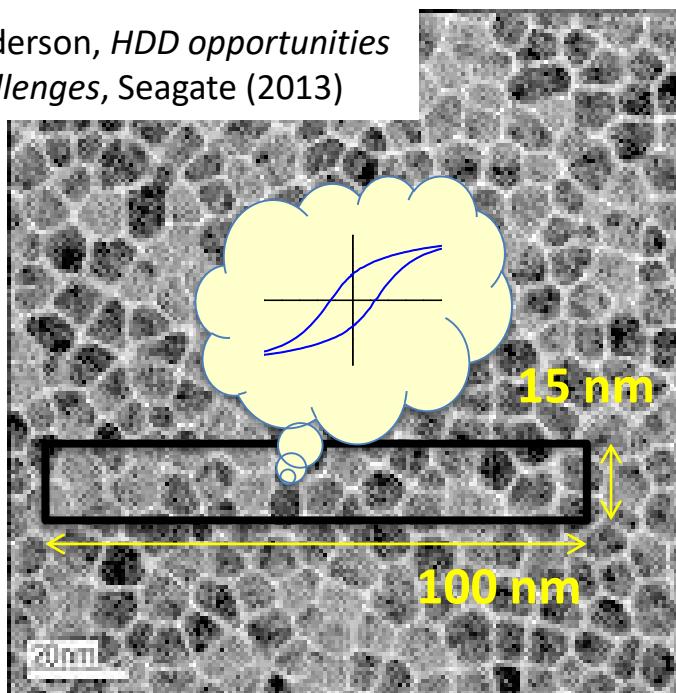
Magnetic hard disk
2021



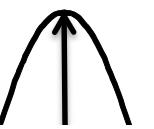
D. Anderson, *HDD opportunities & challenges*, Seagate (2013)



D. Anderson, *HDD opportunities & challenges*, Seagate (2013)



M. Mannini *et al*, Nature **468**, 417 (2010)

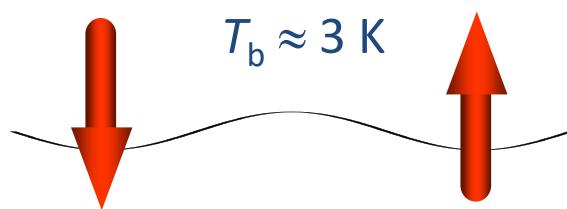

 $U_{\text{cl}}/k_B > 2 \times 10^4 \text{ K}$
 $T_b > 340 \text{ K}$

0.5 Gbit/in²
(5 Gbit/in² expected)

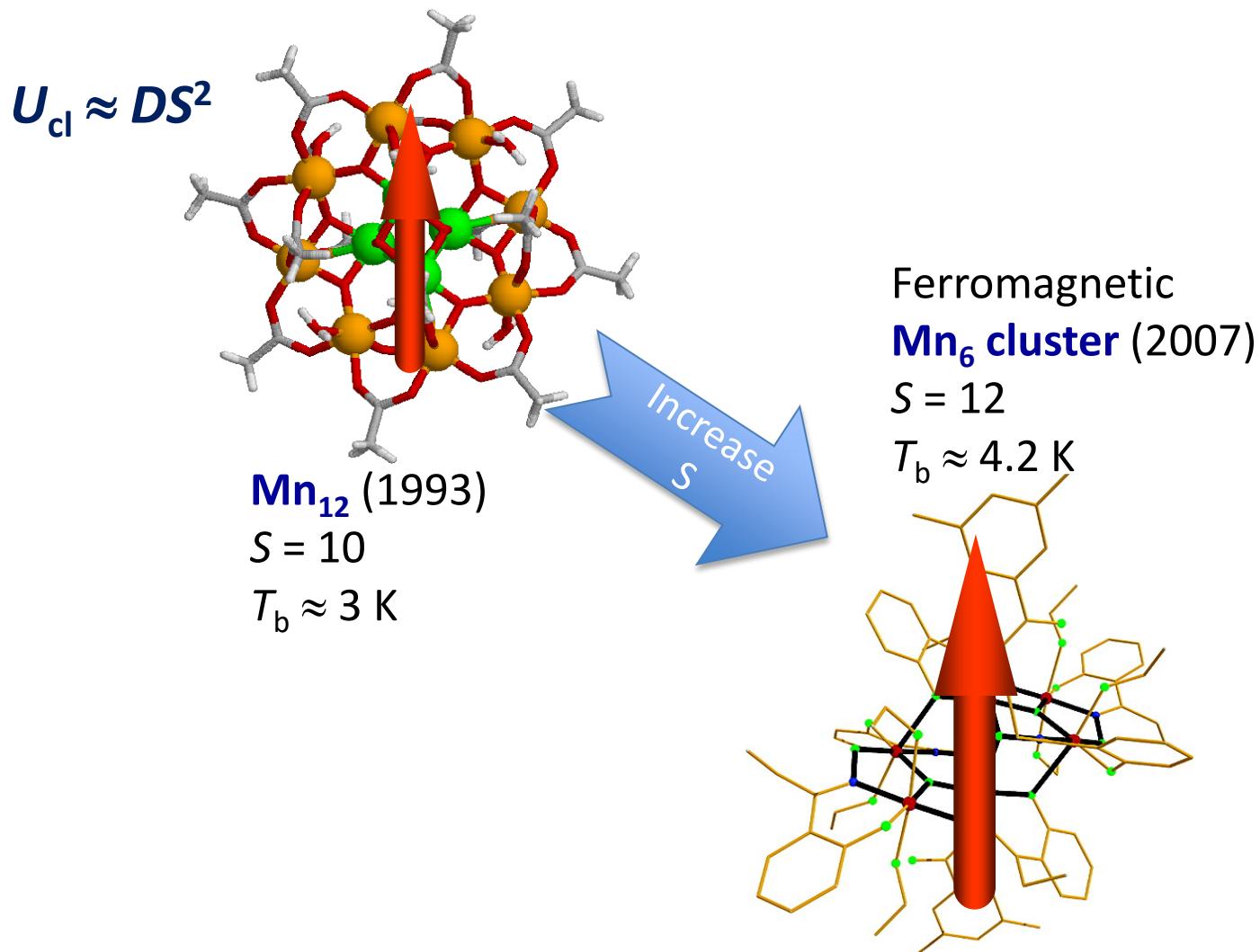
5 Gbit/in² – 50 Gbit/in²

BUT

$U_{\text{cl}}/k_B \approx 70 \text{ K}$
 $T_b \approx 3 \text{ K}$

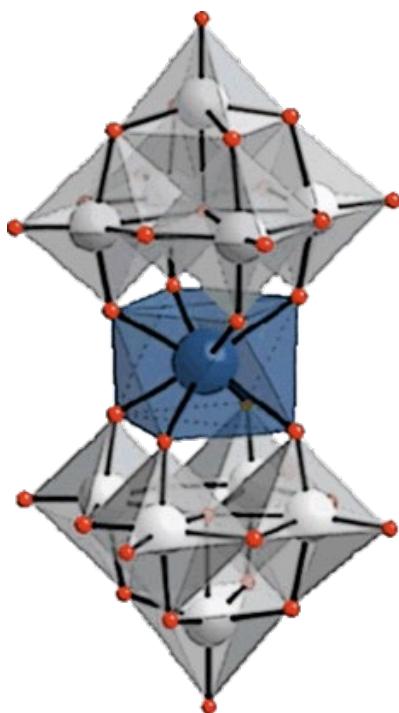


The challenge: enhance T_b



C. Milius *et al*, J. Am. Chem. Soc. **129**, 2754 (2007)

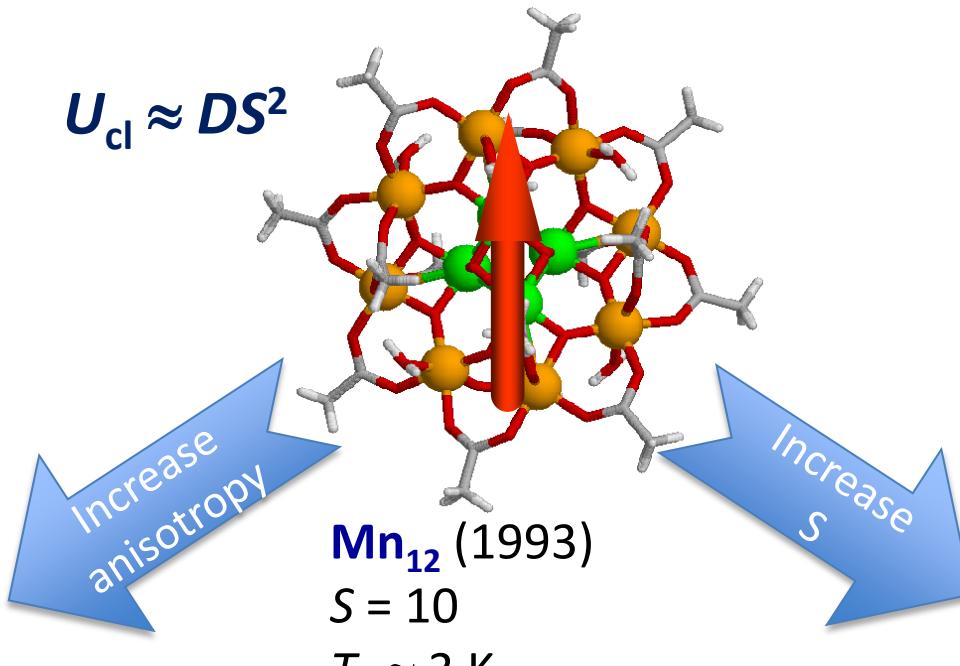
The challenge: enhance T_b



Lanthanide single ion magnets

J. van den Broek and L. C. van der Marel, Physica **29**, 948 (1963);
 N. Ishikawa et al, J. Am. Chem. Soc. **125**, 8694 (2003); M. AlDamen
 et al, J. Am. Chem. Soc. **130**, 8874 (2008); ...

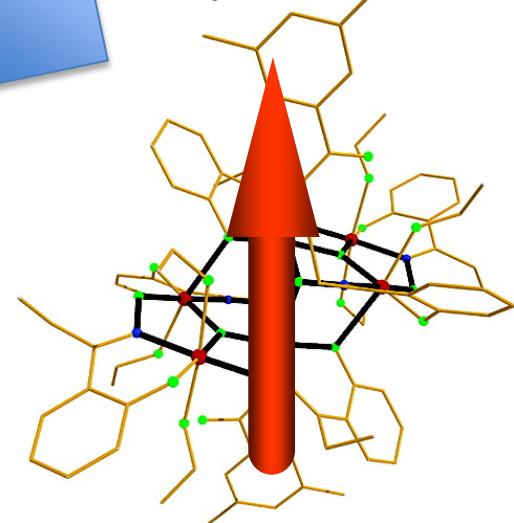
$$U_{\text{cl}} \approx DS^2$$



Ferromagnetic
Mn₆ cluster (2007)

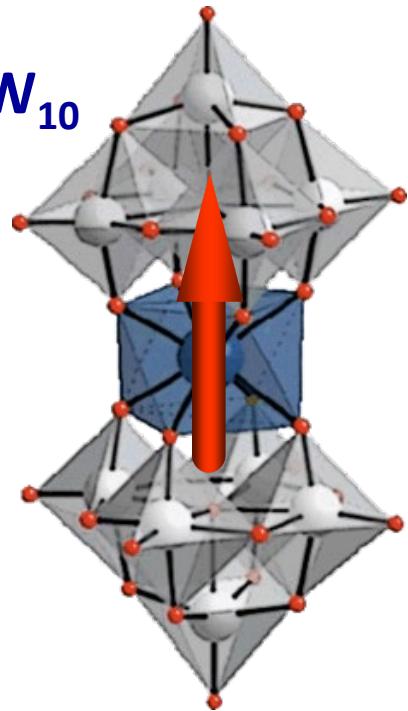
$$S = 12$$

$$T_b \approx 4.2 \text{ K}$$



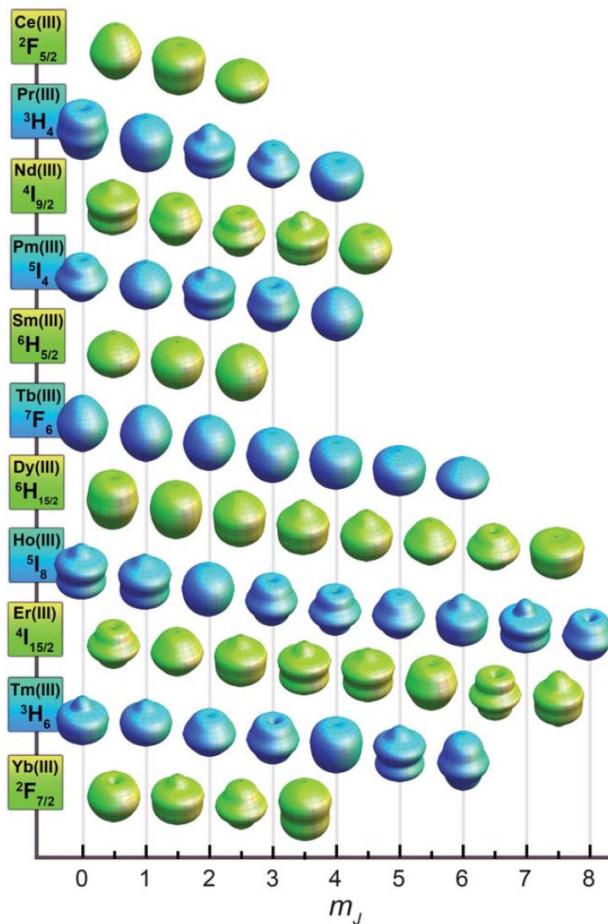
C. Milios et al, J. Am. Chem. Soc. **129**,
 2754 (2007)

LnW₁₀

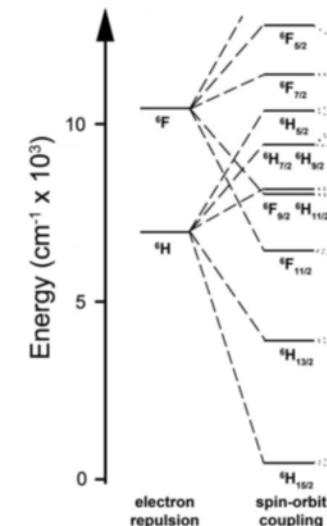


High magnetic moment

$$\vec{\mu} = g_J \mu_B \vec{J}$$

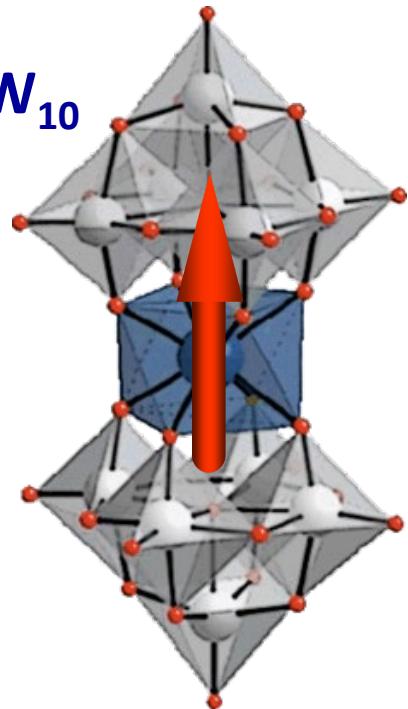


A. Abragam and B. Bleaney, *EPR of transition ions*, Dover (New York 1970); J. D. Rinehart and J. R. Long, Chem. Sci. **2**, 2078 (2011)



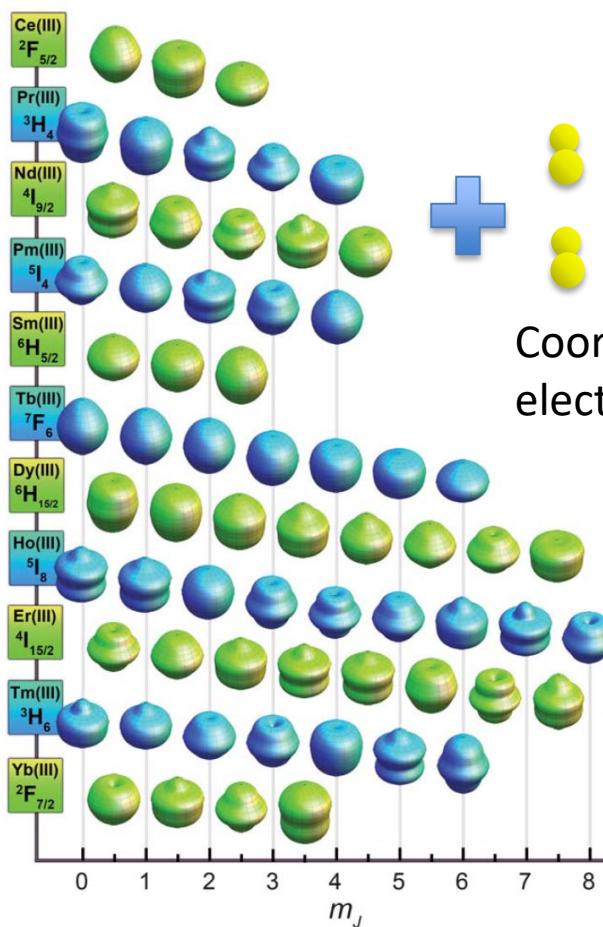
Lanthanide single-ion magnets

LnW₁₀

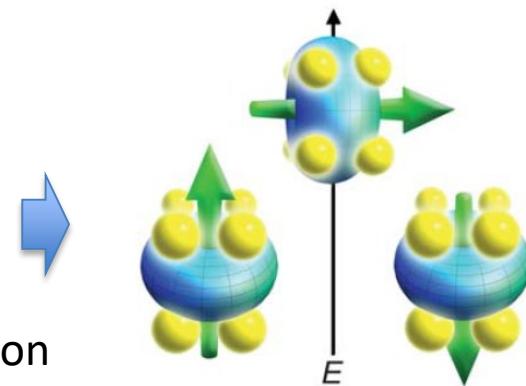


High magnetic moment

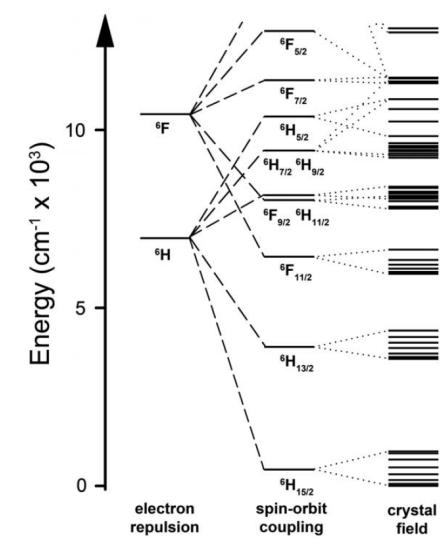
$$\vec{\mu} = g_J \mu_B \vec{J}$$



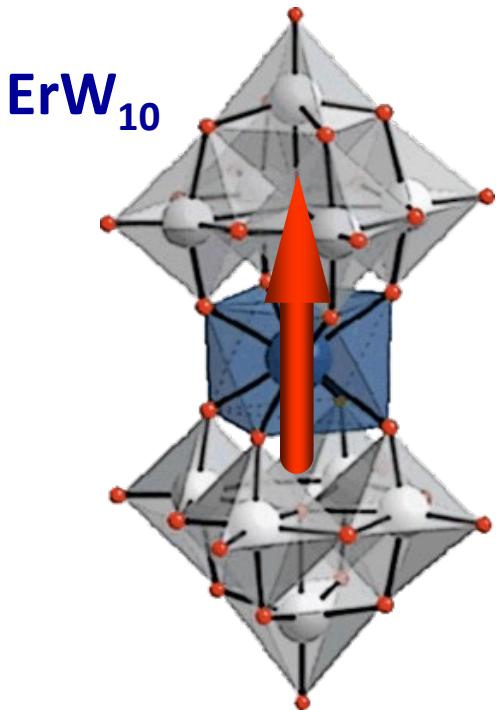
Strong magnetic anisotropy



Coordination
electrons



A. Abragam and B. Bleaney, *EPR of transition ions*, Dover (New York 1970); J. D. Rinehart and J. R. Long, *Chem. Sci.* **2**, 2078 (2011)

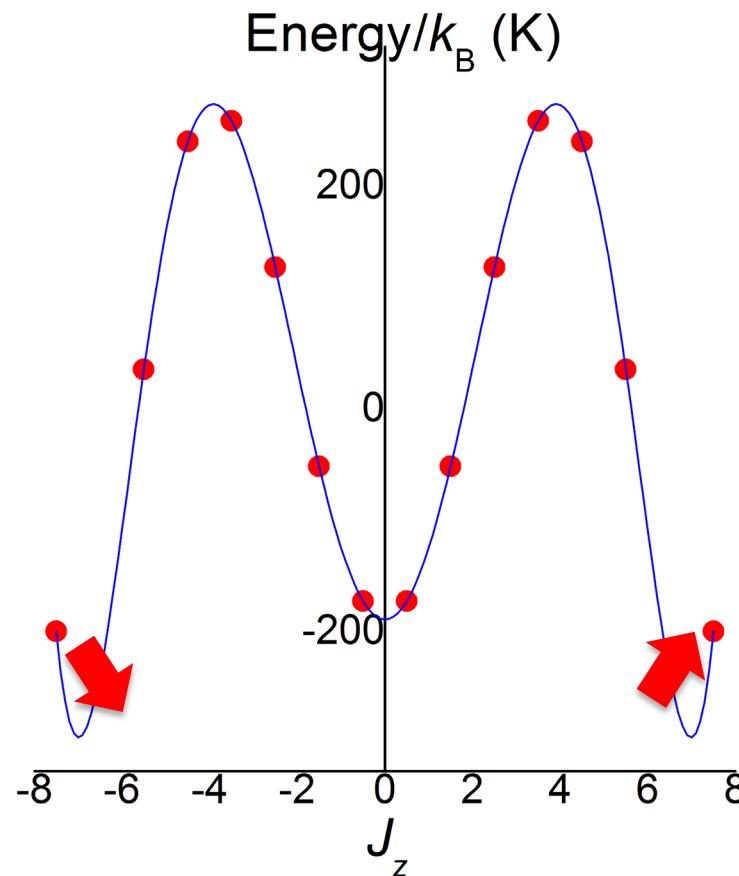


High magnetic moment

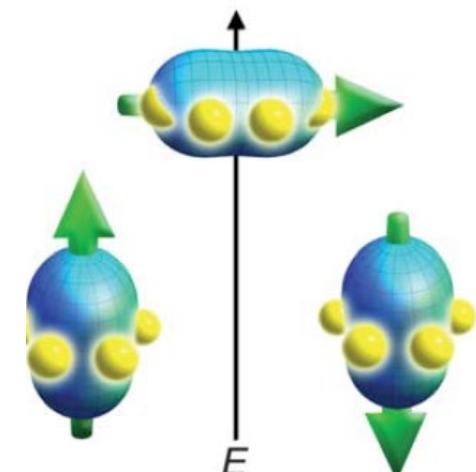
$$\vec{\mu} = g_J \mu_B \vec{J}$$

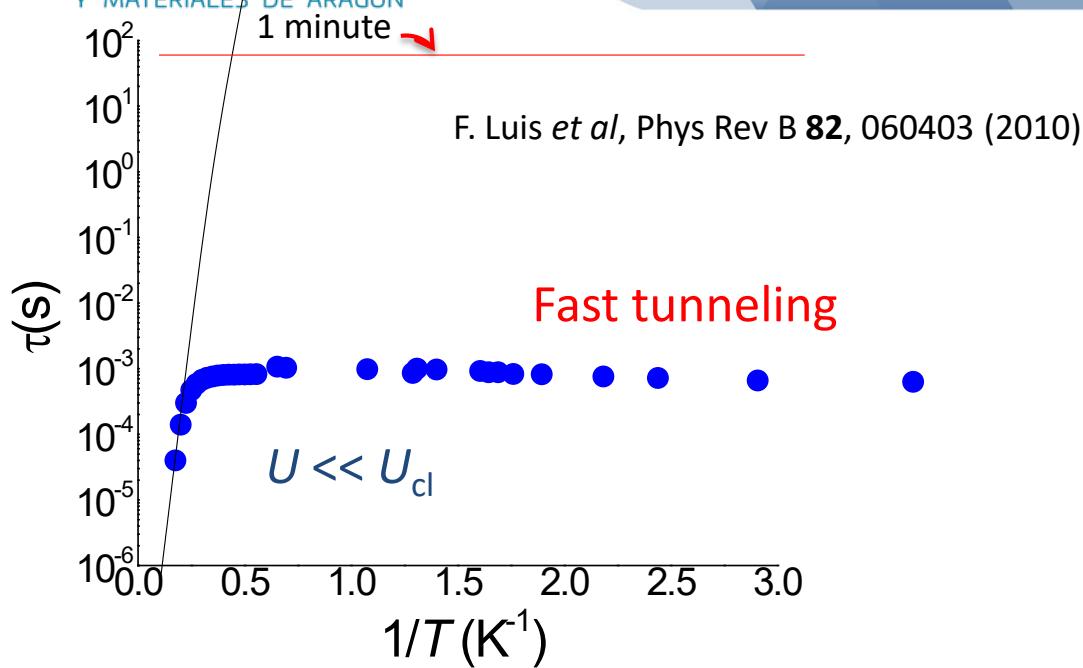
Strong magnetic anisotropy

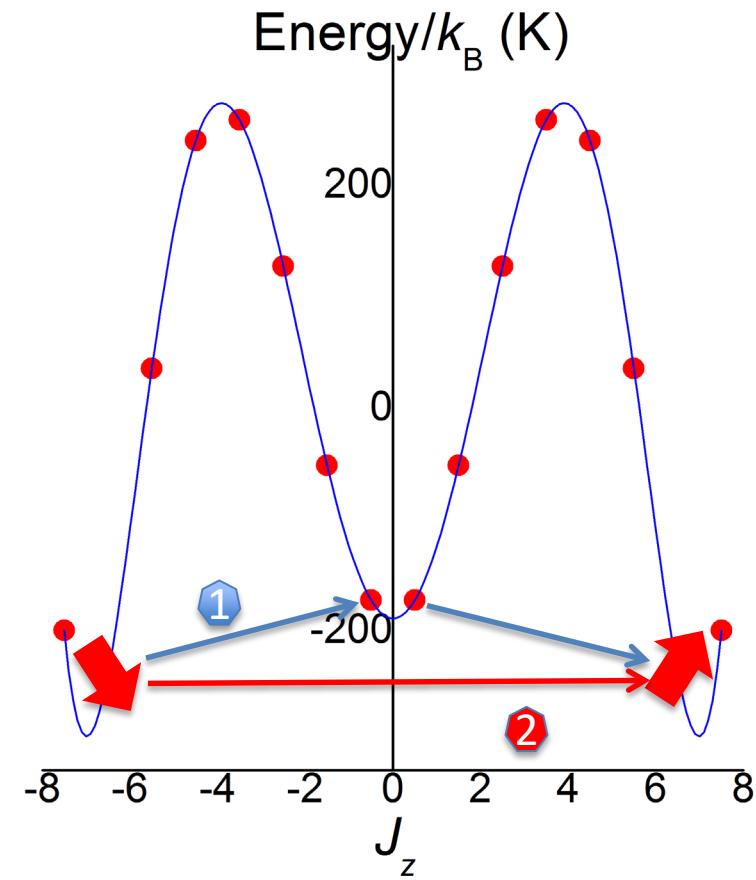
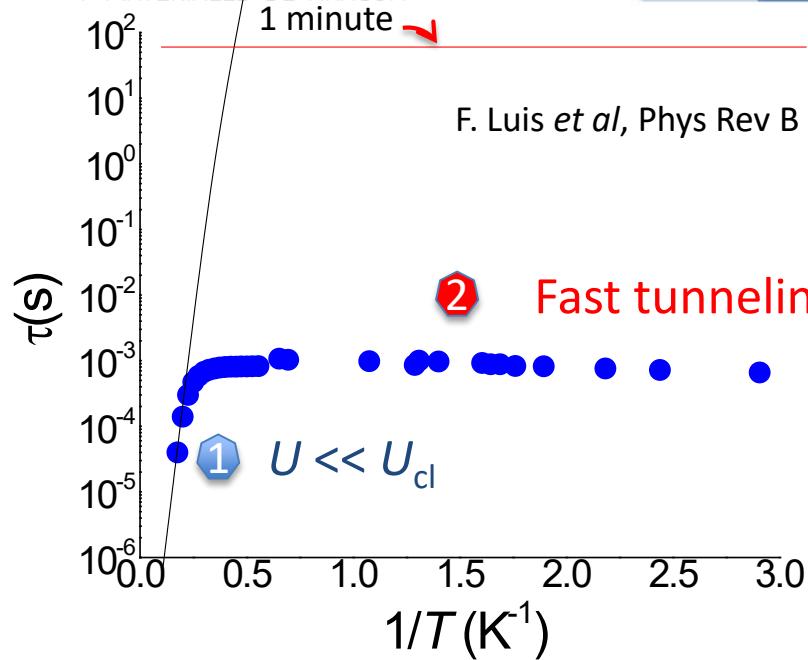
$$\mathcal{H} = \sum_{n,\text{even}} B_n^0 O_n^0 + \sum_{\substack{n,\text{even} \\ m \leq n}} B_n^m O_n^m$$

