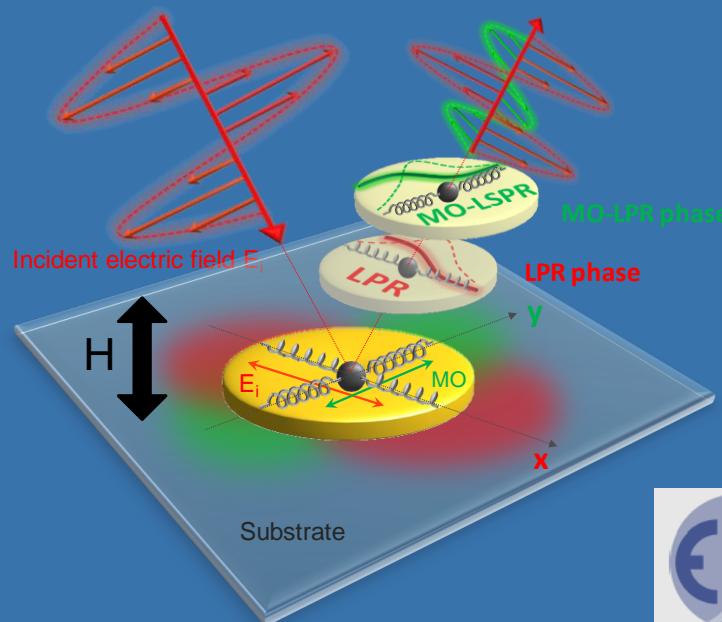


# FT-3: Magneto-optics and Magneto-plasmonics Part 2

P. Vavassori

-IKERBASQUE, Basque Fundation for Science and  
CIC nanoGUNE Consolider, San Sebastian, Spain.



THE EUROPEAN SCHOOL ON  
**MAGNETISM 2018**  
MAGNETISM BY LIGHT



## NANOANTENNAS COMBINING MAGNETIC AND PLASMONIC FUNCTIONALITIES

- *Localized surface plasmons & Magneto-optical Kerr effects (MOKE): Introduction*
- *Physical picture and modeling*
- *LSPR-based sensing: Towards molecular sensing*
- *Photonics technology: control of the non-reciprocal light propagation*

## MAGNETOPLASMONIC METAMATERIALS

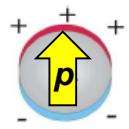
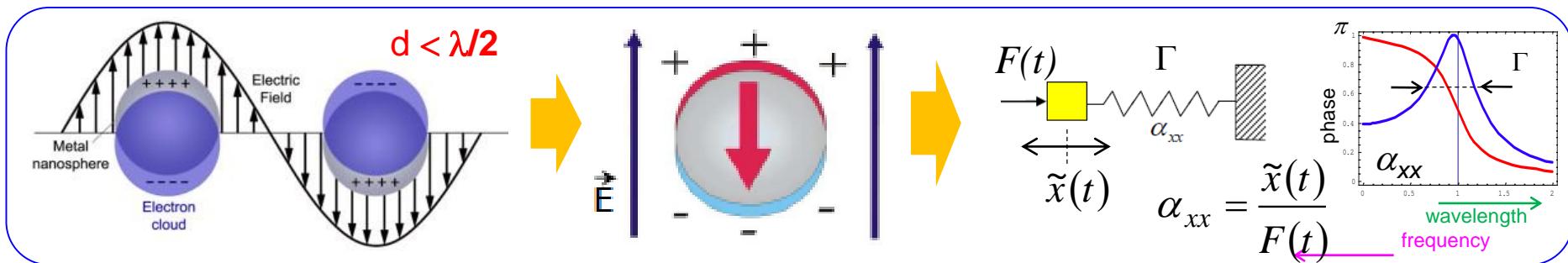
- *Surface lattice resonances in arrays of nanoantennae*
- *Arrays of elliptical nanoantennae*
- *Magnetoplasmonic gratings: arrays of antidots*

## CONCLUSIONS



# Localized surface plasmon resonances (LSPRs)

Localized surface plasmon resonances (LSPRs or LSPs) collective oscillations of conduction electrons in metallic nano structures.



For very small particles,  $a \ll \lambda \iff$  Electrostatics approximation

$$\text{Particle} \rightarrow \text{dipole}: \quad \vec{p} = \alpha(\omega) \vec{E}$$

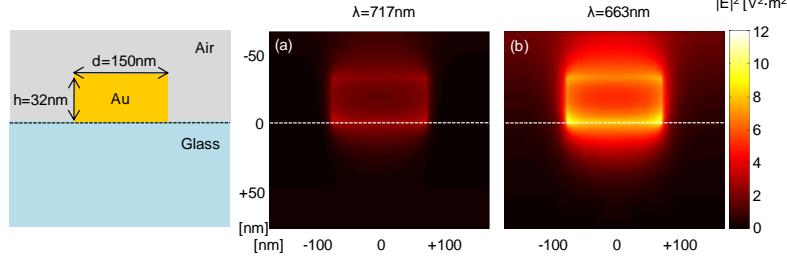
$$\alpha(\omega) = 4\pi\epsilon_d a^3 \frac{\epsilon_m(\omega) - \epsilon_d}{\epsilon_m(\omega) + 2\epsilon_d}$$

Resonance for  $\epsilon_m = -2\epsilon_d$

Small  $\epsilon_d$  for excitation of a LSPR in the optical visible range (air, glass....)

Ellipsoid

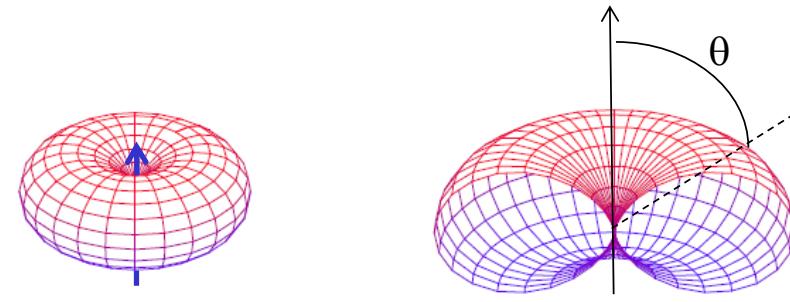
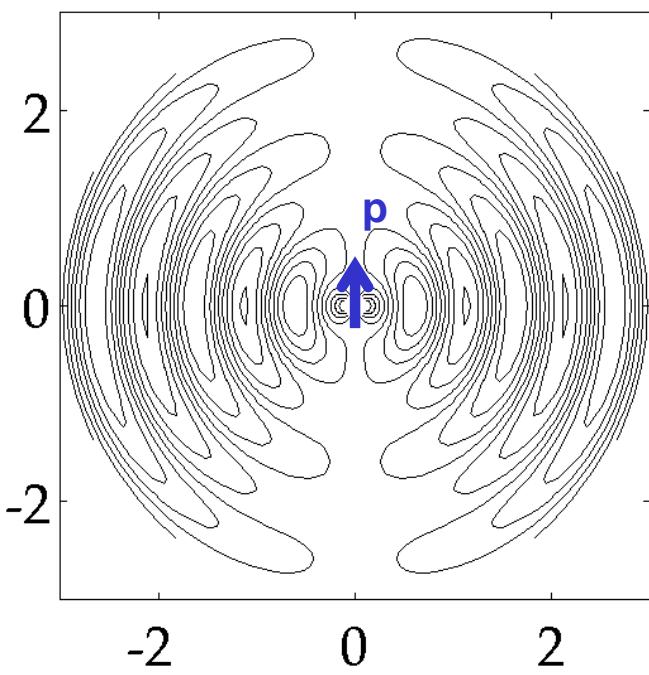
$$\tilde{\alpha} = \begin{bmatrix} \alpha_{xx} & \alpha_{xy} & \alpha_{xz} \\ \alpha_{yx} & \alpha_{yy} & \alpha_{yz} \\ \alpha_{zx} & \alpha_{zy} & \alpha_{zz} \end{bmatrix}$$



Subwavelength localization of electromagnetic energy



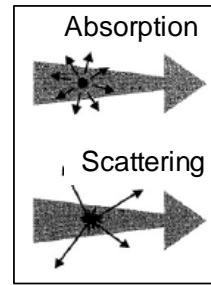
## EM field irradiated by an oscillating dipole



Dipole radiation pattern  $\sin^2 \theta$

Cut-out view of the same

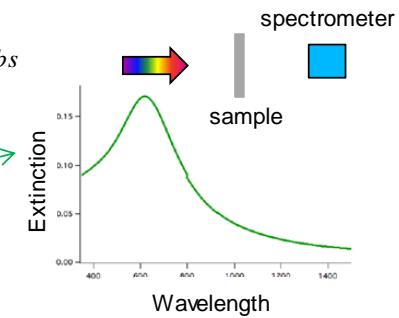
Scattering and absorption remove energy from the incoming EM



$$\sigma_{ext} = \sigma_{sca} + \sigma_{abs}$$

$$\sigma_{sca} \propto |\alpha|^2$$

$$\sigma_{ext} \propto \text{Im}\{\alpha\}$$



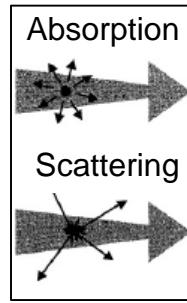
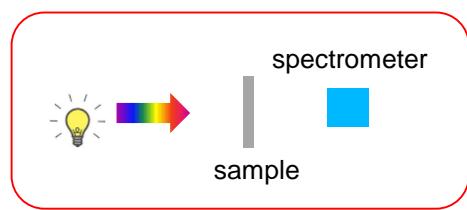
Electric field lines due to an electric dipole oscillating vertically at the origin. Near the dipole, the field lines are essentially those of a static dipole.

At a distance of the order of half wavelength or greater, the field lines are completely detached from the dipole

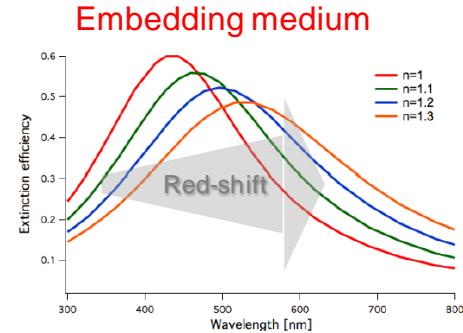
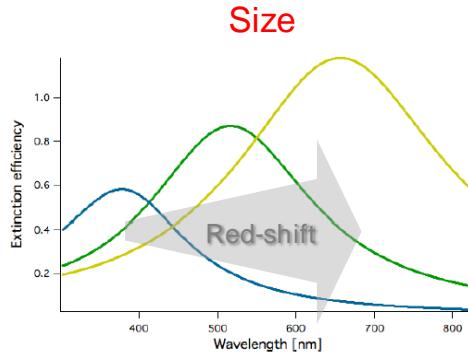
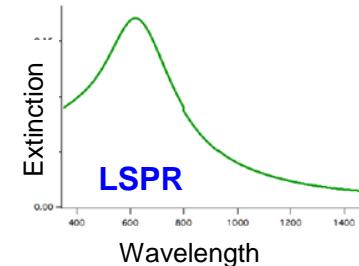


# Localized surface plasmon resonances (LSPRs)

Scattering and absorption remove energy from the incoming EM

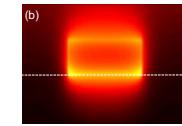


$$\begin{aligned}\sigma_{ext} &= \sigma_{sca} + \sigma_{abs} \\ \sigma_{sca} &\propto |\alpha|^2 \\ \sigma_{abs} &\propto \text{Im}\{\alpha\} \\ \sigma_{ext} &\propto \text{Im}\{\alpha\}\end{aligned}$$



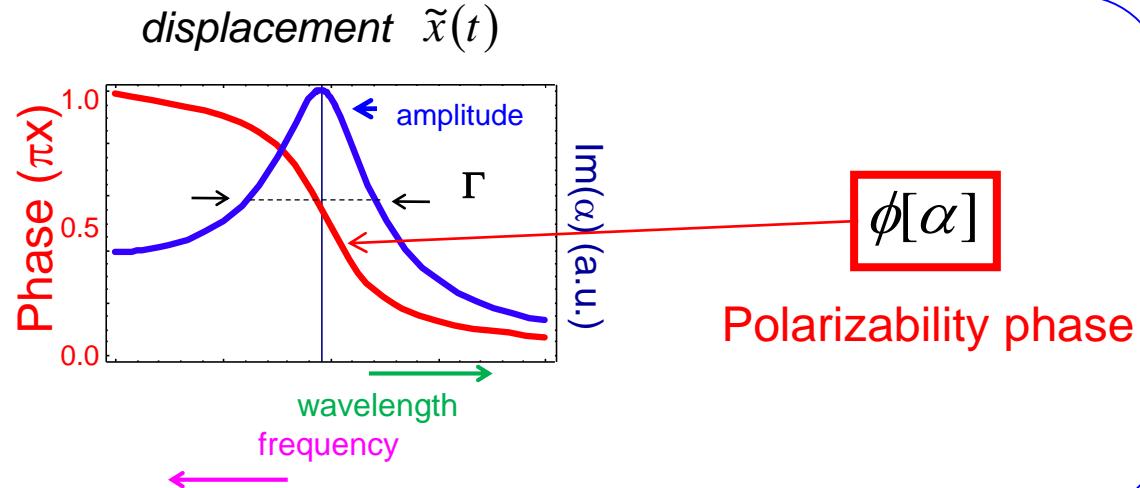
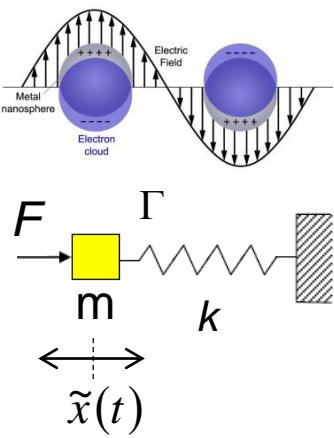
## Applications:

- nanoantennas
- apertureless imaging
- spectroscopic techniques (SERS , SEF, ...)
- information storage
- waveguides
- solar cells
- new optical materials
- sensing, bio-sensing



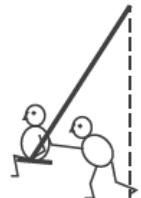
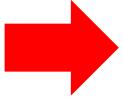


## LSPR as a damped harmonic oscillator

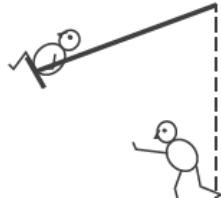


Phase

$\phi[\alpha]$



Low frequency  
Displacement in phase with  $\mathbf{E}$



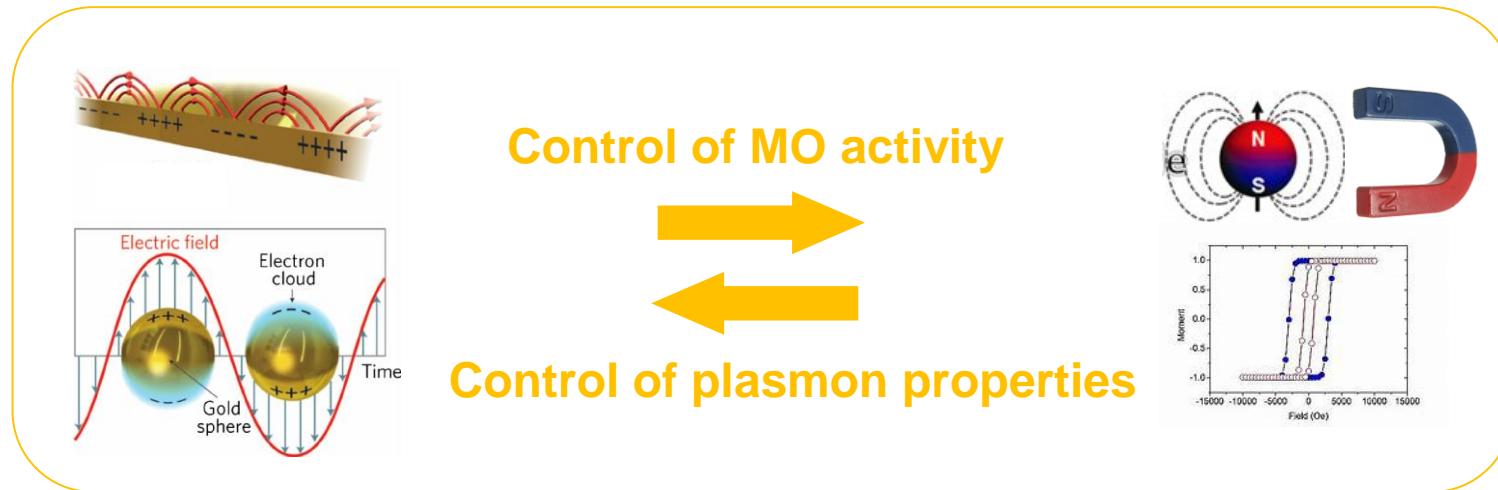
At resonance  
Displacement 90° out of phase with  $\mathbf{E}$



High frequency  
Displacement in anti-phase with  $\mathbf{E}$



# Magnetoplasmonics



- Combination of magnetic materials with nanometer-scale systems supporting surface or localized surface plasmon resonances
  - Plasmons can be controlled by an external magnetic field (active plasmonics)

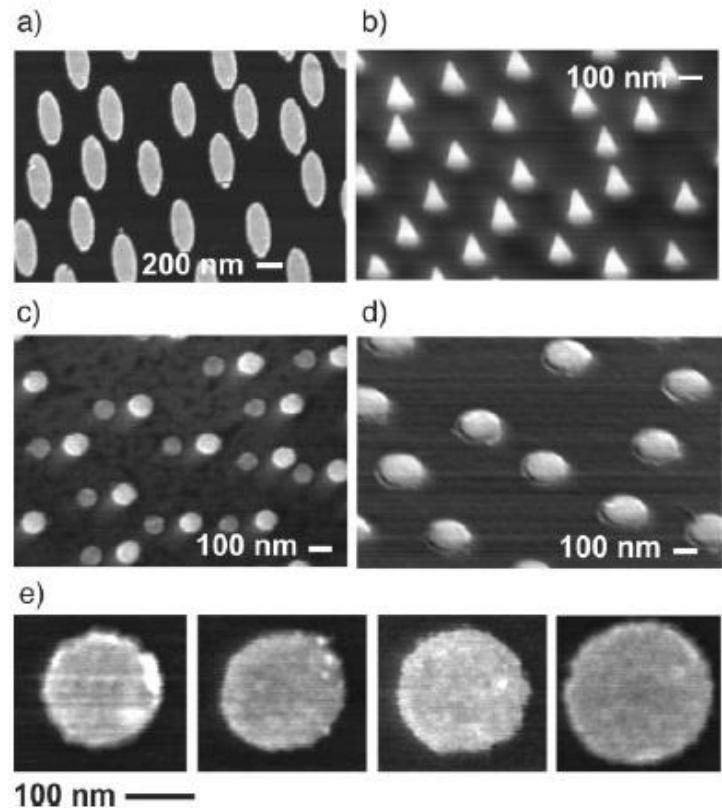
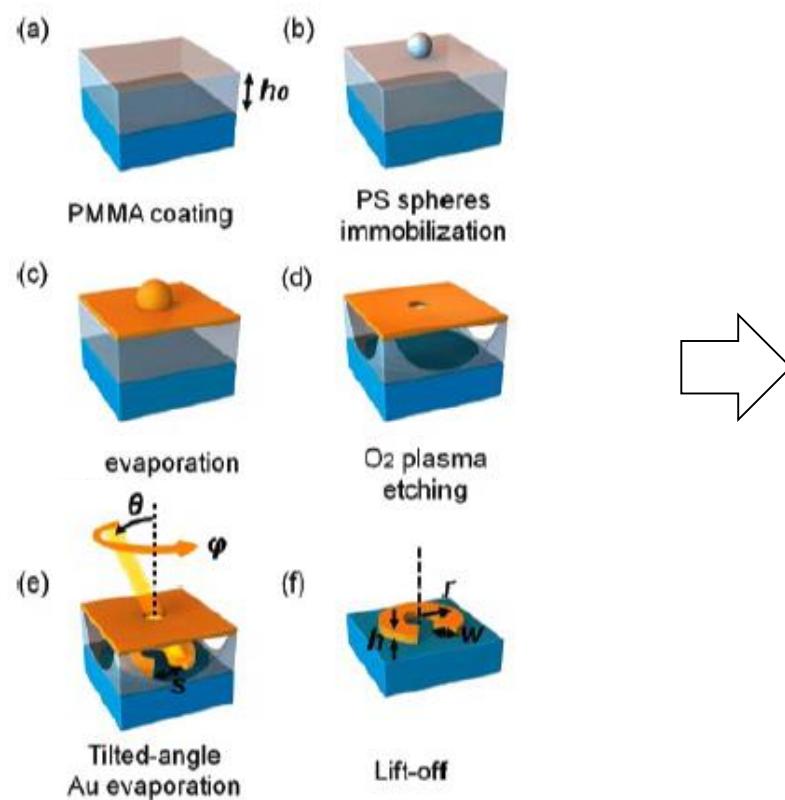
$$(\text{SPPs } M \perp K_{\text{SPP}} \rightarrow K'_{\text{SPP}} = K_{\text{SPP}} \pm \Delta K_{\text{SPP}})$$

- Magneto-optical response can be modified by plasmons: e.g., Faraday or Kerr enhancement

G. Armelles , A. Cebollada , A. García-Martín , and M. Ujué González, *Adv. Optical Mater.* **2013**, 1, 10–35



# Hole-Mask Colloidal Lithography



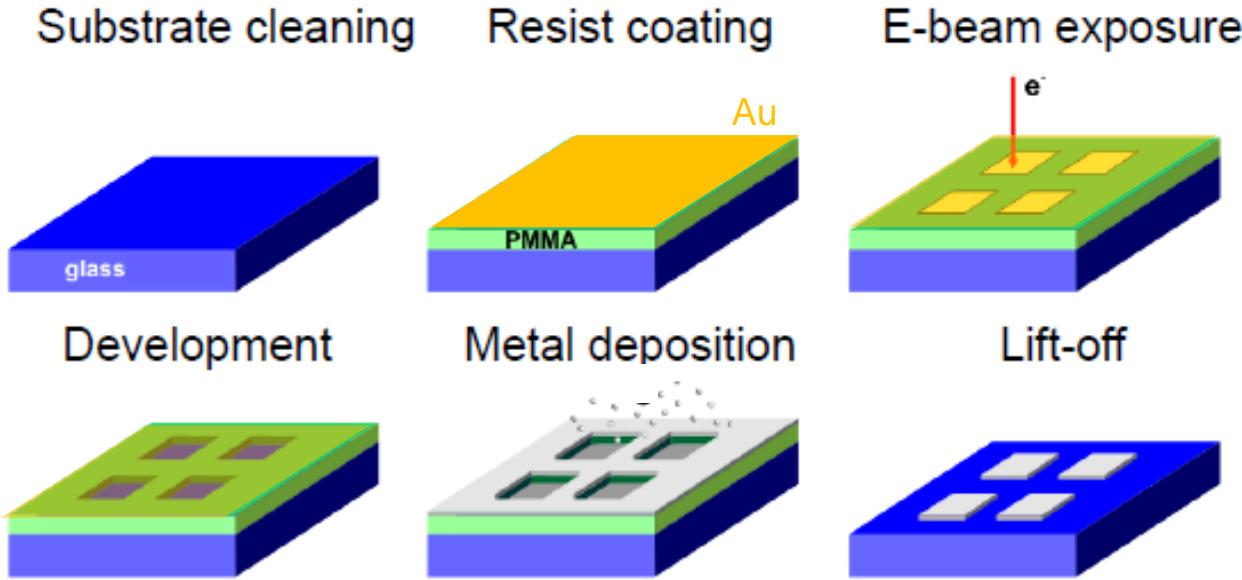
Adv. Mater. 19, 4297 (2007)

- Large areas
- Disordered distribution
- Insulating substrates
- Low concentration to avoid interactions

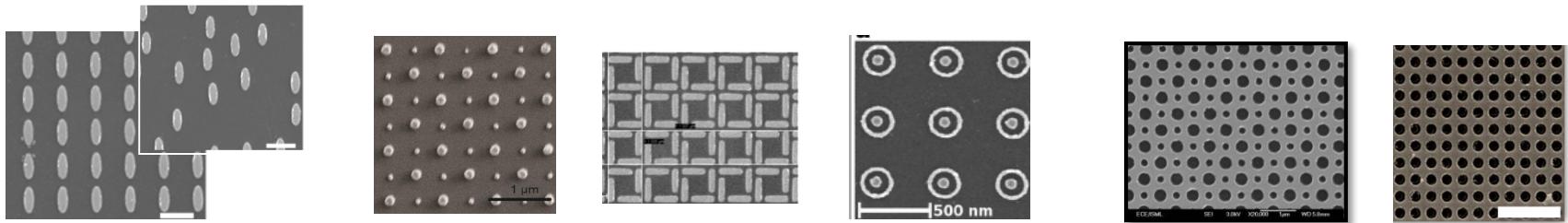
Chalmers



## E-beam lithography on glass



Arrays written with a write field of 50 micron x 50 micron.



**nanoGUNE – Aalto – Stockholm – Singapore**

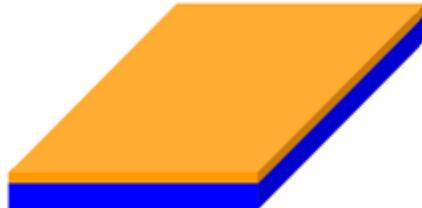


## Negative e-beam lithography on glass

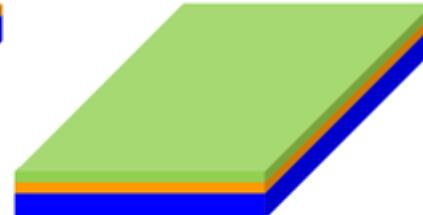
Substrate cleaning



Film growth



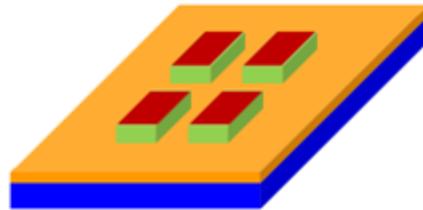
Resist coating



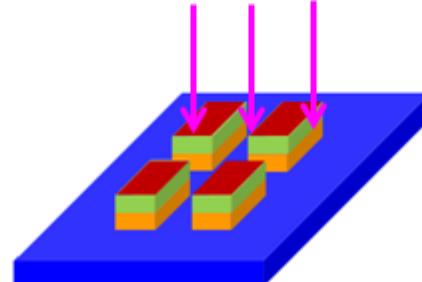
E-beam exposure



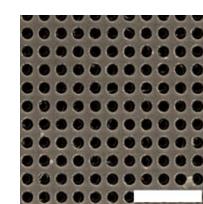
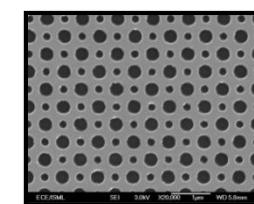
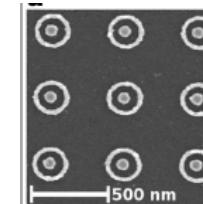
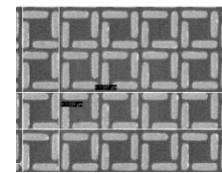
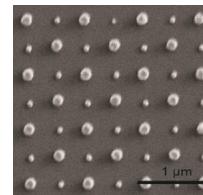
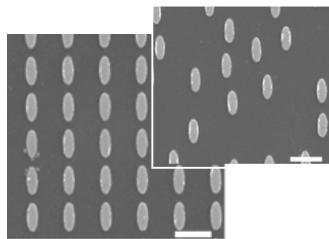
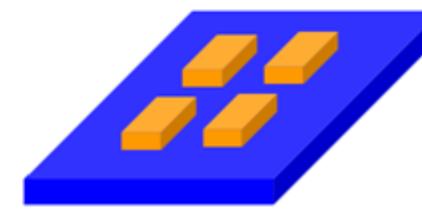
Development



Ion-milling



Lift-off



**nanoGUNE – Aalto – Stockholm – Singapore**



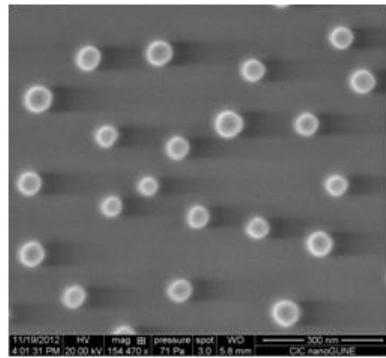
# Ni nanoantennas

## Hole-Mask Colloidal Lithography (Ni disks on glass)

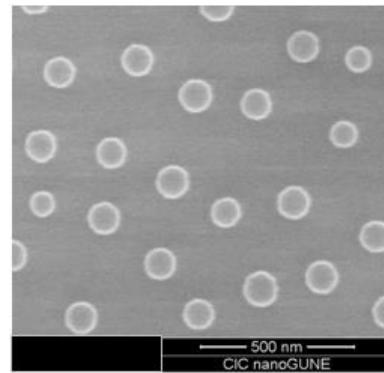
Adv. Mater. 19, 4297 (2007)



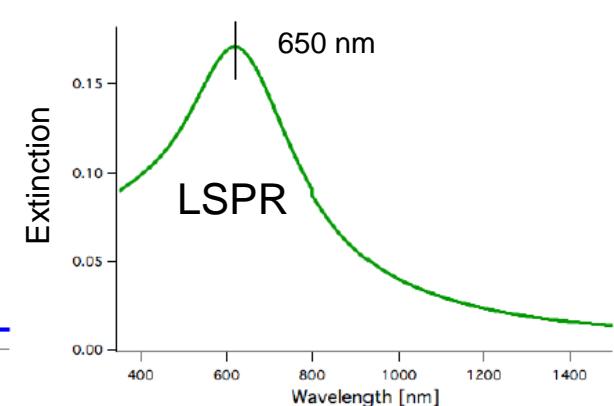
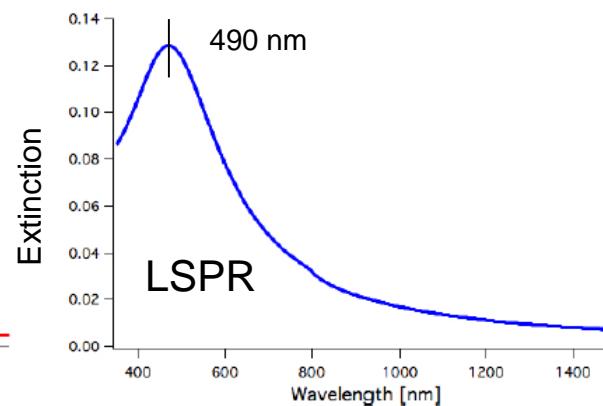
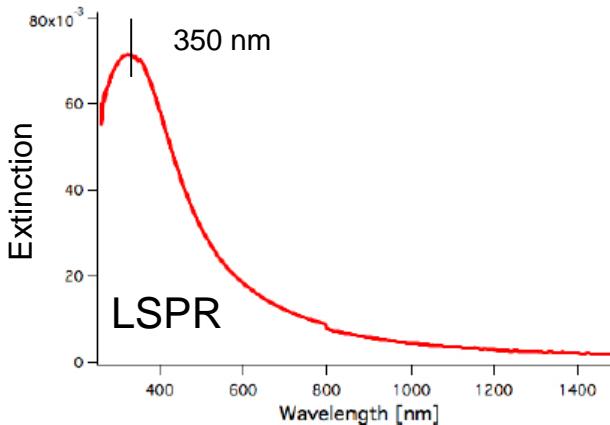
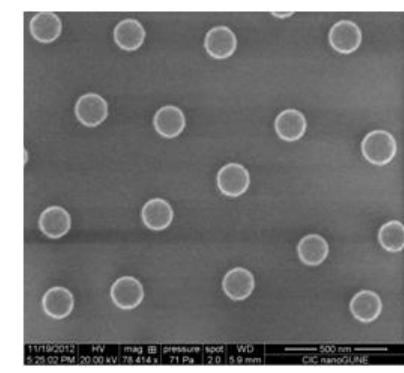
Disks 60x30 nm



Disks 100x30 nm

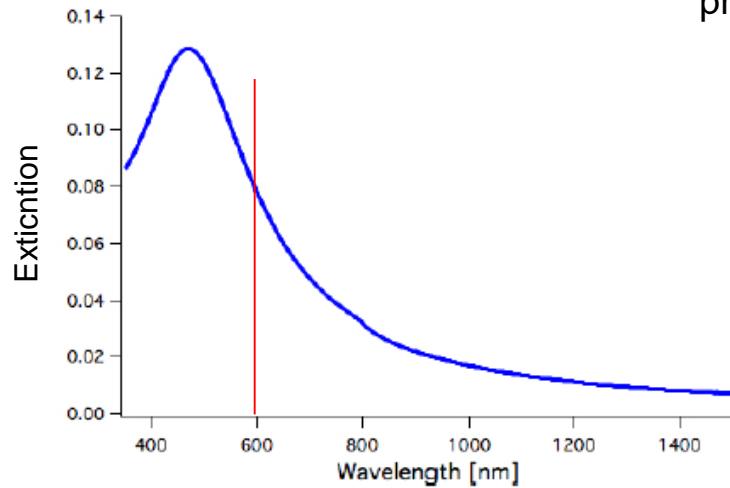
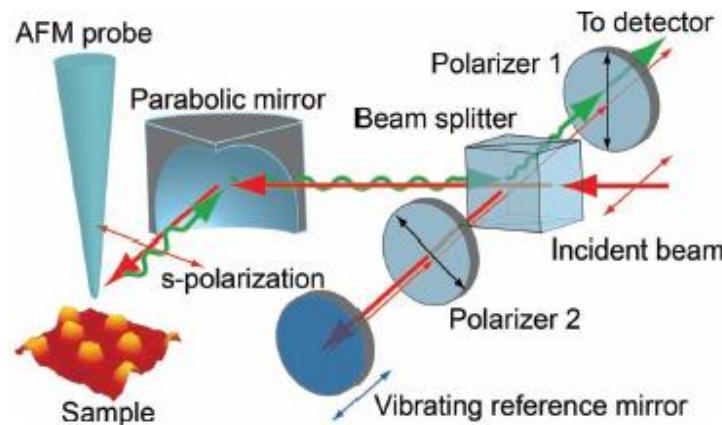


Disks 160x30 nm

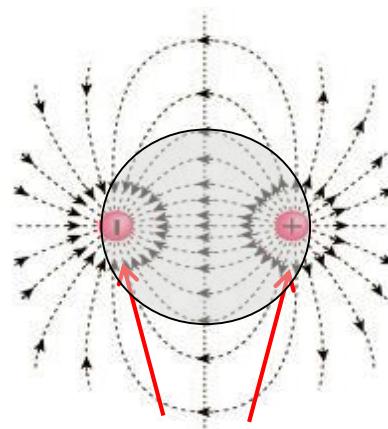




## Is the effect due to a LSPR?

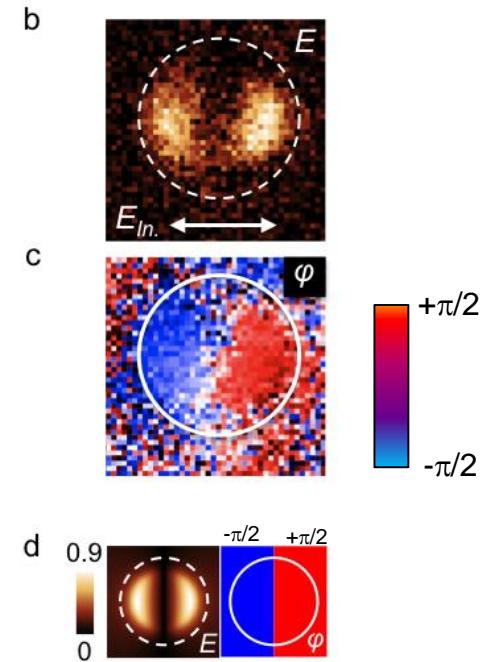


In the NF, electric field is like the one produced by a static electric dipole



Intense E fields of opposite sign  
( $\pi$  out of phase)

Scanning Near-Field Optical (SNOM)  
microscopy: amplitude and phase!

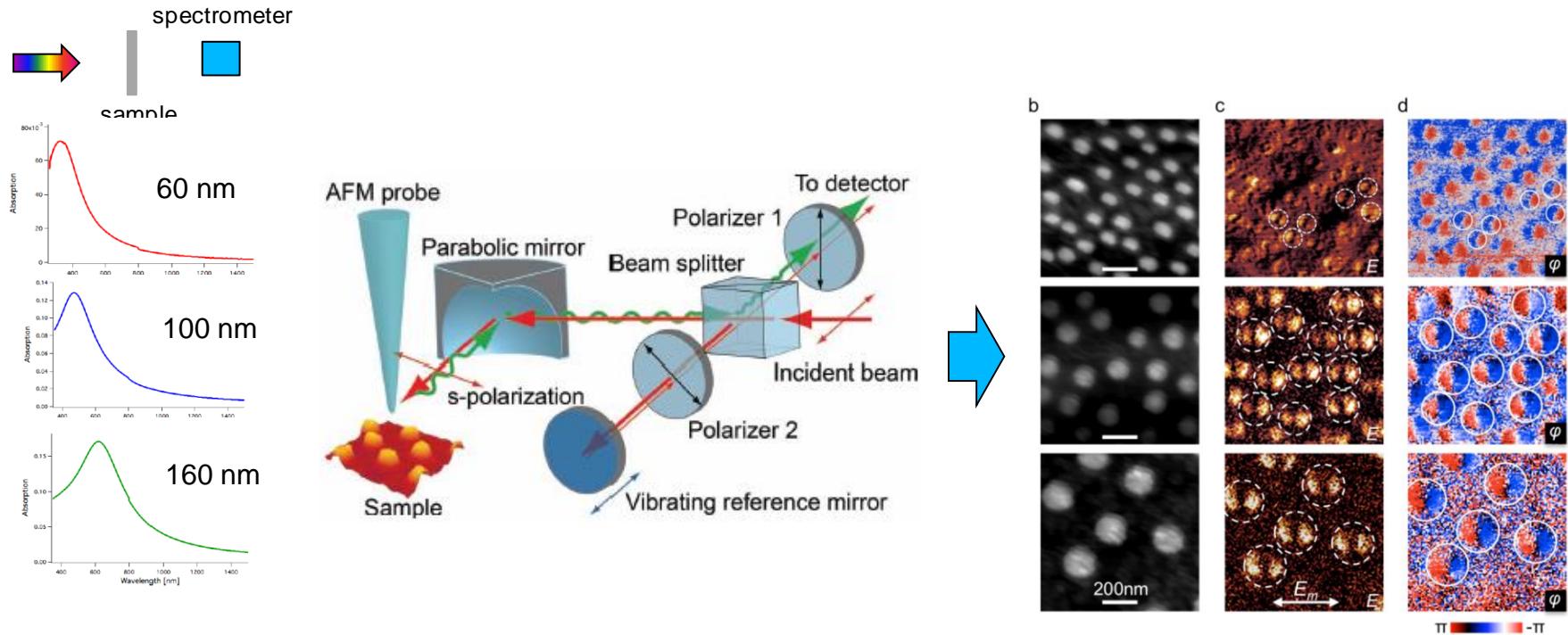


Small 7, 2341 (2011)