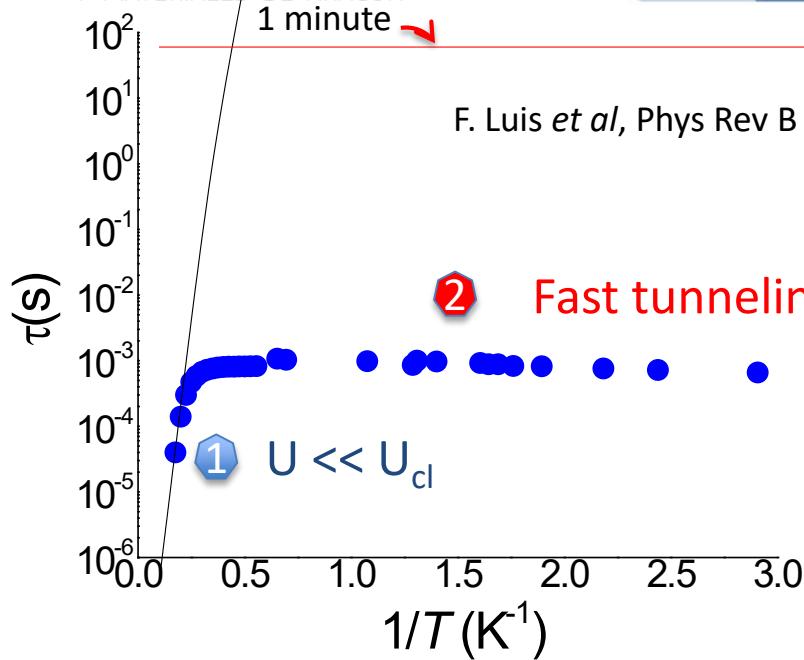


K. W. H. Stevens Proc. Phys. Soc.
London A **65**, 209 (1952)

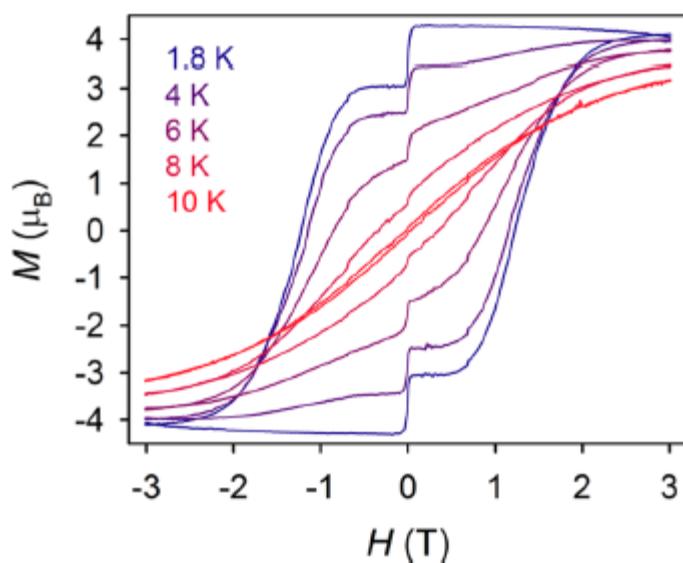








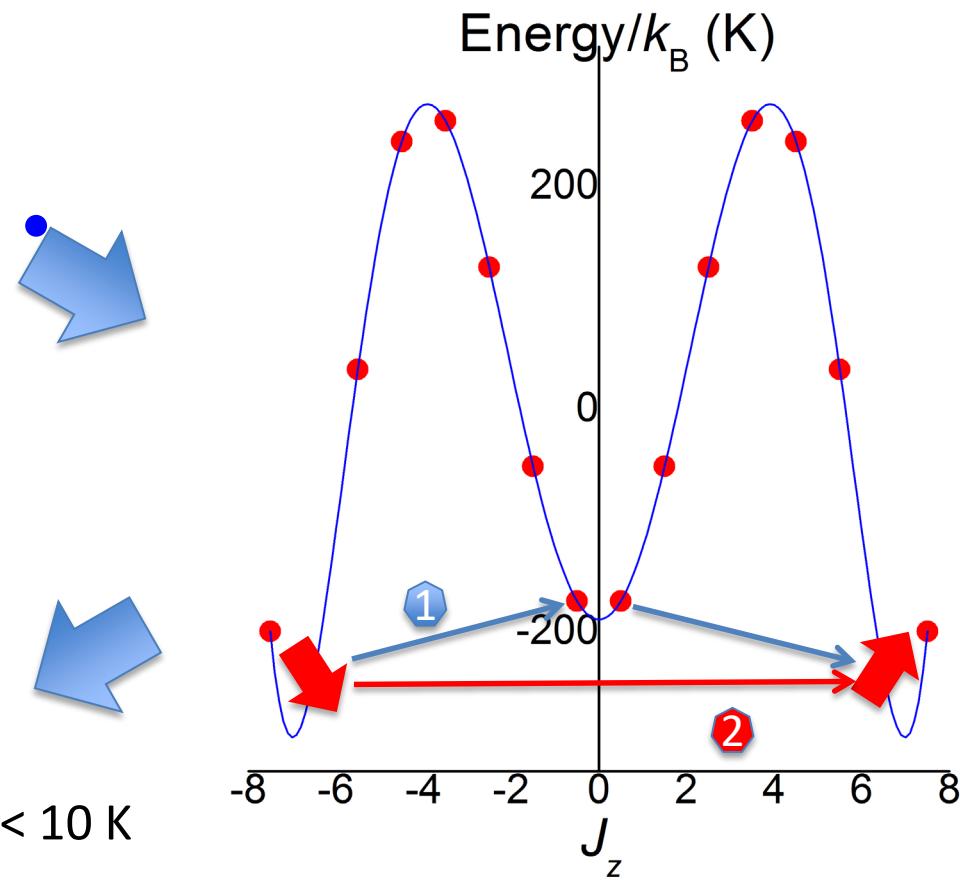
F. Luis *et al*, Phys Rev B **82**, 060403 (2010)



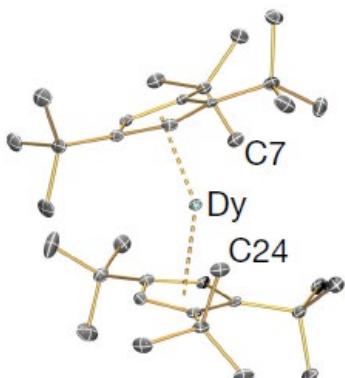
$T_b < 10$ K

$U < 150$ K

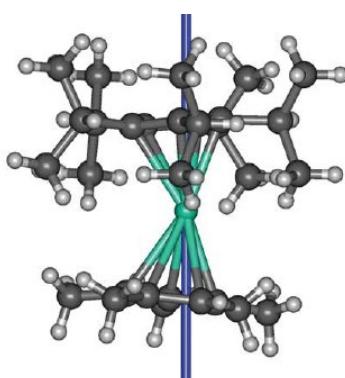
K. R. Meihaus and J. R. Long, J. Am. Chem. Soc. **135**, 17952 (2013)



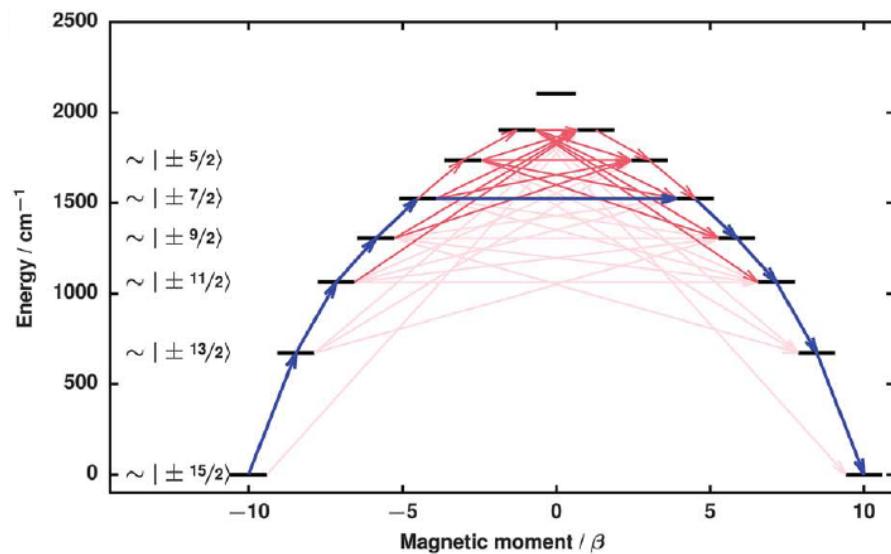
Linear coordination with “oblate” magnetic orbitals (e.g. Dy^{3+})



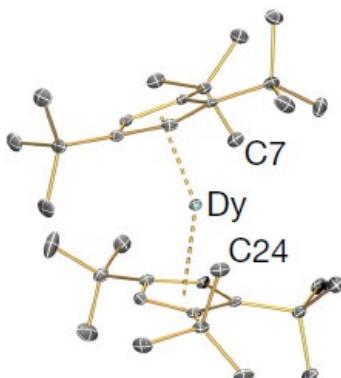
Dysprocenium



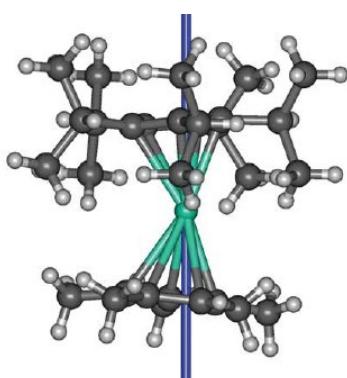
Cp-Dy-Cp*



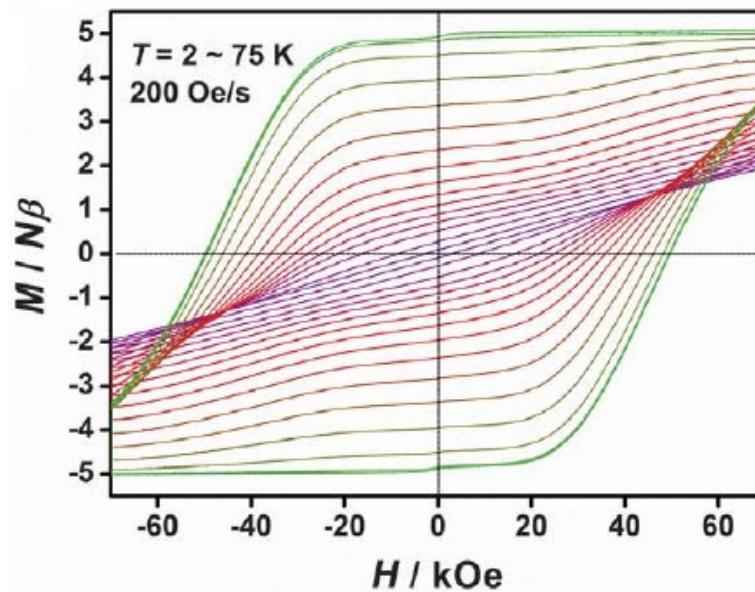
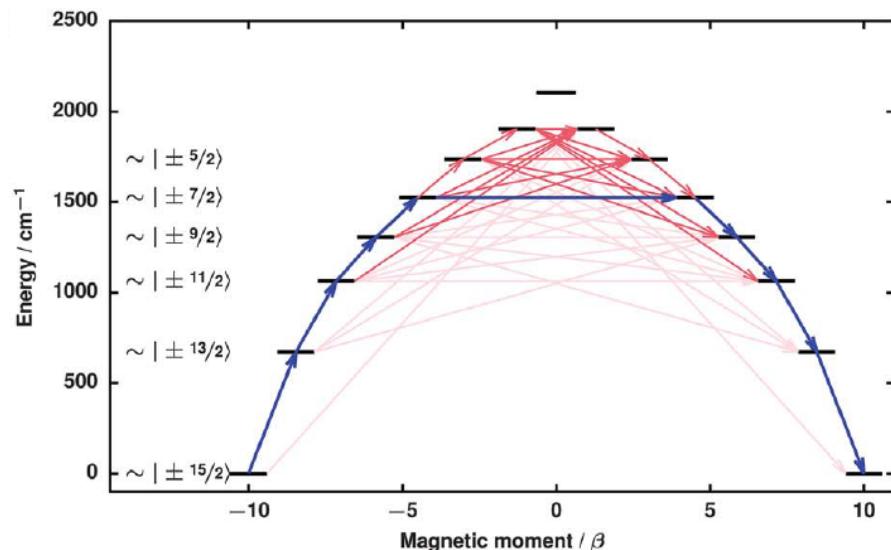
Linear coordination with “oblate” magnetic orbitals (e.g. Dy³⁺)



Dysproceniun

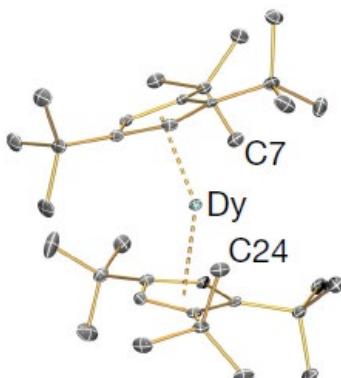


Cp-Dy-Cp*

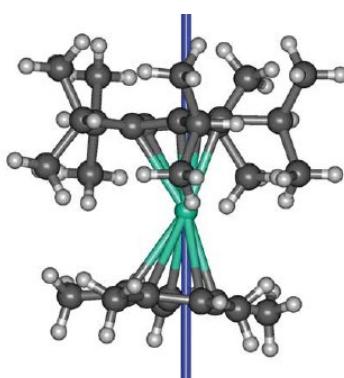


Hysteresis above liquid nitrogen temperatures

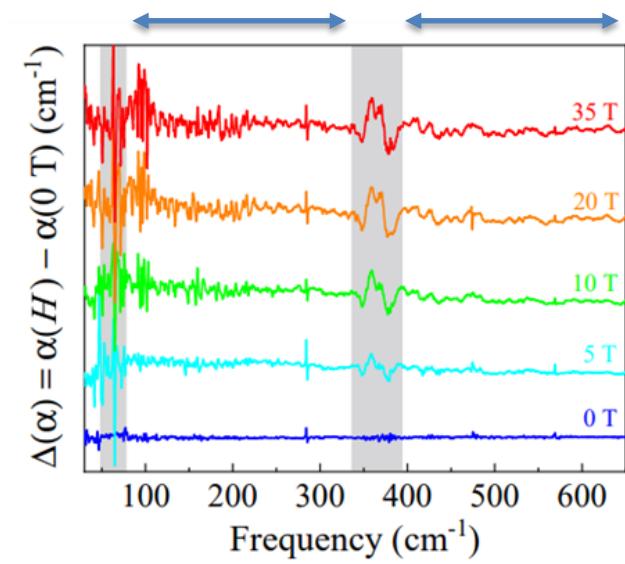
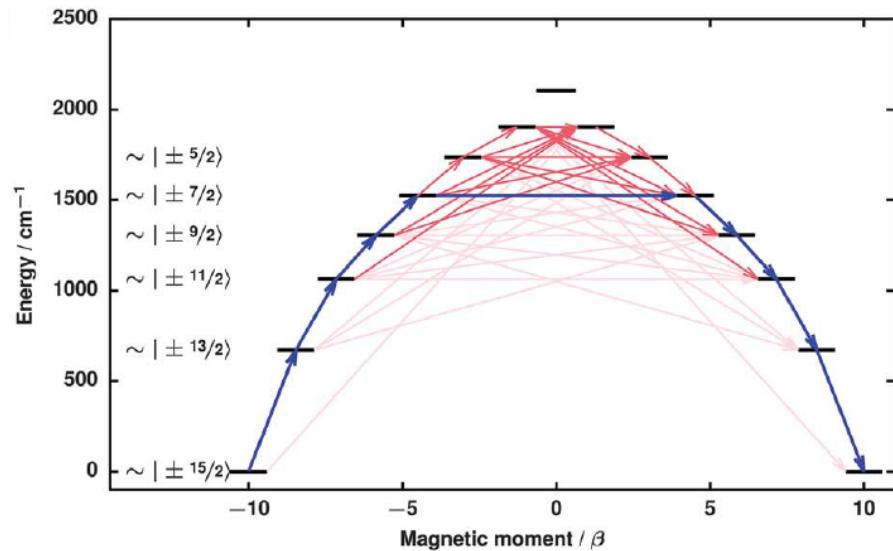
Linear coordination with “oblate” magnetic orbitals (e.g. Dy³⁺)



Dysproceniun



Cp-Dy-Cp*

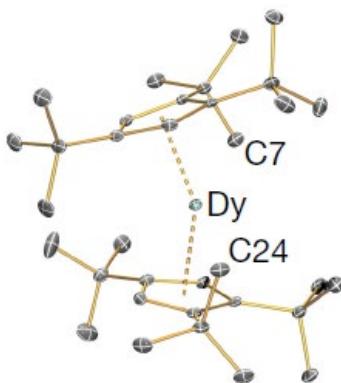


Model and tune key molecular vibrations

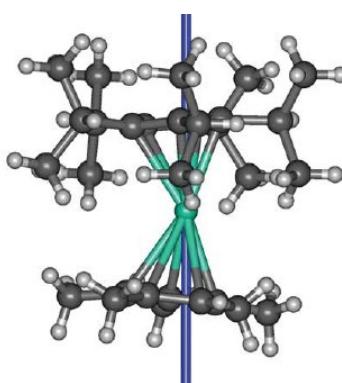


Vibrational “windows”

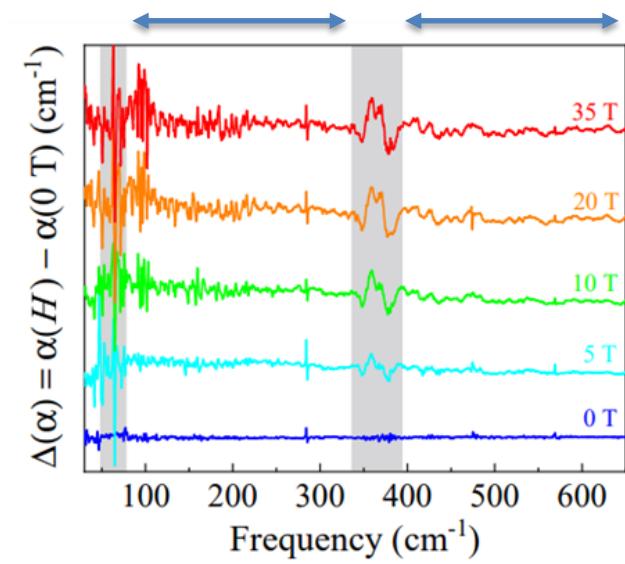
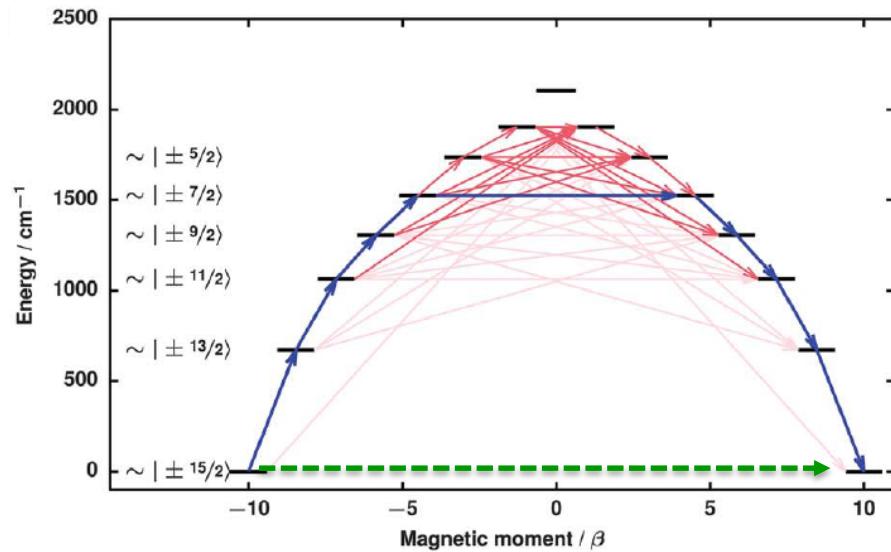
Linear coordination with “oblate” magnetic orbitals (e.g. Dy³⁺)



Dysproceniun



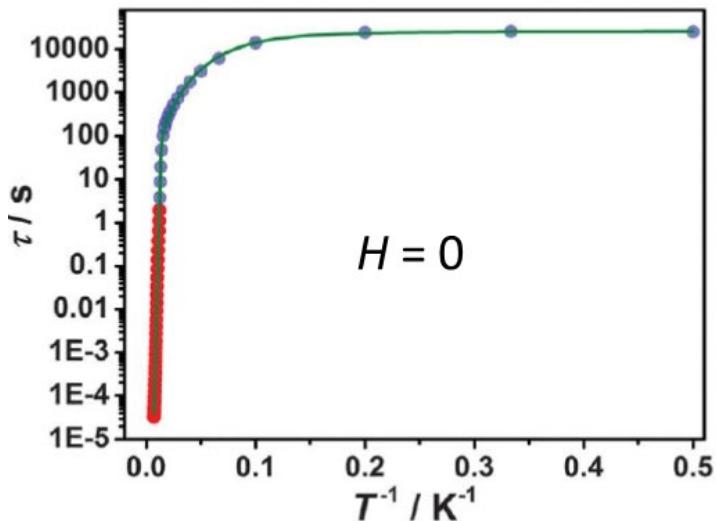
Cp-Dy-Cp*

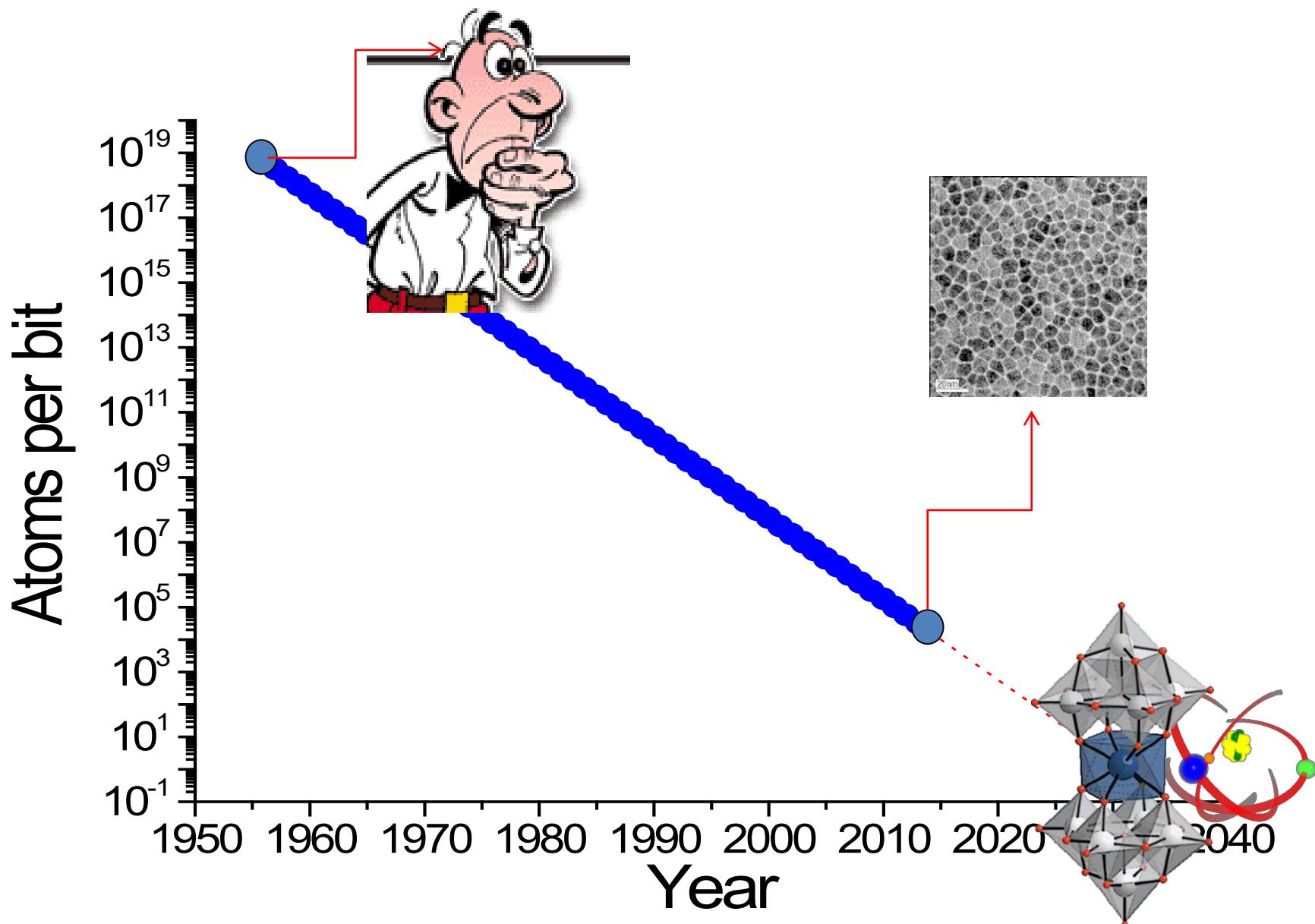


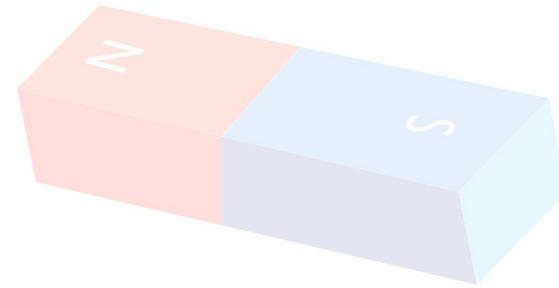
Model and tune key molecular vibrations



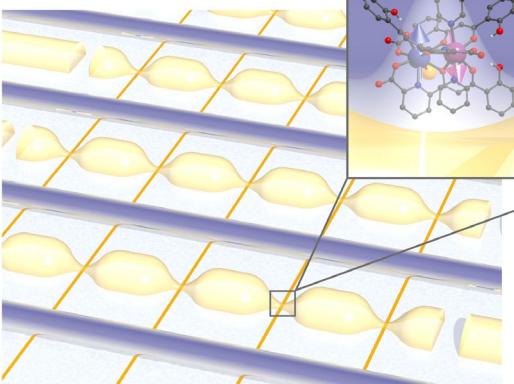
Vibrational “windows”



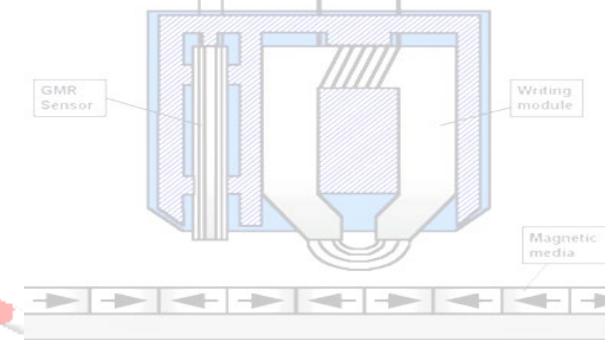
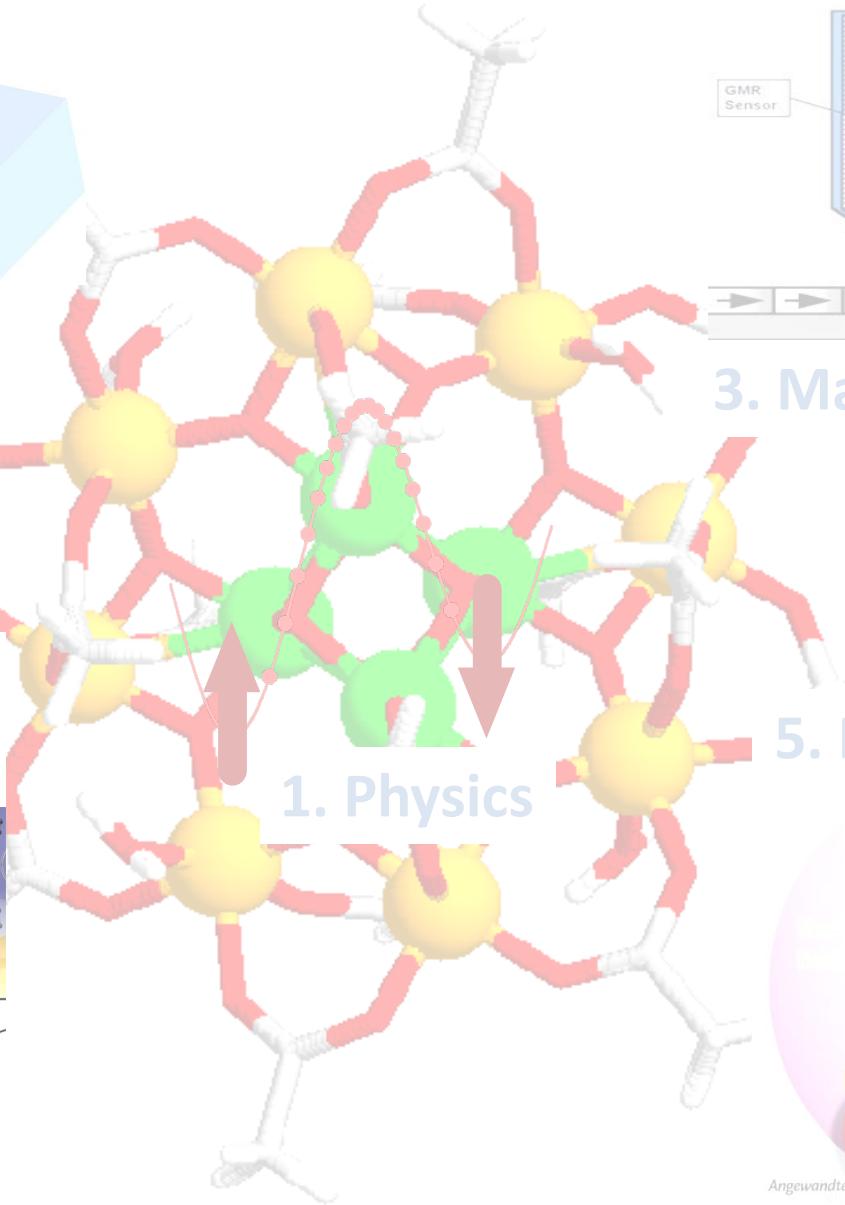




2. Magnets

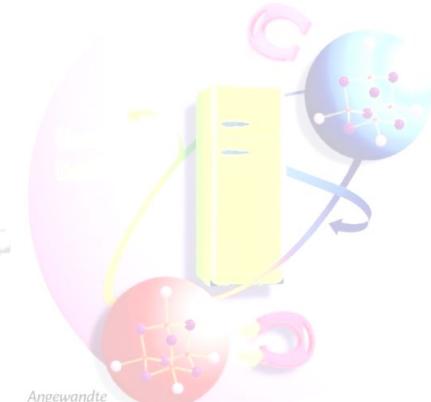


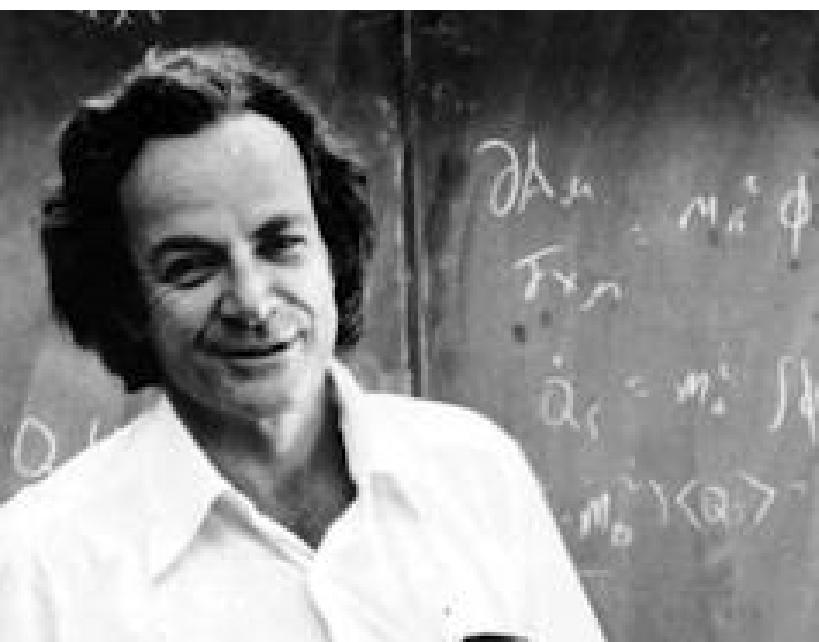
4. Quantum information



3. Magnetic recording

5. Magnetic coolers

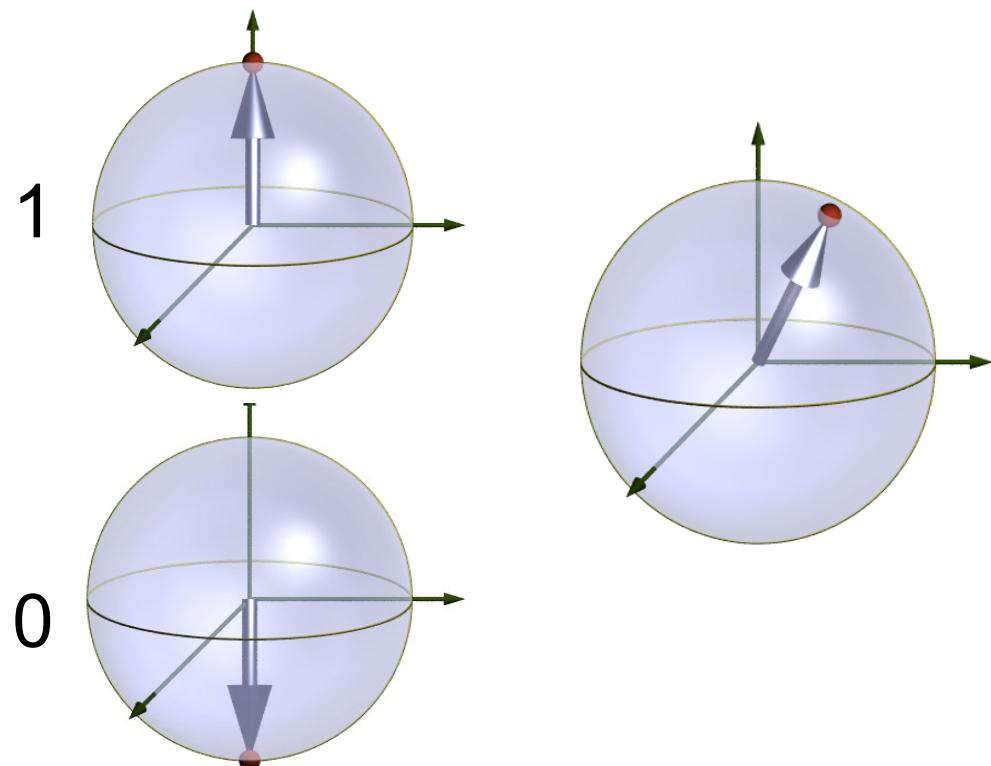


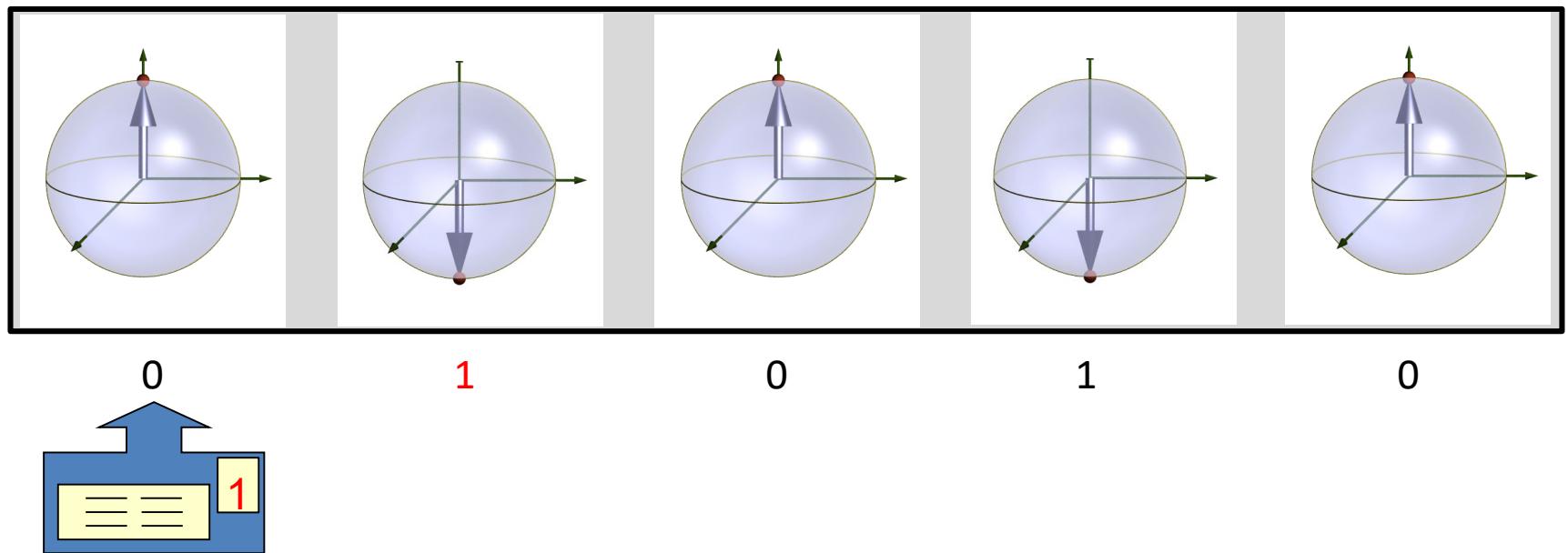


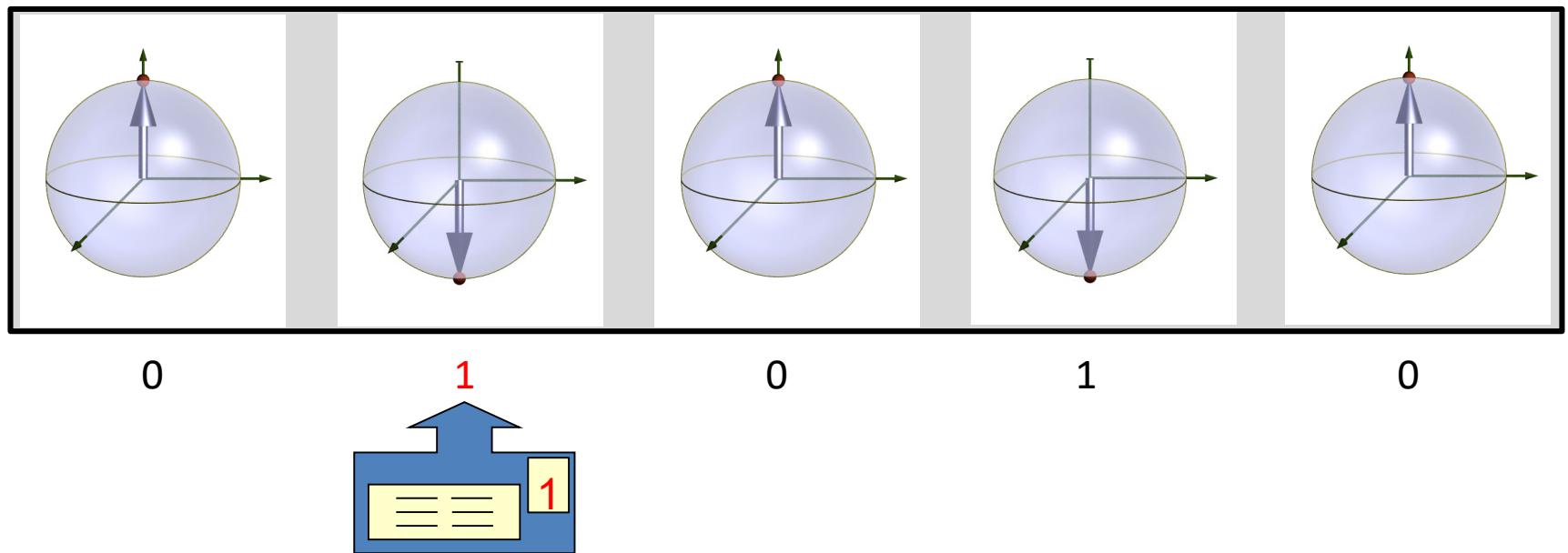
R. P. Feynman, Int. J. Theoret. Phys. **21**,
467 (1982)

D. Deutsch, Proc. Royal Soc. A **400**, 97
(1985)

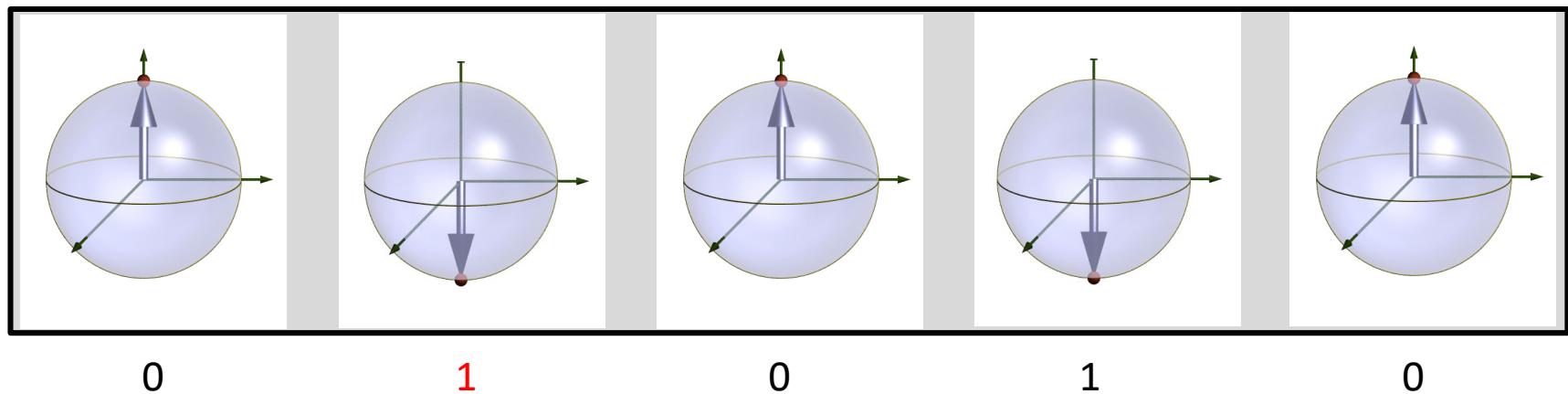
- Process information using quantum laws
- Bit → Qubit



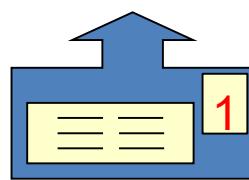
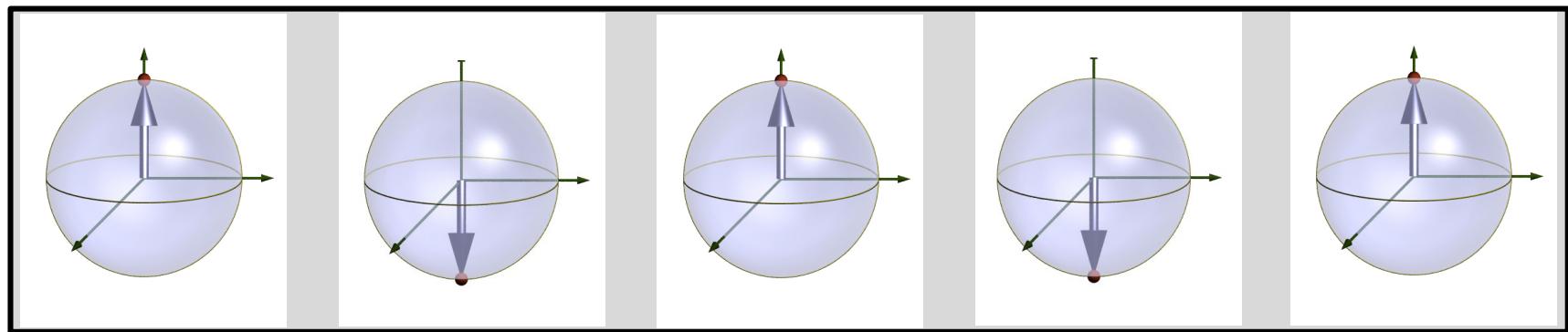




D. Deutsch, Proc. R. Soc. Lond. A **400**, 97 (1985).



+



D. Deutsch, Proc. R. Soc. Lond. A **400**, 97 (1985).

Prime number factorization



Classical $t \propto e^N \Rightarrow$ Quantum $t \propto N^p$

P. W. Shor, in *Proc. Symp. Foundations of Computer Science, IEEE Computer Society Press*, 124 (1994)

Fast database searching



Phone number \Rightarrow Suscriber?

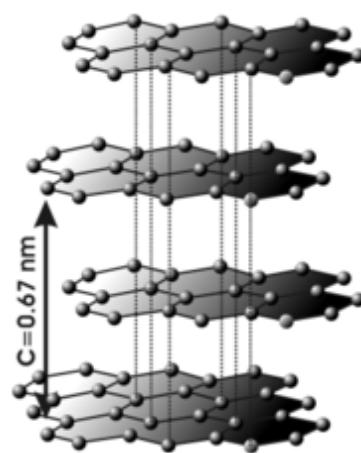
Classical $t \propto N$



Quantum $t \propto \sqrt{N}$

L. K. Grover, Phys. Rev. Lett. **79**, 325 (1997)

Quantum digital simulators



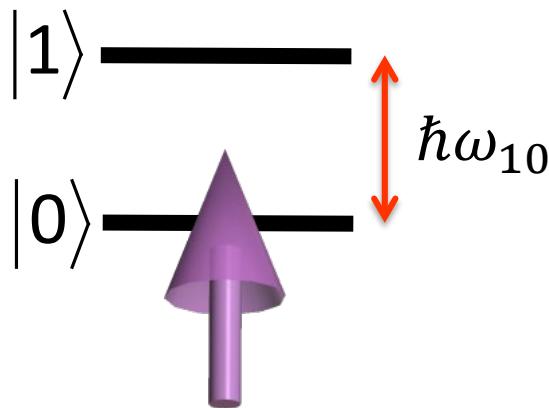
J. I. Cirac & P. Zoller, Nature Phys. **8** 264 (2012)

Classical $t \propto e^N$



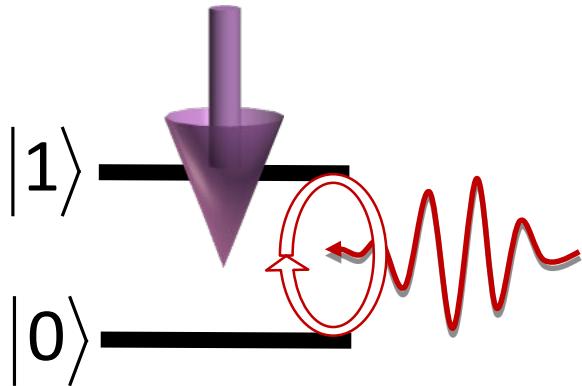
Quantum $t \propto N$

D. P. Di Vincenzo, Fortschr. Phys. **48**, 771 (2000)



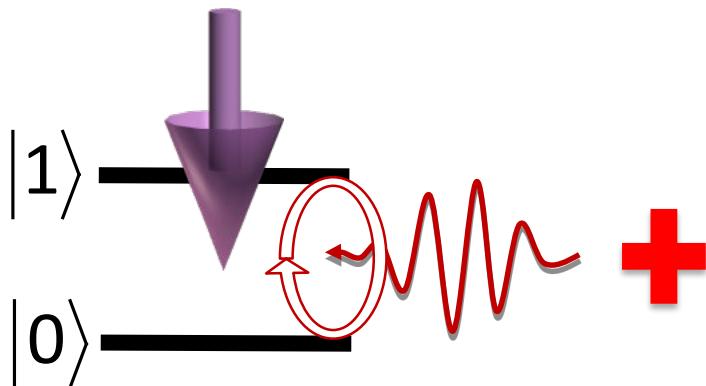
- Two well-defined states + initialization

D. P. Di Vincenzo, Fortschr. Phys. **48**, 771 (2000)

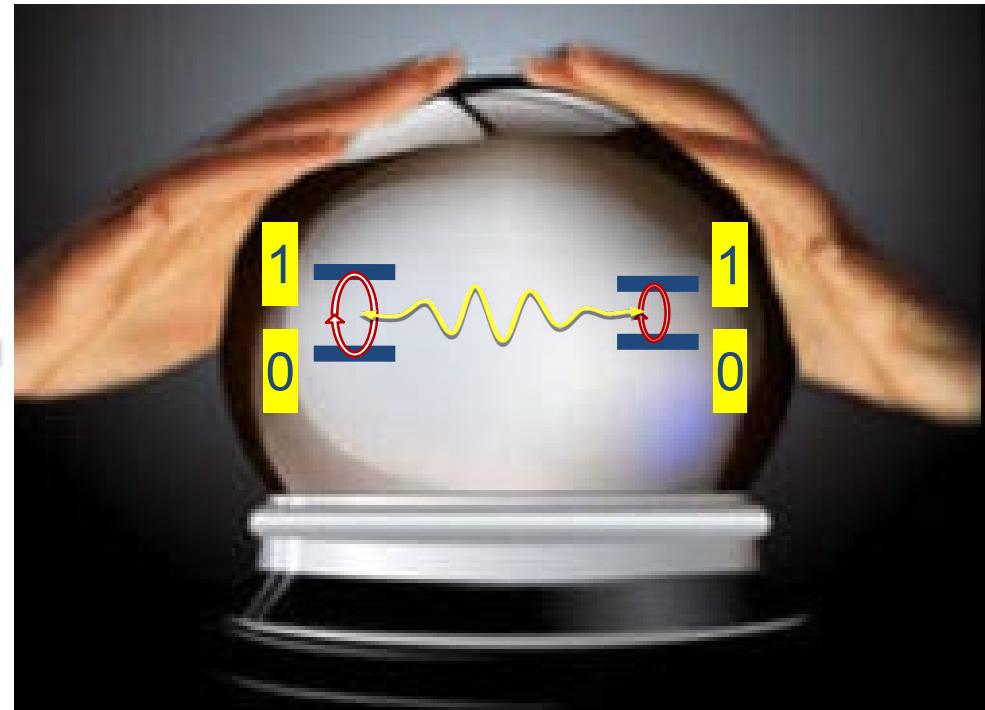


- Two well-defined states + initialization
- External control of the wave function
- Sufficiently high quantum coherence $T_2\Omega_R \gg 1$ (≥ 100)

D. P. Di Vincenzo, Fortschr. Phys. **48**, 771 (2000)

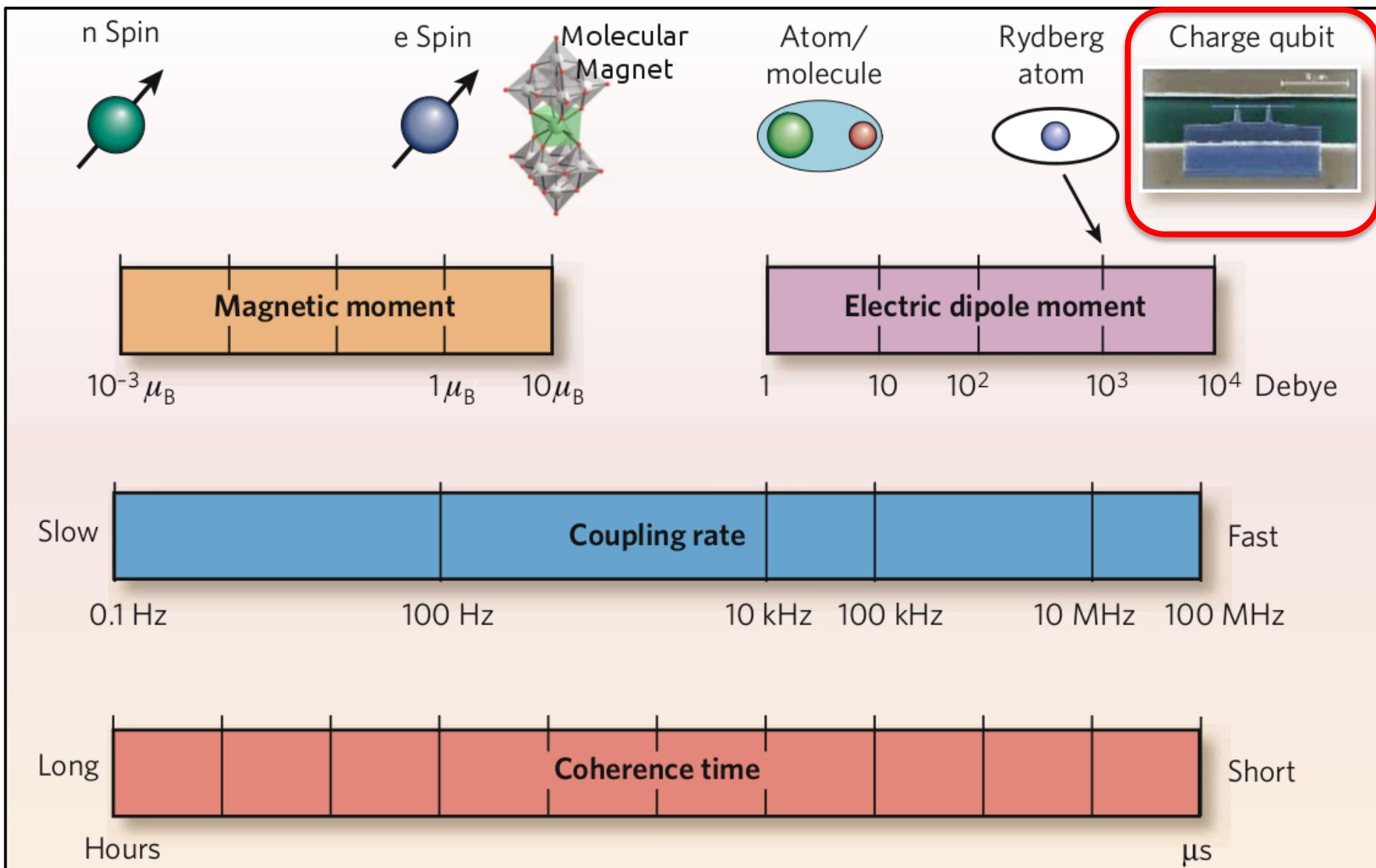


D. P. Di Vincenzo, Phys. Rev. A **51**, 1015 (1995)

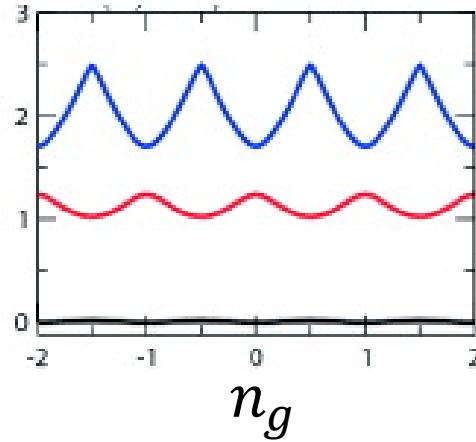
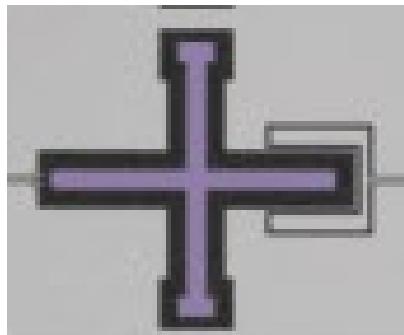
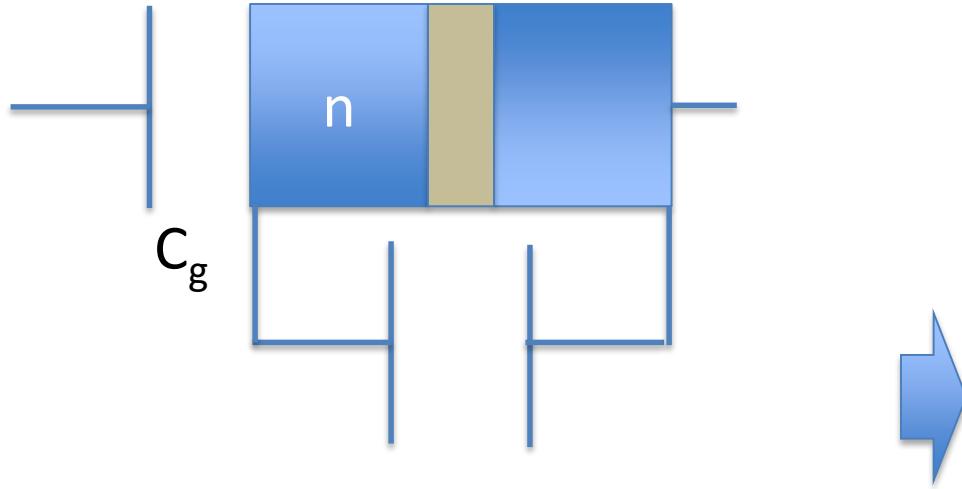


- Two well-defined states + initialization
- External control of the wave function
- Sufficiently high quantum coherence $T_2\Omega_R \gg 1$ (≥ 100)
- Scalability: wire up ≥ 2 qubits

R. J. Schoelkopf & S. M. Girvin, Nature **451**, 664–669 (2008)



Quantum supremacy: NISQs era

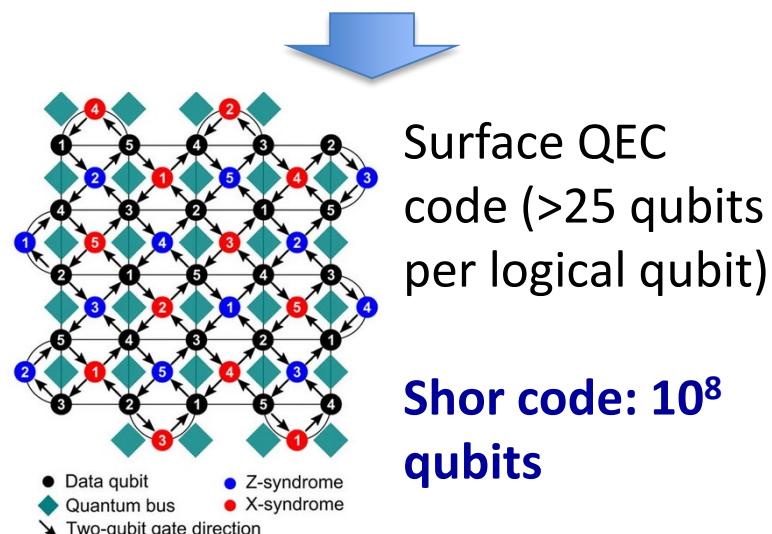


Transmon

J. A. Schreier *et al.*, Phys. Rev. B **77**, 180502(R) (2008)

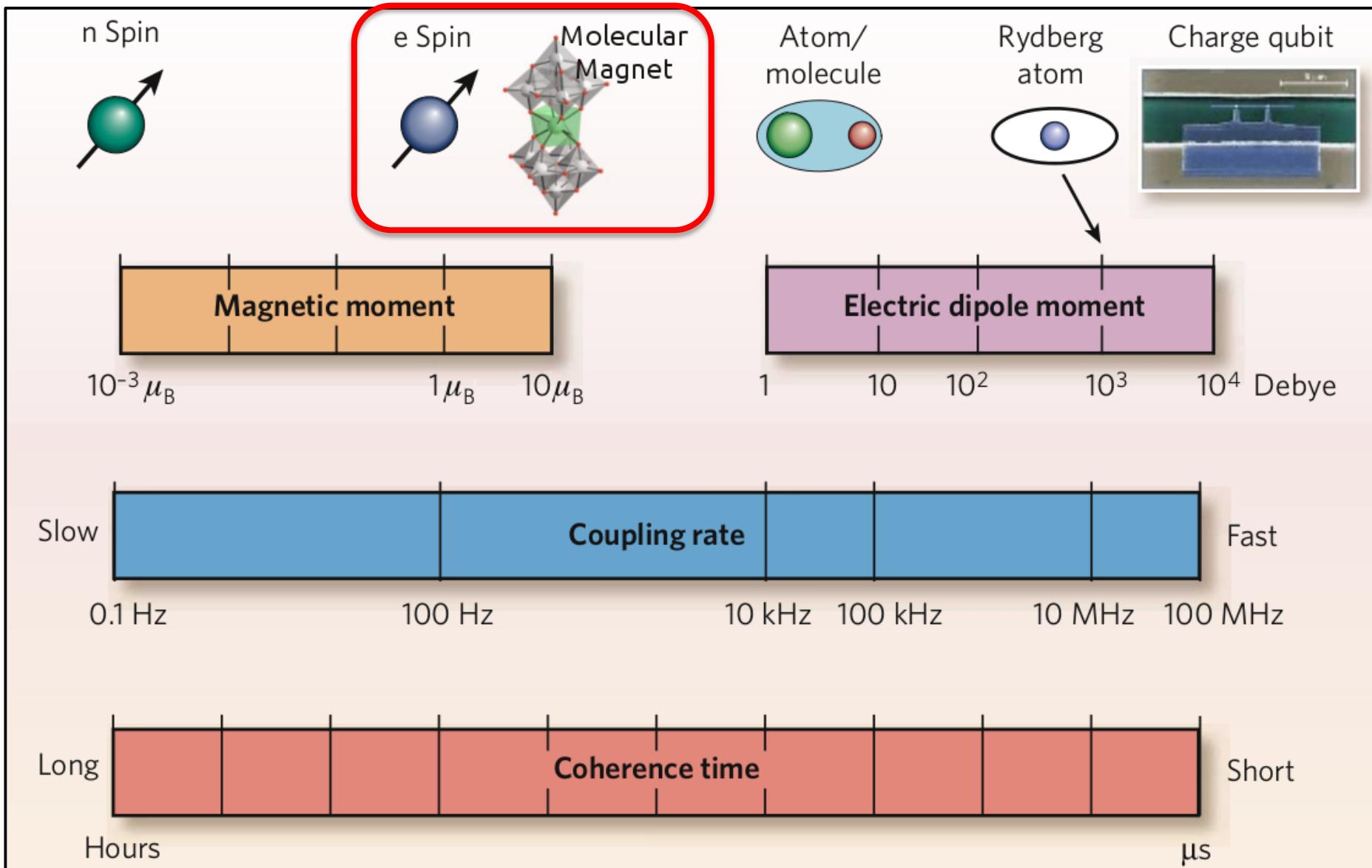


F. Arute, *et al.* Nature **574**, 505–510 (2019)



A. Fowler, Phys. Rev. A **86**, 032324 (2012)

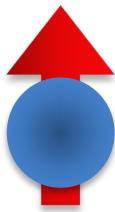
R. J. Schoelkopf & S. M. Girvin, Nature **451**, 664–669 (2008)



Electron in a magnetic field

$$S = \frac{1}{2}$$

$$g = 2$$



$$B_{\text{dc}}$$

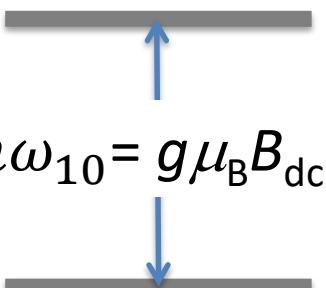


$$|1\rangle \equiv |\downarrow\rangle$$



$$26 \text{ GHz/T}$$

$$|0\rangle \equiv |\uparrow\rangle$$



$$1.3 \text{ K/T}$$

$$\hbar\omega_{10} = g\mu_B B_{\text{dc}}$$

Electron in a magnetic field

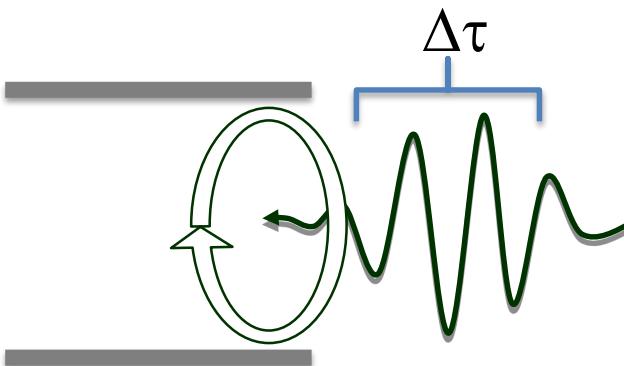
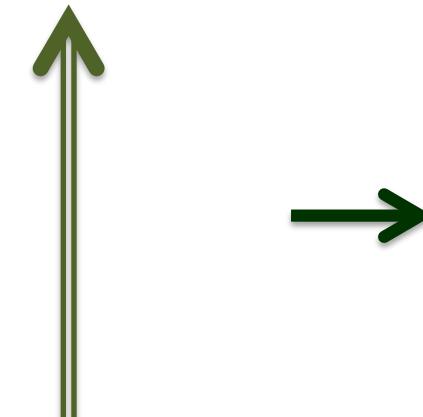
$$S = \frac{1}{2}$$

$$g = 2$$

$$|1\rangle \equiv |\downarrow\rangle$$

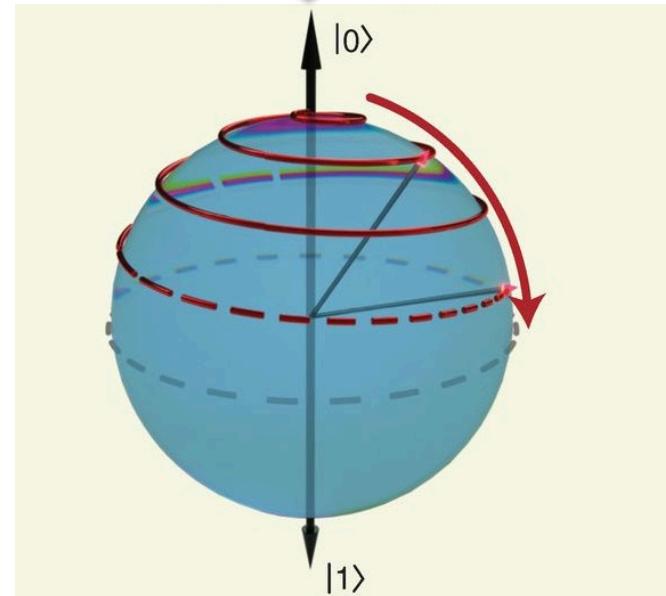
$$|0\rangle \equiv |\uparrow\rangle$$

$$B_{dc} \quad B_1 e^{i\omega t}$$



I. I. Rabi, Phys. Rev. B 51, 652 (1937)

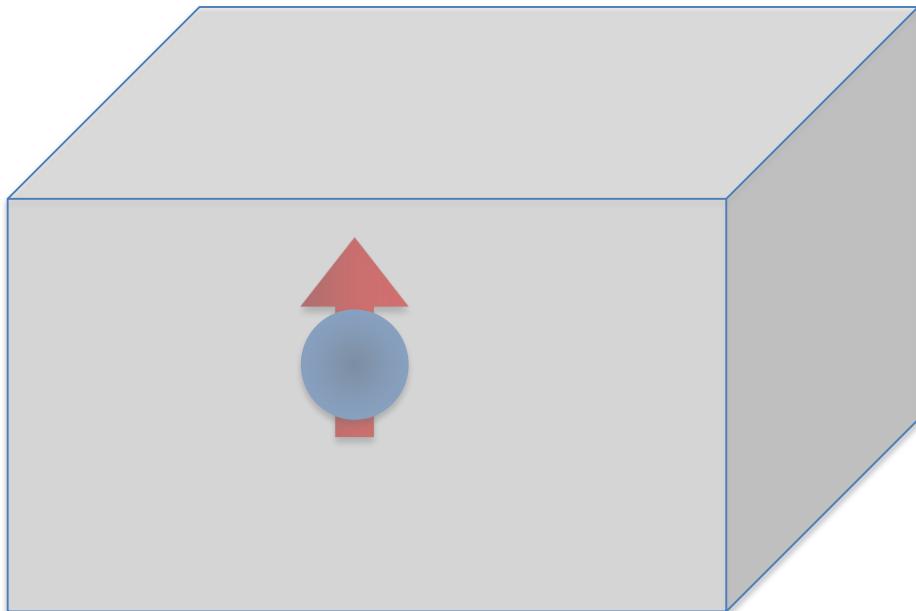
In resonance: $\omega = \omega_{10}$



$$|0\rangle \rightarrow \cos\left(\frac{\Omega_R t}{2}\right)|0\rangle + e^{i\phi(t)} \sin\left(\frac{\Omega_R t}{2}\right)|1\rangle$$