# A real LSPR?

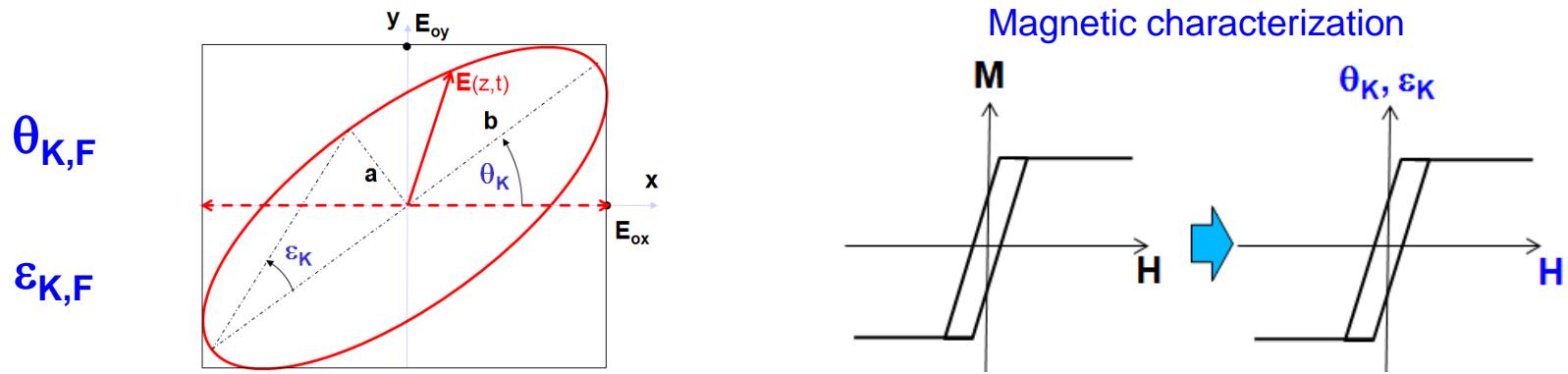
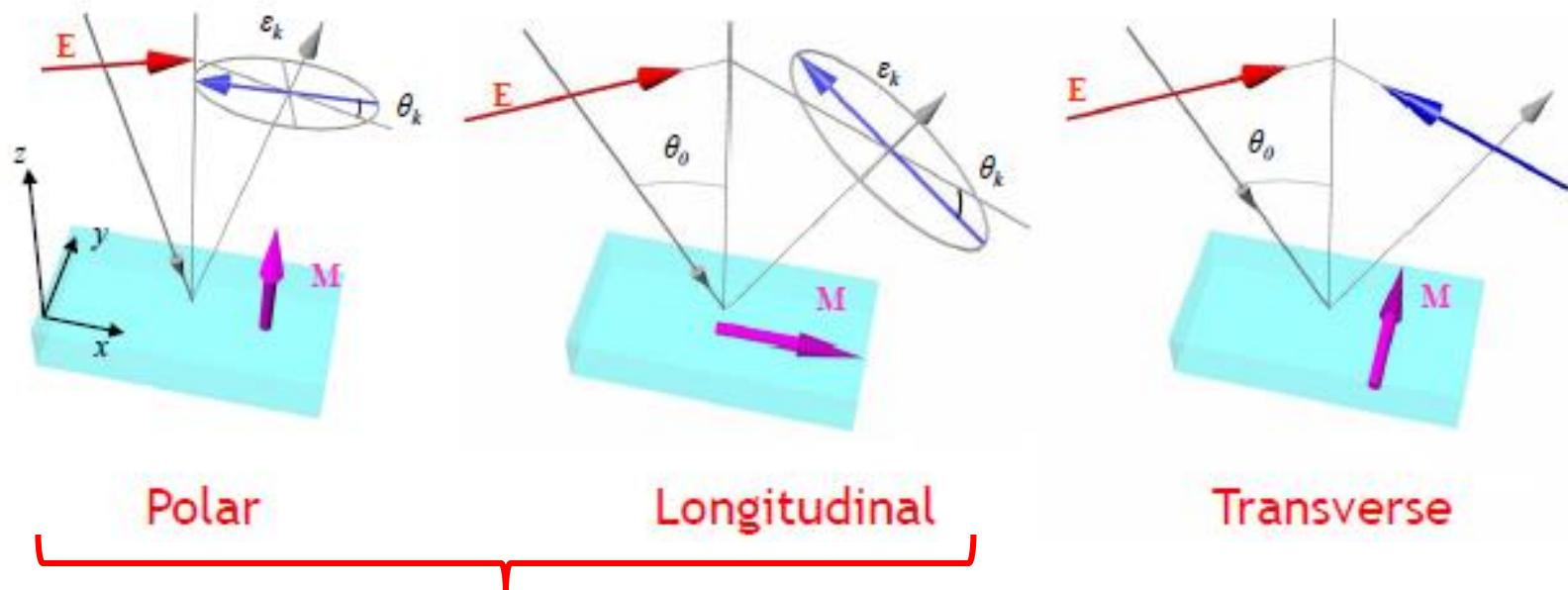
Scanning Near-Field Optical (SNOM) microscopy: amplitude and phase!



Small 7, 2341 (2011)



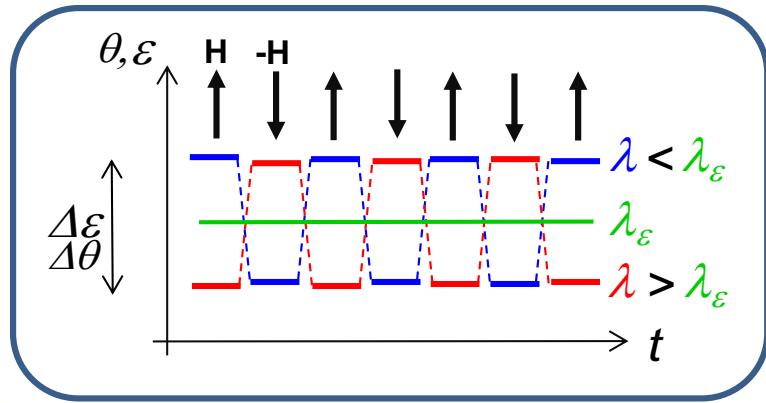
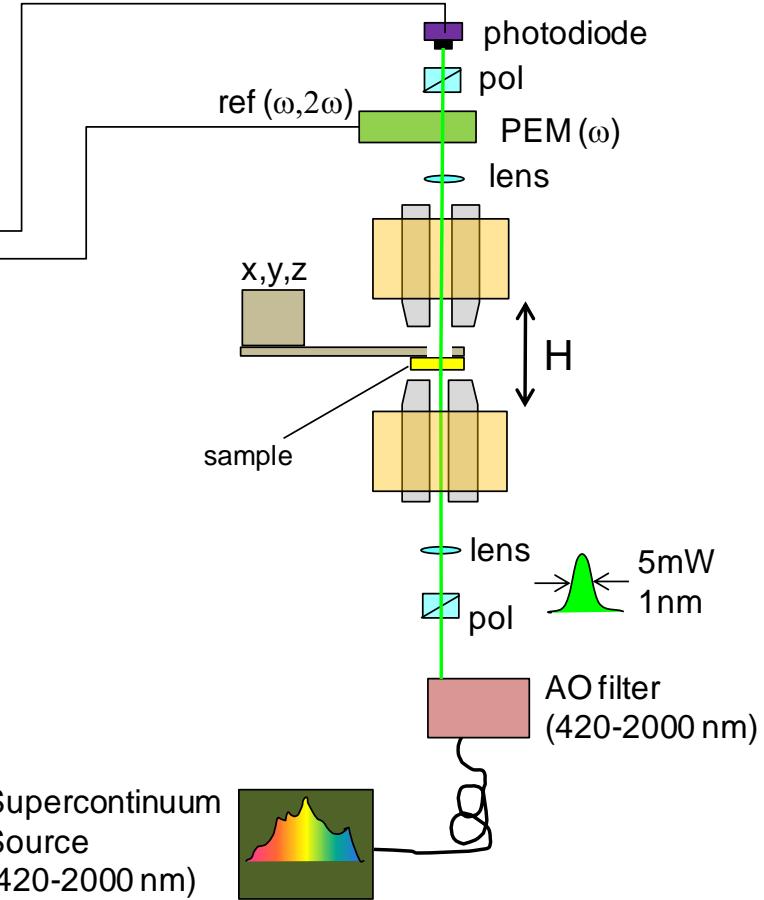
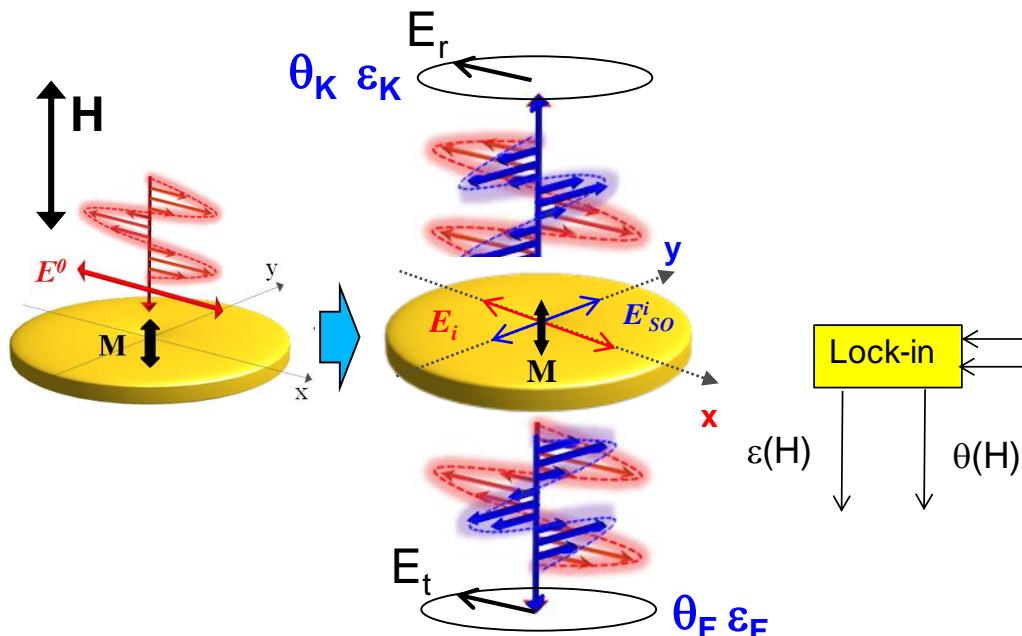
# Magneto-Optical Kerr effect configurations



P. Vavassori, APL 77, 1605 (2000)

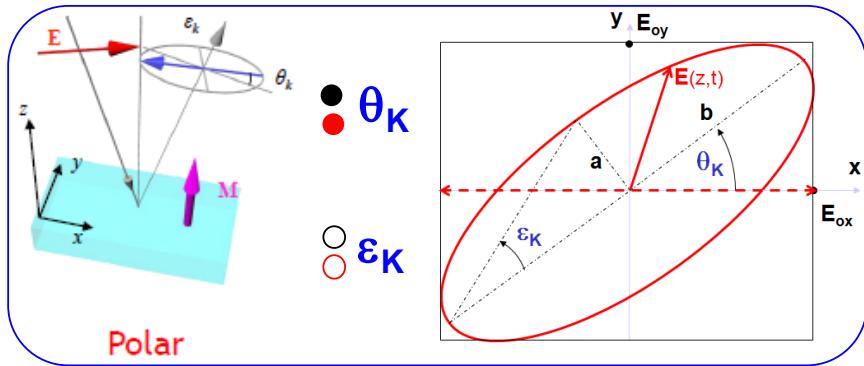


# Spectroscopic Polar MOKE



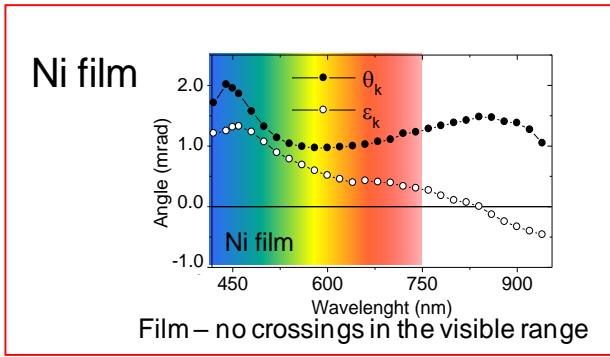


# Polar MOKE spectra: polarization of reflected light linked to the LSPR position

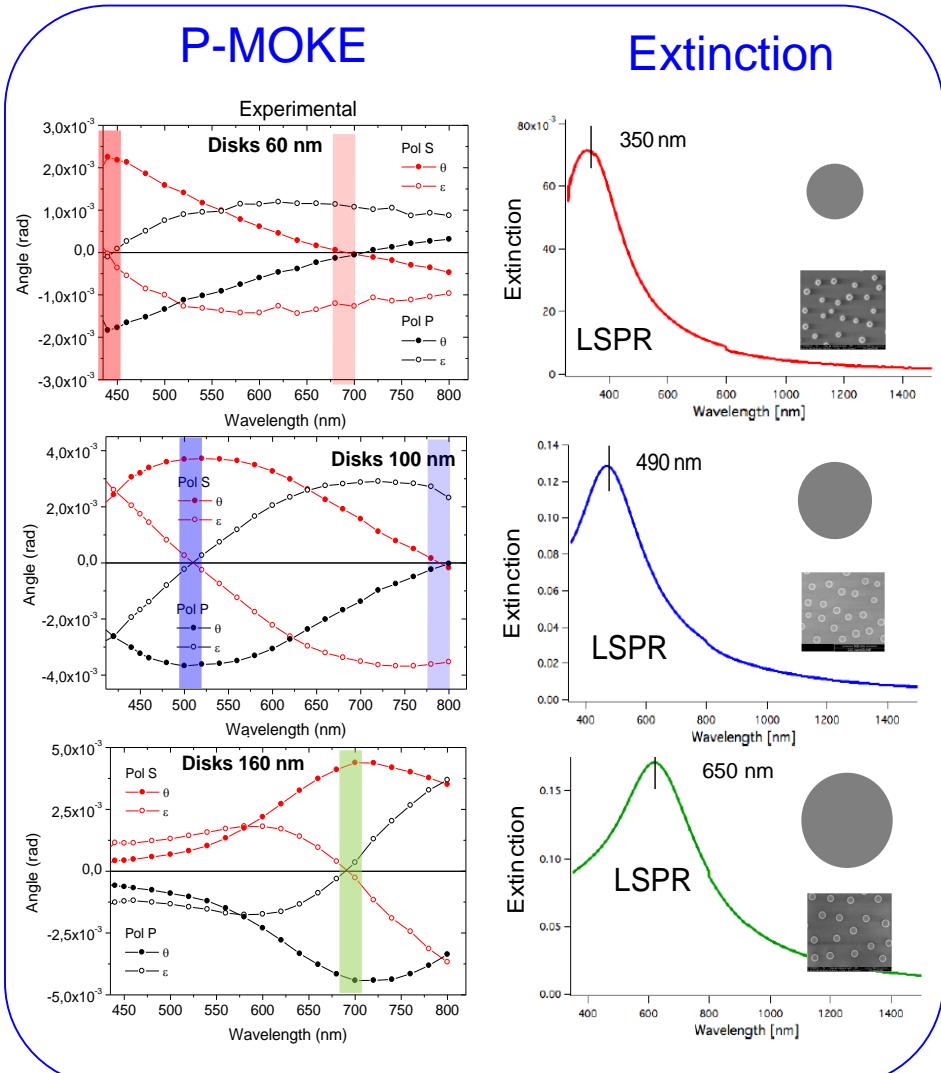


P. Vavassori, Appl. Phys. Lett. **77**, 1605 (2000)

## Refence Ni film



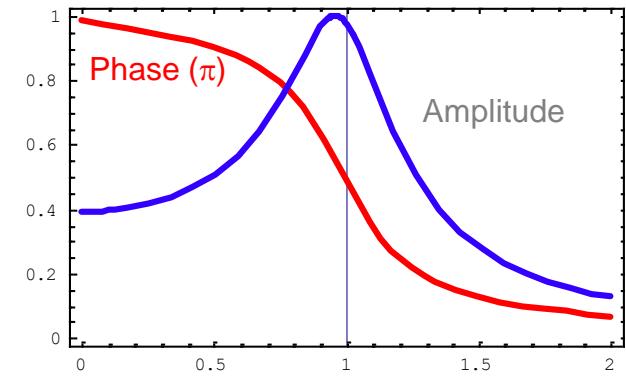
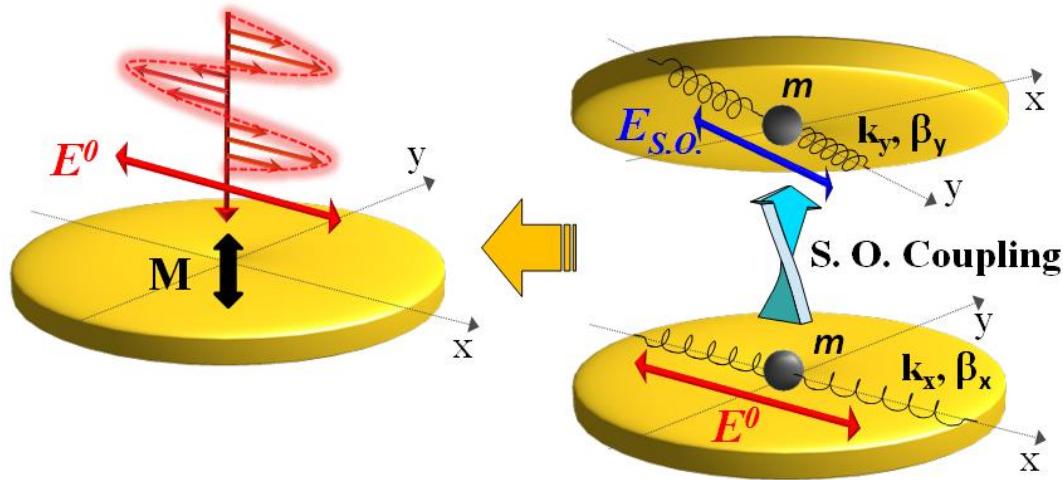
➤ Maximum of  $\theta_K$  and crossing of  $\epsilon_K$  follow the LSPR position



Phys. Rev. Lett. **111**, 167401 (2013)



## Simple physical picture: two coupled damped harmonic oscillators!!!



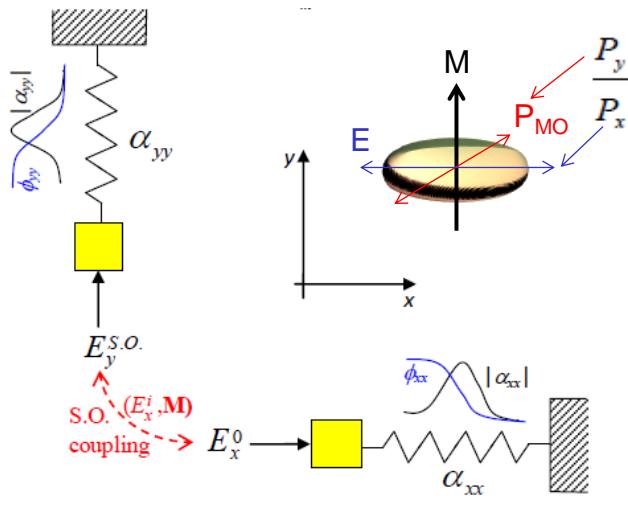
Damped harmonic oscillator  
Phase contribution

- Damped H.O.: confinement
- S.O. coupling: material property

Fundamental hypothesis here: linear and perturbative regime



# Induced electric dipoles



$$\frac{p_y}{p_x} = \frac{\epsilon_{yx} \alpha_{yy}}{(\epsilon - \epsilon_m)^2}$$

Gives the polarization of the far-field radiated in the z-direction by these two mutually orthogonal oscillating electric dipoles

- MO enhancement depends only on  $\alpha_{yy}$  (shape can improve enhancement)
- Relative phase on both  $\alpha_{yy}$  and  $\epsilon_{yx}$