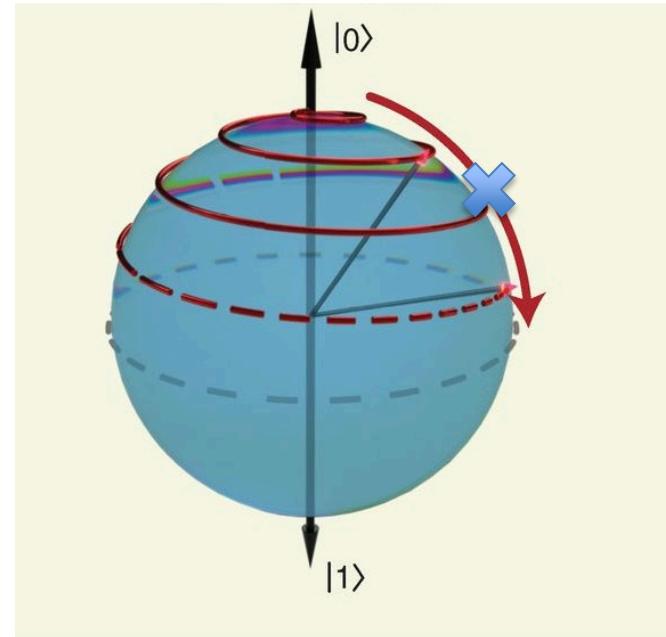
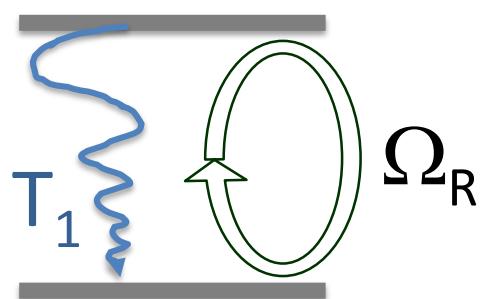
$$\frac{\Omega_R}{2\pi} = \frac{g\mu_B \langle 1 | \vec{S} \cdot \vec{B}_1 | 0 \rangle}{h} \approx 13 \text{ MHz/mT}$$

$$\phi(t) = \frac{g\mu_B B_{dc}}{\hbar} t$$

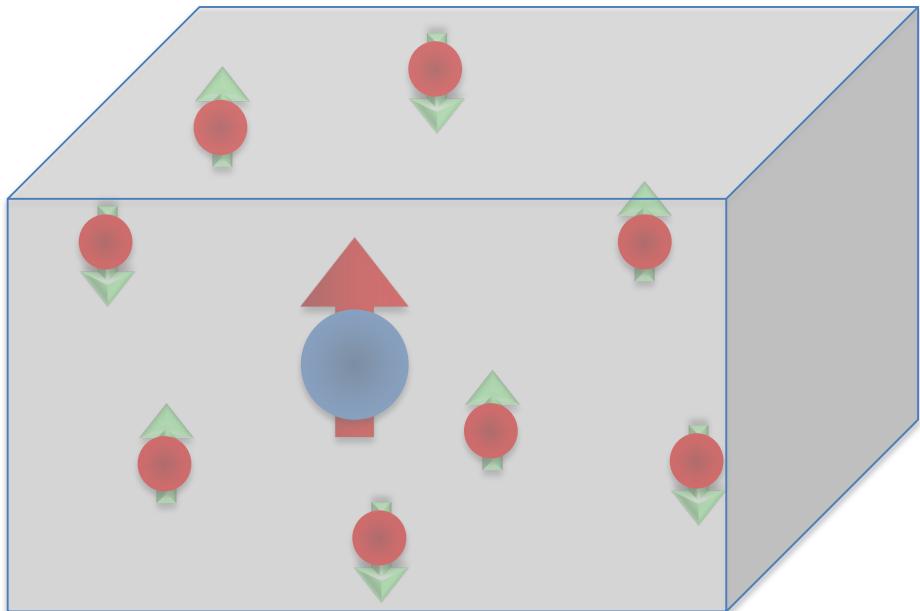


$$|1\rangle \equiv |\downarrow\rangle$$

$$|0\rangle \equiv |\uparrow\rangle$$

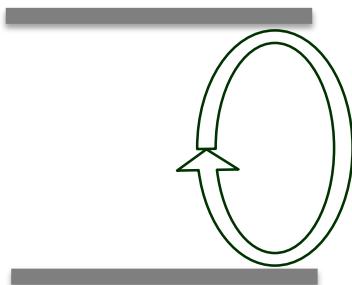


$$|0\rangle \rightarrow \cos\left(\frac{\Omega_R t}{2}\right)|0\rangle + e^{i\phi(t)} \sin\left(\frac{\Omega_R t}{2}\right)|1\rangle$$

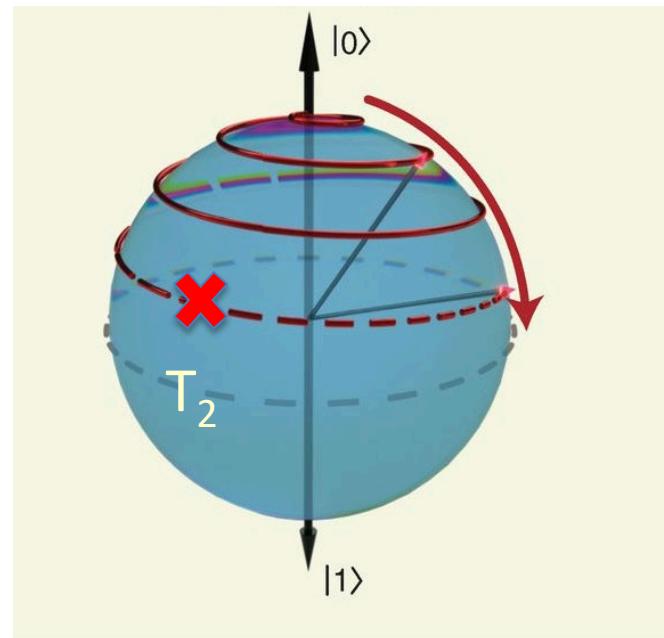


$$|1\rangle \equiv |\downarrow\rangle$$

$$|0\rangle \equiv |\uparrow\rangle$$



Ω_R

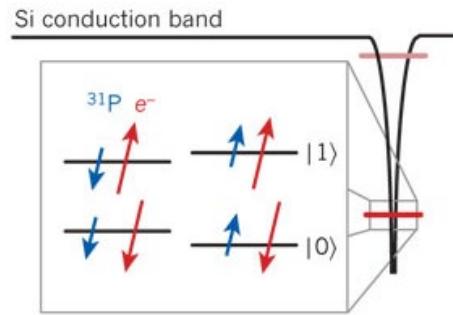
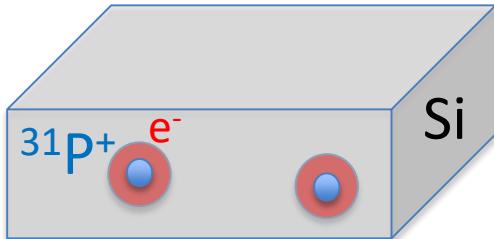


$$|0\rangle \rightarrow \cos\left(\frac{\theta(t)}{2}\right)|0\rangle + e^{\text{red } X} \sin\left(\frac{\theta(t)}{2}\right)|1\rangle$$

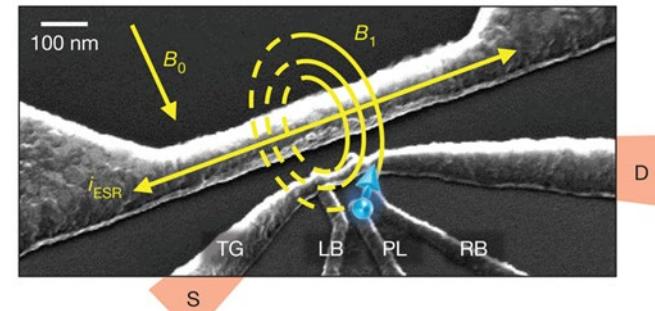
$$\boxed{\tau_{\text{decoherence}}^{-1} = \frac{1}{2T_1} + \frac{1}{T_2} \approx \frac{1}{T_2}}$$

$^{31}\text{P}^+$ in Si

B. E. Kane, Nature **393**, 133 (1998)



A. Morello et al., Nature **467**, 687 (2010)



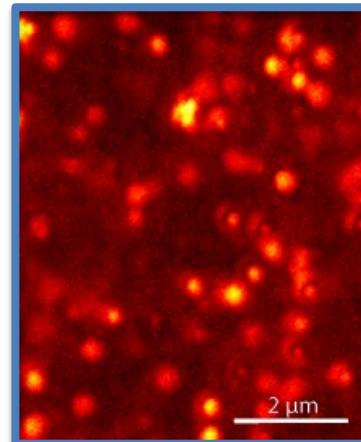
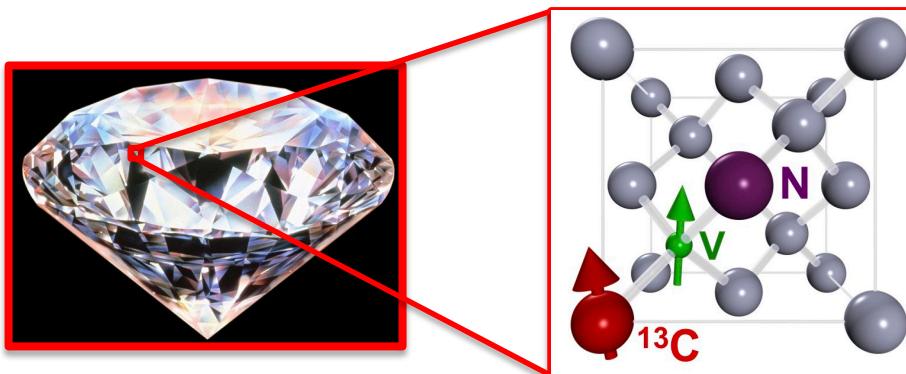
$$T_{2e} = 500 \text{ ms}$$

$$T_{2n} = 30 \text{ s}$$

NV⁻ in diamond

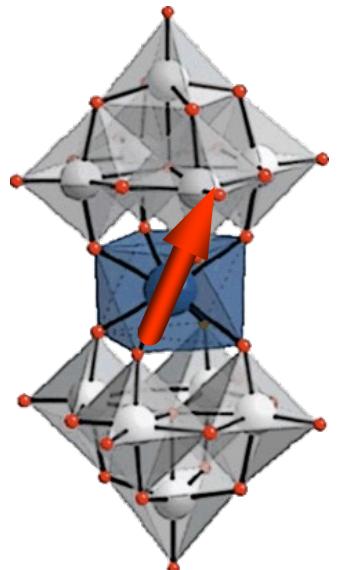
F. Jelezko et al., Phys. Rev. Lett. **92**, 076401 (2004)

G. De Lange et al., Science **330**, 60 (2010)

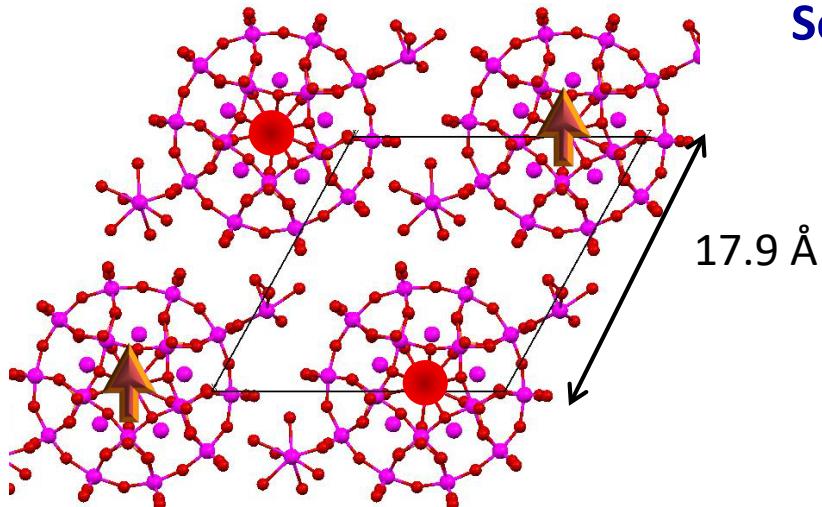


$$T_2 \approx 20-30 \mu\text{s}$$

A. Gaita-Ariño, F. Luis, S. Hill, E. Coronado, Nature Chem.
11, 301–309 (2019).

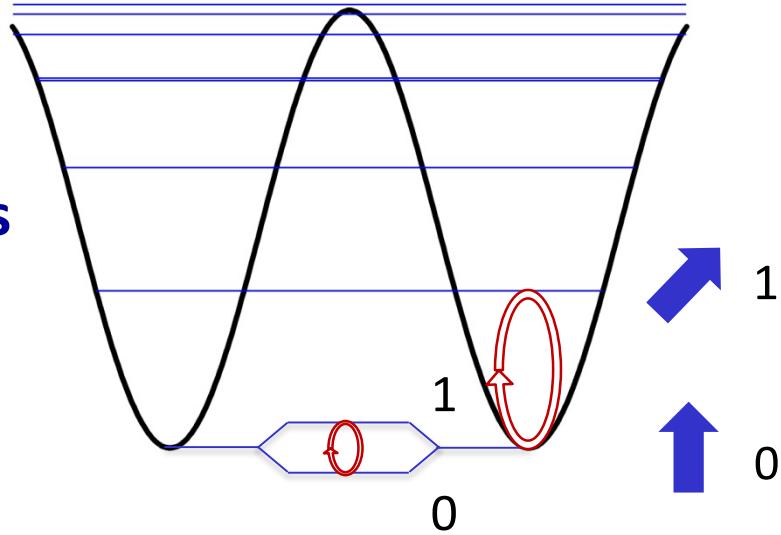


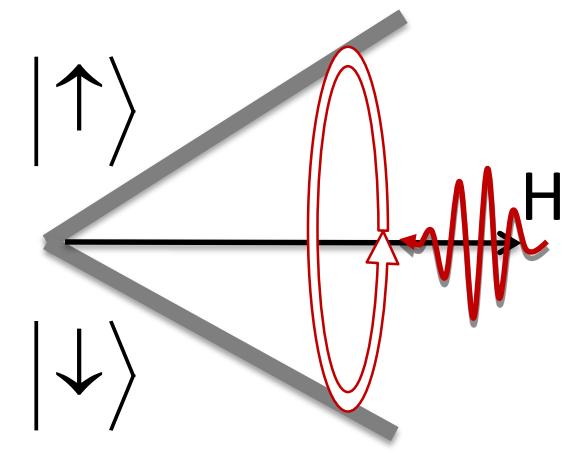
Single ion magnets



Some appealing properties

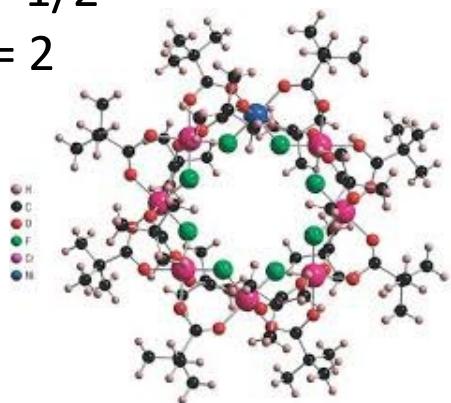
- Simples (1 magnetic ion)
- Weak spin-spin interactions
- Magnetically soluble



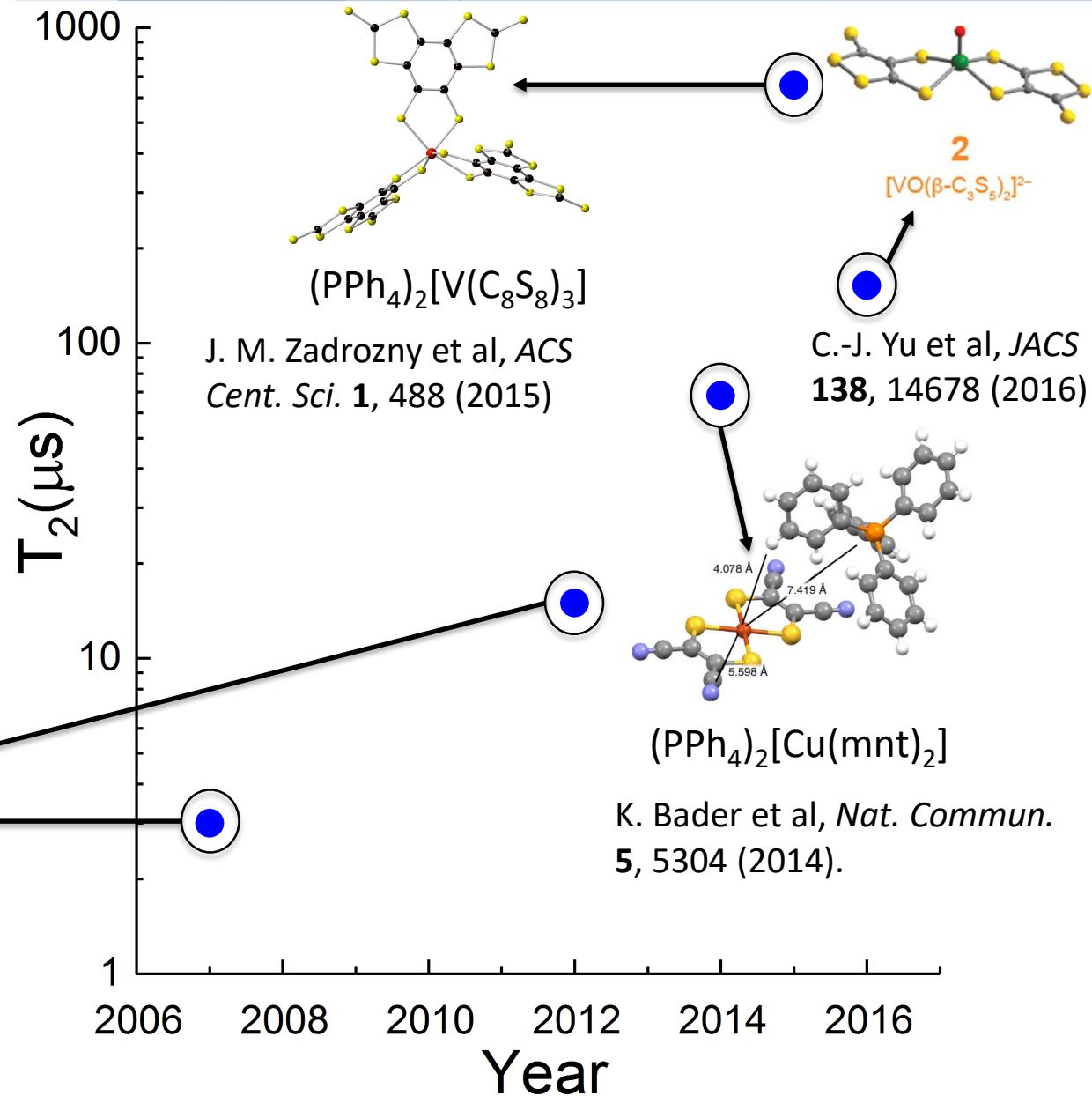


Cr₇Ni

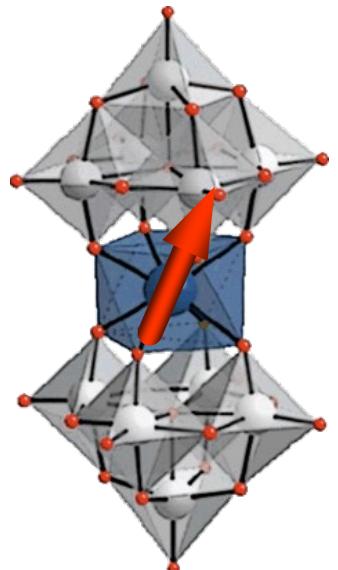
$S = 1/2$
 $g = 2$



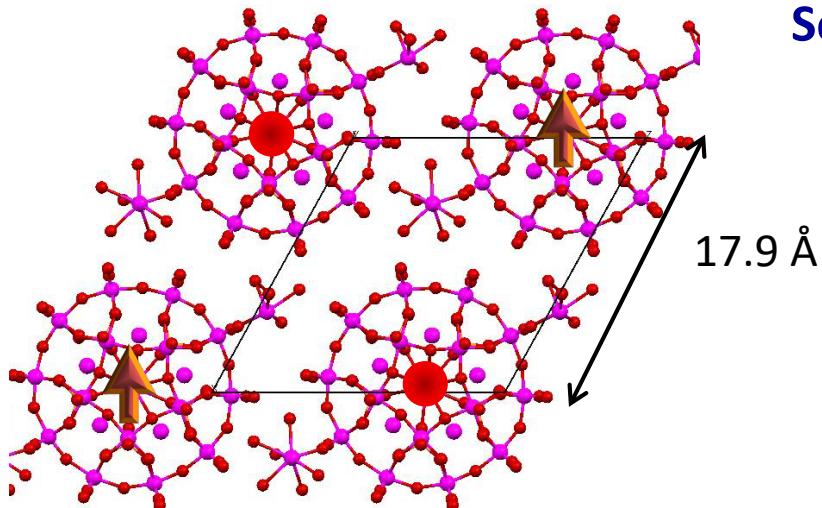
A. Ardavan et al, *Phys. Rev. Lett.* **98**, 057201 (2007); C. J. Wedge et al. *Ph Rev. Lett.* **108**, 107204 (2012).



A. Gaita-Ariño, F. Luis, S. Hill, E. Coronado, Nature Chem.
11, 301–309 (2019).

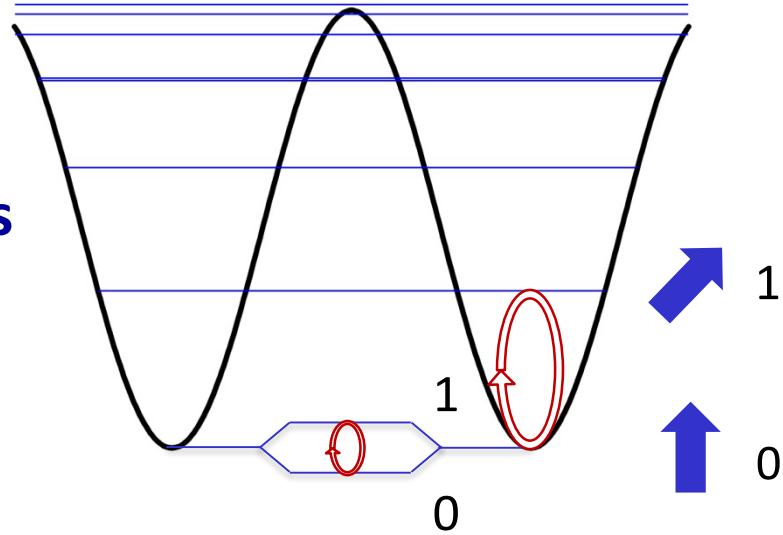


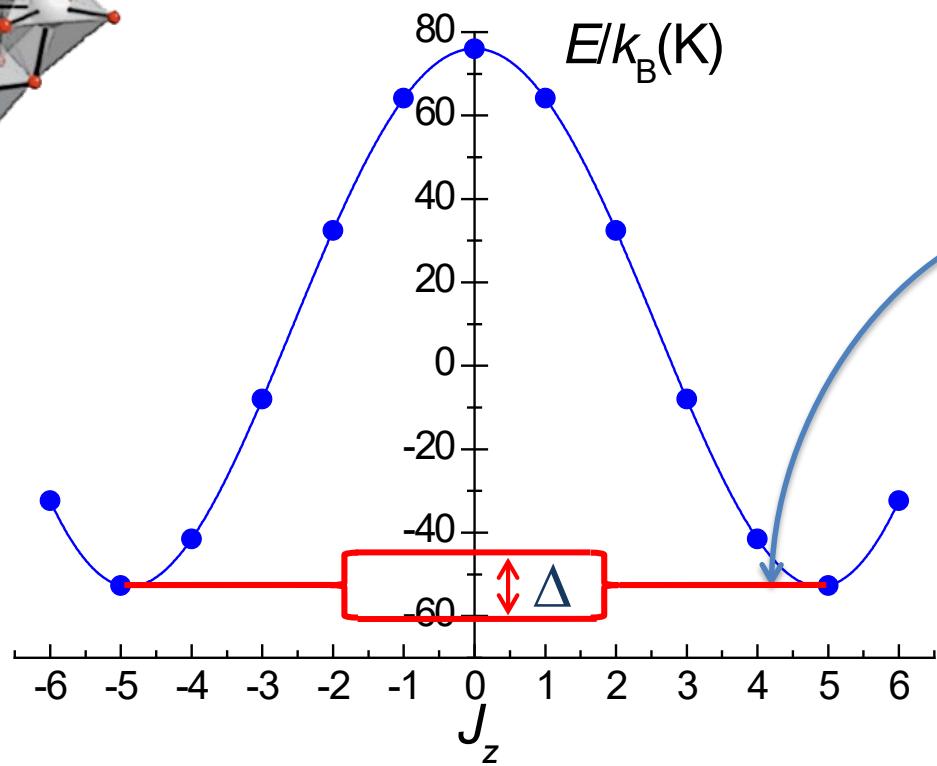
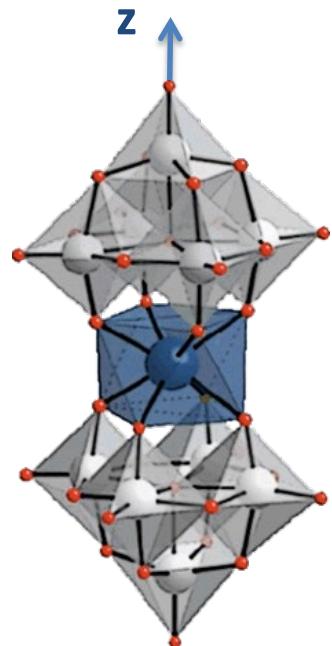
Single ion magnets



Some appealing properties

- Simples (1 magnetic ion)
- Weak spin-spin interactions
- Magnetically soluble
- Tunable



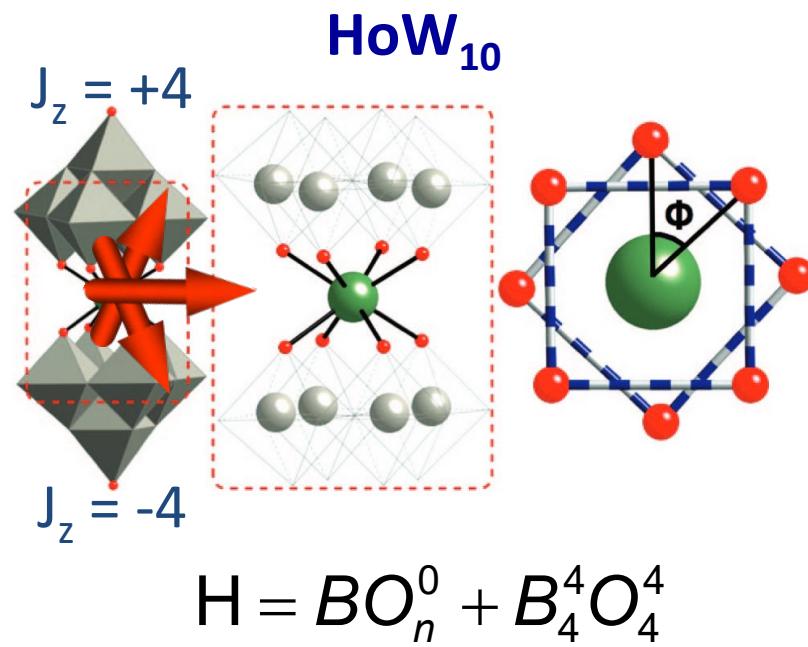


$$H = B_2^0 O_2^0 + B_4^0 O_4^0 + B_6^0 O_6^0 + B_n^m O_n^m$$

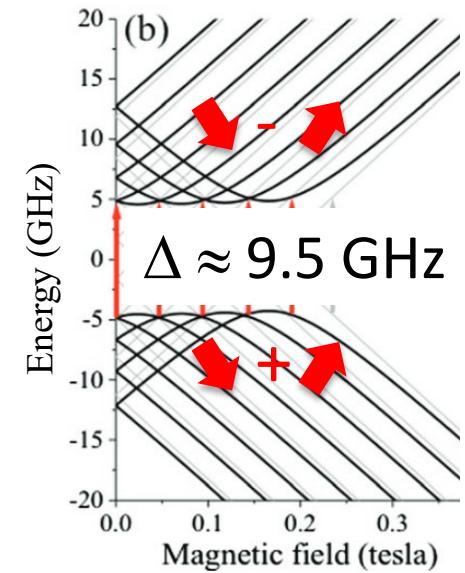
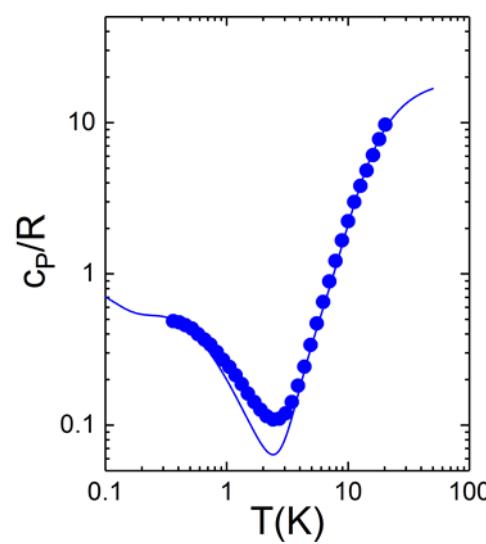
Off-diagonal terms

$$[J_z, O_m^0] \neq 0$$

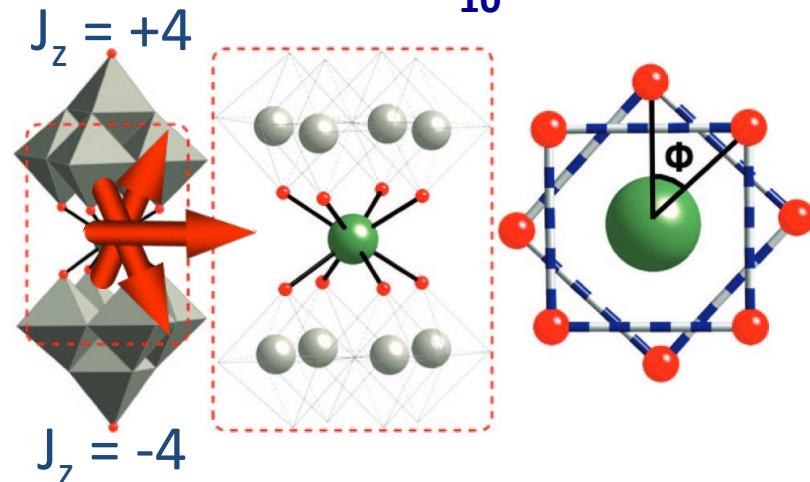
Quantum tunnel splitting



M. AlDamen et al, Inorg. Chem. **48**, 3467 (2009)



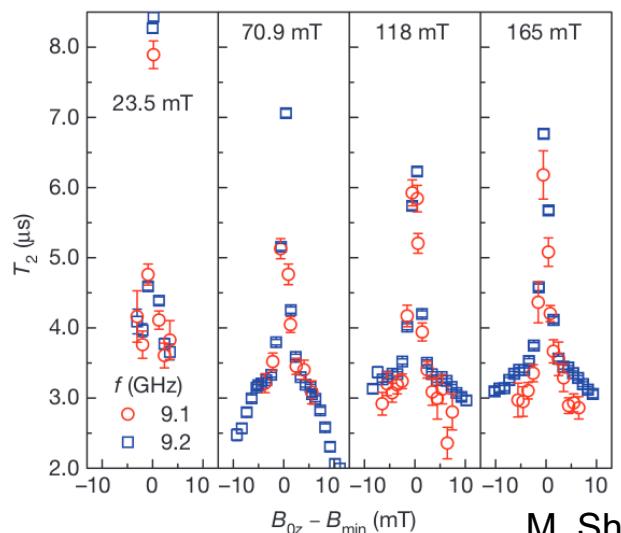
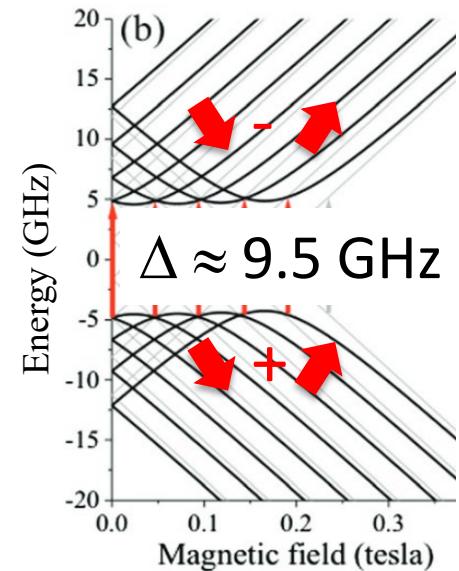
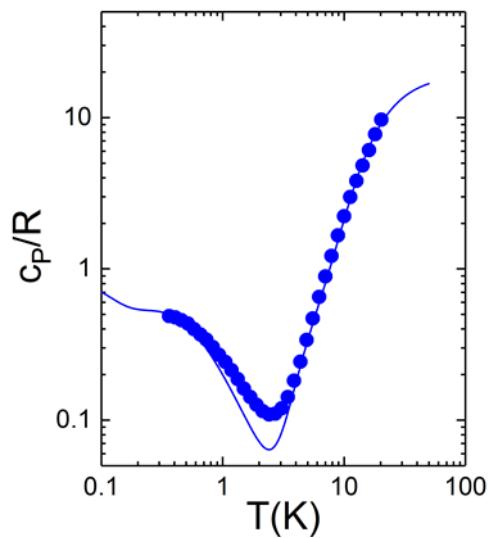
HoW₁₀



$$H = BO_n^0 + B_4^4 O_4^4$$

$$\frac{1}{T_2} \propto \frac{\partial \omega_{10}}{\partial B}$$

M. AlIDamen et al, Inorg. Chem. **48**, 3467 (2009)

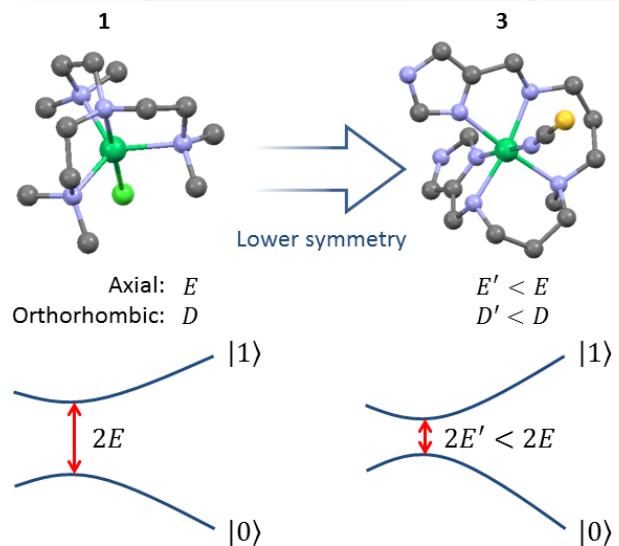
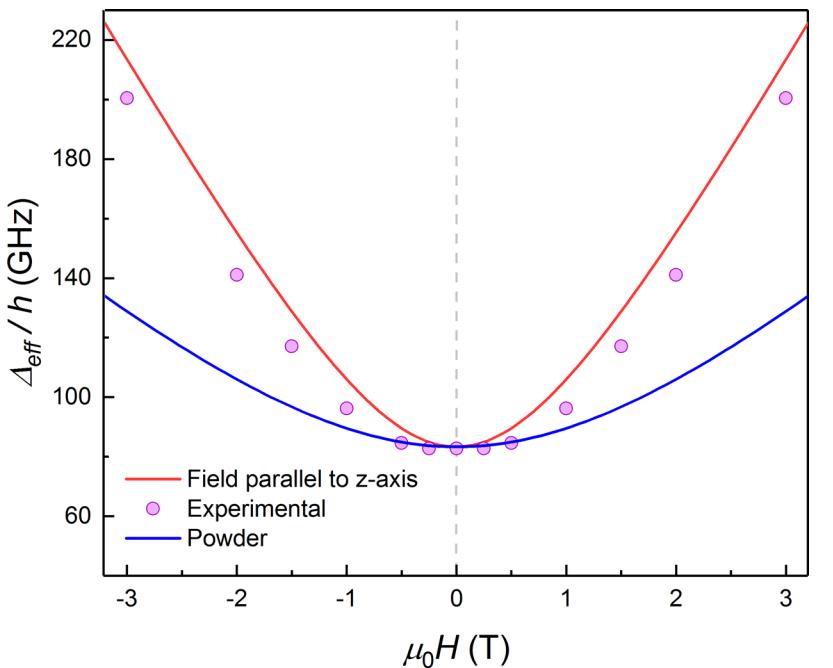


M. Shiddiq et al, Nature **531**, 348 (2016)

[Ni(Me₆tren)Cl](ClO₄)

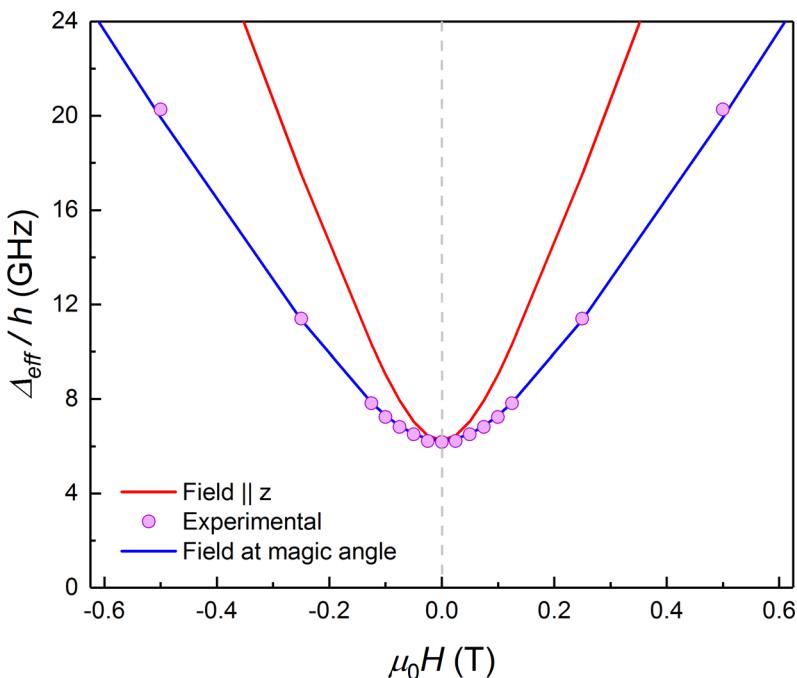
Ni(II) $S = 1$

$$H = BO_2^0 + B_2^2 O_2^2$$

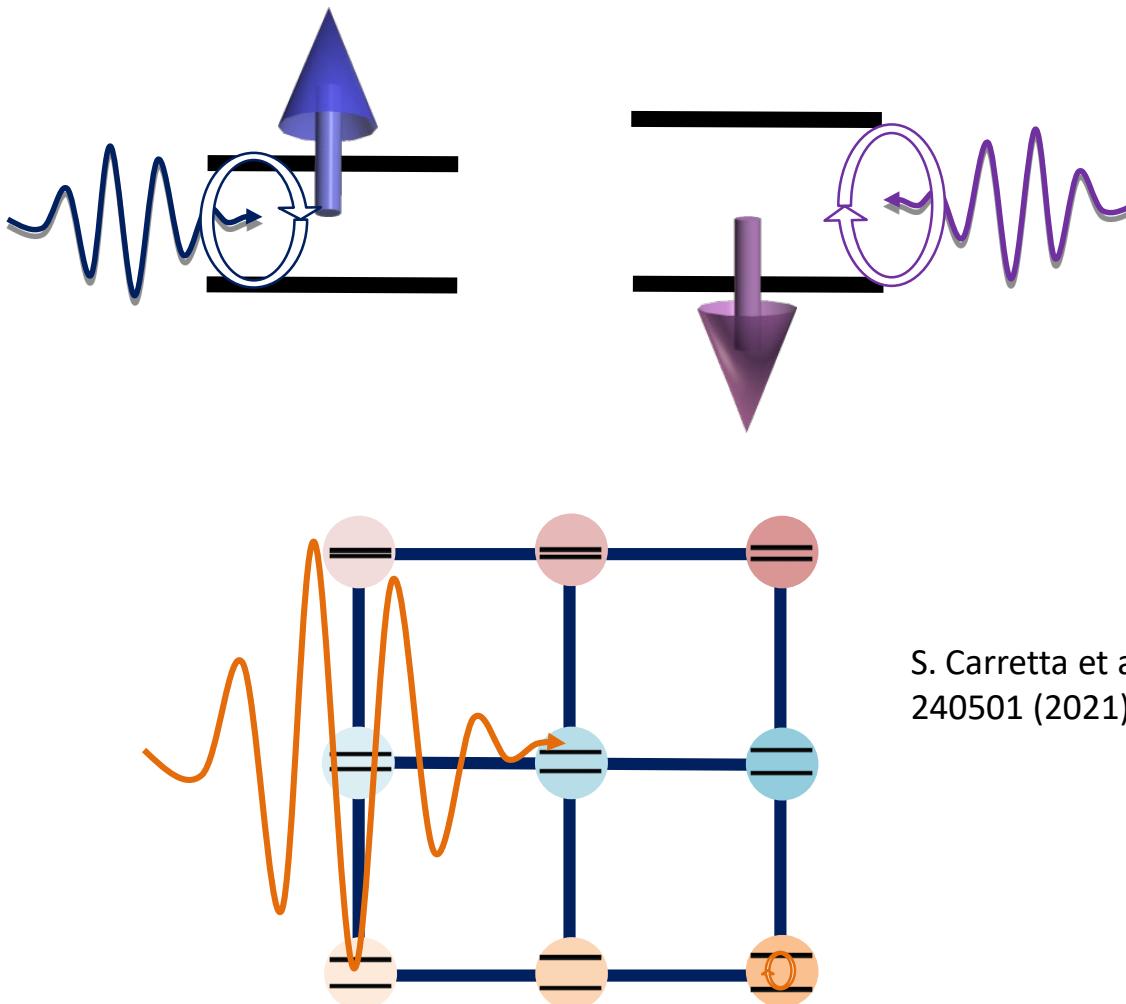


[Ni-Imdipa]-(NCS)

M. Rubín et al, Chem. Sci. **12**, 5123 (2021)

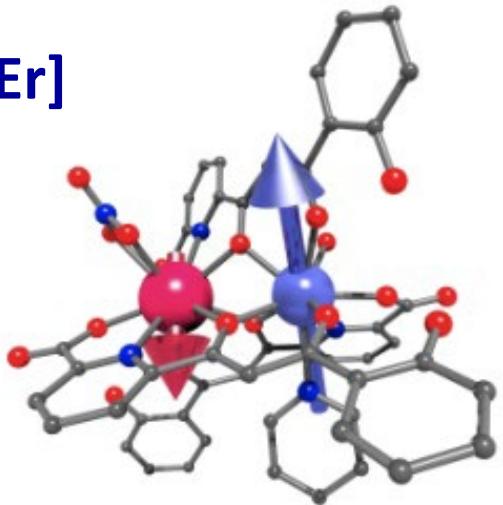


Spectroscopic addressing

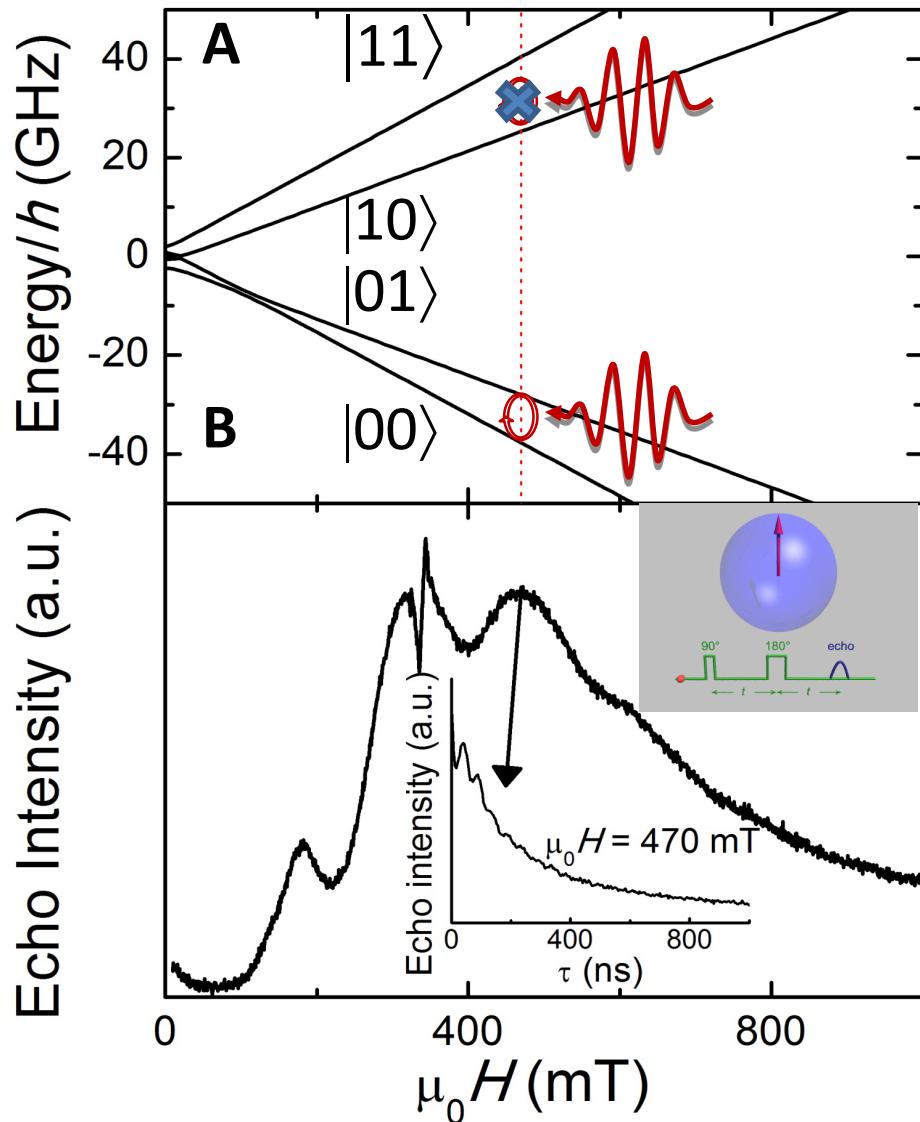
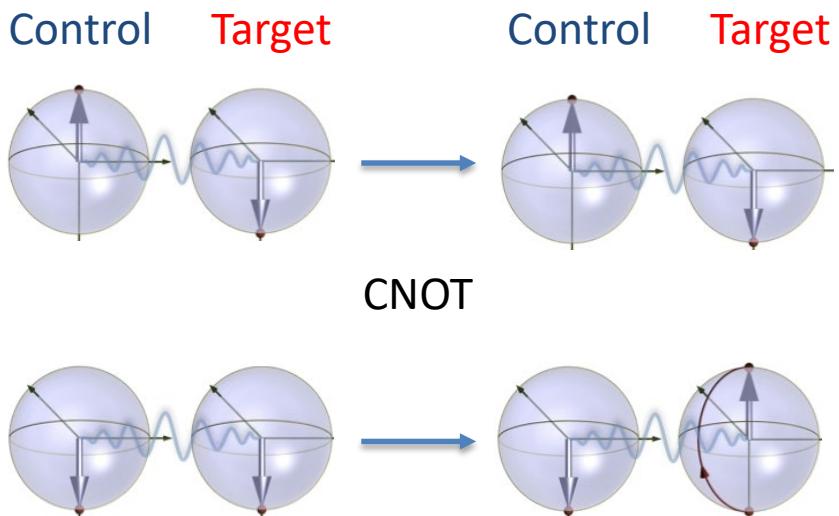


S. Carretta et al, Appl. Phys. Lett. **118**,
240501 (2021)

[CeEr]

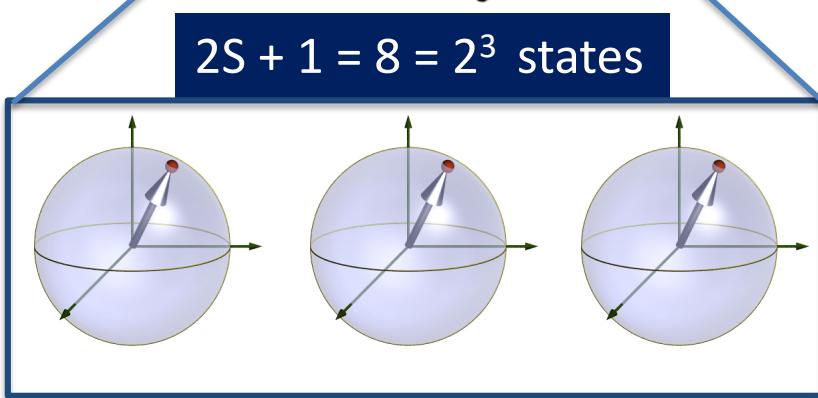
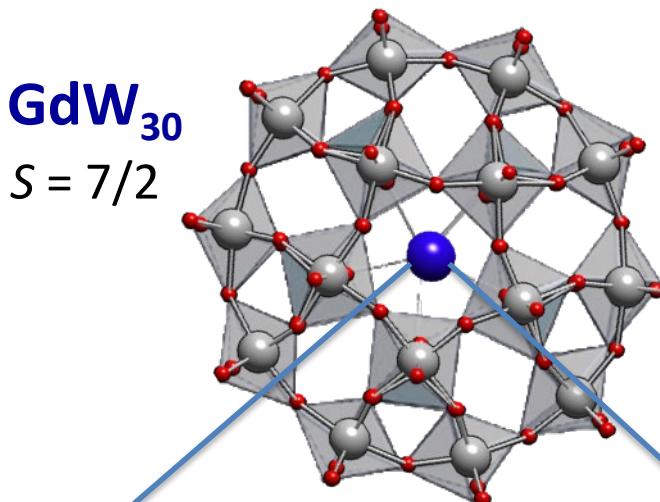
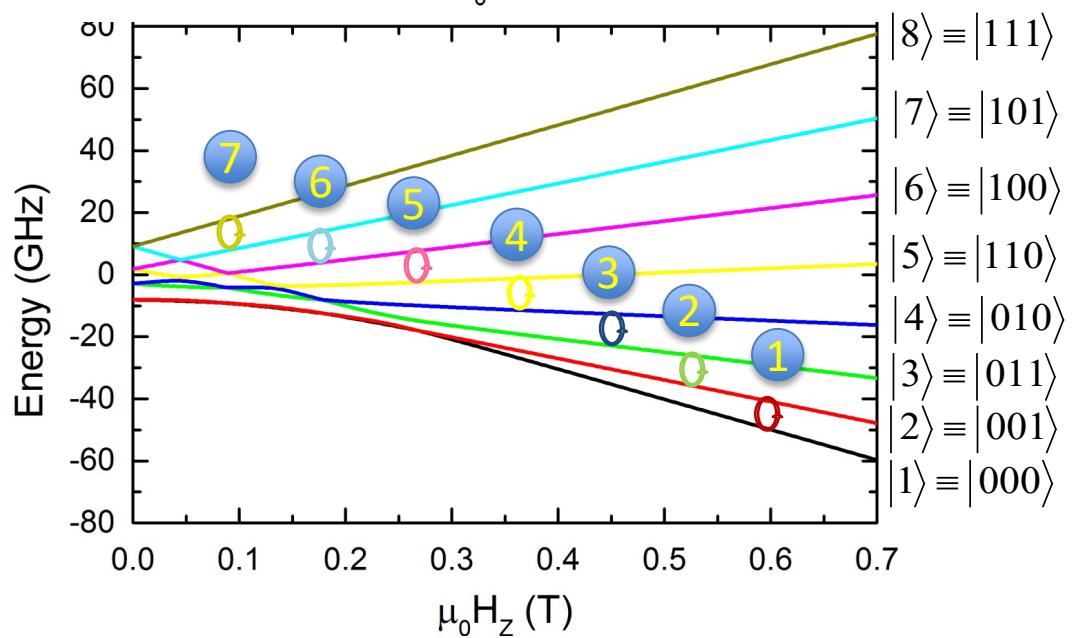
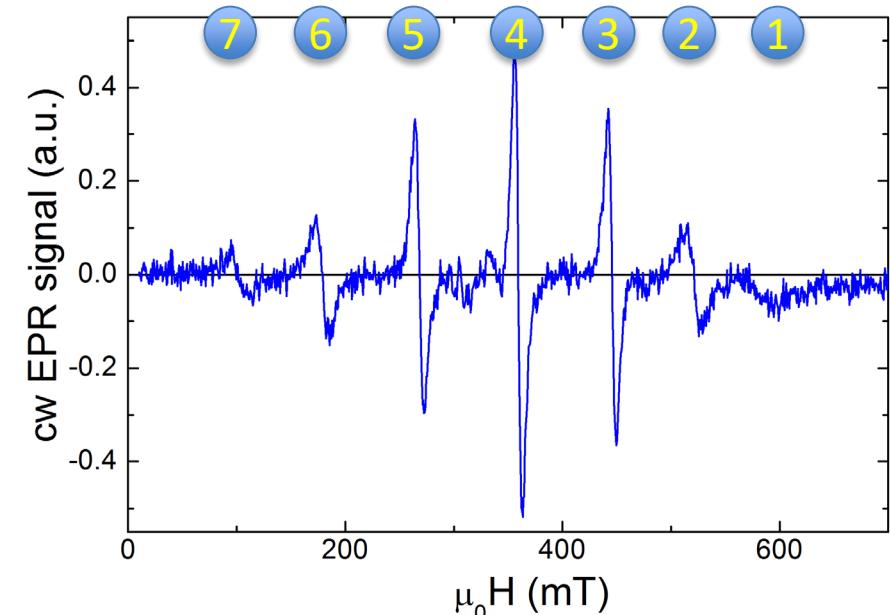


$$\mathcal{H} = g_1 \mu_B \vec{H} \vec{S}_1 + g_2 \mu_B \vec{H} \vec{S}_2 - J \vec{S}_1 \vec{S}_2$$

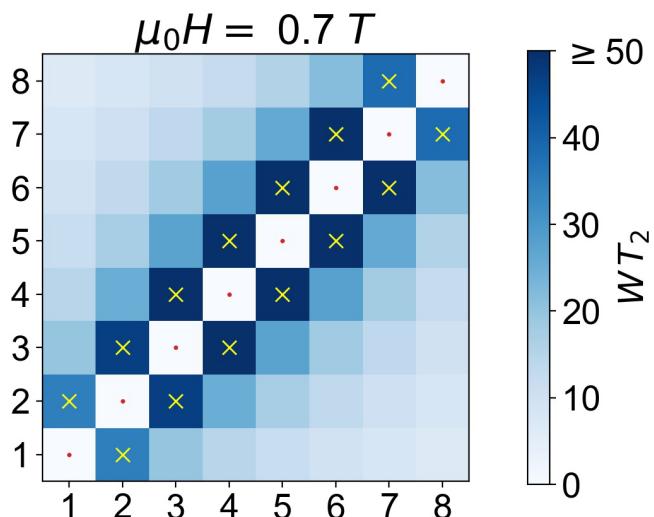
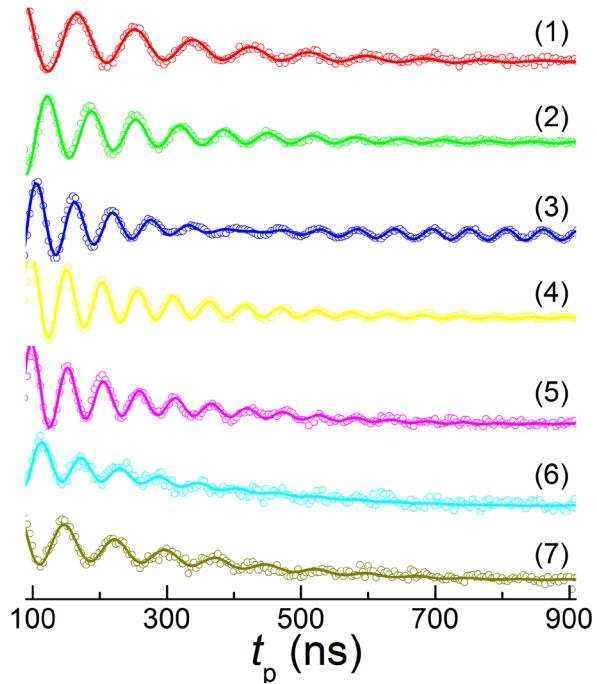


F. Luis et al, Phys. Rev. Lett. **107**, 117203 (2011);
D. Aguilà et al., JACS **136**, 14215 (2014)

M. Jenkins et al, *Phys. Rev. B* **95**, 064423 (2017)



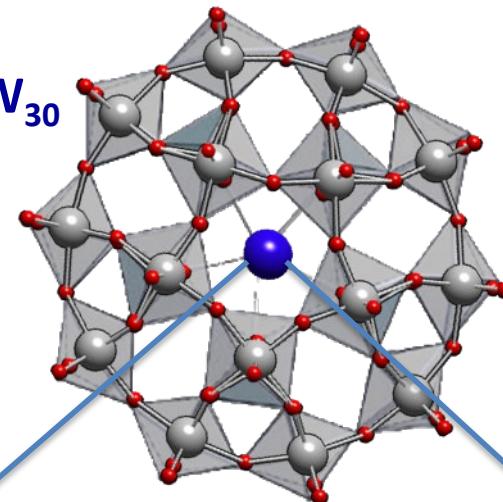
Three qubits



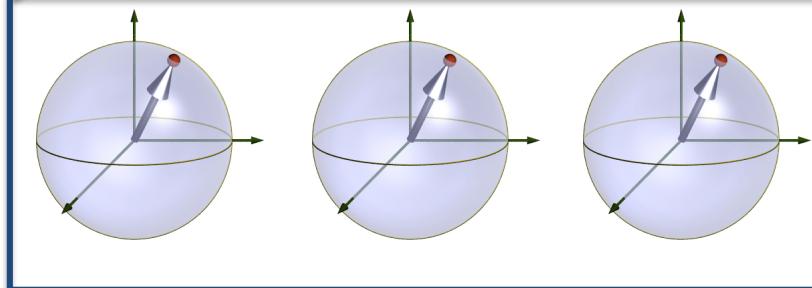
M. Jenkins et al, *Phys. Rev. B* **95**, 064423 (2017)

Gd_{0.01}Y_{0.99}W₃₀

$S = 7/2$



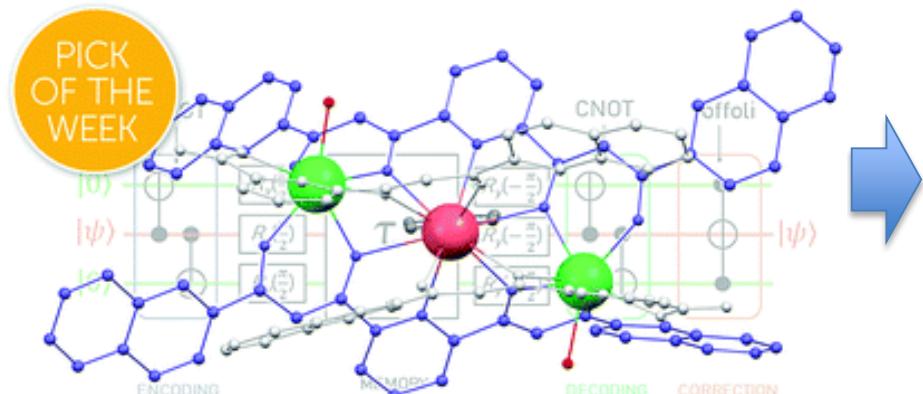
$2S + 1 = 8 = 2^3$ states



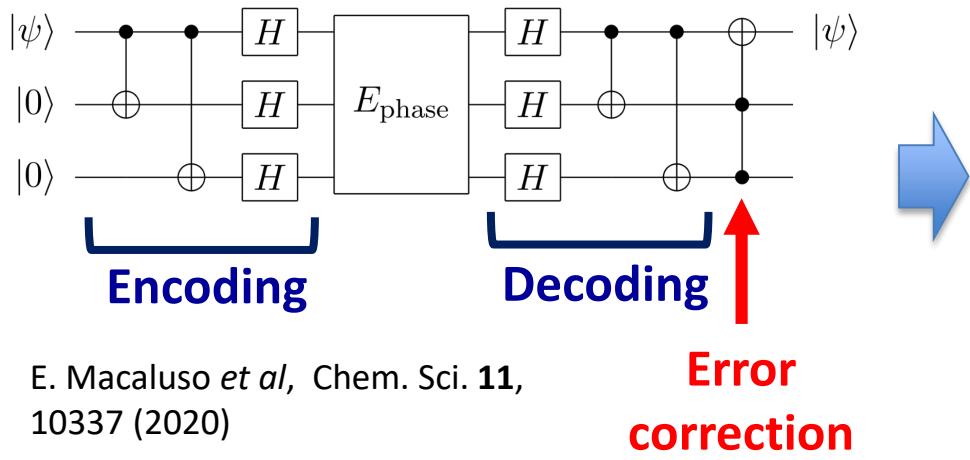
Three qubits
+
Universal set of operations