## 1. Oscillator along x

$$p_x = \chi_{xx} E_x^i = (\epsilon - \epsilon_m) E_x^i \quad p_x = \alpha_{xx} E^0$$

$$E_x^i = E^0 - E_x^d$$

## 2. S.O. Coupling

S.O. coupling induces an electric dipole  $P_y^{S.O.}$ .  
Neglecting the y-confinement for now ( $E_y^d = 0$ ) and since  $E_y^{ext} = E_y^0 = 0$

$$p_y^{S.O.} = \chi_{yx} E_x^i = \epsilon_{yx} E_x^i$$

$$E_y^{S.O.} = p_y^{S.O.}/\chi_{yy} = p_y^{S.O.}/(\epsilon - \epsilon_m)$$

## 3. Oscillator along y

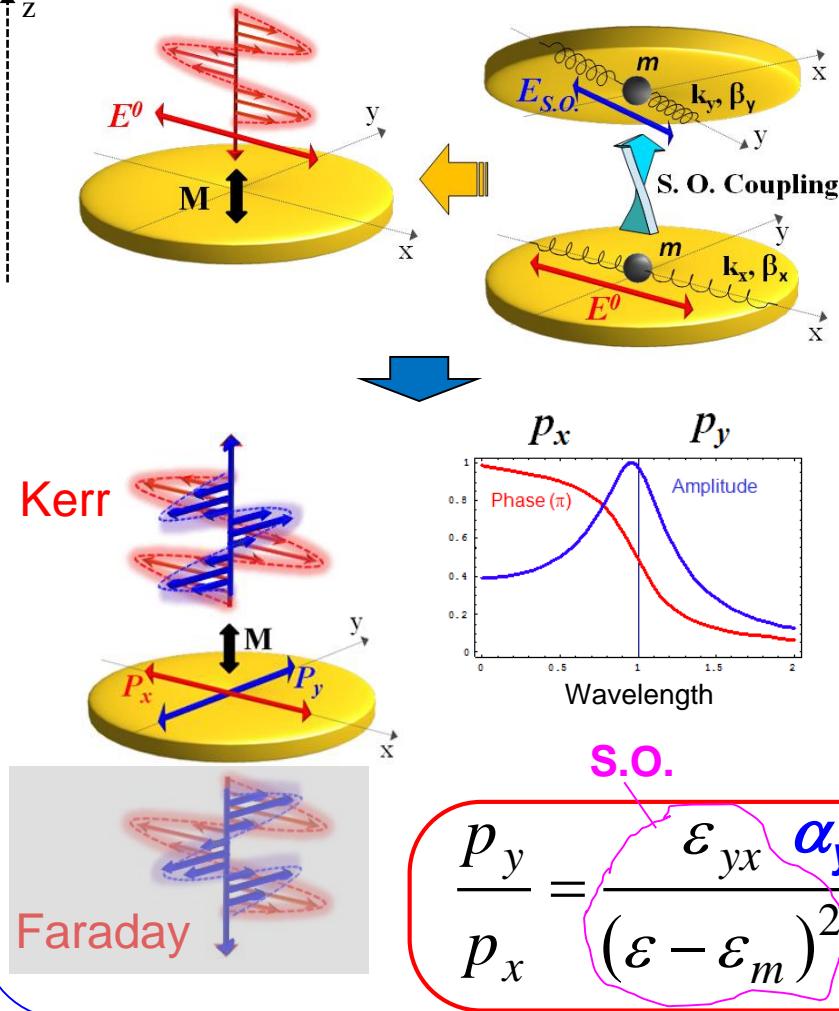
Now introducing the lateral confinement along y.

$$p_y = \alpha_{yy} E_y^{S.O.} = E_x^i (\alpha_{yy} \epsilon_{yx}) / (\epsilon - \epsilon_m)$$



## Simple physical picture: two S.O. coupled damped harmonic oscillators: relative phase

- Damped H.O.: confinement
- S.O. coupling: material property



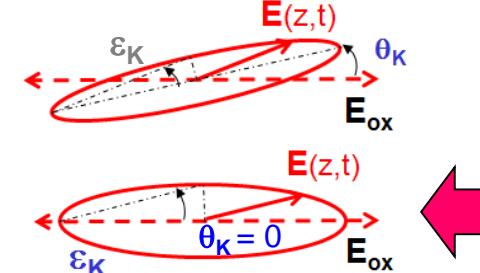
Polarization of the radiated field  $\mathbf{E}(z, t)$

$$\Delta\phi = \phi\left[\frac{\tilde{p}_y}{\tilde{p}_x}\right] = \phi[\tilde{p}_y] - \phi[\tilde{p}_x] =$$

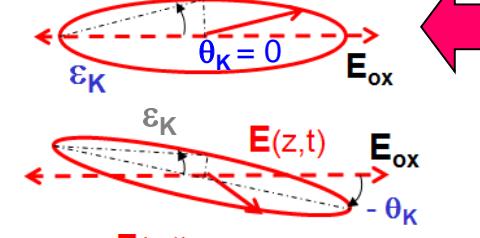
$$= \phi\left[\frac{\epsilon_{yx}}{(\epsilon - \epsilon_m)^2}\right] + \phi[\alpha_{yy}]$$



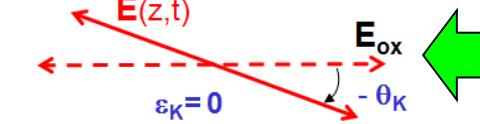
$0 < \Delta\phi < \pi/2$



$\Delta\phi = \pi/2$



$\pi/2 < \Delta\phi < \pi$



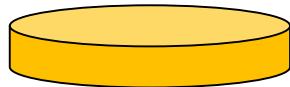
$\Delta\phi = \pi$

Phys. Rev. Lett. 111, 167401 (2013)

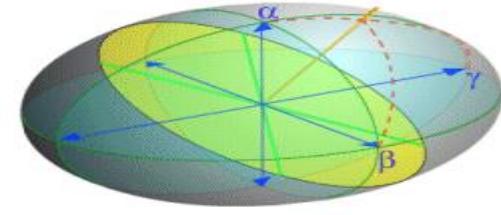


## Depolarizing field is the key

Cylindrical disk



Oblate ellipsoid



Internal field

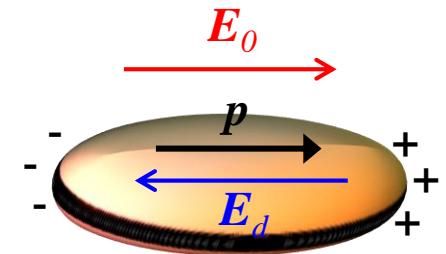
Embedding medium

$$\mathbf{p} = (\tilde{\epsilon} - \epsilon_m) \mathbf{E}_i ;$$

External field

$$\mathbf{E}_i = \mathbf{E}_0 + \mathbf{E}_d$$

Depolarizing field



N. Maccaferri et al., Opt. Express 21, 9875-89 (2013)



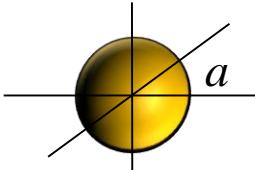
## Internal and depolarizing fields: quasi static approx

Static depolarization: the sphere case

$$E_d = -\frac{1}{\epsilon_m} L p \quad L = \frac{1}{3}$$

$$p = \frac{3\epsilon_m(\tilde{\epsilon} - \epsilon_m)}{(\tilde{\epsilon} + 2\epsilon_m)} E_0$$

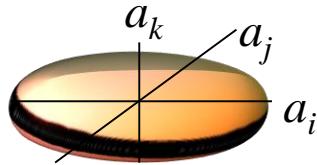
Clausius-Mossotti



$$p = (\tilde{\epsilon} - \epsilon_m) E_i \quad E_i = \mathbf{E}_0 + \mathbf{E}_d$$

$$p = \tilde{\alpha} E_0$$

$$P = \frac{3V\epsilon_m(\tilde{\epsilon} - \epsilon_m)}{(\tilde{\epsilon} + 2\epsilon_m)} E_0 = \frac{4\pi a^3 \epsilon_m (\tilde{\epsilon} - \epsilon_m)}{(\tilde{\epsilon} + 2\epsilon_m)} E_0 = \alpha E_0$$



More in general, for an ellipsoid:

$$E_d = -\frac{1}{\epsilon_m} \tilde{N} p \quad \Rightarrow \quad \tilde{\alpha} = \frac{(\tilde{\epsilon} - \epsilon_m \tilde{I}) \epsilon_m \tilde{I}}{\epsilon_m \tilde{I} + \tilde{N} (\tilde{\epsilon} - \epsilon_m \tilde{I})}$$

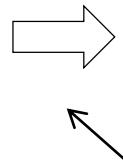
$$N_{ii} = L_i$$

$$L_i = \frac{a_i a_j a_k}{2} \int_0^\infty (q + a_i^2)^{-\frac{3}{2}} (q + a_j^2)^{-\frac{1}{2}} (q + a_k^2)^{-\frac{1}{2}} dq$$

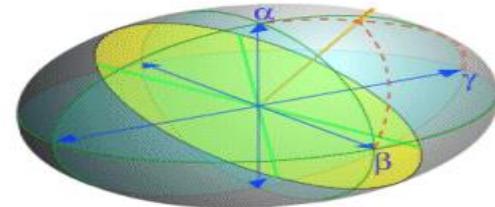


# Wavelength dependent corrections to polarizability: modified long-wavelength approximation (MLWA)

Cylindrical disk



Oblate ellipsoid



$$\mathbf{E}_d = \int d\mathbf{E}_d = \int \left( \frac{3\hat{\mathbf{u}}(\mathbf{P} \cdot \hat{\mathbf{u}}) - \mathbf{P}}{r^3} + i \frac{2\mathbf{P}}{3} k^3 + \frac{\hat{\mathbf{u}}(\mathbf{P} \cdot \hat{\mathbf{u}})}{2r} k^2 \right) dV$$

Static depolarization due to a uniform  $\mathbf{E}_0$  (shape of the nanoparticle)  $\rightarrow L_i$

Radiative reaction due to the recoil force (Abraham–Lorentz force) acting on an oscillating dipole emitting electromagnetic radiation

$k$  is the light wave vector modulus,  $r$  the distance from the center of the ellipsoid, and  $\hat{\mathbf{u}}$  a unit vector in the direction of  $r$ .

Dynamic depolarization arising from de-phasing of the radiation emitted by different points in the ellipsoid

$$\mathbf{E}_d = -\frac{1}{\epsilon_m} \tilde{N} \mathbf{p}$$

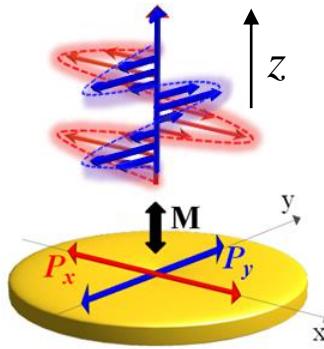
$$N_{ii} = L_i - \frac{Vk^2}{4\pi} D_i - i \frac{Vk^3}{6\pi}$$

$$D_i = \int_V \frac{x_i^2 + r^2}{r^2} dV \quad ; x_i = x, y, z$$

N. Maccaferri et al., Opt. Express **21**, 9875-89 (2013)



# It is a phase business

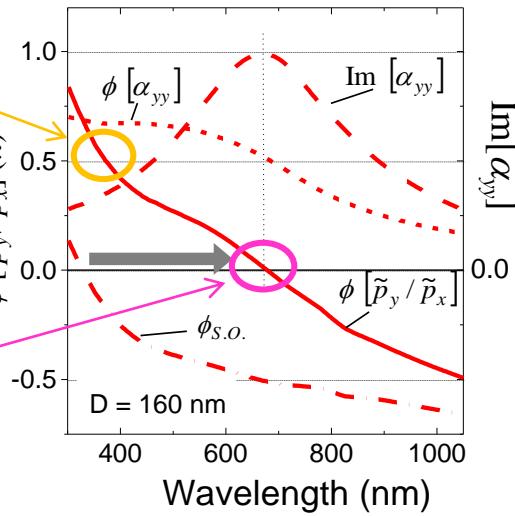
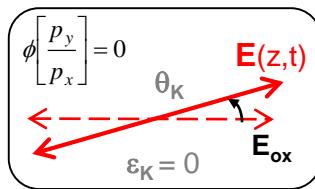
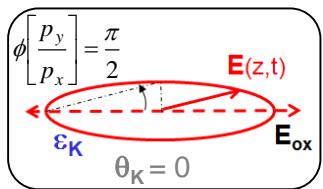


The polarization of the far-field radiated in the  $z$ -direction by these two mutually orthogonal oscillating electric dipoles is given by the ratio

$$\frac{\tilde{p}_y}{\tilde{p}_x} = \frac{\varepsilon_{yx}\alpha_{yy}}{(\varepsilon - \varepsilon_m)^2}$$

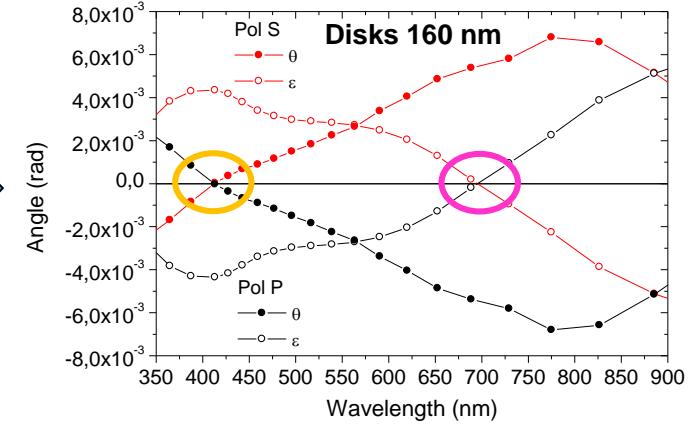
Phase difference between the two radiating dipoles  $p_x$  and  $p_y$

$$\Delta\phi = \phi\left[\frac{p_y}{p_x}\right] = \phi\left[\frac{\varepsilon_{yx}}{(\varepsilon - \varepsilon_m)^2}\right] + \phi[\alpha_{yy}] = \phi_{S.O.} + \phi_{\alpha_{yy}}$$



Kerr rotation and ellipticity spectra for an isolated nanostructure

$$\theta_K = Re[p_y/p_x] \text{ and } \varepsilon_K = Im[p_y/p_x].$$

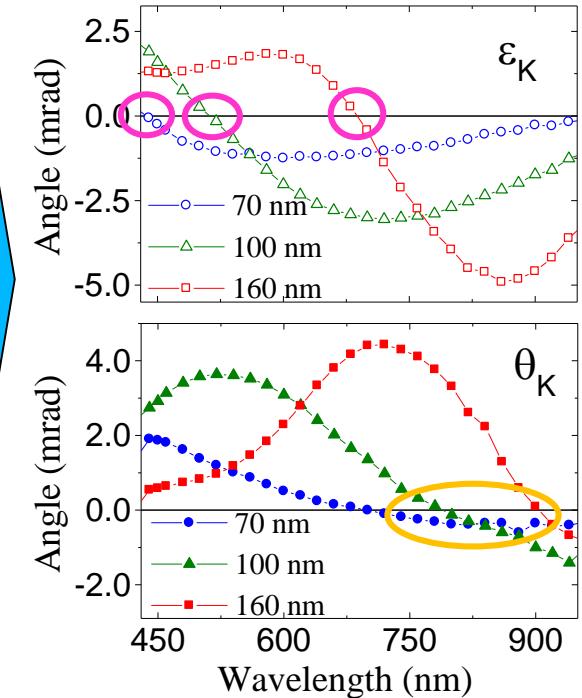
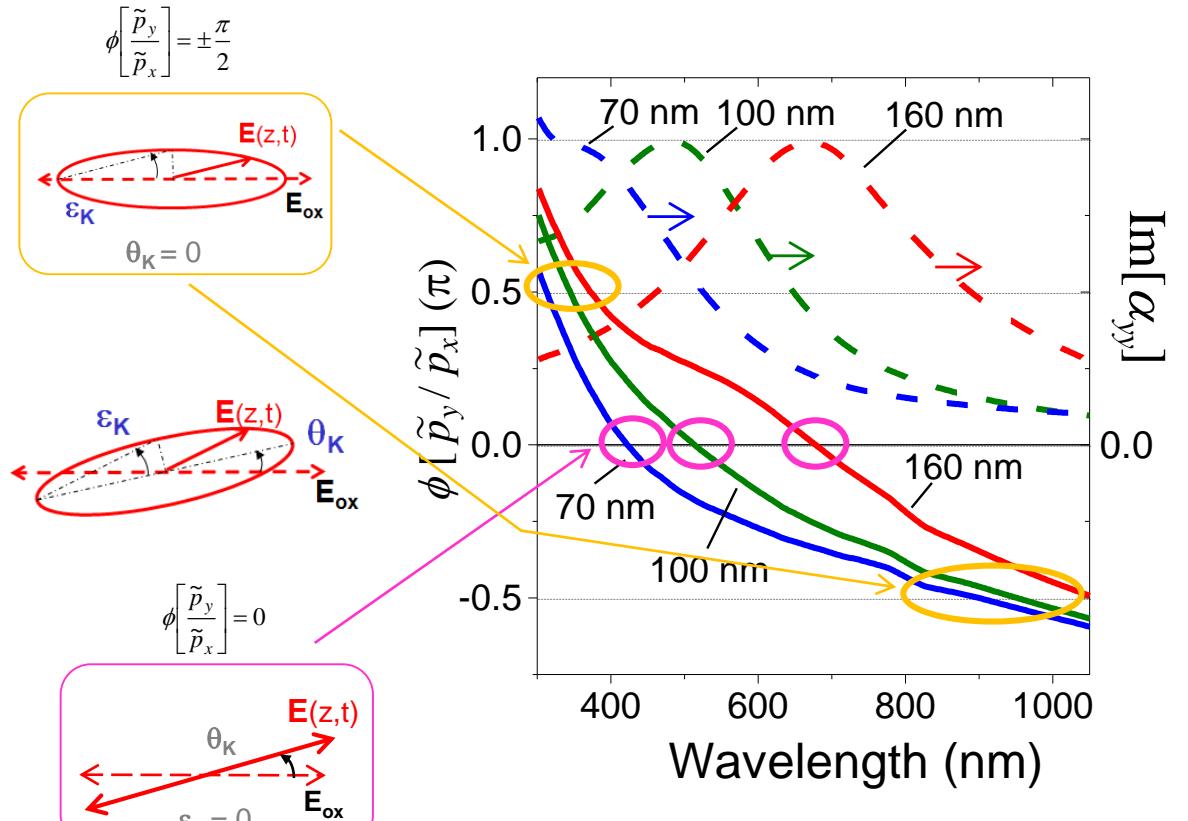


Phys. Rev. Lett. 111, 167401 (2013)



# It is a phase business

$$\frac{\tilde{p}_y}{\tilde{p}_x} = \frac{\varepsilon_{yx}\alpha_{yy}}{(\varepsilon - \varepsilon_m)^2} \quad \Rightarrow \quad \Delta\phi = \phi\left[\frac{\tilde{p}_y}{\tilde{p}_x}\right] = \phi\left[\frac{\varepsilon_{yx}}{(\varepsilon - \varepsilon_m)^2}\right] + \phi[\alpha_{yy}] = \phi_{S.O.} + \phi_{\alpha_{yy}}$$

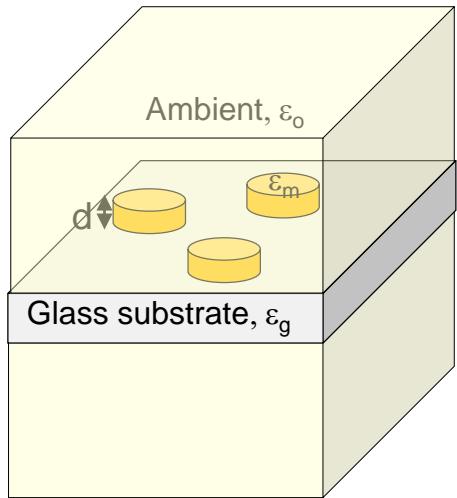


Phys. Rev. Lett. **111**, 167401 (2013)

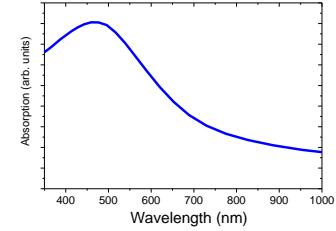
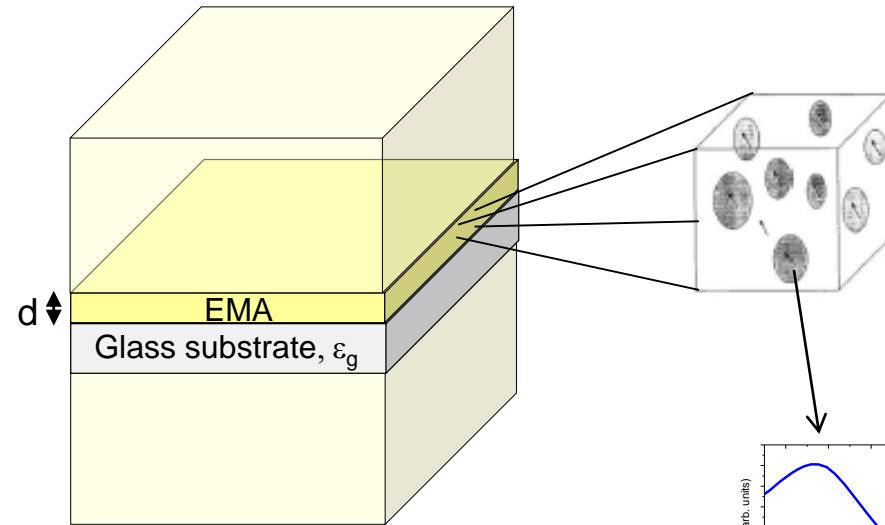