Quantum error correction in a molecular NISQ

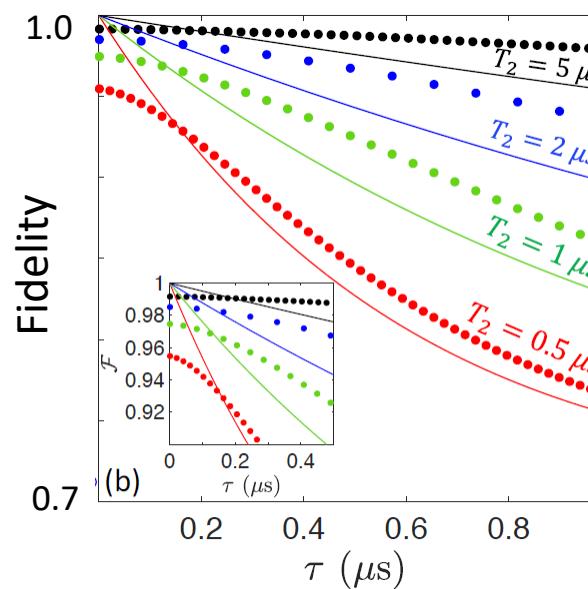
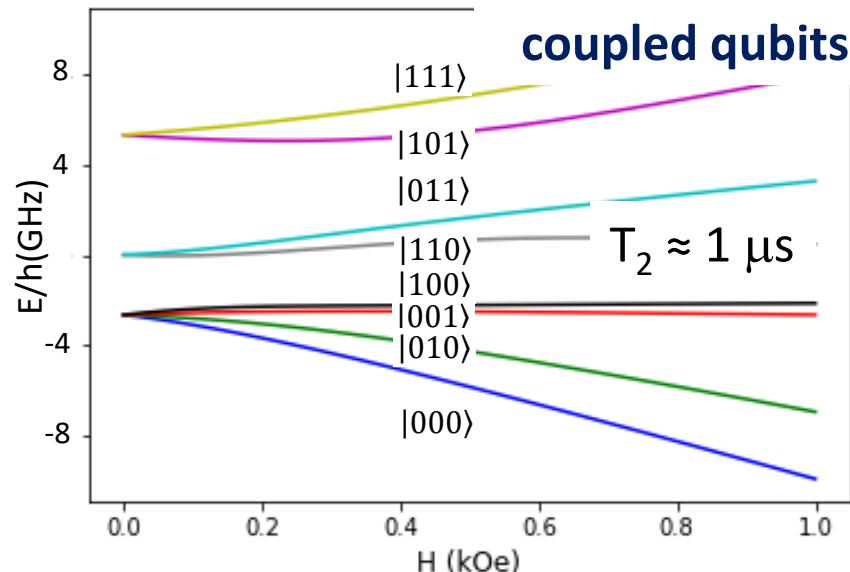
[ErCeEr]



Three-qubit repetition code



Three different & coupled qubits



NUCLEAR SPIN

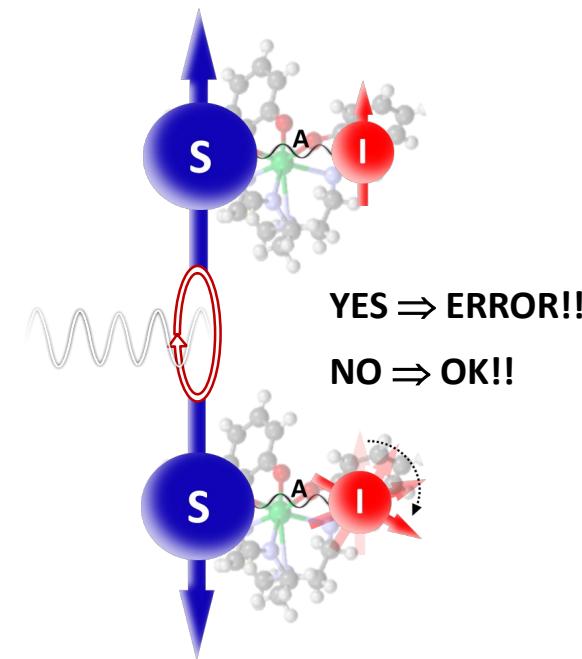
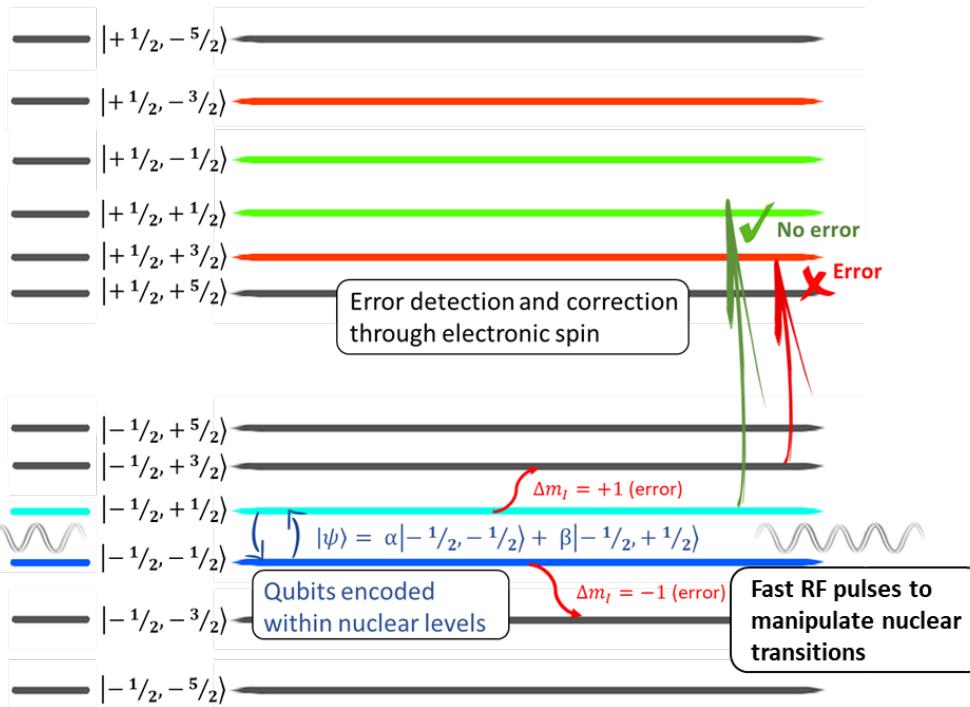


ENCODES LOGIC QUBIT STATES

ELECTRONIC SPIN

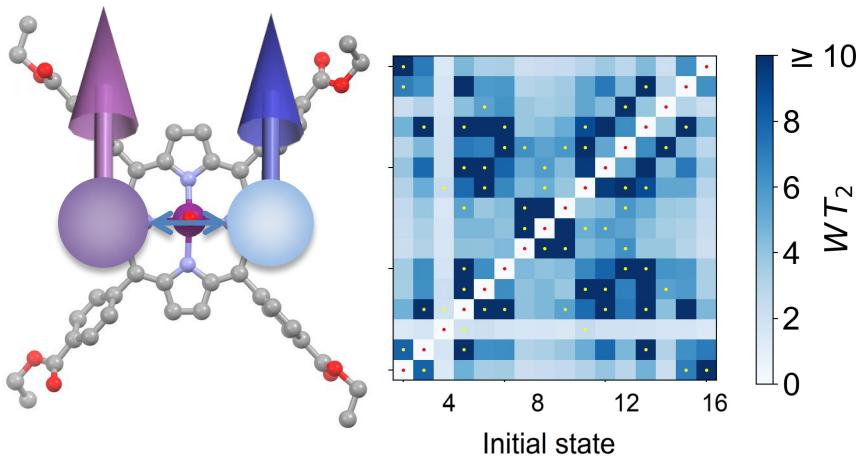
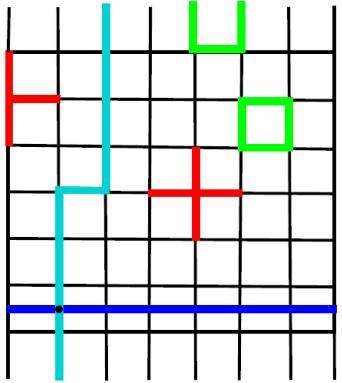
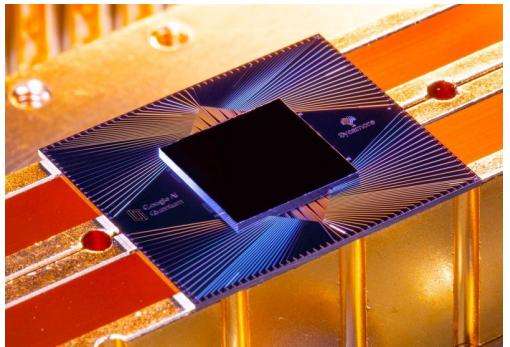


DETECTS ERRORS



A single molecule can perform as a logical qubit with embedded error correction

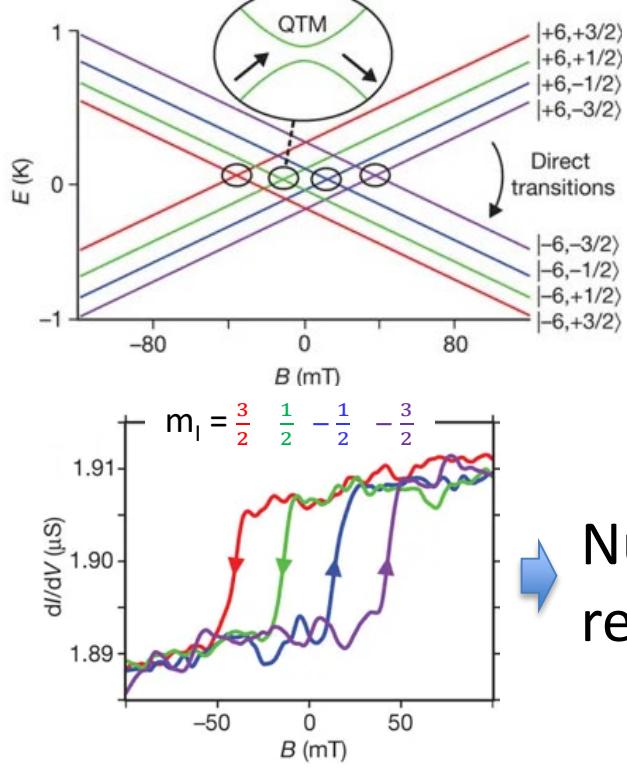
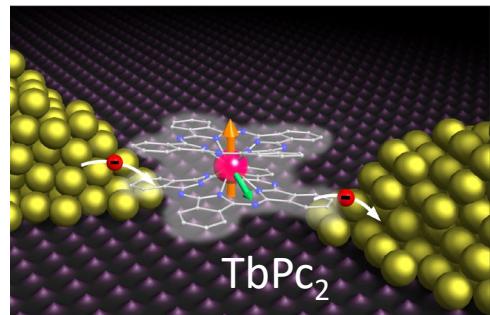
Competitive advantages & challenges



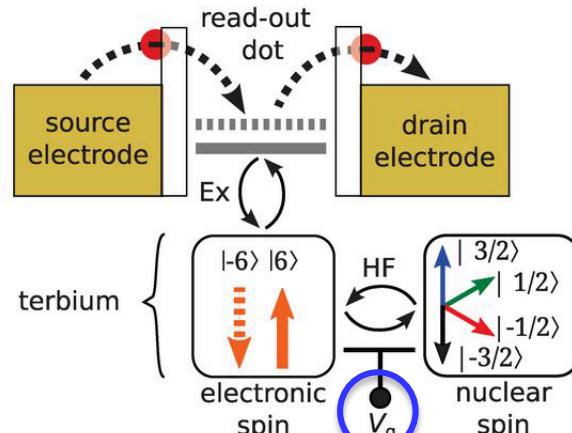
- Tuneable and interconectable
- Well-established protocols and technologies for control & read-out
- Challenging for large-scale computing

- Tuneable small and reproducible
- Multiply connected qubits/qudits in each molecular unit
- Specific algorithms save resources
- Control, read-out & wire up multiple molecules

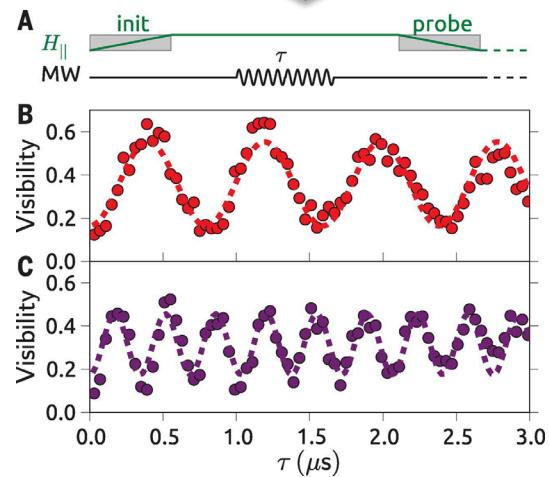
Read-out and coherent control of individual nuclear spins



Nuclear spin read-out

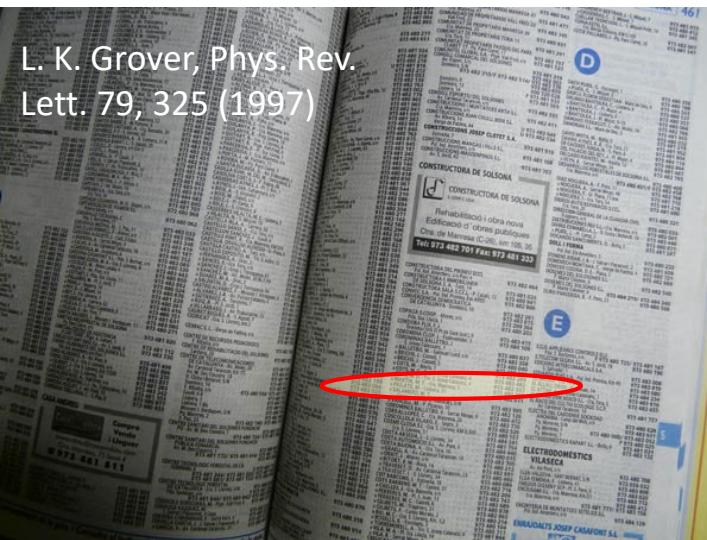


Electrical modulation of the hyperfine interaction

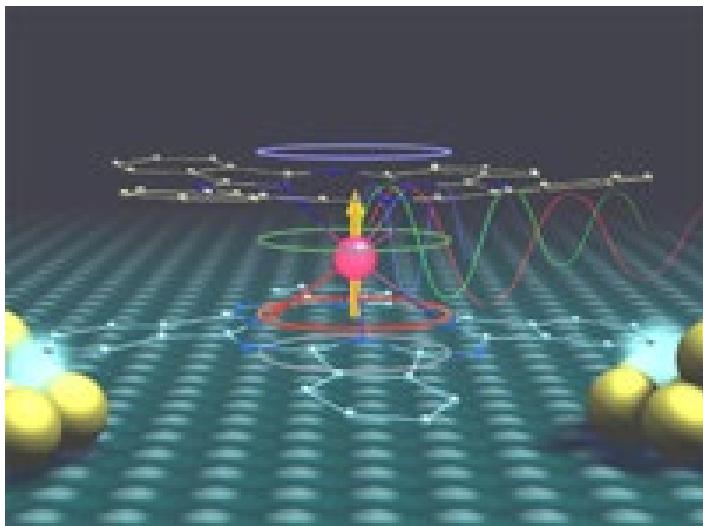


Coherent control

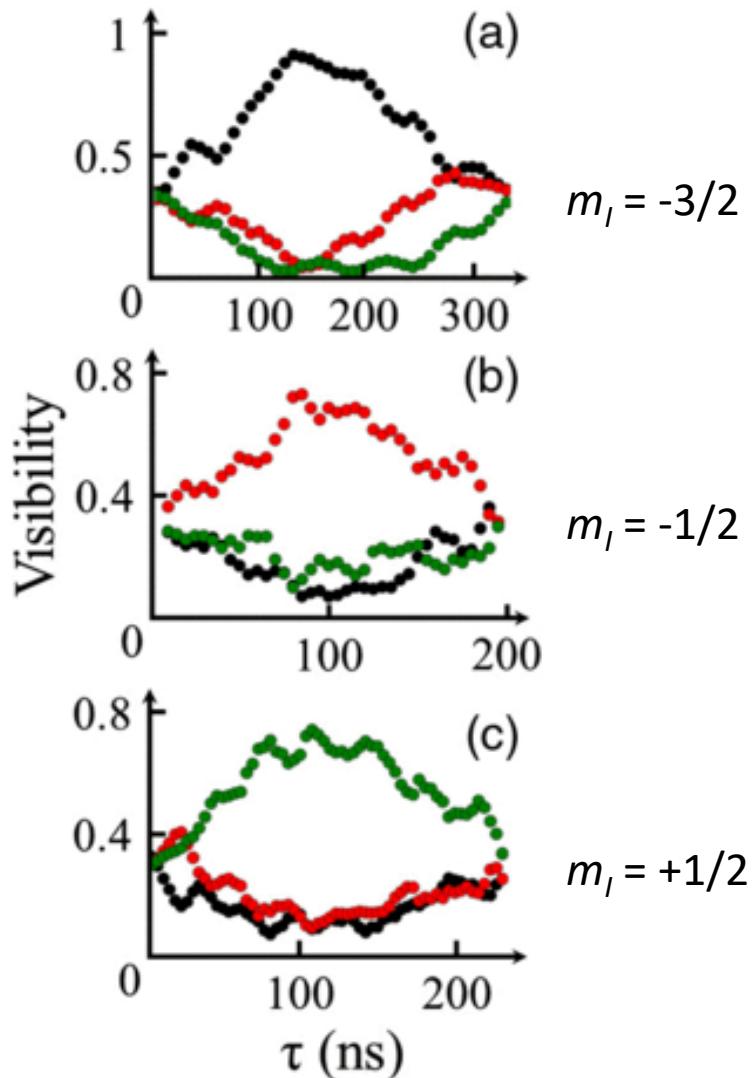
Grover search algorithm in a single molecule



Phone number \Rightarrow name??

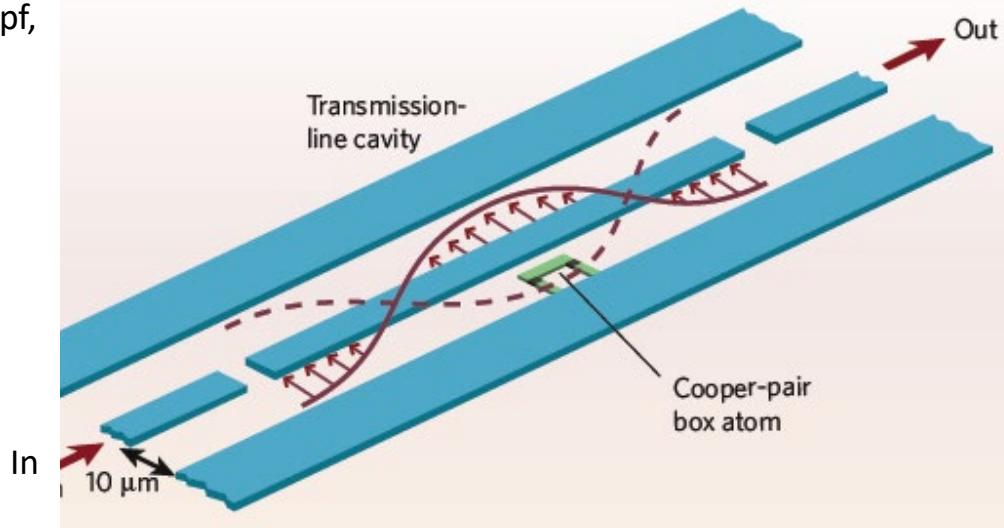


Nuclear spin \Rightarrow state??

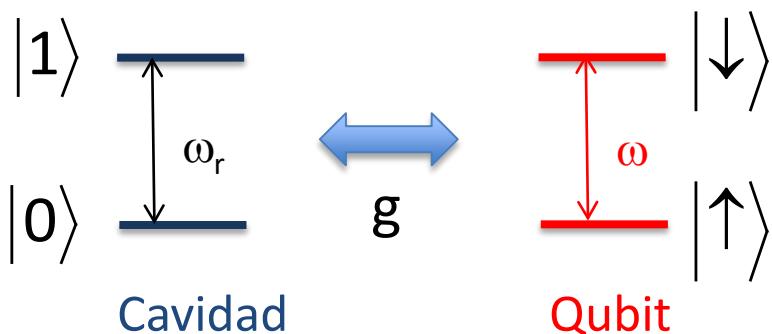


A. Blais, R.-S. Huang, A. Wallraff, S. Girvin, & R. Schoelkopf,
Phys. Rev. A **69**, 062320 (2004)
A. Wallraff et al., Nature (London) **431**, 162 (2004).

Light-matter interaction in a chip



$$\mathcal{H} = \hbar\omega_r(n + 1/2) + \frac{\hbar\omega}{2}\sigma_z + \hbar g(a^+\sigma^- + a^-\sigma^+)$$

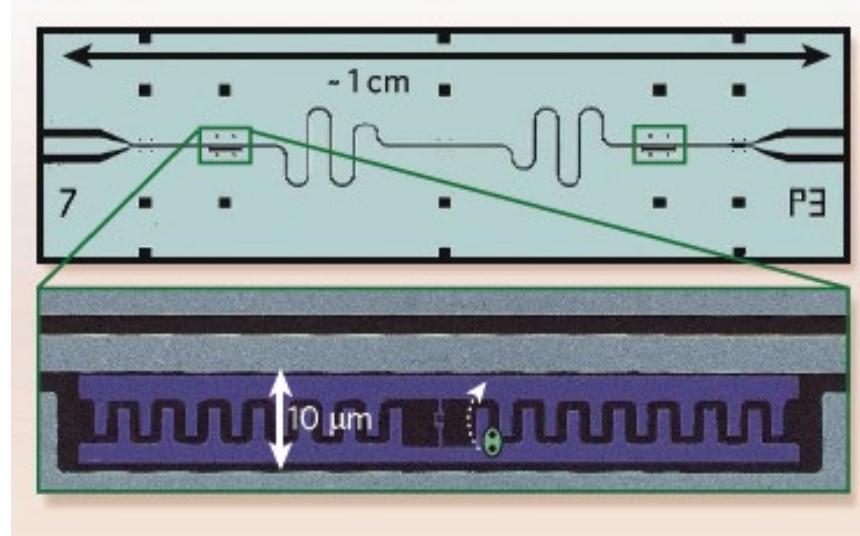


$$2g \begin{array}{c} \text{---} \\ \text{---} \end{array} \begin{array}{c} |0\rangle|\downarrow\rangle - |1\rangle|\uparrow\rangle \\ |0\rangle|\downarrow\rangle + |1\rangle|\uparrow\rangle \\ |0\rangle|\uparrow\rangle \end{array}$$

$g T_2 \gg 1$ “Strong coupling”

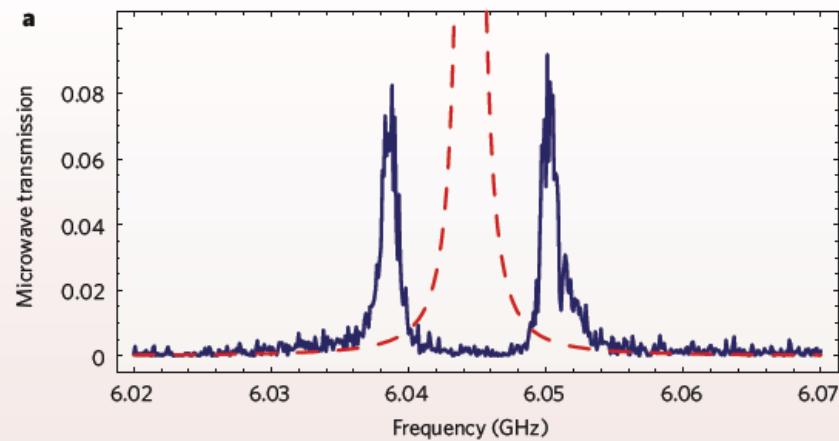
A. Blais, R.-S. Huang, A. Wallraff, S. Girvin, & R. Schoelkopf, Phys. Rev. A **69**, 062320 (2004)
 A. Wallraff et al., Nature (London) **431**, 162 (2004).

Light-matter interaction in a chip

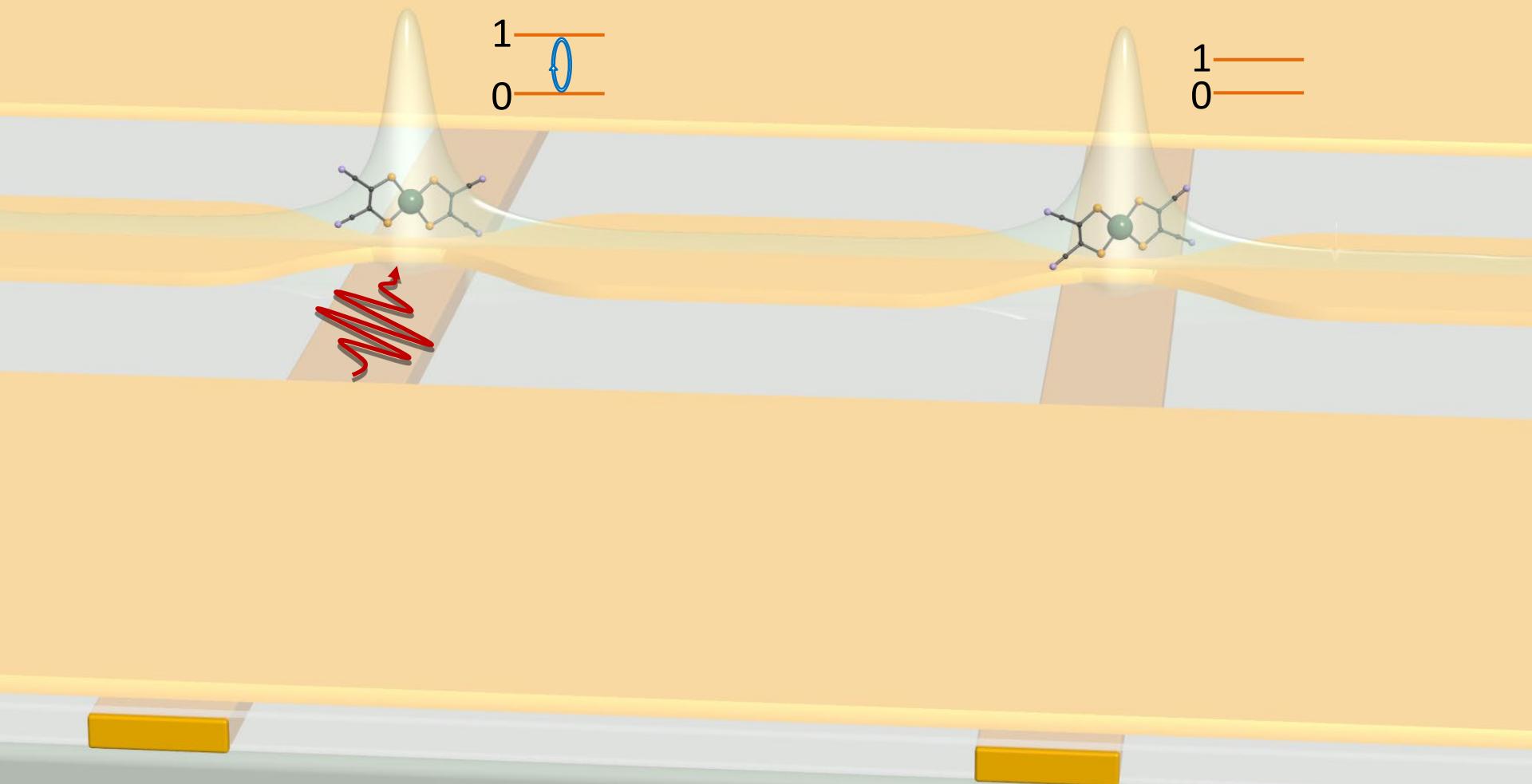


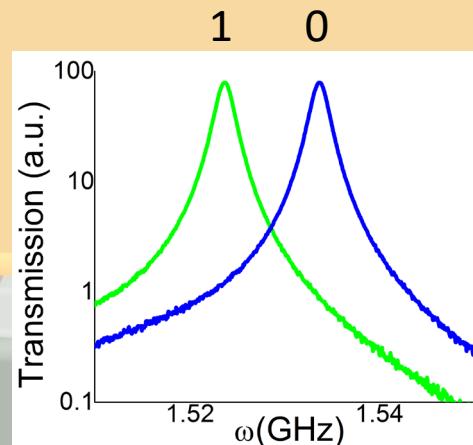
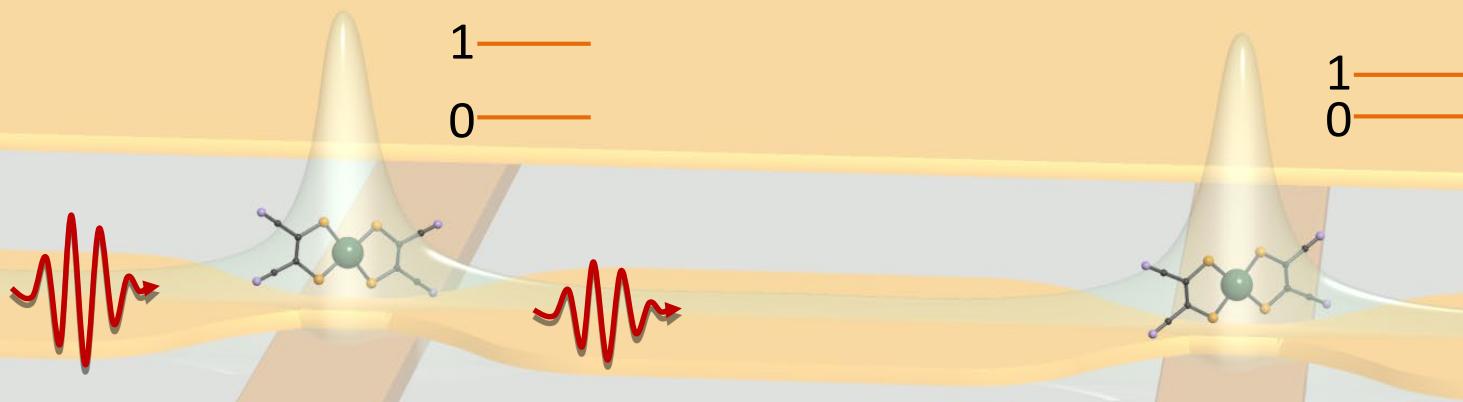
$$\mathcal{H} = \hbar\omega_r(n + 1/2) + \frac{\hbar\omega}{2}\sigma_z + \hbar g(a^\dagger\sigma^- + a^-\sigma^\dagger)$$

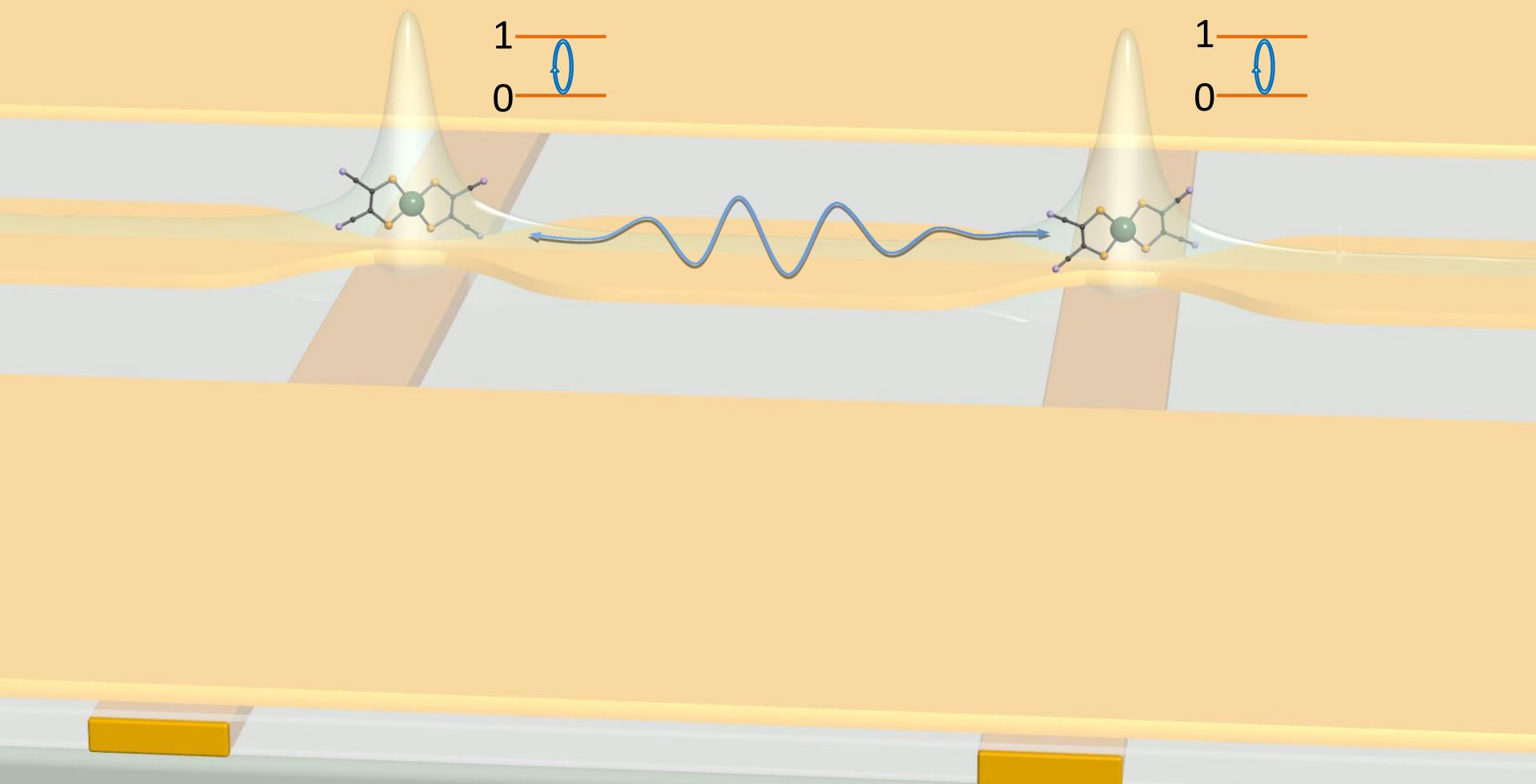
- Read-out
- Effective couplings

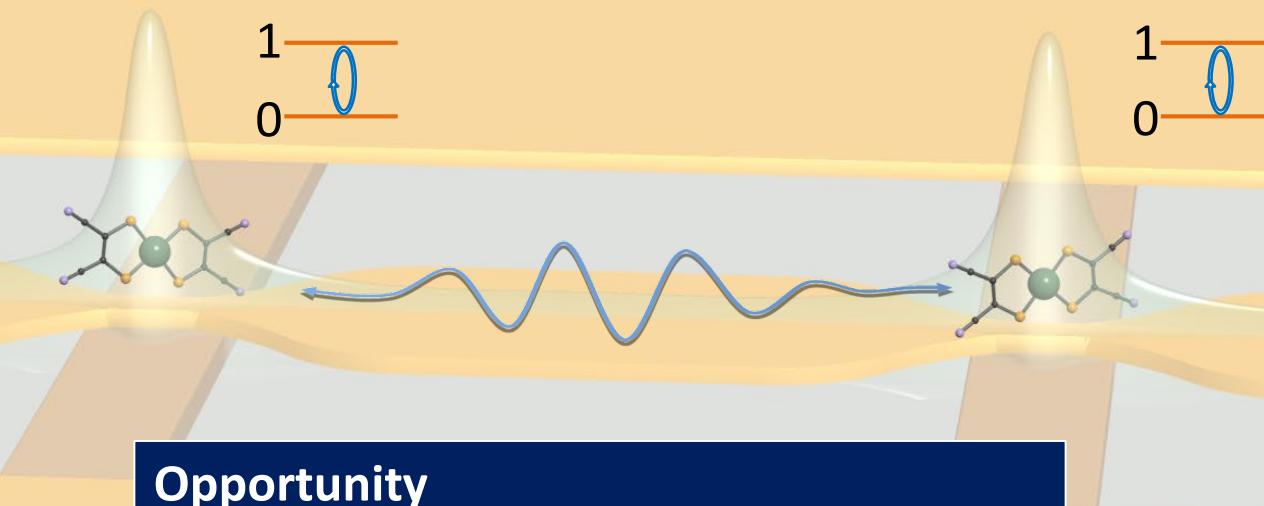


$g T_2 \gg 1$ “Strong coupling”









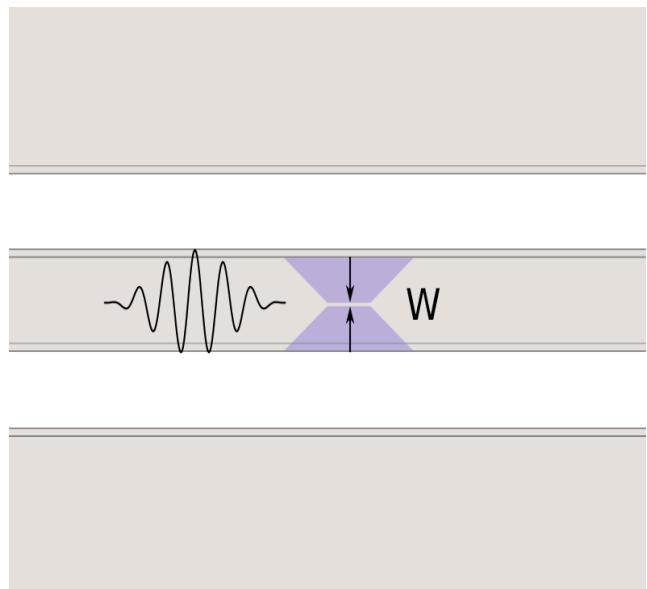
Opportunity

Up to **100** qubits in a chip

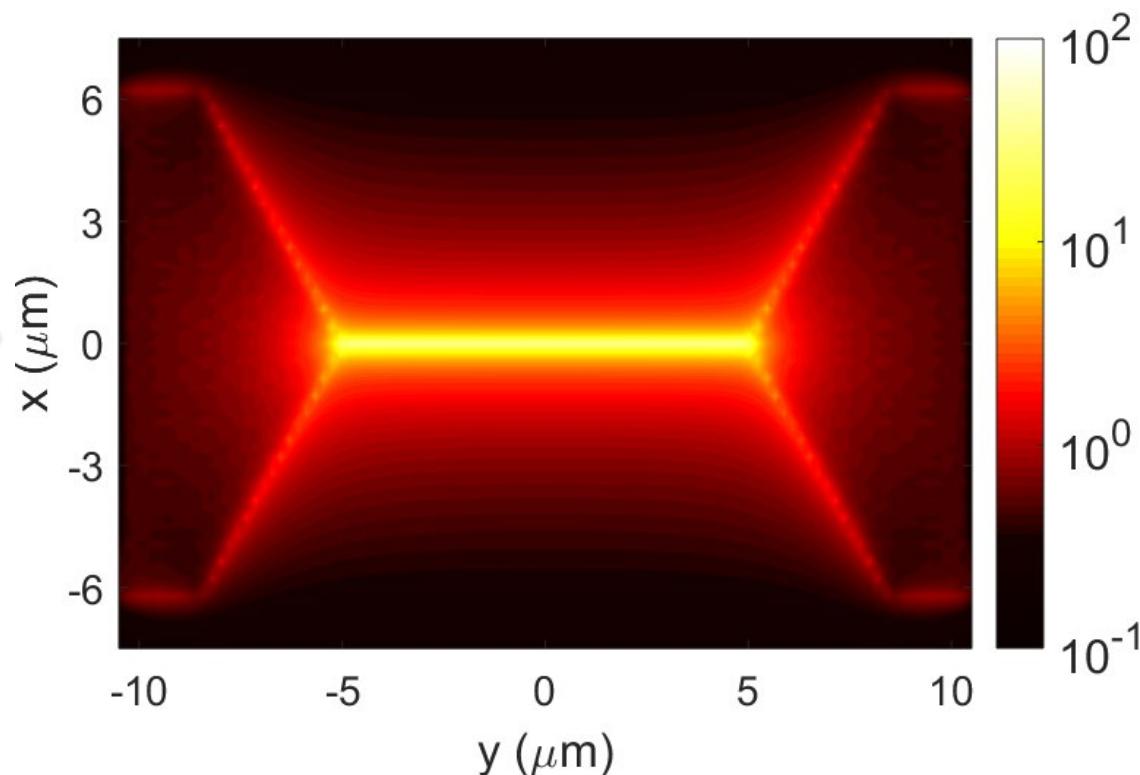
Challenge

Can the spin-photon coupling $g \gg 1/T_2$?

Nanoscale constriction

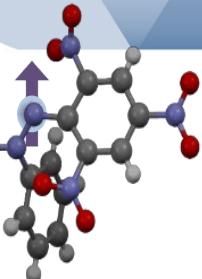
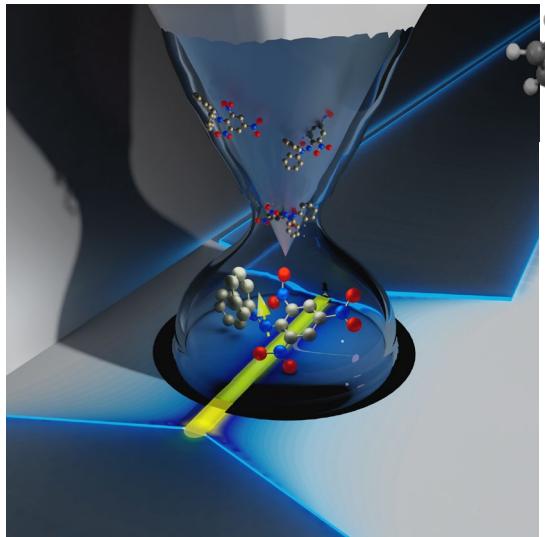
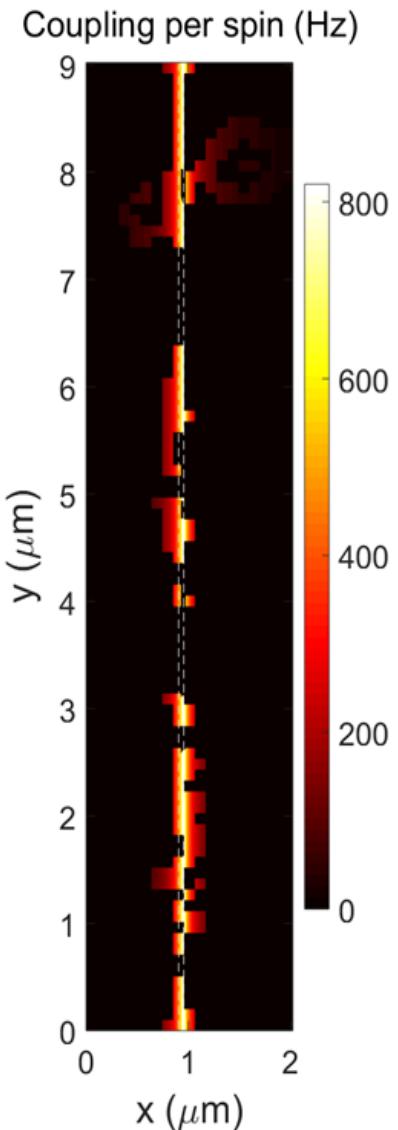
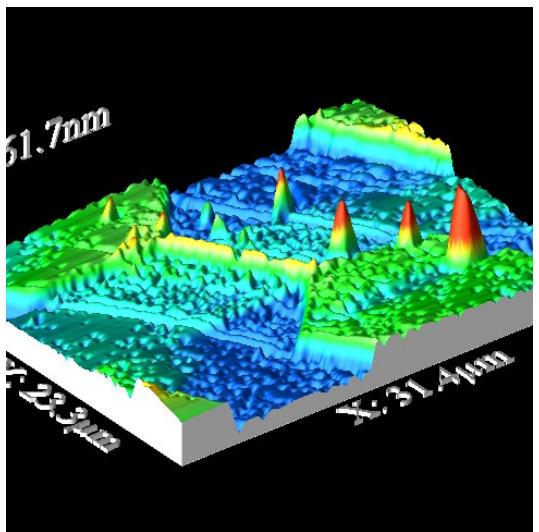
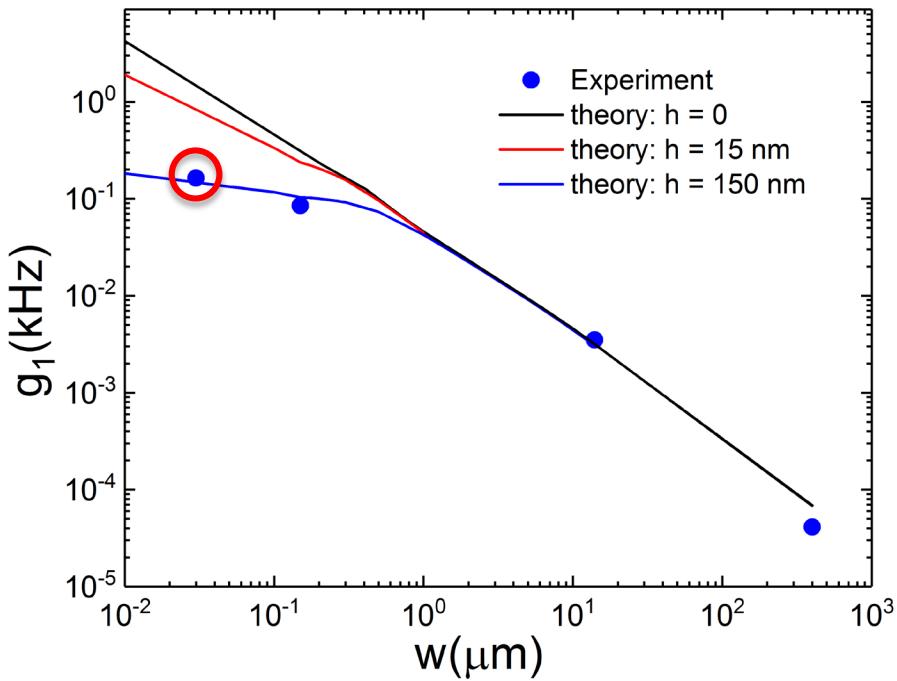


Microwave magnetic field (simulation)

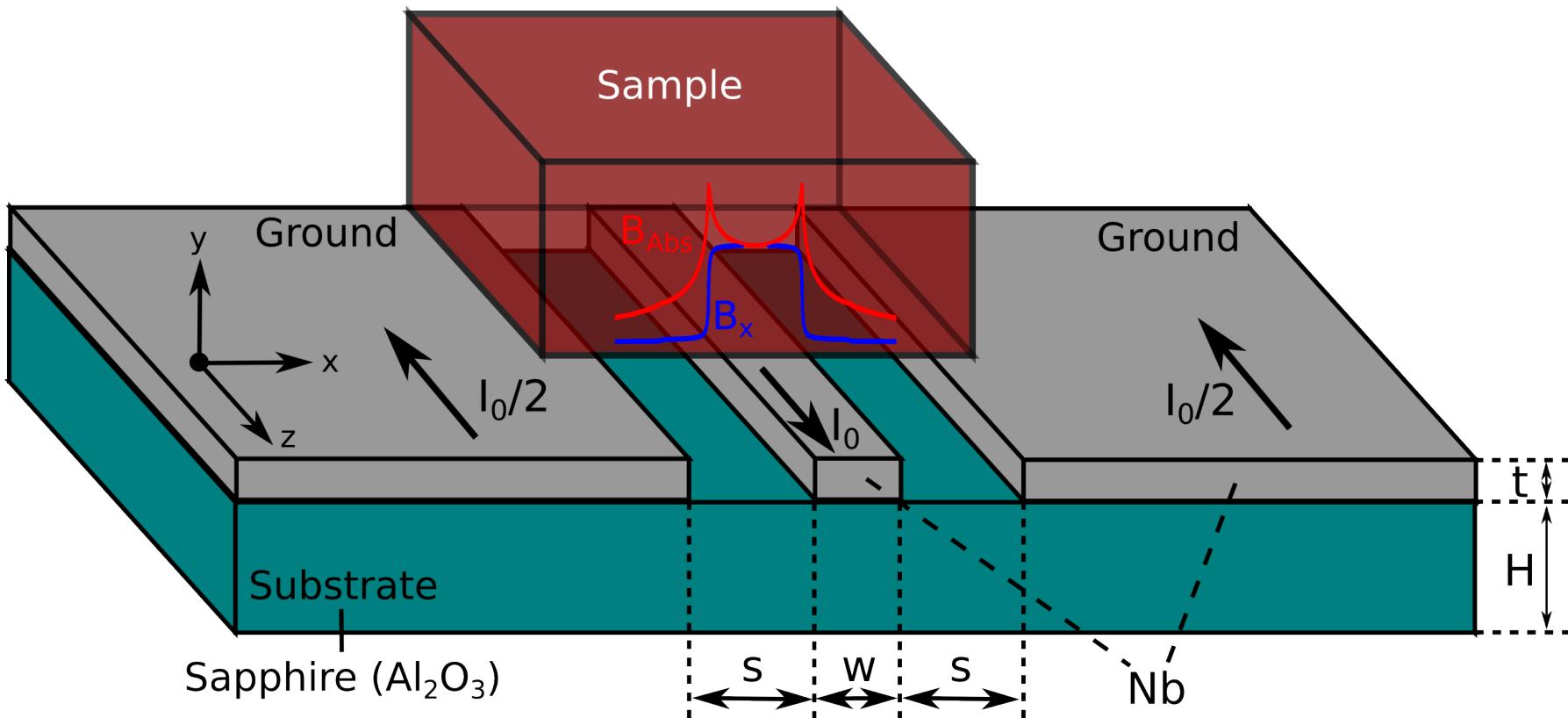


Enhances current density and microwave magnetic field

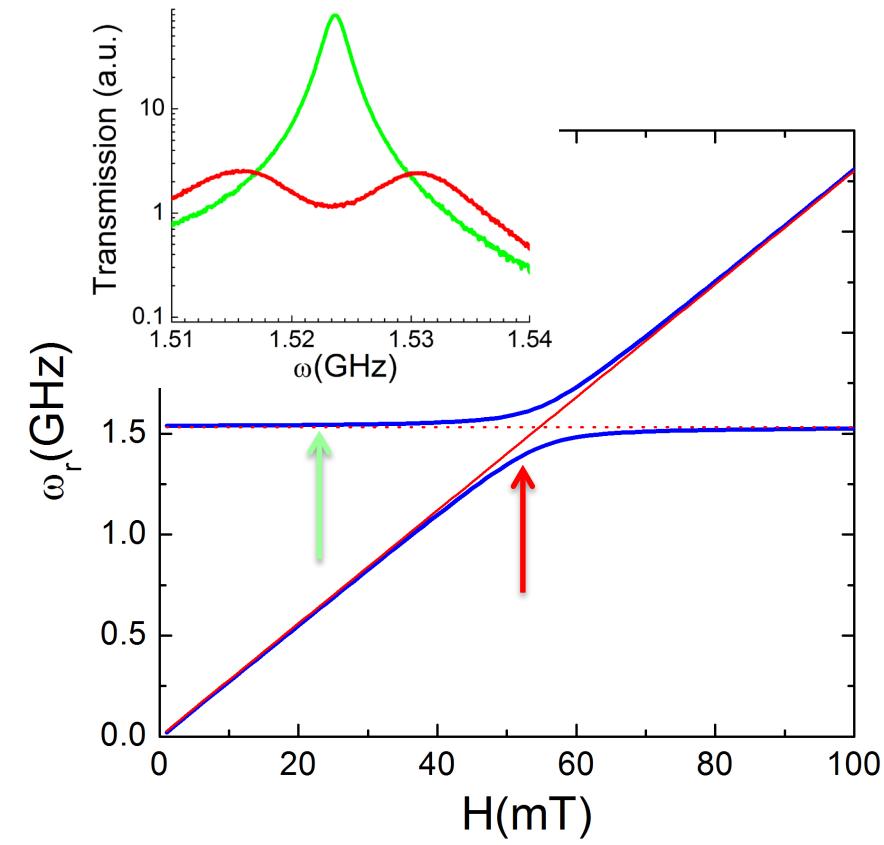
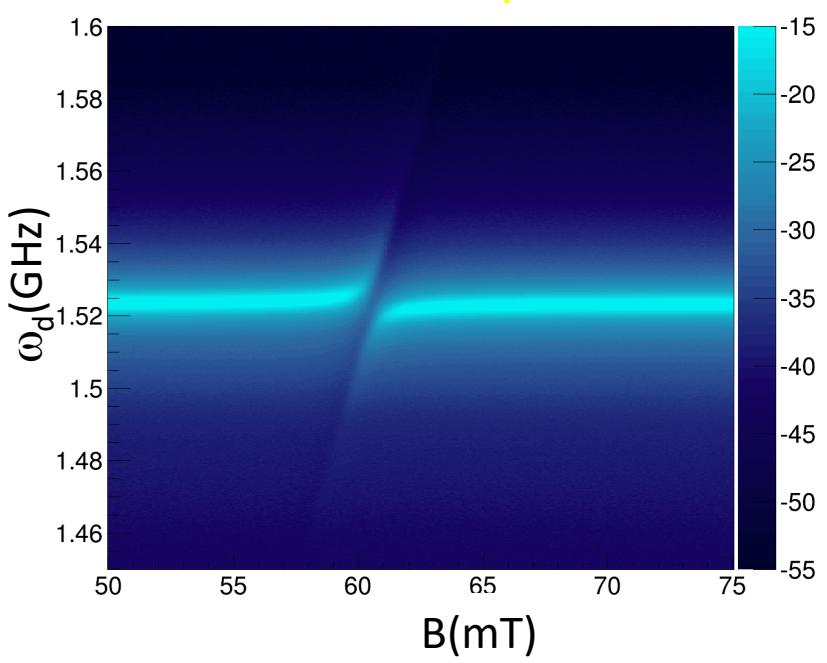
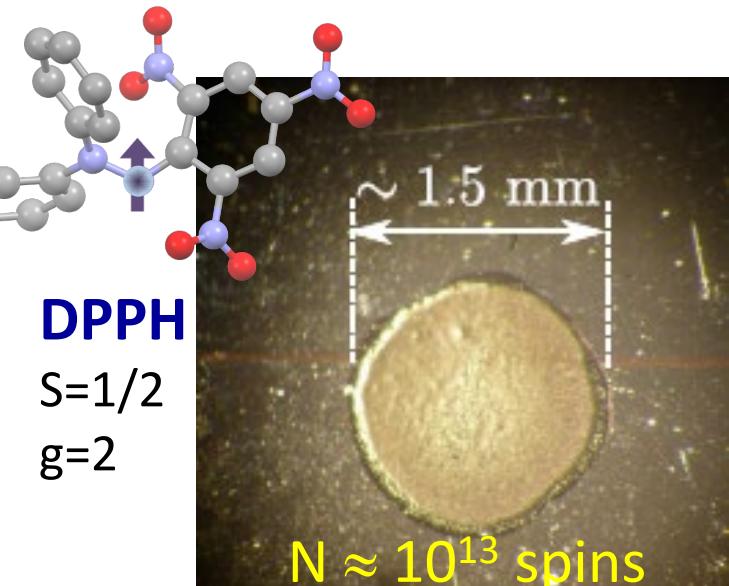
Spin ensemble integration: Dip-pen nanolithography

DPPH, $S = 1/2$ 

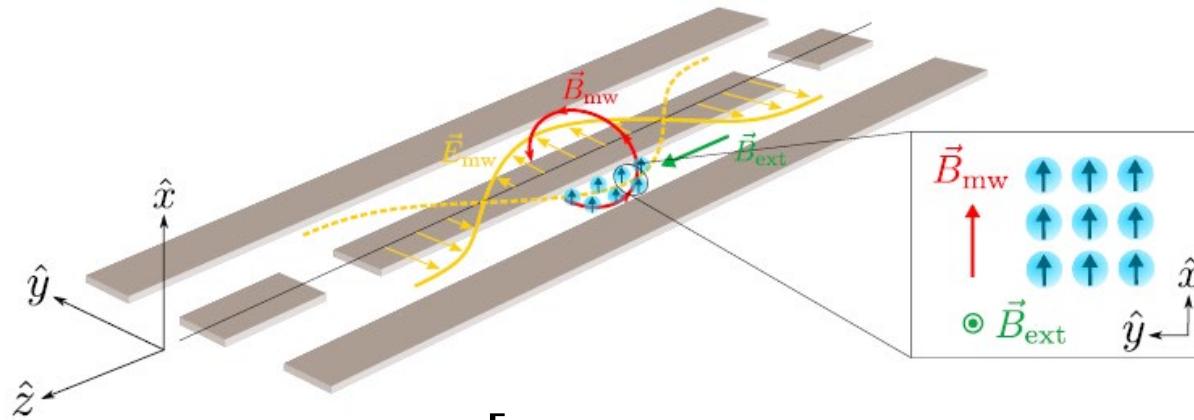
**10^3 enhanced coupling near
nanoconstrictions**
 $g_1 T_2 \sim 0.001\text{-}0.01$



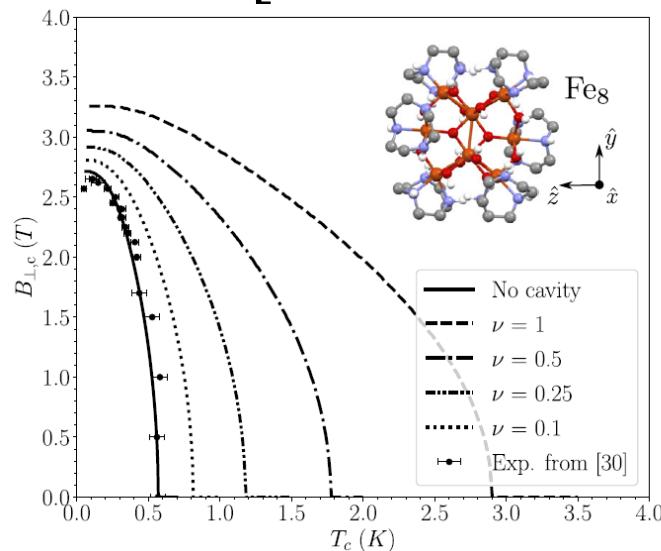
$$g_N \approx \sqrt{N} \frac{2g_J\mu_B J b_{rf}}{h}$$

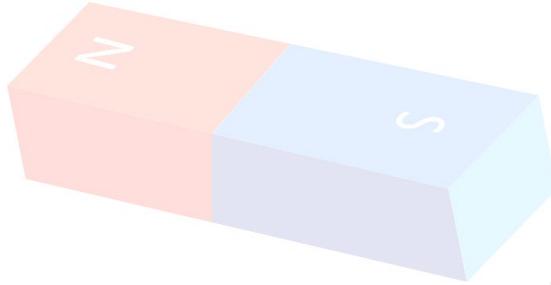


Coupling to cavity photons introduces effective ferromagnetic correlations

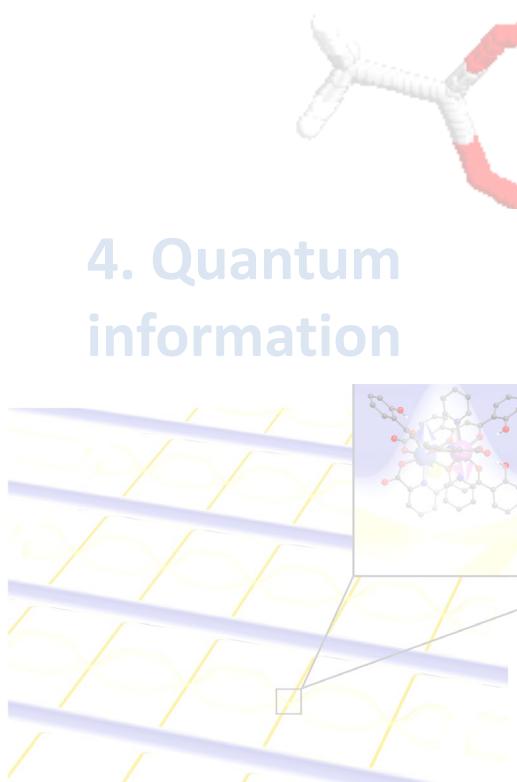


$$\mathcal{H} \xrightarrow{\text{cavity}} \mathcal{H}_{\text{eff}} = \mathcal{H} - \frac{1}{\hbar\omega_r} \left[\sum_{j=1}^N \frac{g\mu_B}{2} B_{mw}(\vec{r}_j) (e^{i\theta_j} S_j^+ + e^{-i\theta_j} S_j^-) \right]^2$$

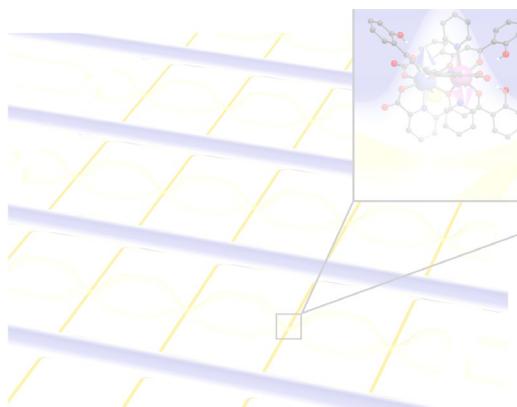




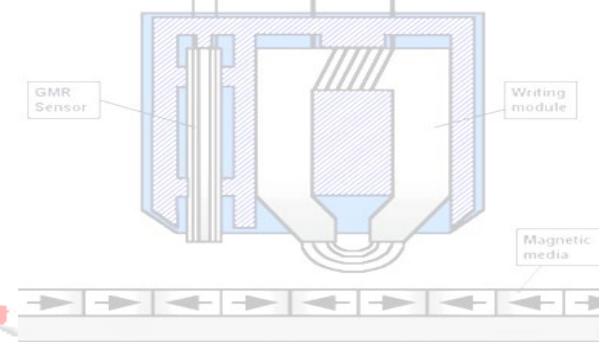
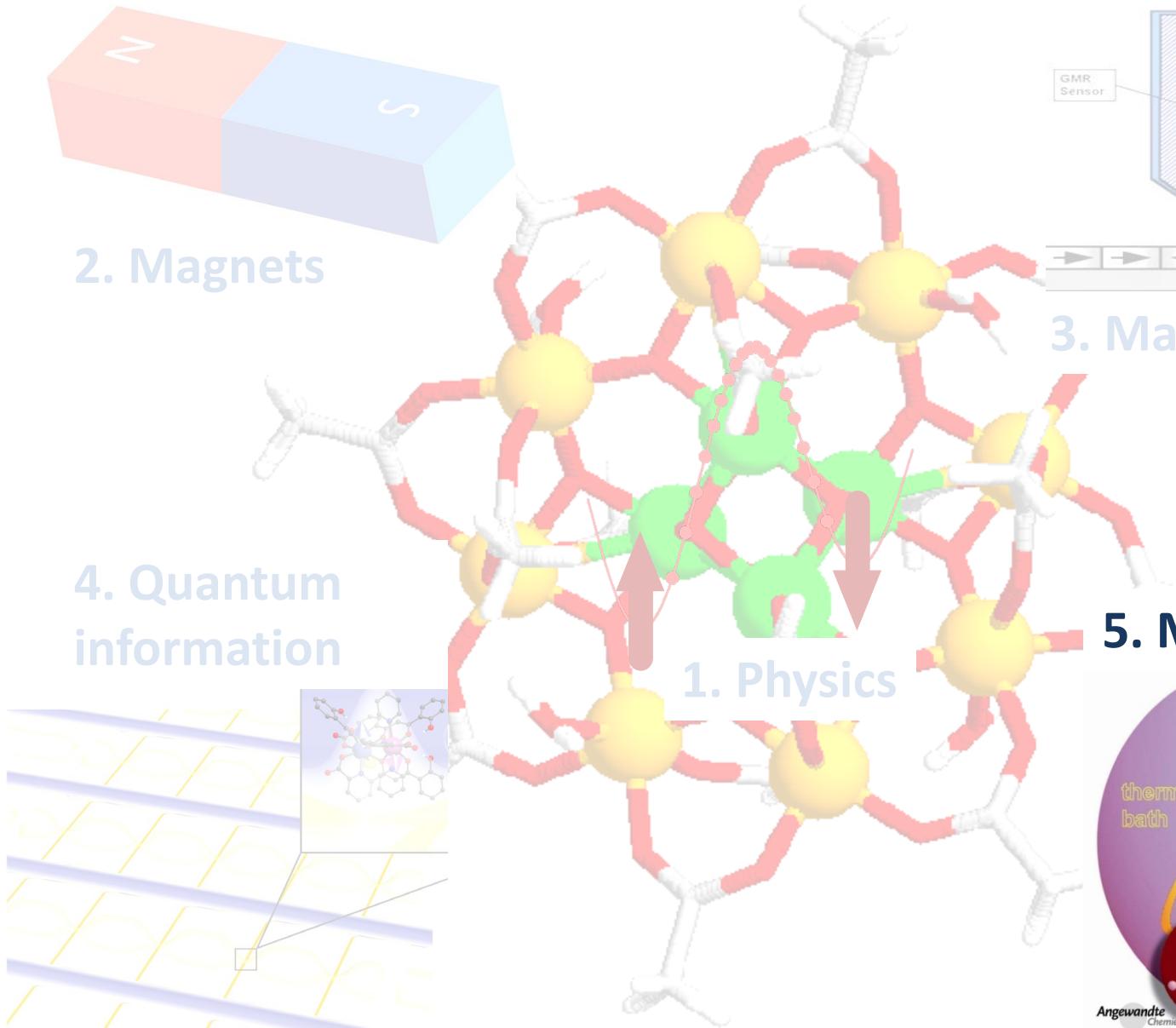
2. Magnets