## Modeling the spectra

Our system



Model system

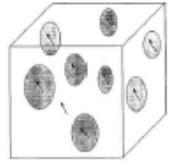




## Modeling the spectra: steps 2&3

### Step 2 (far-field)

Effective medium approximation (EMA)



$$\tilde{\epsilon}_{\text{eff}} = \tilde{\epsilon}_1 + f(\tilde{\epsilon}_2 - \tilde{\epsilon}_1) \left[ \tilde{\mathbf{1}} + (1-f) \left( \tilde{\mathbf{L}} - \frac{k^2 V}{4\pi} \tilde{\mathbf{D}} - \frac{ik^3 V}{6\pi} \tilde{\mathbf{1}} \right) (\tilde{\epsilon}_2 - \tilde{\epsilon}_1) \epsilon_1^{-1} \right]^{-1}$$

$$\Rightarrow R = \begin{pmatrix} r_{s \rightarrow s} & r_{p \rightarrow s} \\ r_{s \rightarrow p} & r_{p \rightarrow p} \end{pmatrix} \Rightarrow \theta_K \text{ Re} \left[ \frac{r_{sp}}{r_{pp}} \right] \text{ Re} \left[ \frac{r_{ps}}{r_{ss}} \right]$$

$$\epsilon_K \text{ Im} \left[ \frac{r_{sp}}{r_{pp}} \right] \text{ Im} \left[ \frac{r_{ps}}{r_{ss}} \right]$$

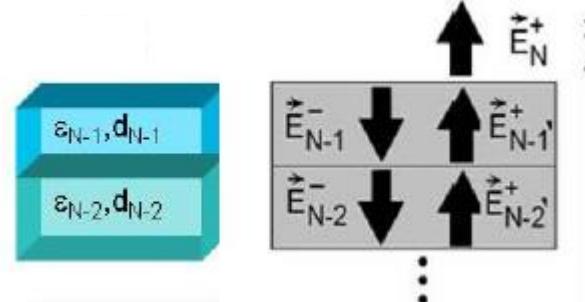
D. Stroud, Phys. Rev. **B 12** (8), 3368 (1975)

M. Abe, Phys. Rev. **B 53** (11), 7065 (1996)

M. Abe and T. Suwa, Phys. Rev. **B 70**, 235103 (2004)

Transfer matrix method  
(multilayers)

### Step 3 (far-field including substrate)



$$\Rightarrow R = \begin{pmatrix} r_{s \rightarrow s} & r_{p \rightarrow s} \\ r_{s \rightarrow p} & r_{p \rightarrow p} \end{pmatrix} \Rightarrow \theta_K \text{ Re} \left[ \frac{r_{sp}}{r_{pp}} \right] \text{ Re} \left[ \frac{r_{ps}}{r_{ss}} \right]$$

$$\epsilon_K \text{ Im} \left[ \frac{r_{sp}}{r_{pp}} \right] \text{ Im} \left[ \frac{r_{ps}}{r_{ss}} \right]$$

M. Schubert, T. E. Tiwald and J. A. Woollam, Applied Optics **38** (1), 177 (1999)

J. Zak, E. R. Mook, C. Liu and S. D. Bader, JMMM **89**, 107 (1990)

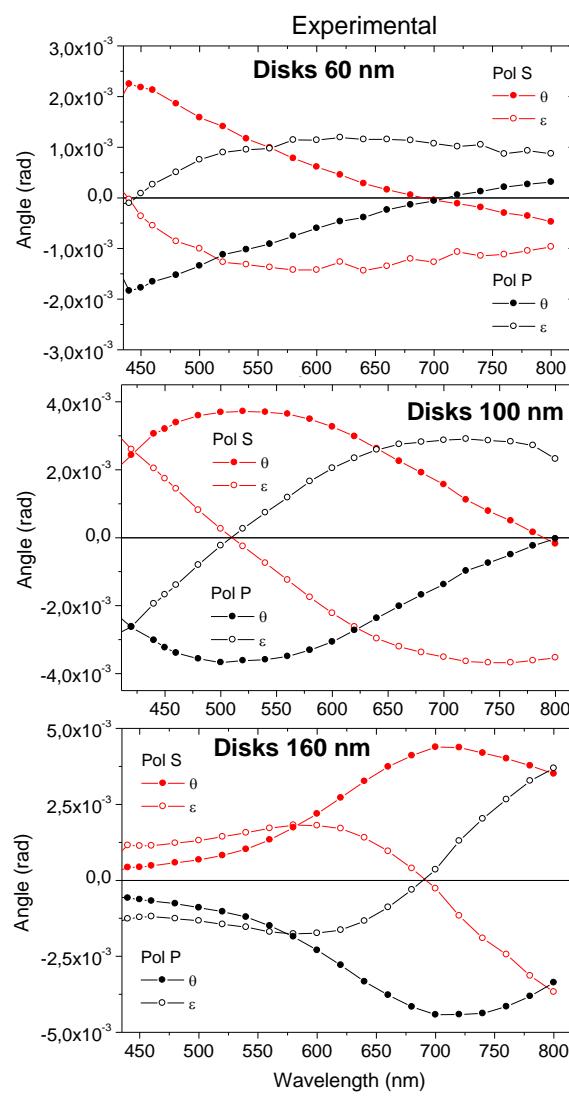
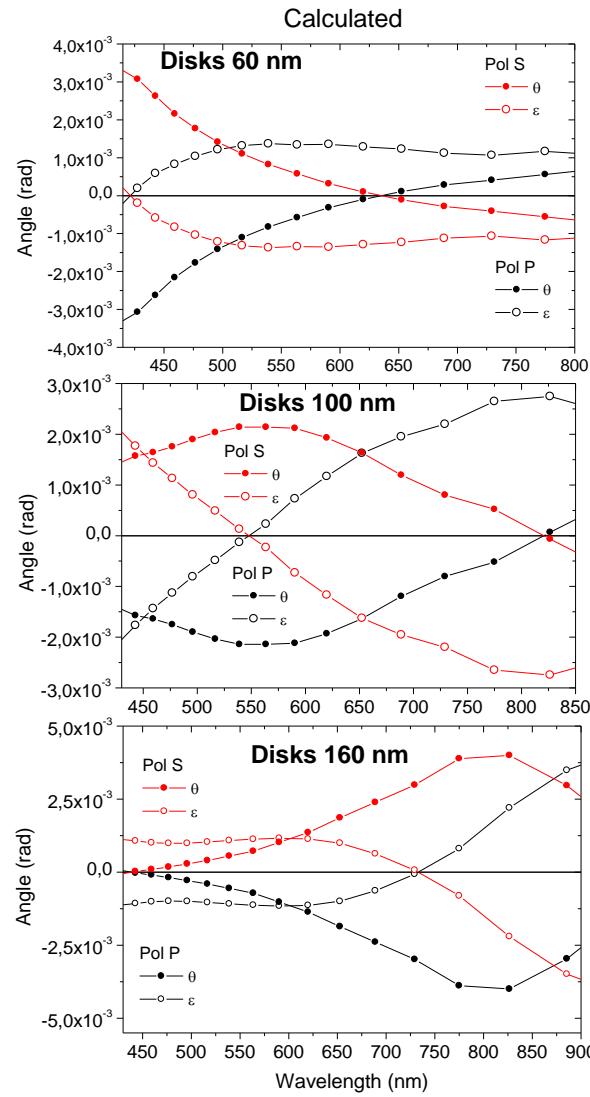
S. Visnovsky et al., Optics Express **9** (3), 121 (2001)

N. Maccaferri et al., Opt. Express **21**, 9875-89 (2013)

N. Maccaferri et al., Phys. Stat. Solidi (a) (2014)



# Response of an ensemble of such oscillators randomly distributed on a glass substrate (EMA)



Agreement between calculated and experimental spectra is almost perfect!

No adjustable parameters:  
tabulated optical and MO constants;  
sizes and nanoantennae density from SEM images

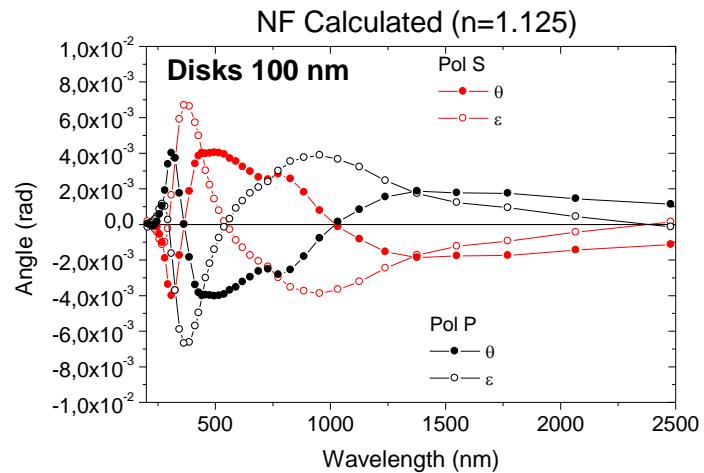
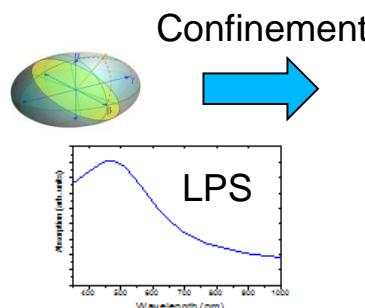
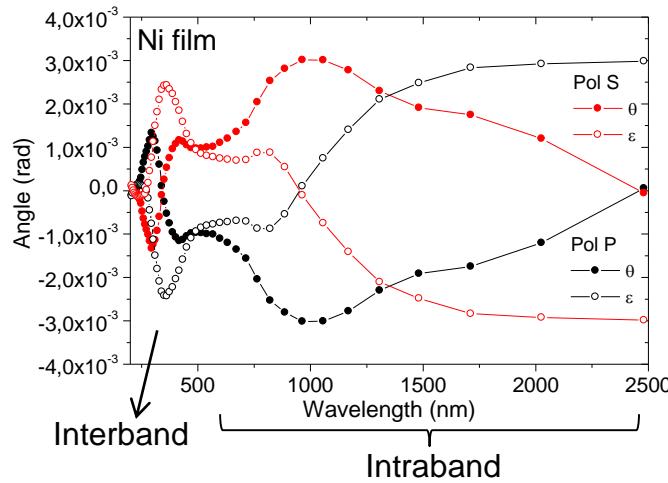
N. Maccaferri et al.,  
Opt. Express **21**, 9875-89 (2013)

Substrate plays a role

N. Maccaferri et al.,  
Phys. Status Solidi A **211**, 1067-75 (2014)



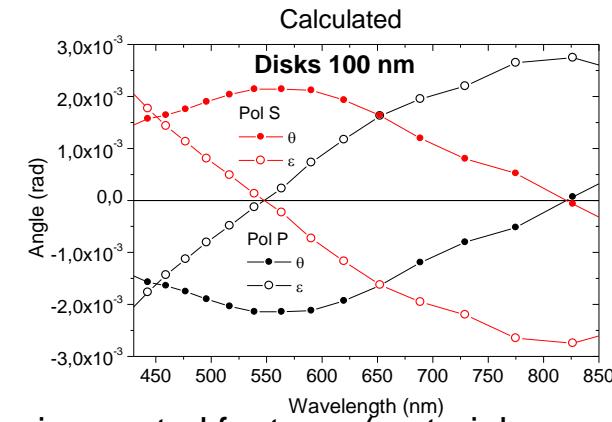
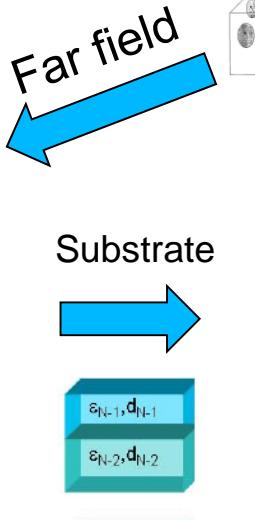
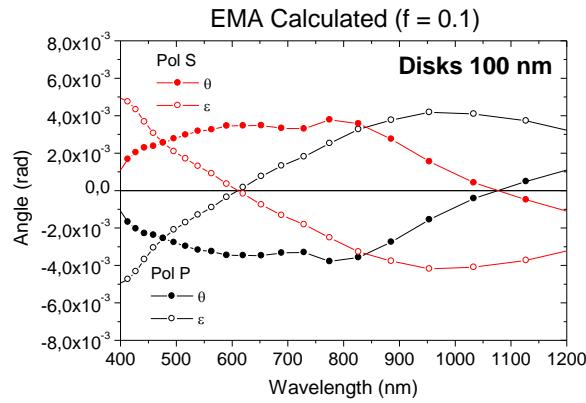
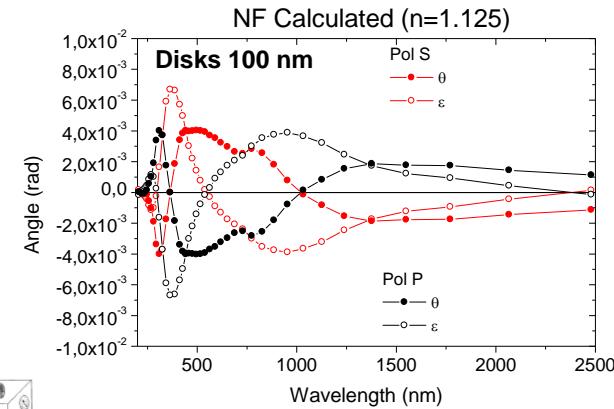
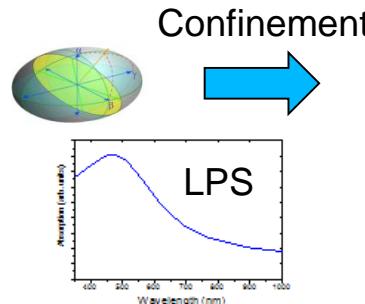
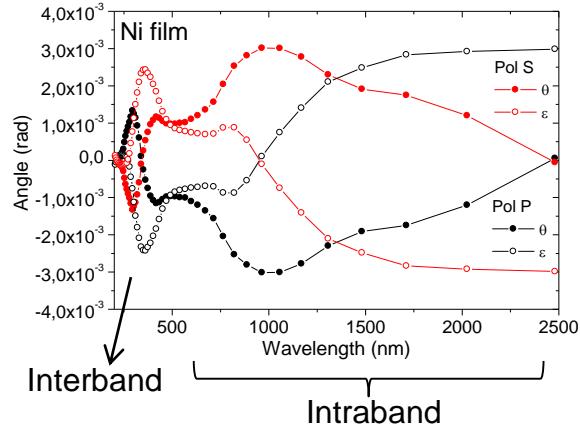
## Phase adjustment: spectral features redistribution



- Confinement (LSPR) – redistribution (blue shift) of the main spectral features due to intraband transitions (material properties,  $\theta$  and  $\epsilon$  linked via Kramers-Kronig relations)



## Let's have a look at the individual steps

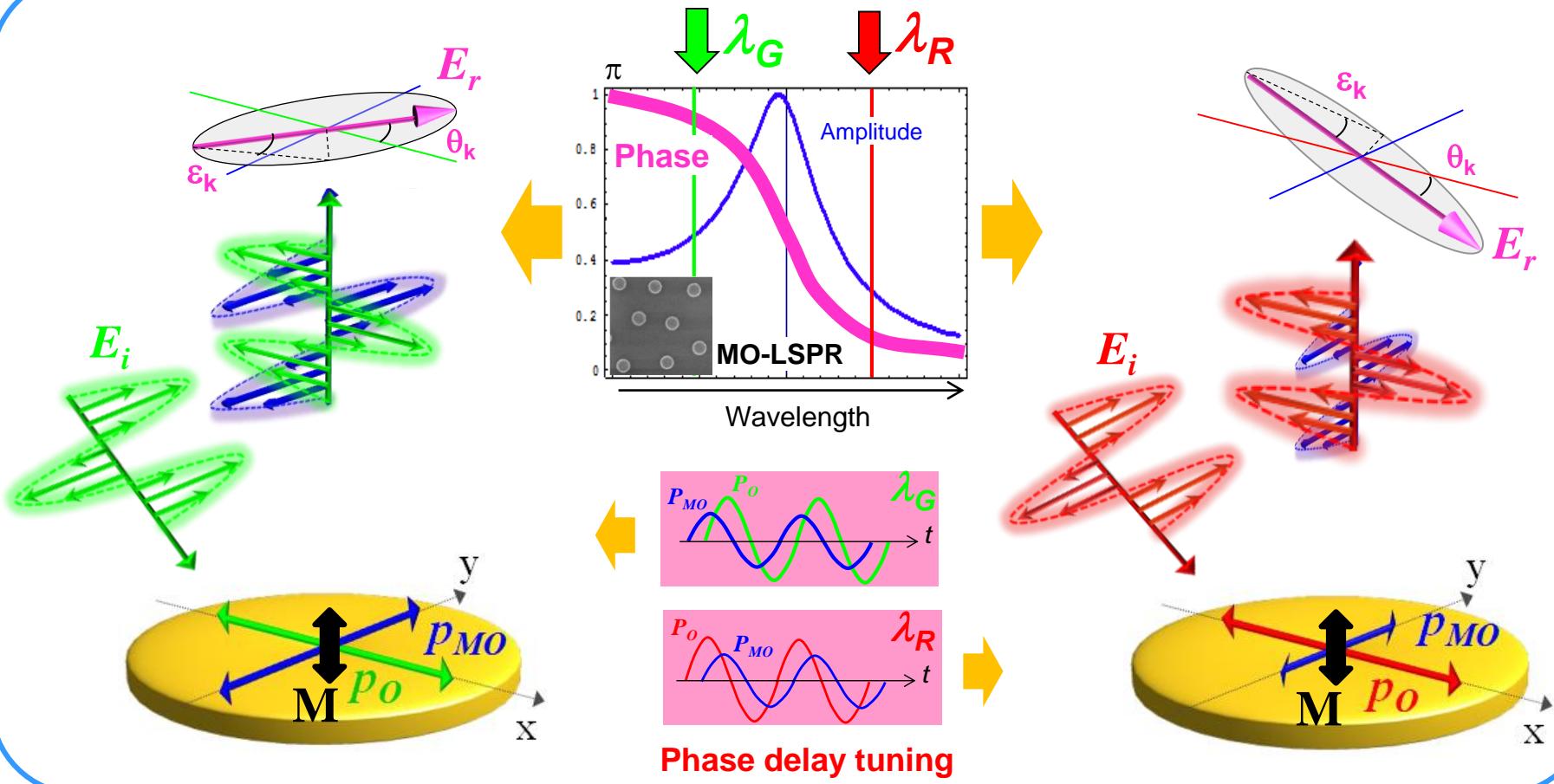


- Confinement (LSPR) – redistribution (**blue shift**) of the main spectral features (material properties,  $\theta$  and  $\epsilon$  linked via Kramers-Kronig relations)
- Substrate – reduction of MOKE contrast and slight additional **blue shift** of the spectral features

Phys. Rev. Lett. **111**, 167401 (2013); Phys. Status Solidi A **211**, 1067-75 (2014)



## Summary for an individual magnetic nano-antenna

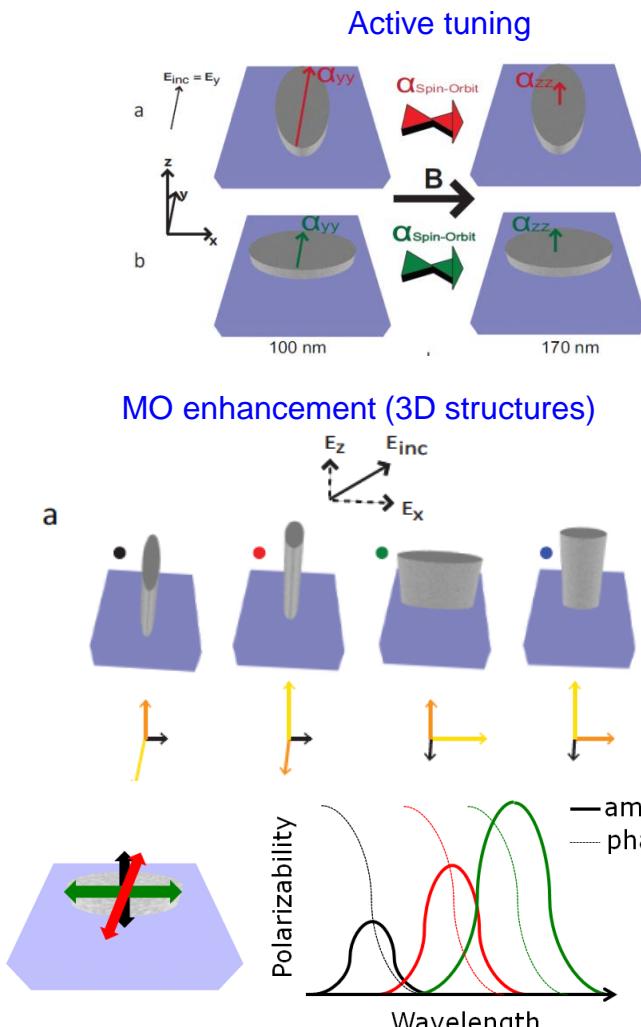


The concerted action of LSPRs and MO activity allows for the controlled manipulation of Kerr rotation/ellipticity of ferromagnetic nanostructures (beyond intrinsic material properties).