4. Quantum information



1. Physics



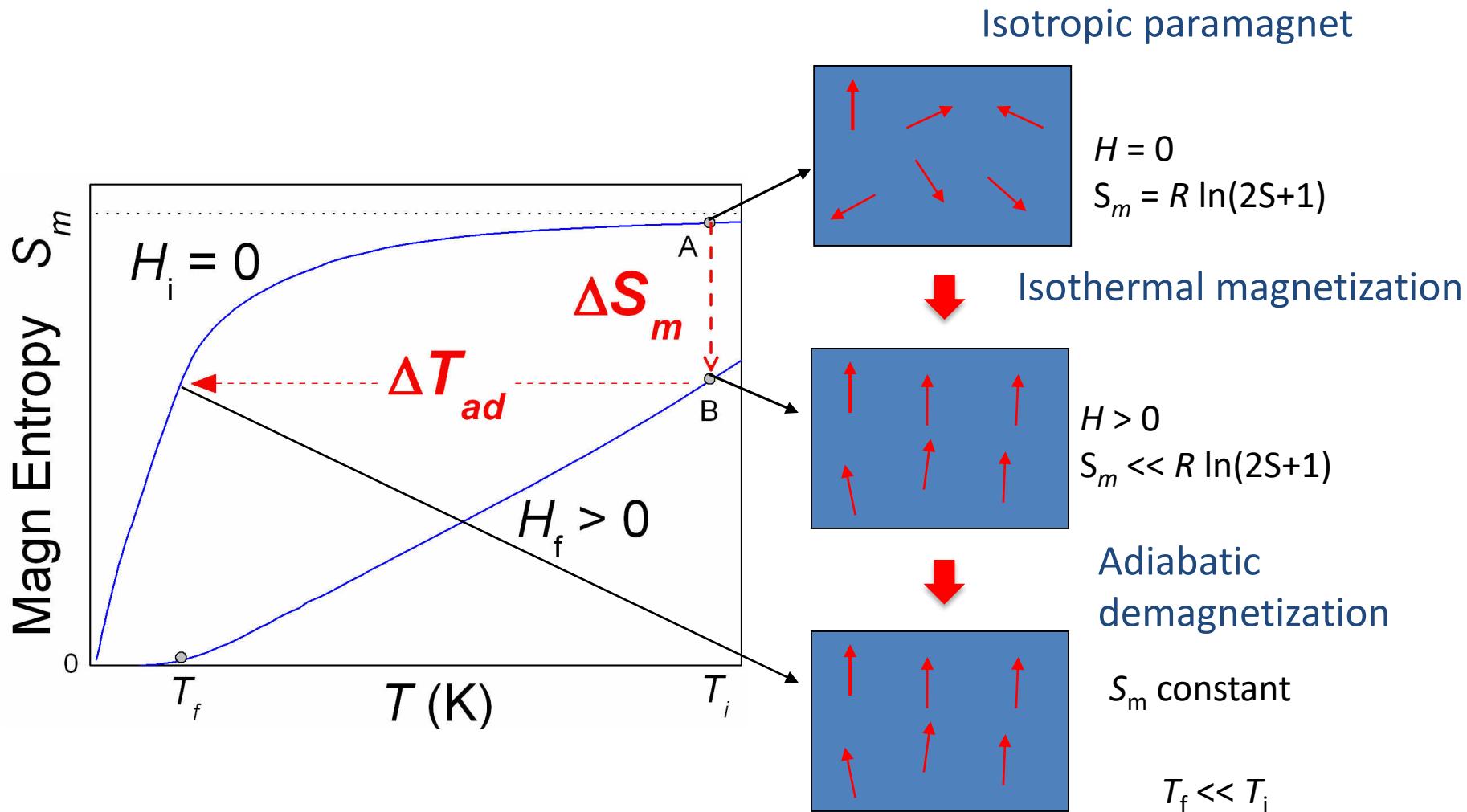
3. Magnetic recording

5. Magnetic coolers



Magnetocaloric effect (MCE)

W. F. Giauque and D. P. MacDougall, Phys Rev **43**, 768 (1933)



Magnetic coolers for very low temperatures

Gd: low anisotropy & high spin

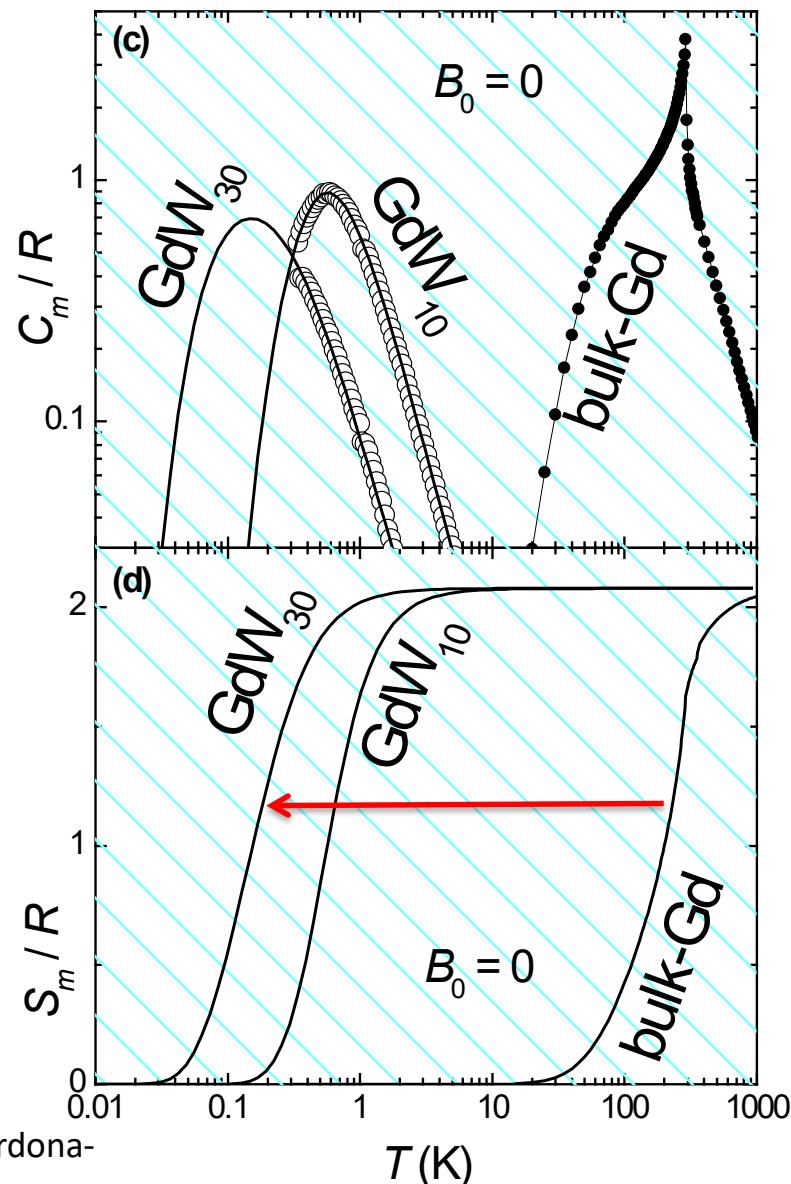
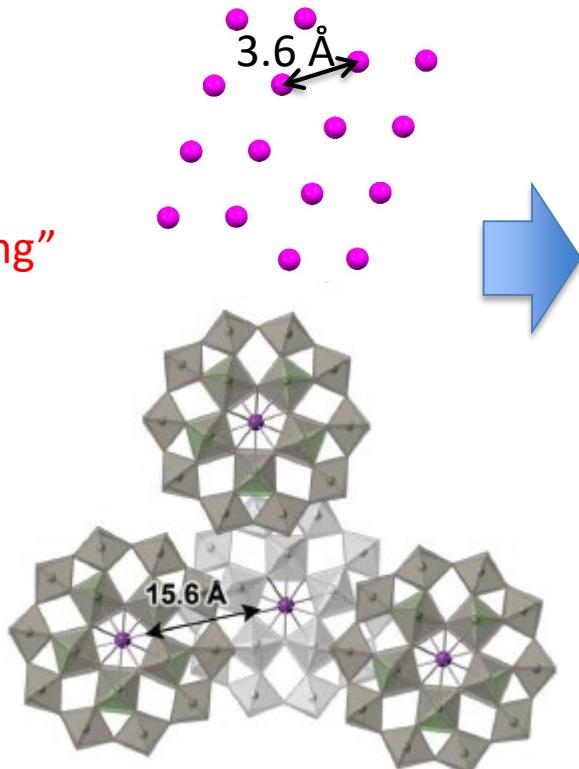
$$\Delta S_m = R(\ln 8)$$

Large entropy content per spin: magnetic cooler

Pure Gd
 $T_c \approx 300$ K

↓
“Fragmenting”
Gadolinium

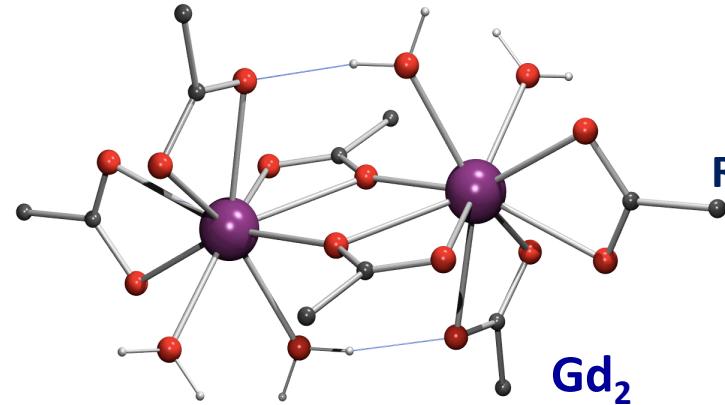
GdW₃₀
 $T_c < 0.02$ K



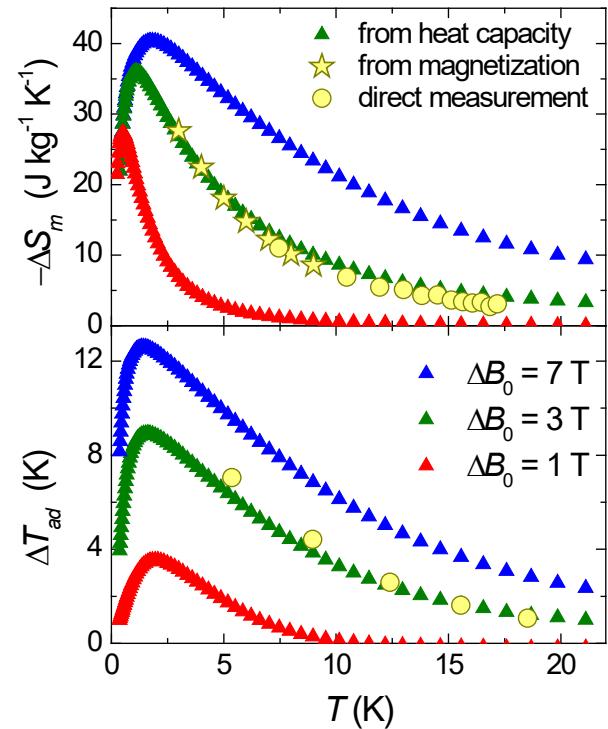
On chip refrigeration

M. Evangelisti et al., Angew. Chem. Int. Ed.

50, 6606 (2011); G. Lorusso, M. Evangelisti *et al*, Adv. Mater. **25**, 2984 (2013); L. X. Chang et al, Chem. Commun. **49**, 1055 (2013).



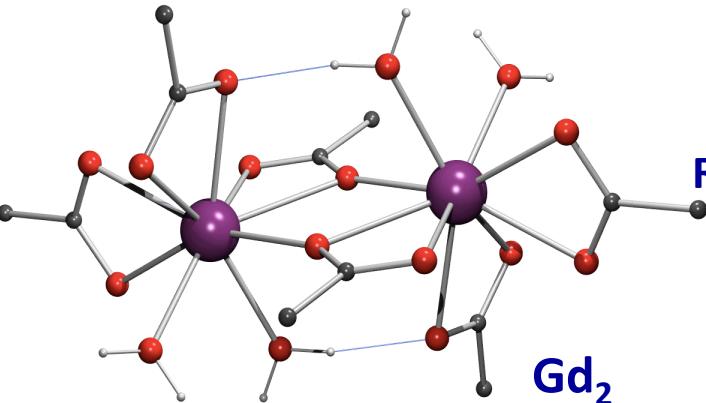
Record MCE for $T < 4.2$ K



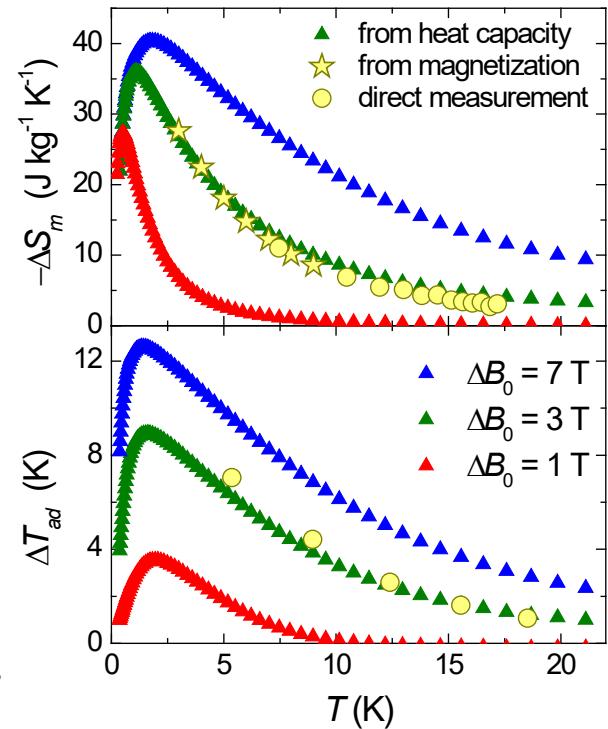
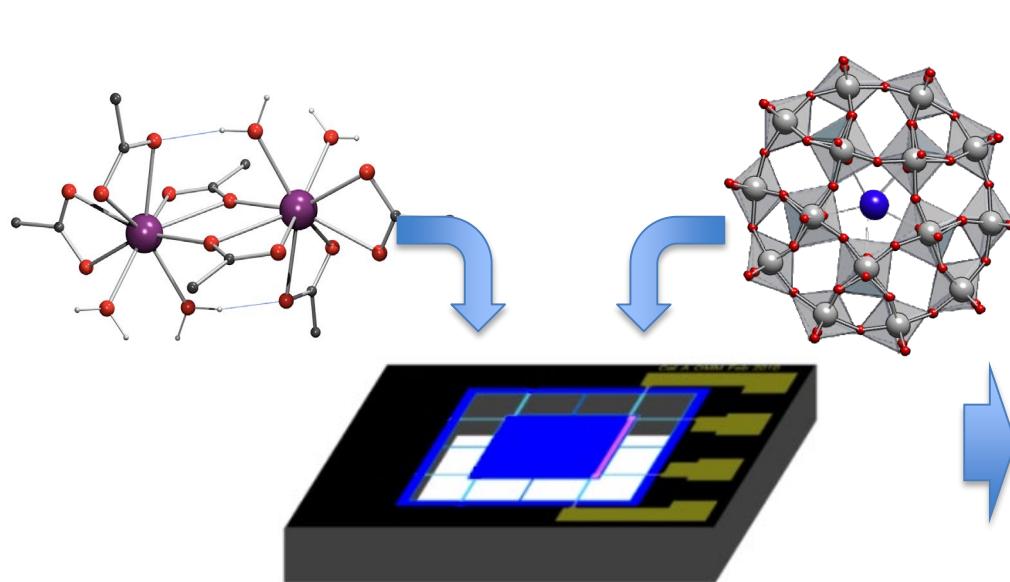
On chip refrigeration

M. Evangelisti et al., Angew. Chem. Int. Ed.

50, 6606 (2011); G. Lorusso, M. Evangelisti et al, Adv. Mater. 25, 2984 (2013); L. X. Chang et al, Chem. Commun. 49, 1055 (2013).

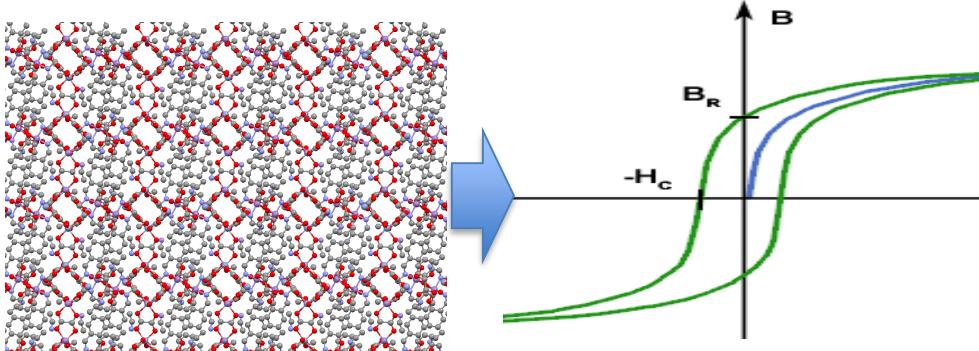
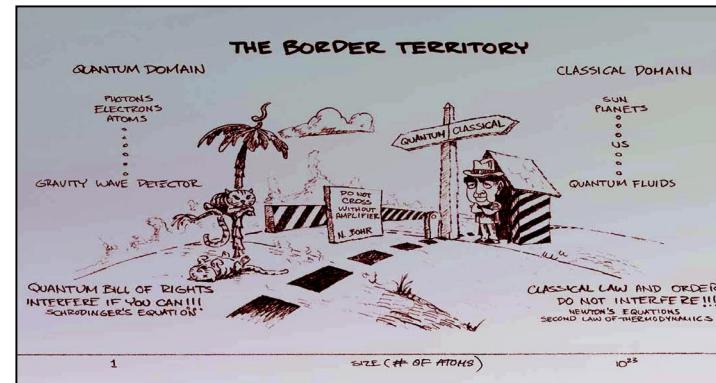


Record MCE for $T < 4.2 \text{ K}$



Quantum physics at the mesoscopic scale

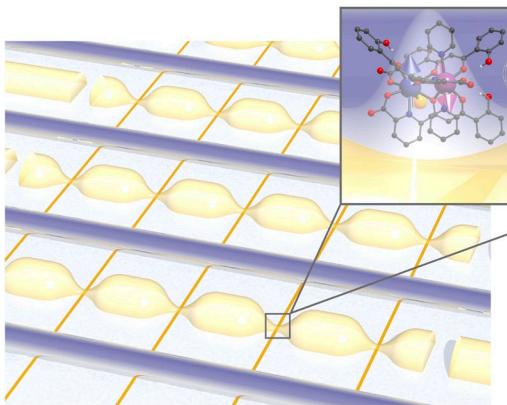
⇒ quantum relaxation, multipartite entanglement , non-equilibrium QPTs, control of magnetic order by q-light, ...



Magnetic recording: High potential of miniaturization ⇒ enhance T_b

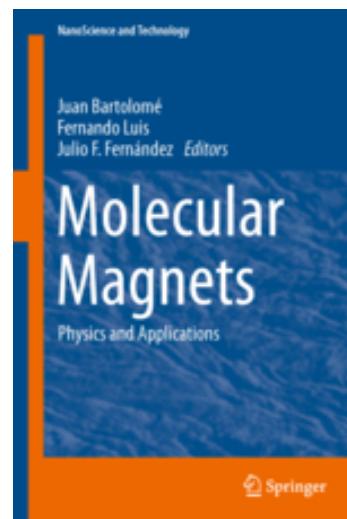
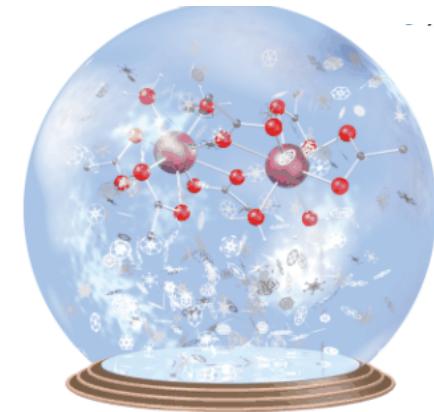
Lanthanide-free permanent magnets ⇒ enhance T_c





Solid candidates to realize basic units of a quantum computer + potential for scaling up \Rightarrow proof-of-concept implementations

Best coolers in the liquid Helium region
and below \Rightarrow devices





INSTITUTO DE NANOCIENCIA
Y MATERIALES DE ARAGÓN



Quantum
Materials and
Devices



Mark Jenkins



Ignacio Gimeno



Marcos Rubín



David Zueco



Olivier Roubeau



Pablo Alonso



María José Martínez



Javier Sesé



Pablo Hermosilla



Ana Isabel Lostao

IFF



Alessandro Chiesa



J. J. García-Ripoll



Stefano Carretta

instituto
iMdea
nanociencia



Enrique Burzurí



CENTRO DE ASTROBIOLOGÍA
ASOCIADO AL NASA ASTROBIOLOGY INSTITUTE



Marina Calero



Alicia Gómez



Andreas Angerer



Johannes Majer



Leoni Barrios

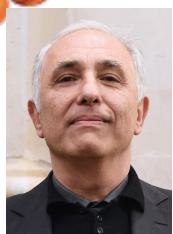
Verónica Velasco



Guillem Aromí



Talal Mallah



ICMM

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Salvador Cardona-Serra

Helena Prima

Alejandro Gaita-Ariño

Yan Duan



Eugenio Coronado



QUANTERA

FATMOLS



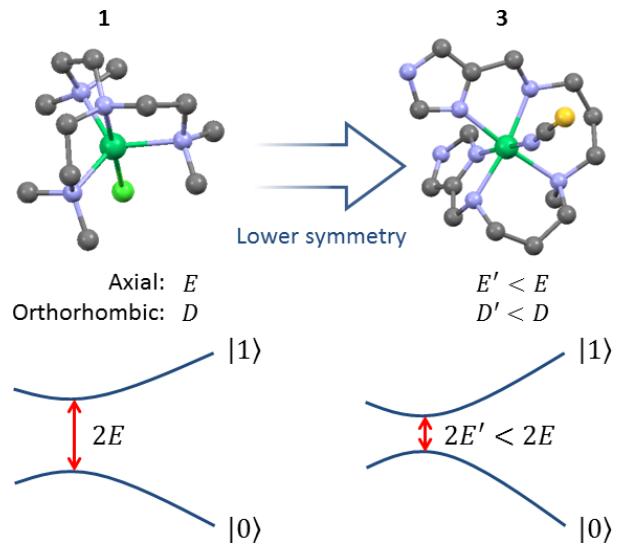
European
Commission

This project has received funding from the European Union's Horizon 2020 research and innovation programme under grant agreement No 862893 (FATMOLS).

[Ni(Me₆tren)Cl](ClO₄)

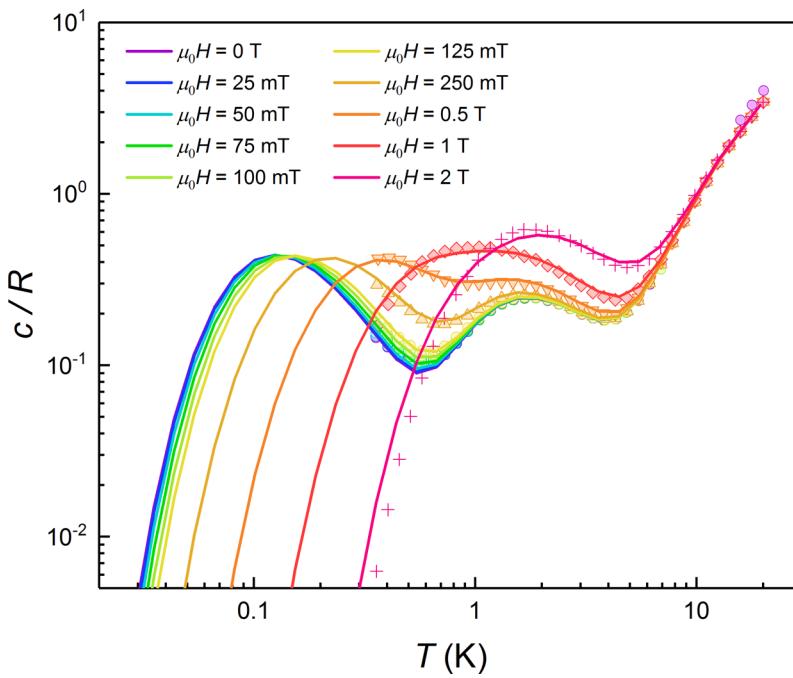
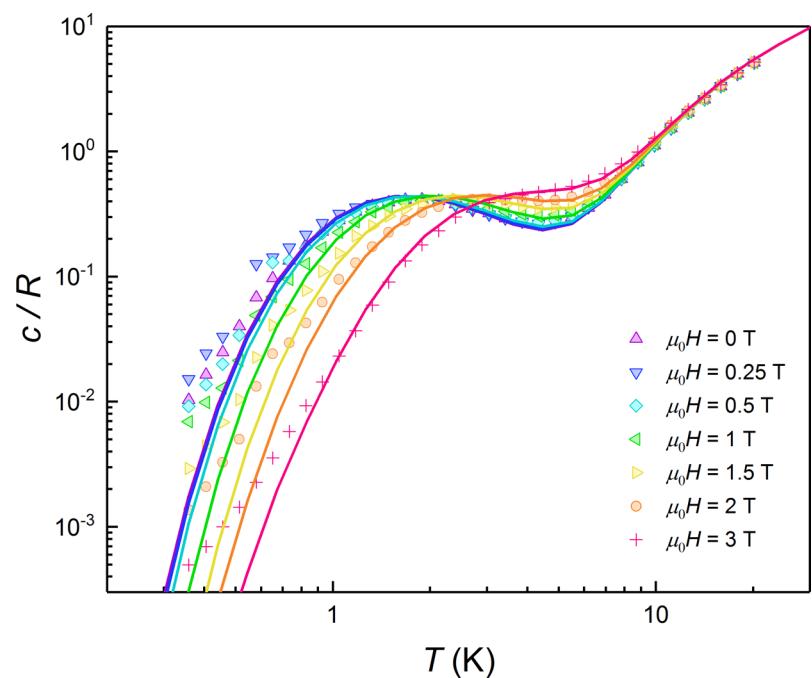
Ni(II) $S = 1$

$$H = BO_2^0 + B_2^2 O_2^2$$

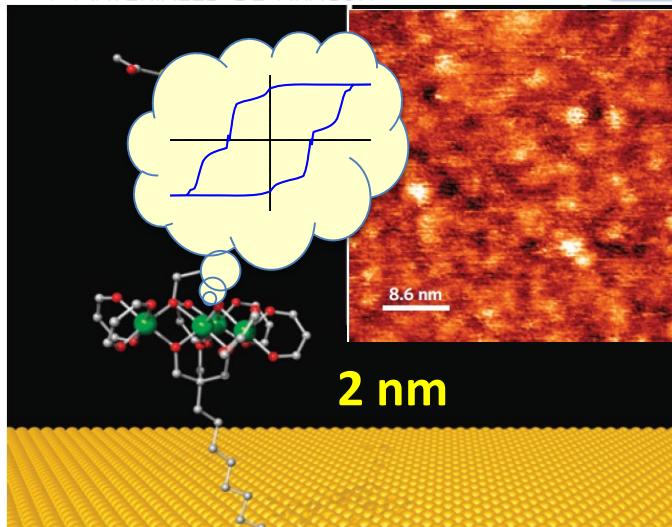


[Ni-Imdipa]-(NCS)

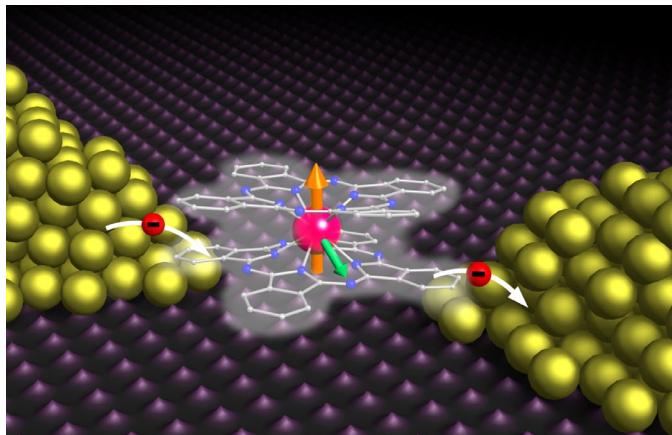
M. Rubín et al, Chem. Sci. **12**, 5123 (2021)



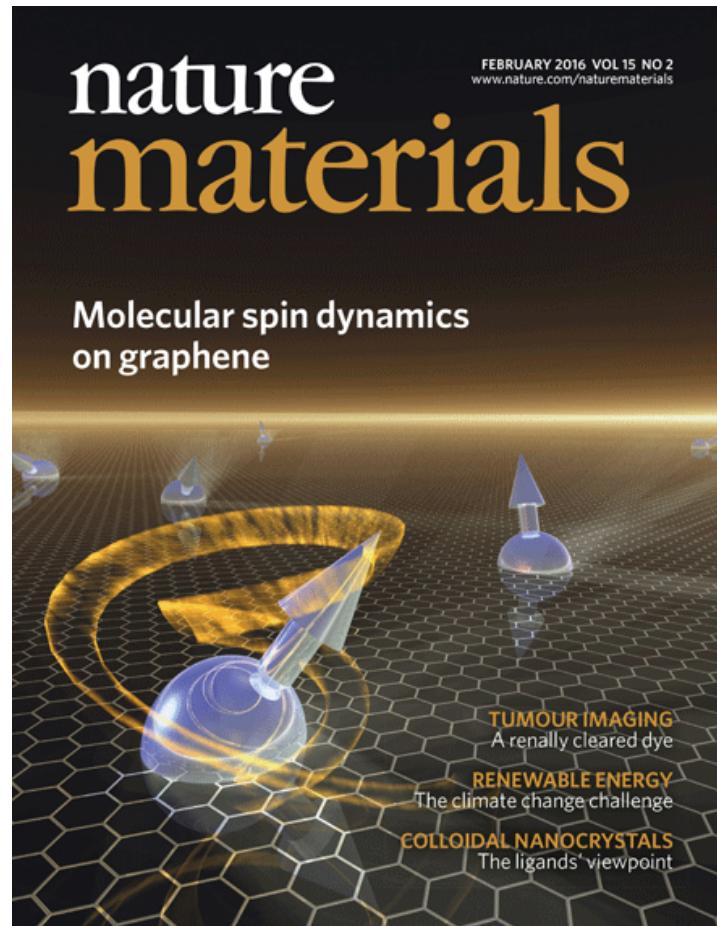
From the bulk to single molecules



M. Mannini, F. Pineider, C. Danieli, F. Totti, L. Sorace, P. Sainctavit, M. A. Arrio, E. Otero, L. Joly, J. C. Cesar, A. Cornia & R. Sessoli Nature **468**, 417 (2010)



R. Vincent S. Klyatskaya, M. Ruben, W. Wernsdorfer & F. Balestro, Nature **488**, 357 (2012)



C. Cervetti, A. Rettori, M. G. Pini, A. Cornia, A. Repollés, F. Luis, M. Dressel, S. Rauschenbach, K. Kern, M. Burghard & L. Bogani, Nature Mater **15**, 164 (2016)