Phys. Rev. Lett. 111, 167401 (2013)



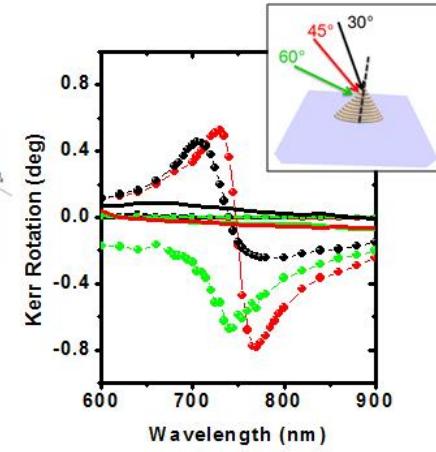
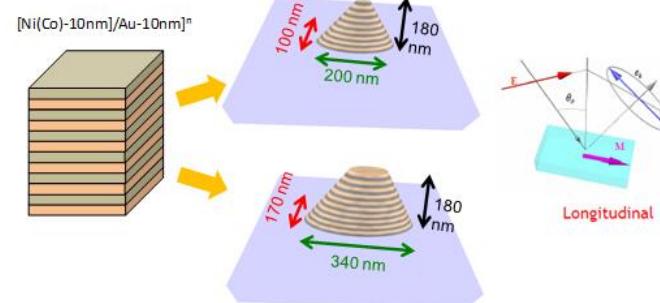
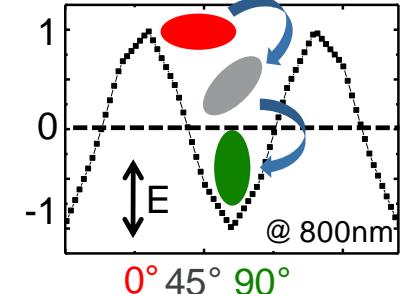
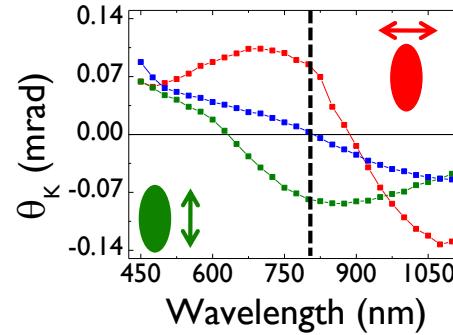
# Control of magneto-optics via magnetoplasmonic anisotropy



## Shape engineering

## L-MOKE

170/240 nm; t = 30 nm

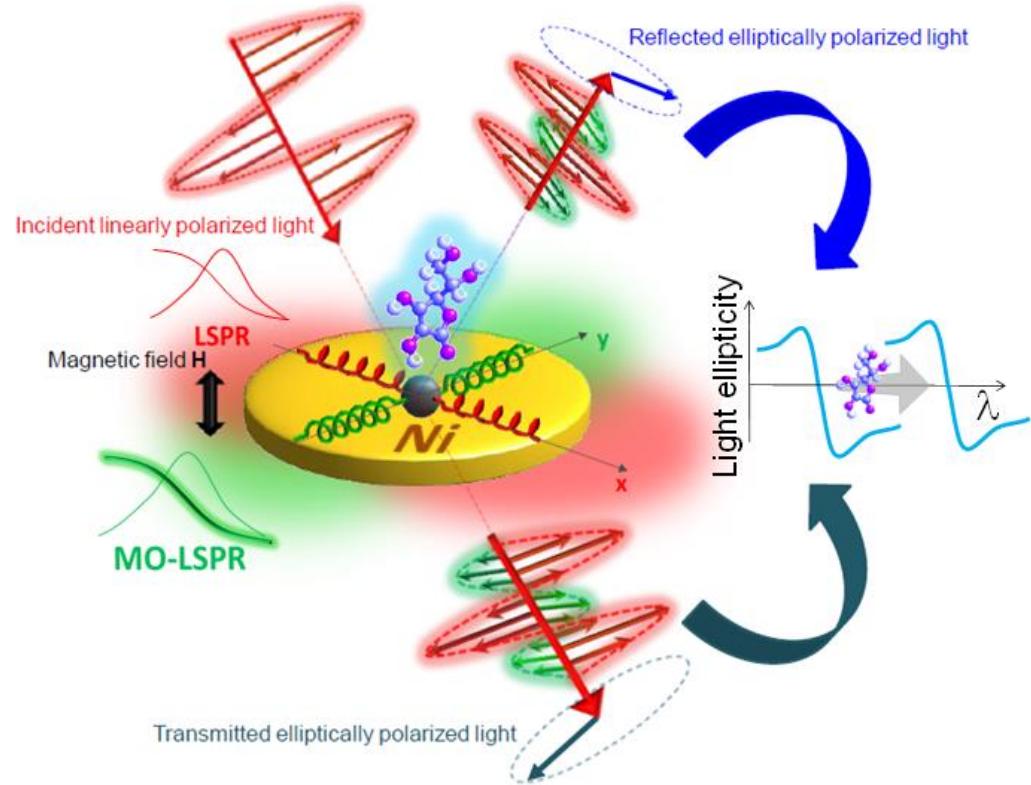
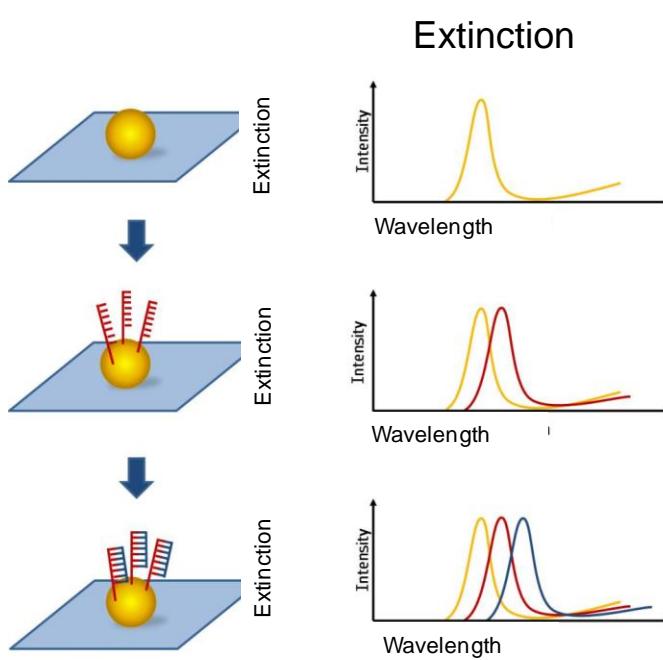


**"Magnetoplasmonic design rules for active magneto-optics"**  
Enhancement by a factor of 20

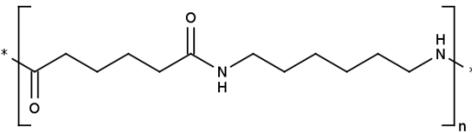
Nano Letters 14, 7207 (2014)



# LPRS phase-sensitivity in the reflected/transmitted light polarization



ALD deposition



Nylon 66 ( $n=1.51$ )

Min  $\Delta\lambda$  detectable  $\sim 0.5$  nm

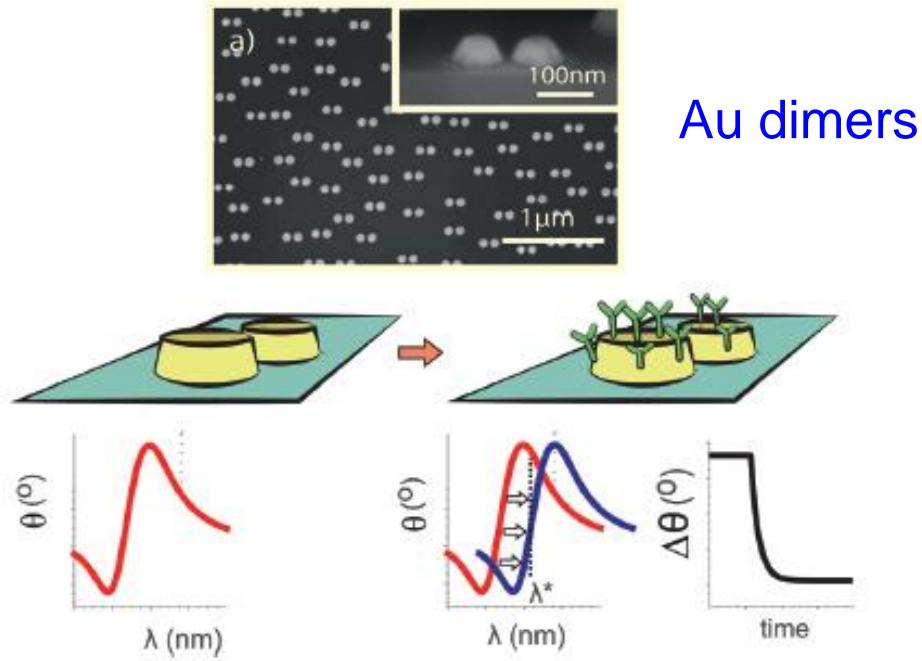
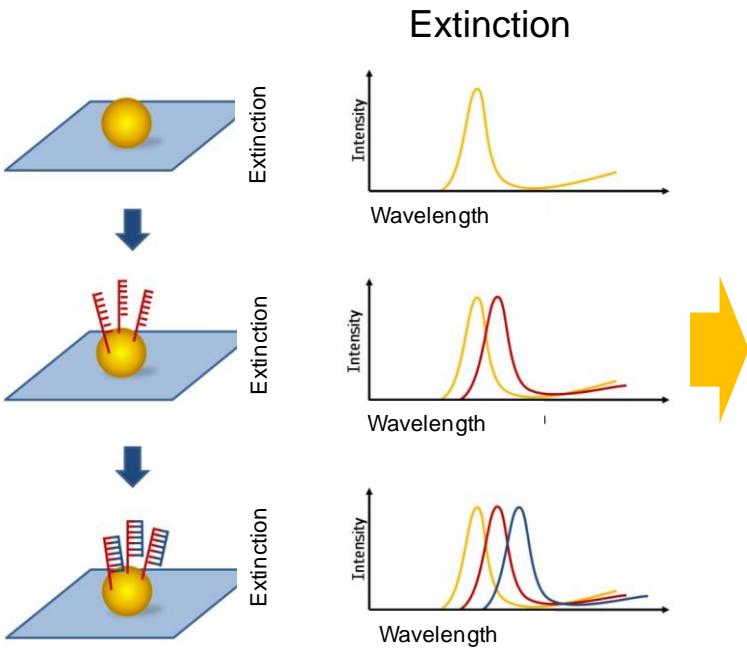
$$\Delta t_{Min} = \frac{1}{10} ML \text{ of PA-6.6}$$

N. Maccaferri et al., Nature Commun. 6, 6150 (2015)

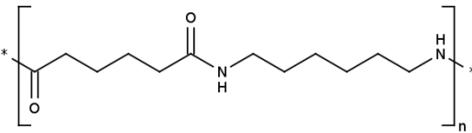


# LPRS phase-sensitivity in the reflected/transmitted light polarization

R. Verre et al. Nanoscale 8, 10576 (2016)



ALD deposition



Nylon 66 ( $n = 1.51$ )

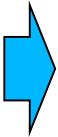
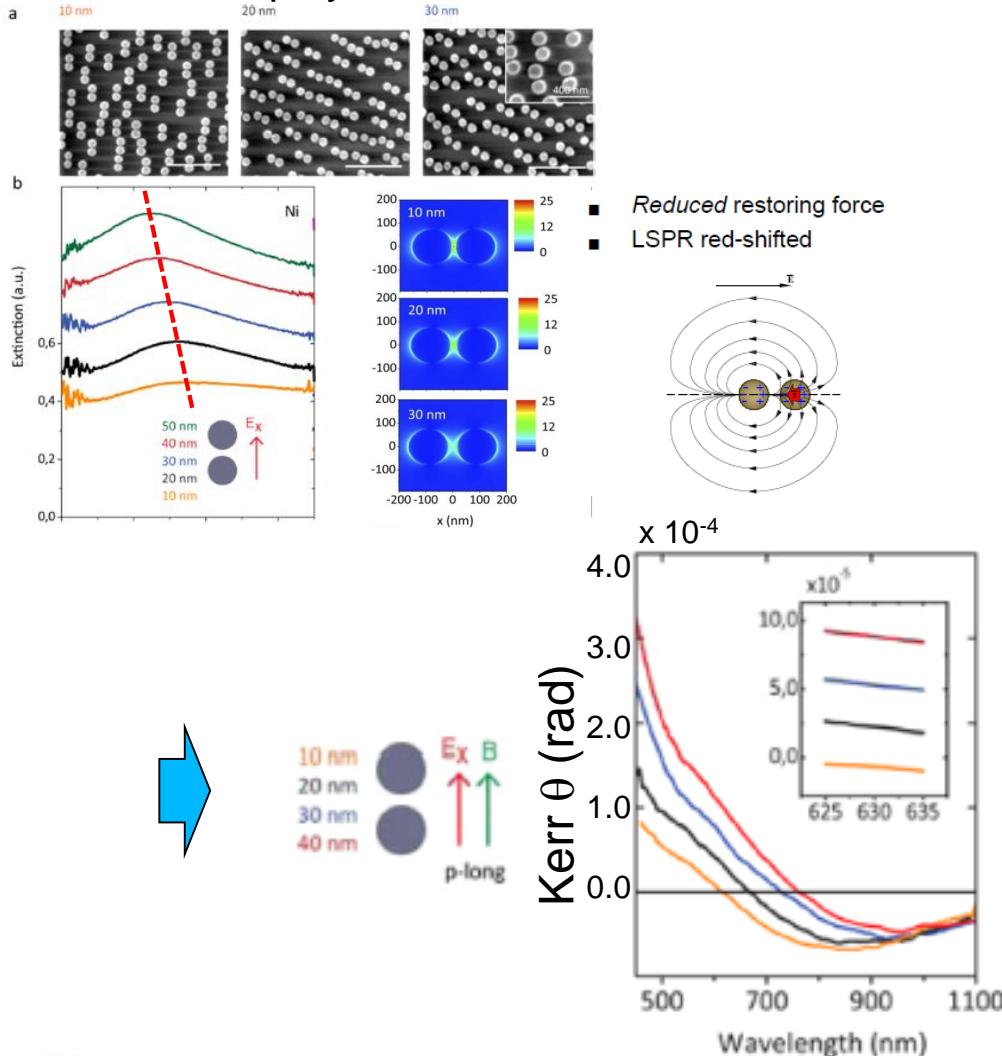
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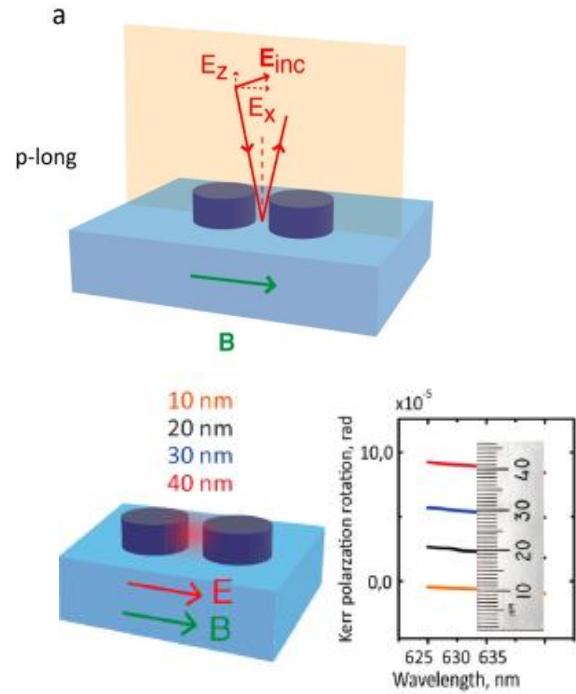


## Near field interactions: Magnetoplasmonic ruler

Plasmon ruler is an emerging concept where strong **near-field** coupling of plasmon nanoantenna elements is employed to obtain the structural information at the nanoscale (nanoscale distances).



### Magnetoplasmonic ruler concept



MP ruler: two orders of magnitude higher precision compared to the state-of-the-art plasmon rulers.

*Nano Letters 15, 3204 (2015)*



## NANOANTENNAS COMBINING MAGNETIC AND PLASMONIC FUNCTIONALITIES

- Localized surface plasmons & Magneto-optical Kerr effects (MOKE): *Introduction*
- Physical picture and modeling
- LSPR-based sensing: Towards molecular sensing
- Photonics technology: control of the non-reciprocal light propagation

## MAGNETOPLASMONIC METAMATERIALS

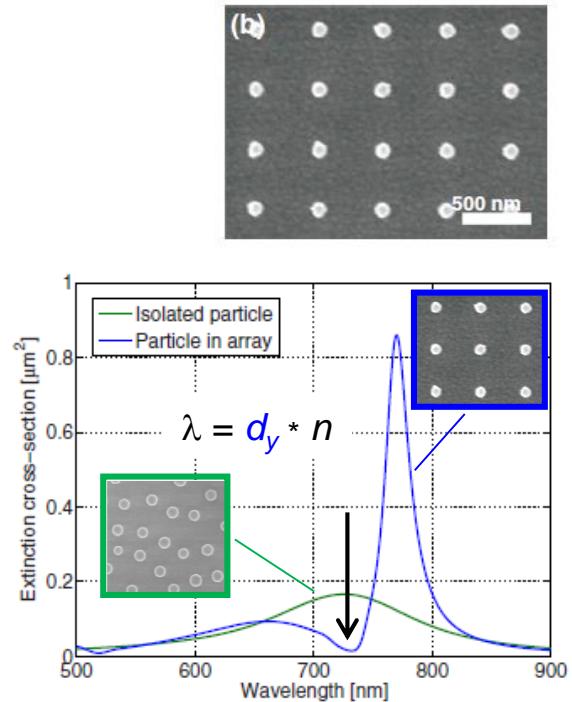
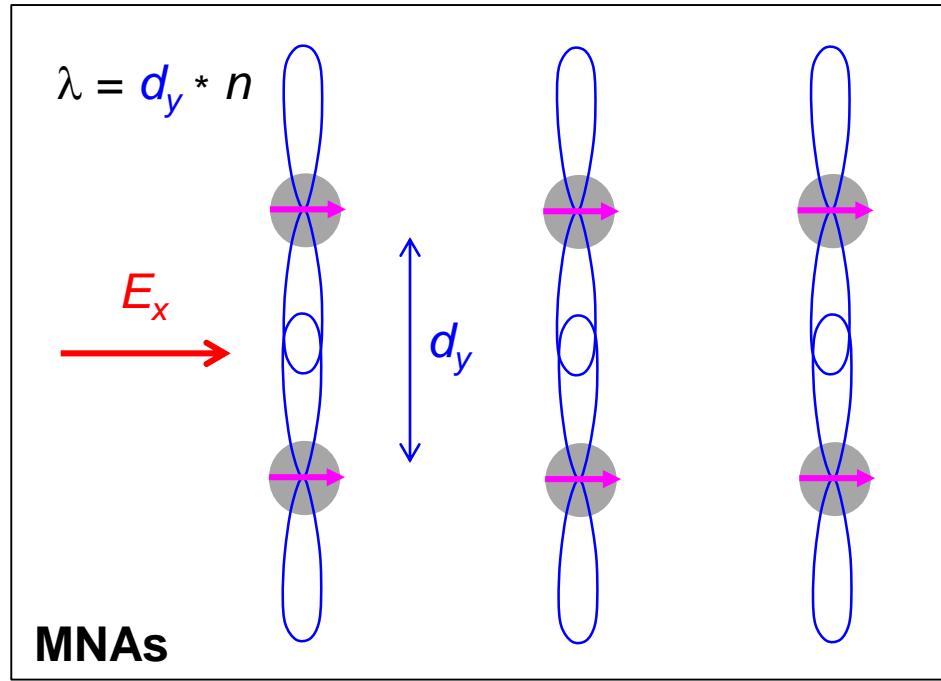
- Surface lattice resonances in arrays of nanoantennae
- Arrays of elliptical nanoantennae
- Magnetoplasmonic gratings: arrays of antidots

## CONCLUSIONS



# Reduced plasmon radiative damping – Fano-like resonance

Ordered arrays of metallic nano-antennas (MNAs) placed in symmetric or quasi-symmetric refractive index environment exhibit **surface lattice resonances (SLRs)** which arise from diffraction-induced coupling between LSPRs of the MNAs.

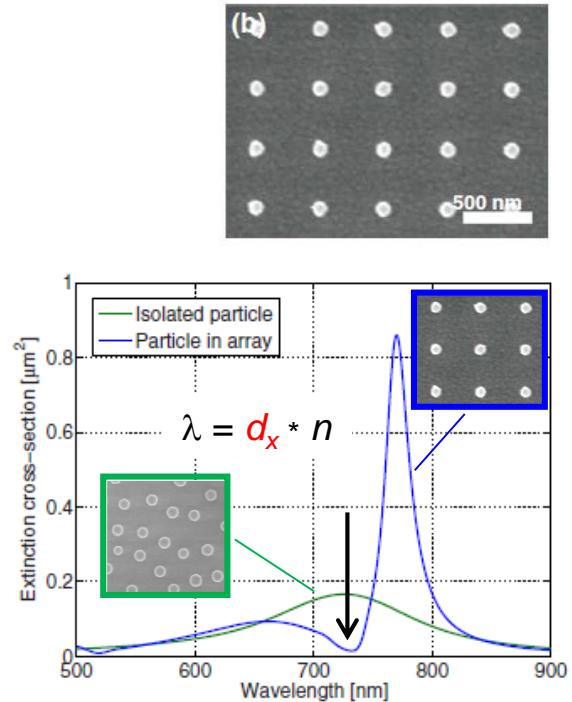
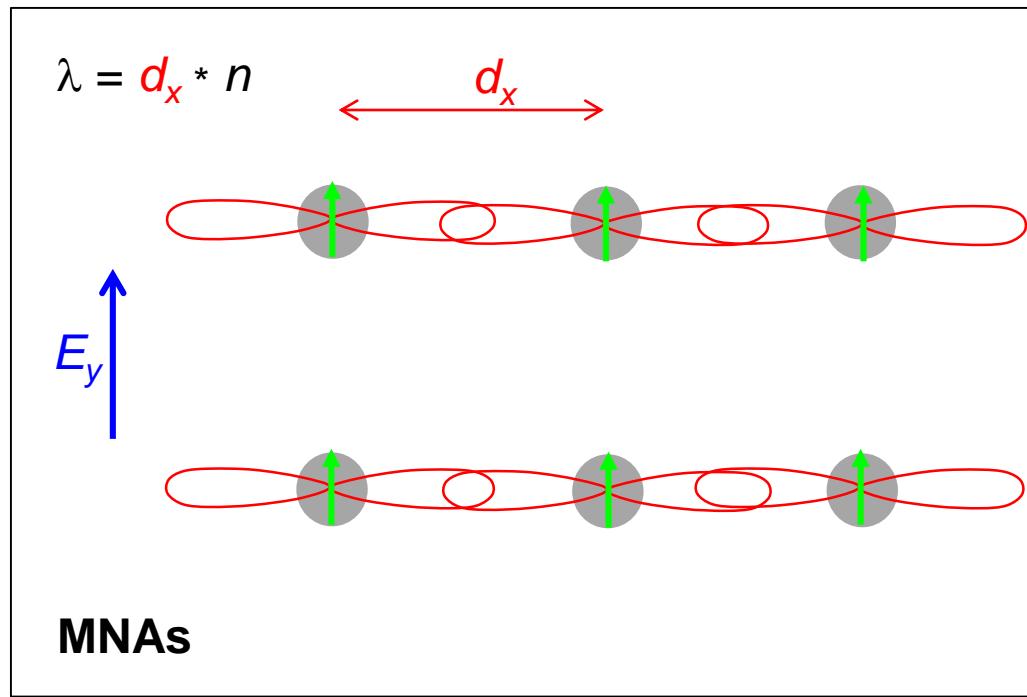


This coupling may result in significant reduction of plasmon radiative damping, and therefore, narrowing of plasmon resonance, which is of interest for plasmon based sensors.



## Reduced plasmon radiative damping – Fano-like resonance

Ordered arrays of metallic nano-antennas (MNAs) placed in symmetric or quasi-symmetric refractive index environment exhibit **surface lattice resonances (SLRs)** which arise from diffraction-induced coupling between LSPRs of the MNAs.

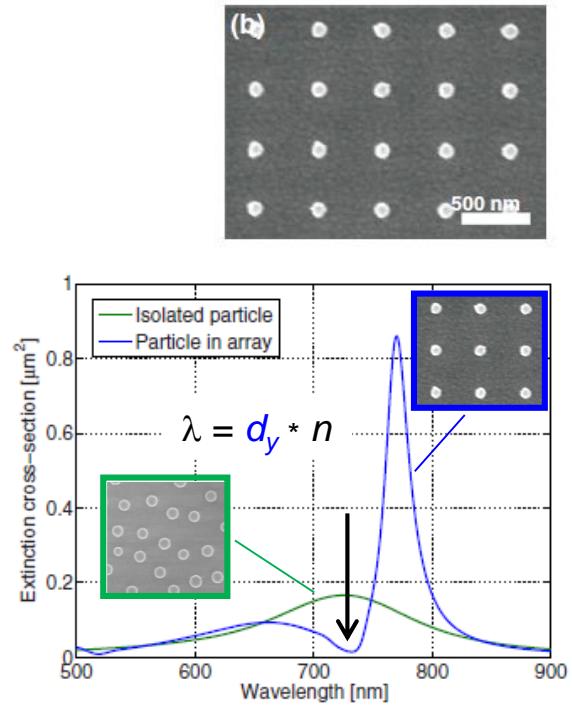
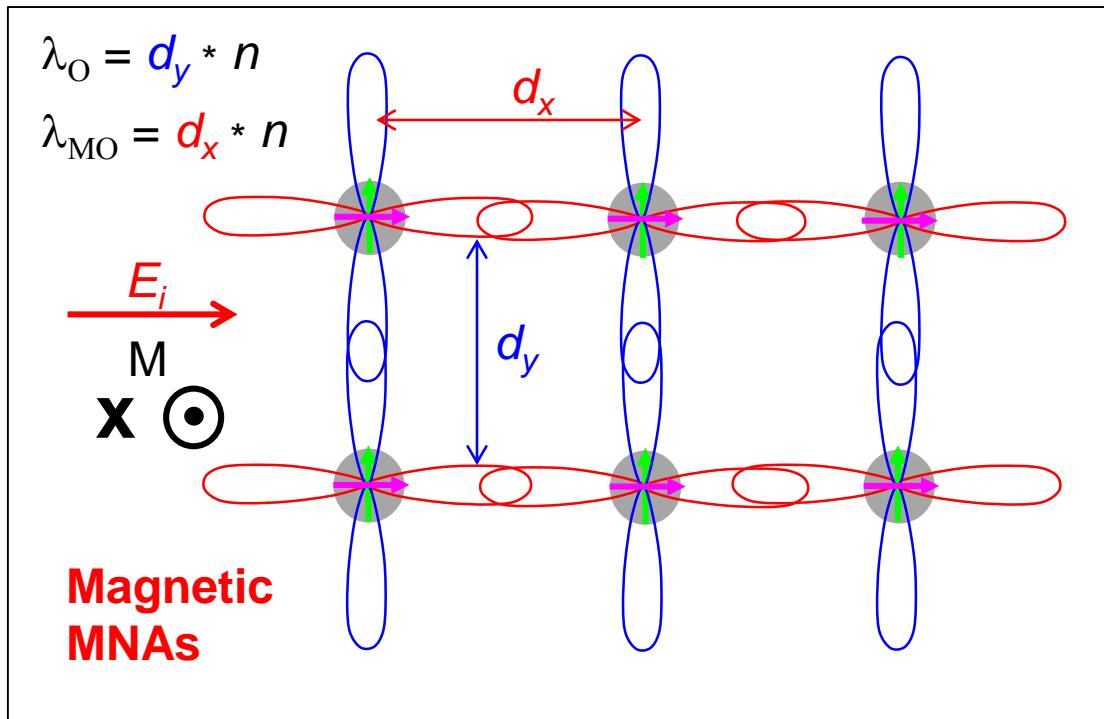


This coupling may result in significant reduction of plasmon radiative damping, and therefore, narrowing of plasmon resonance which is of interest for plasmon based sensors.



## Arrays of magnetoplasmonic nanoantennas

Ordered arrays of metallic nano-antennas (MNAs) placed in symmetric or quasi-symmetric refractive index environment exhibit **surface lattice resonances (SLRs)** which arise from diffraction-induced coupling between LSPRs of the MNAs.



This coupling may result in significant reduction of plasmon radiative damping, and therefore, narrowing of plasmon resonance which is of interest for plasmon based sensors.



## From random to ordered arrays: Polarizability

$$\vec{p}_{\text{single}} = \alpha \vec{E}_{\text{inc}}$$

$$\vec{p}_{\text{arr}} = \frac{1}{(1/\alpha - S)} \vec{E}_{\text{inc}}$$

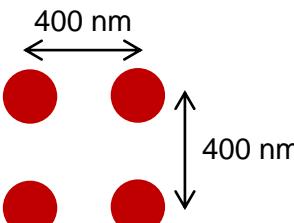
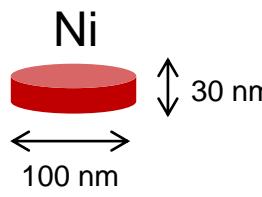
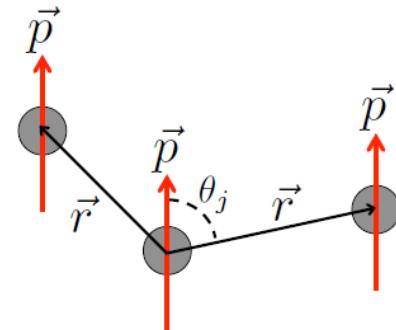
$$\vec{p}_{\text{arr}} = \alpha^* \vec{E}_{\text{inc}}$$

$$\alpha^* = \frac{1}{1/\alpha - S}$$

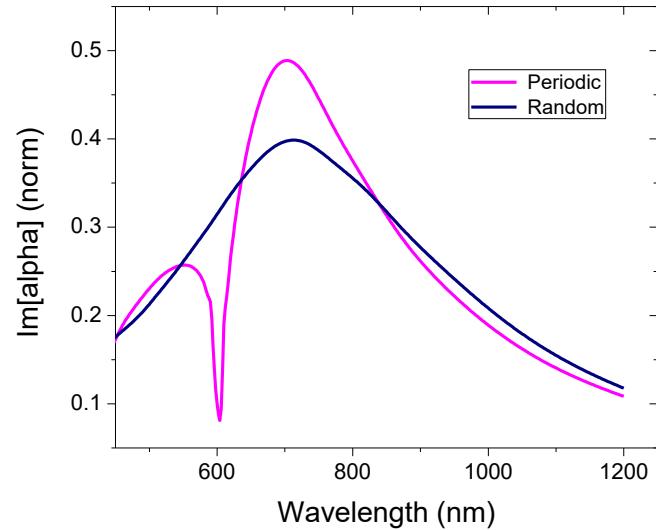
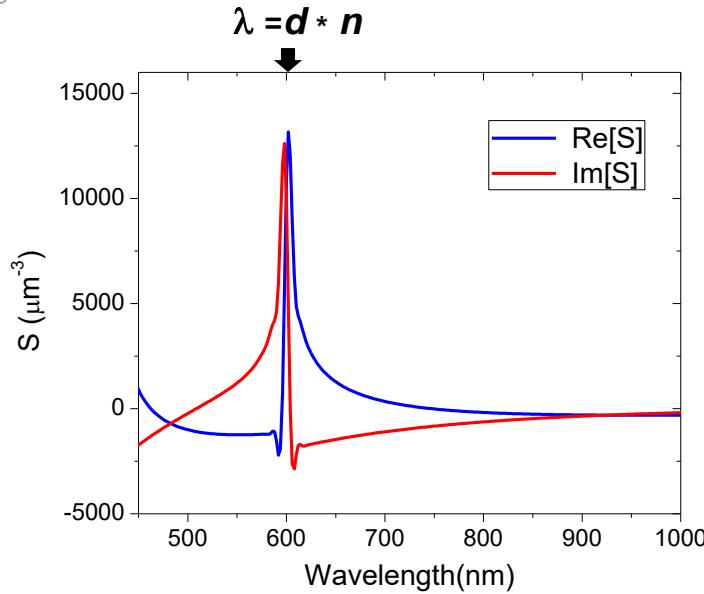
SLRs occur when  
 $\frac{1}{\alpha} = S \rightarrow \lambda = \mathbf{d} * \mathbf{n}$

How does  $S$  depend on lattice?

$$S = \sum_j \exp(i k r_j) \left[ \frac{(1 - i k r_j)(3 \cos^2 \theta_j - 1)}{r_j^3} + \frac{k^2 \sin^2 \theta_j}{r_j} \right]$$

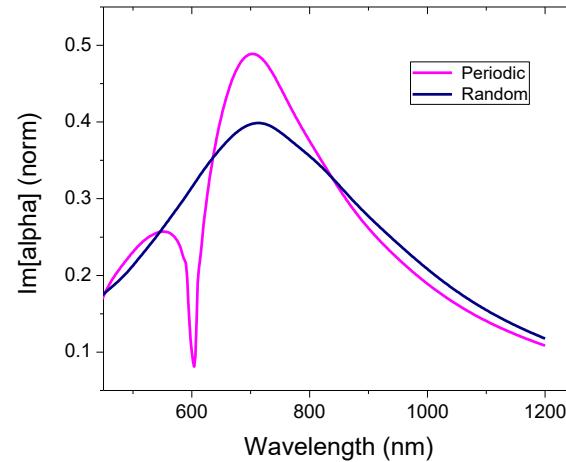
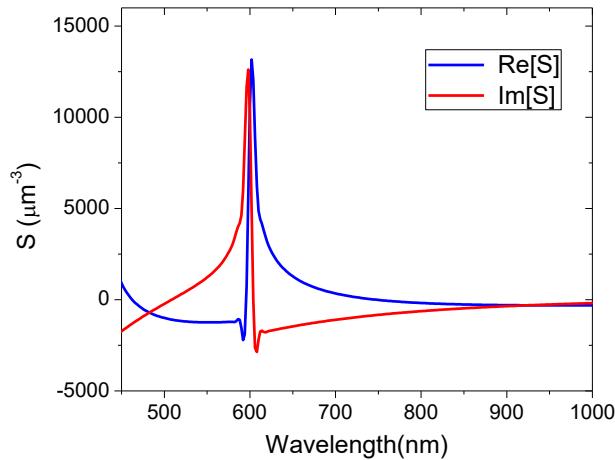


$n = 1.5$



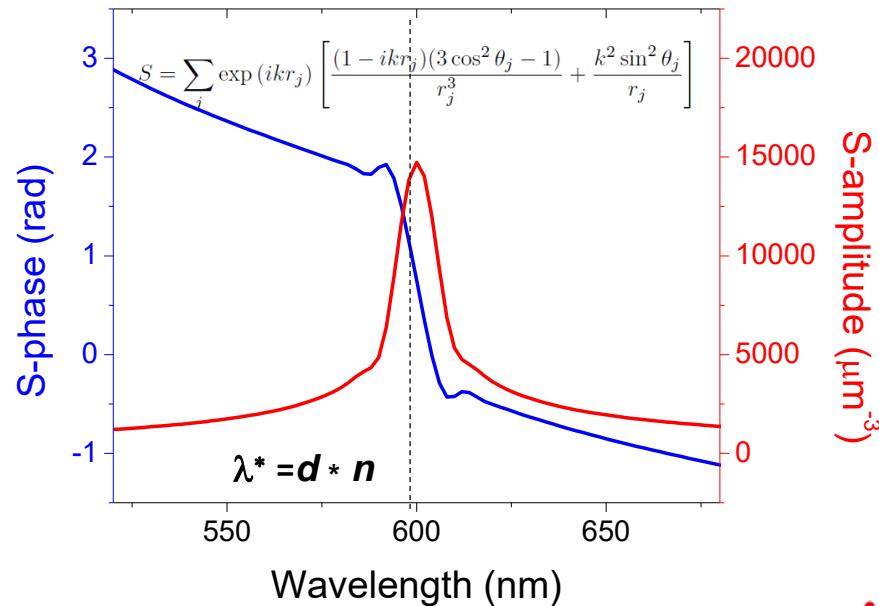


# On the origin of SLMs



The  $S$  coupling factor shows a sudden and large phase change around  $\lambda^*$ .

Constructive/destructive interference.





# On the origin of SLMs

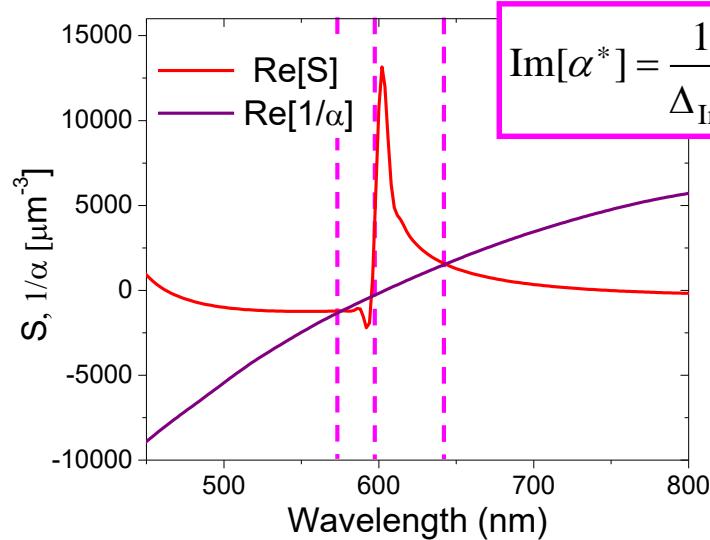
$$\alpha^* = \frac{1}{1/\alpha - S}$$

$$\text{Im}[\alpha^*] = \frac{\Delta_{\text{Im}}}{\Delta_{\text{Re}}^2 + \Delta_{\text{Im}}^2}$$

$$\Delta_{\text{Re}} = \text{Re}[1/\alpha] - \text{Re}[S]$$

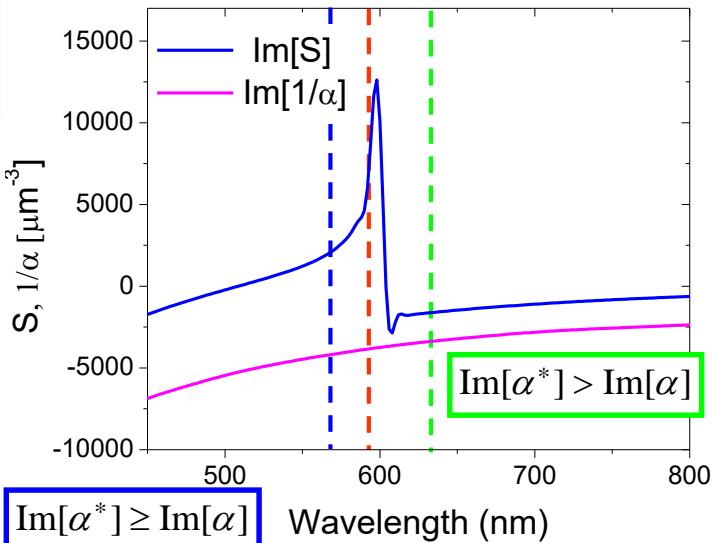
$$\Delta_{\text{Im}} = \text{Im}[S] - \text{Im}[1/\alpha]$$

Resonance position mainly determined by crossing points of real parts.



$$\text{Im}[\alpha^*] = \frac{1}{\Delta_{\text{Im}}}$$

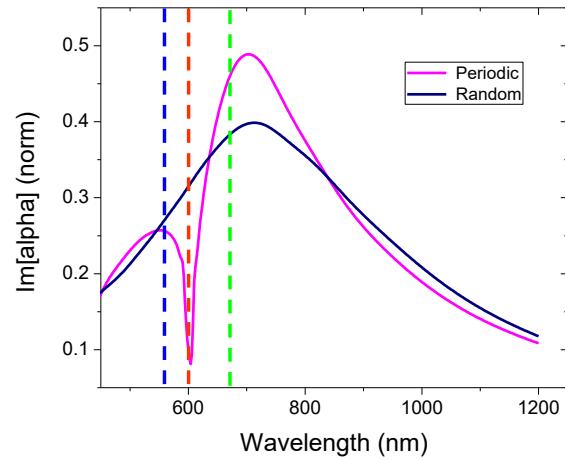
Strength of resonance determined by difference between imaginary parts



$$\text{Im}[\alpha^*] \geq \text{Im}[\alpha]$$

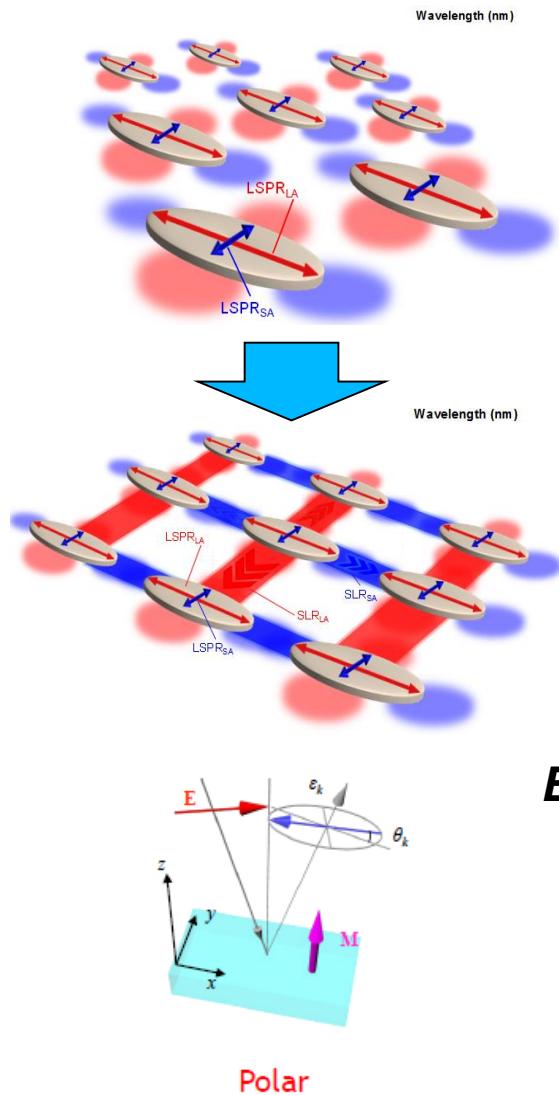
$$\text{Im}[\alpha^*] \ll \text{Im}[\alpha]$$

$$\lambda \approx d * n$$

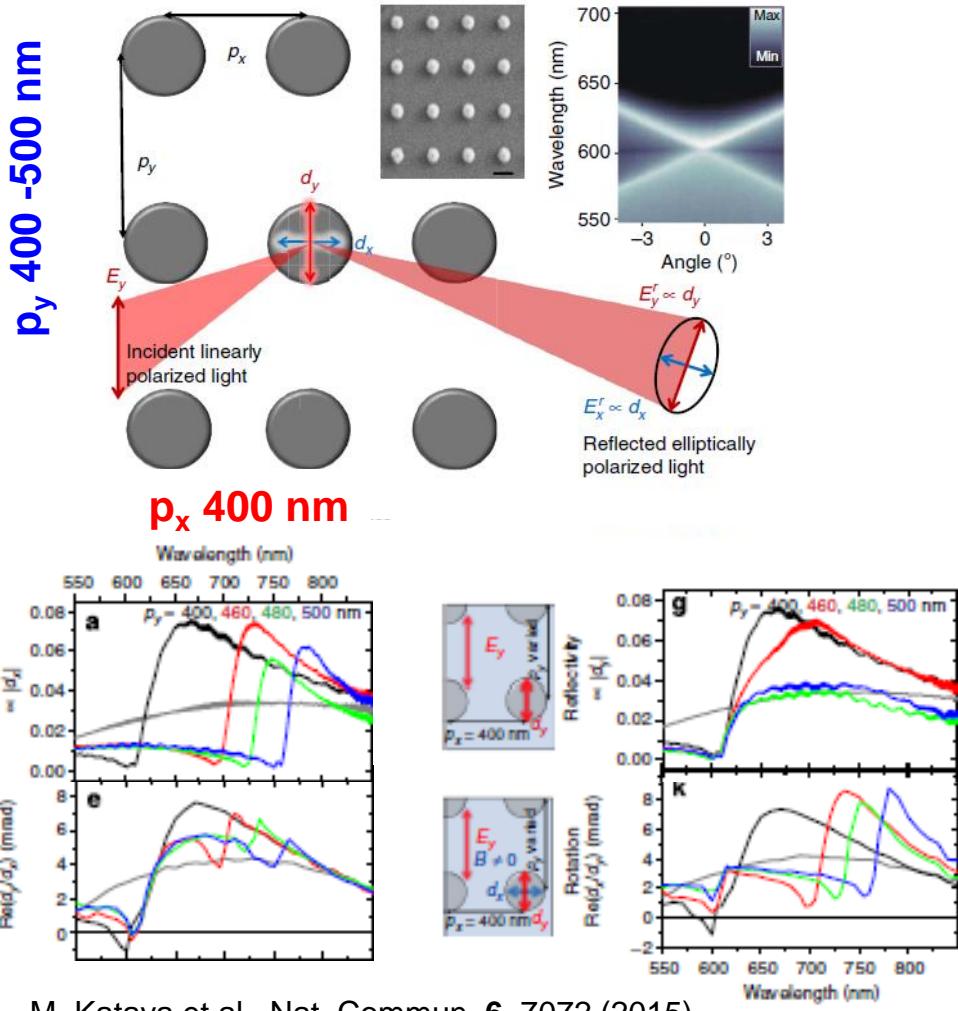




# From random to ordered arrays: MP crystals



Material: Py; Lattice parameters:  $p_x$  400 nm  $p_y$  400 -500 nm  
Refractive index matching oil ( $n = 1.5$ )



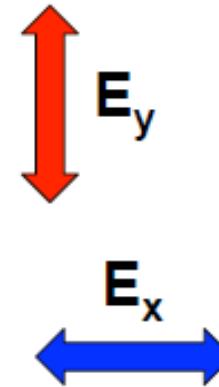
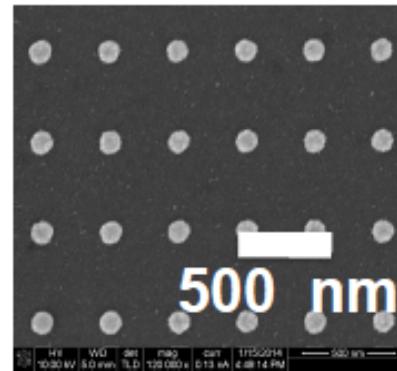
M. Kataya et al., Nat. Commun. 6, 7072 (2015)



## Rectangular arrays

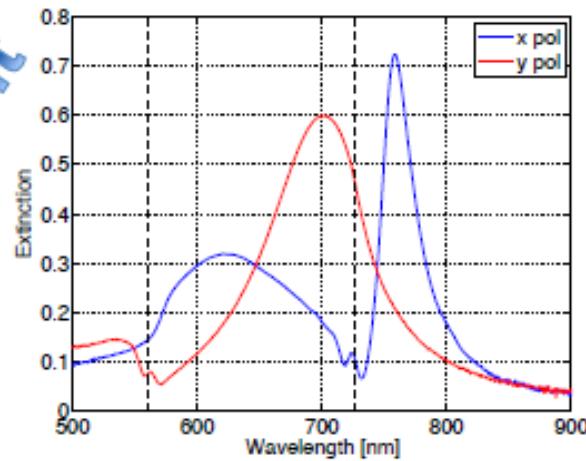
- Index matched to give homogeneous environment.

$a_y=480 \text{ nm}$

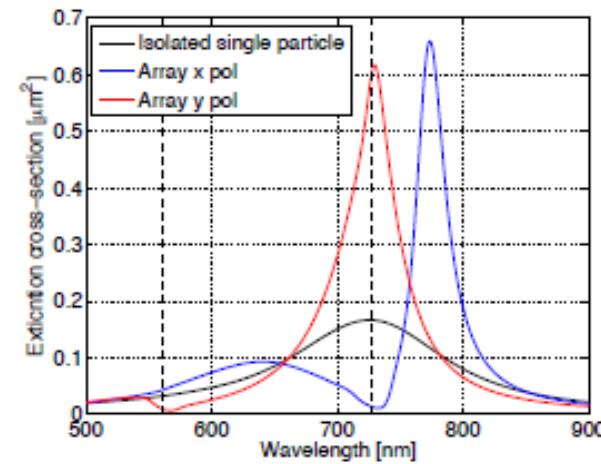


$a_x=370 \text{ nm}$

Experiment



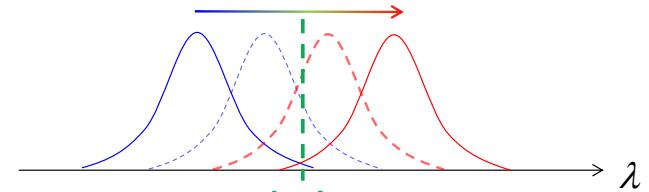
Model



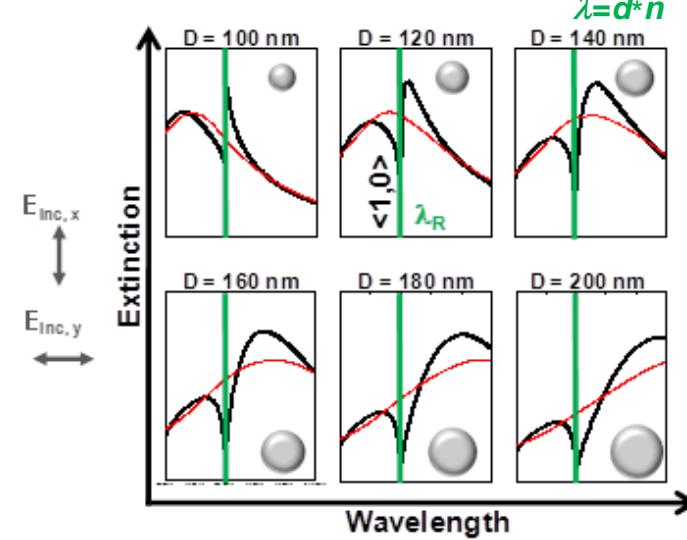
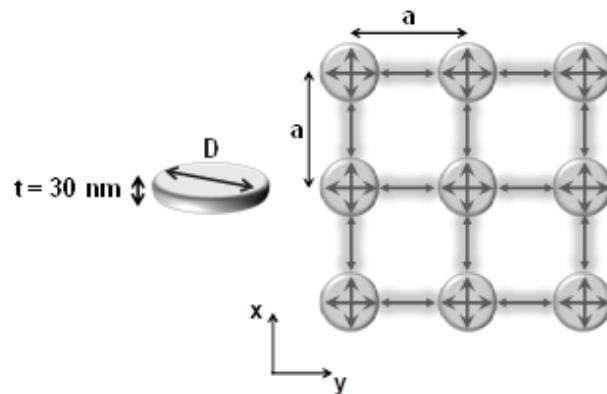


## Relative position of the LSPR and the diffractive interference

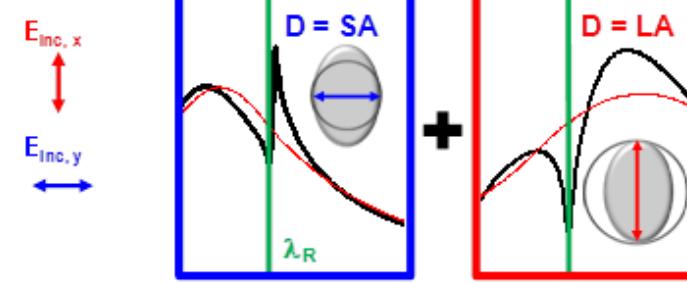
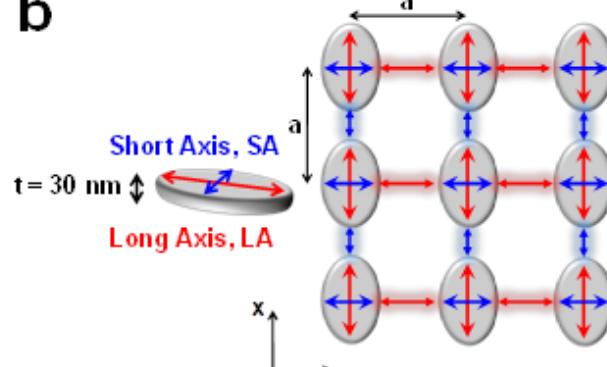
Resonance lineshape evolution varying the relative position of the LSPR with respect to the Rayleigh's anomaly



**a**



**b**

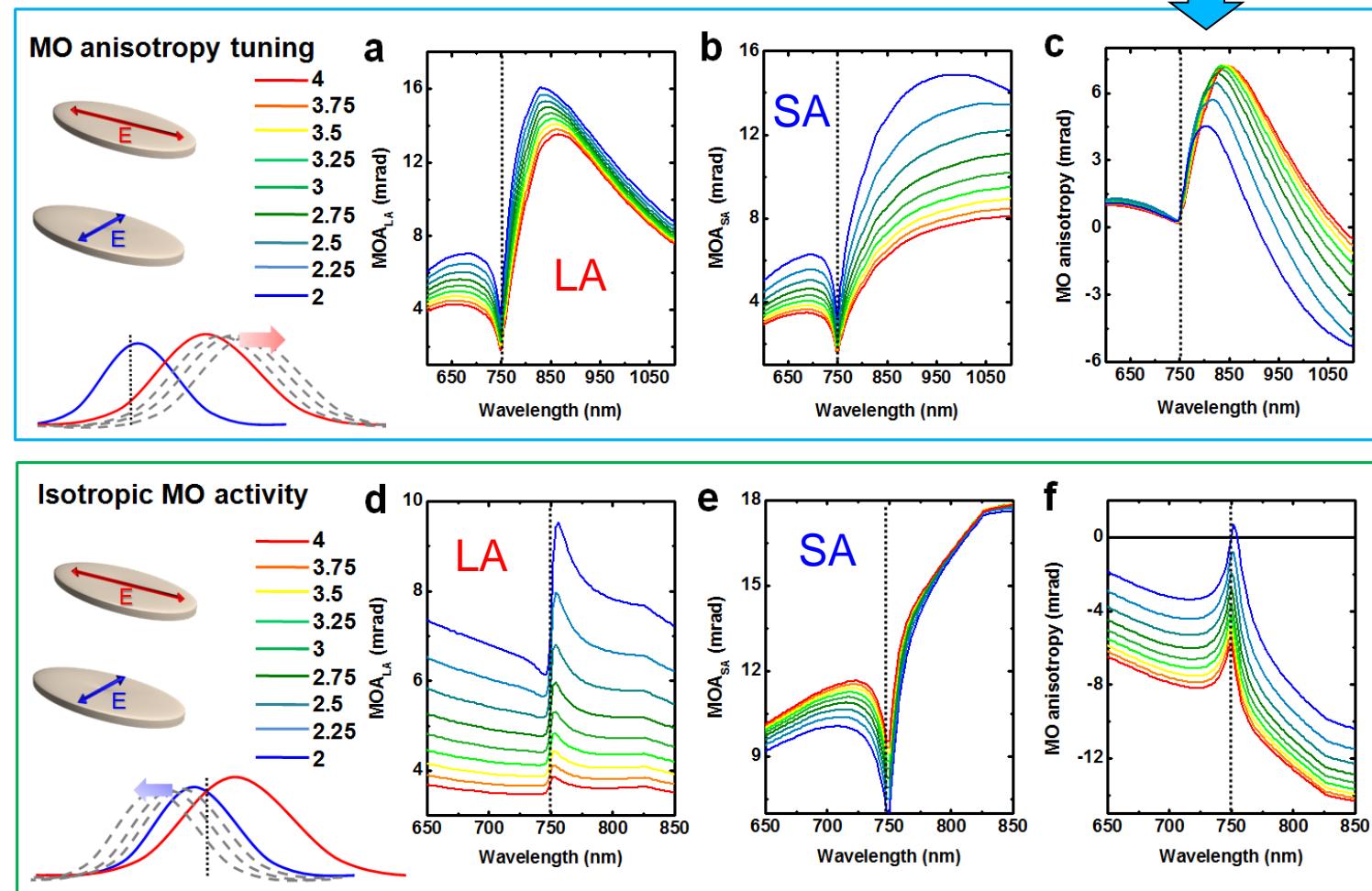




# *Enhanced and tunable O and MO-Anisotropy*

$$\text{MOA} = \sqrt{\theta_K^2 + \varepsilon_K^2}$$

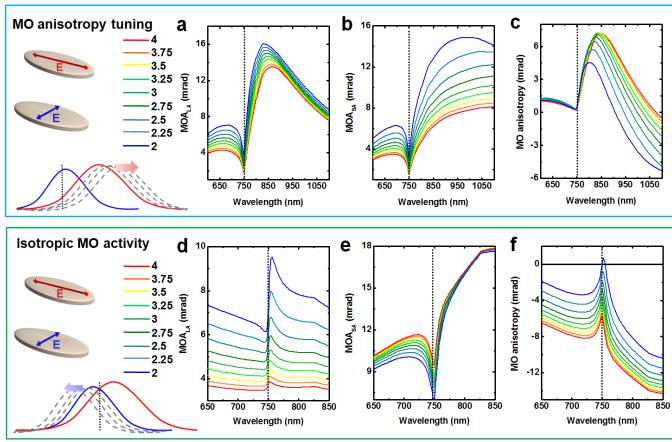
## Short Axis, SA



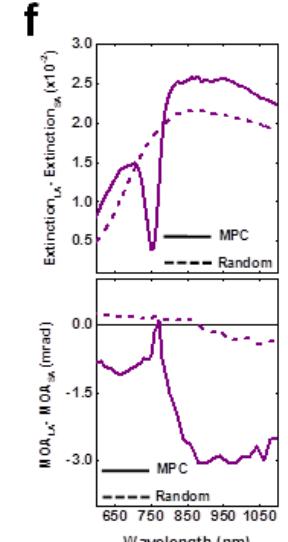
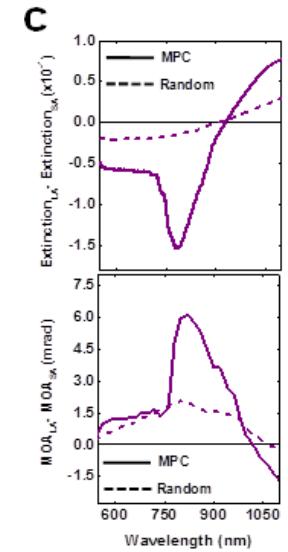
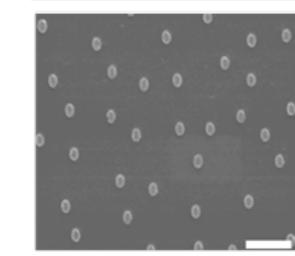
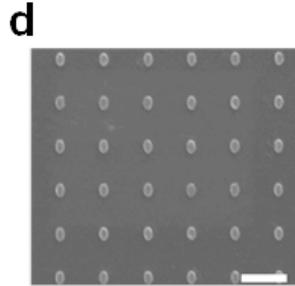
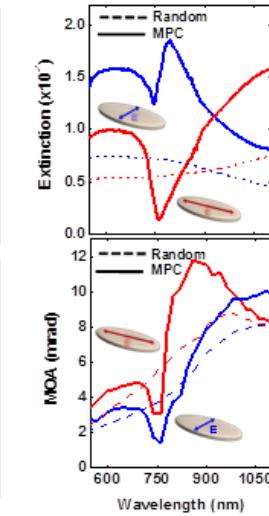
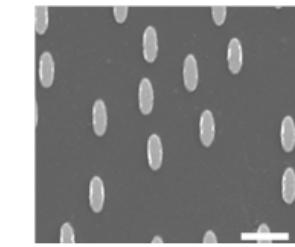
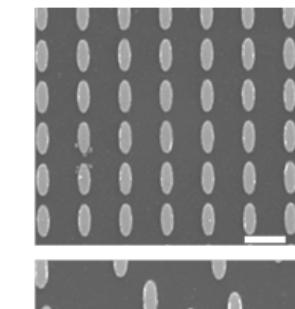
N. Maccaferri et al., Nano Lett. **16**, 2533 (2016)



# Enhanced and tunable O and MO-Anisotropy



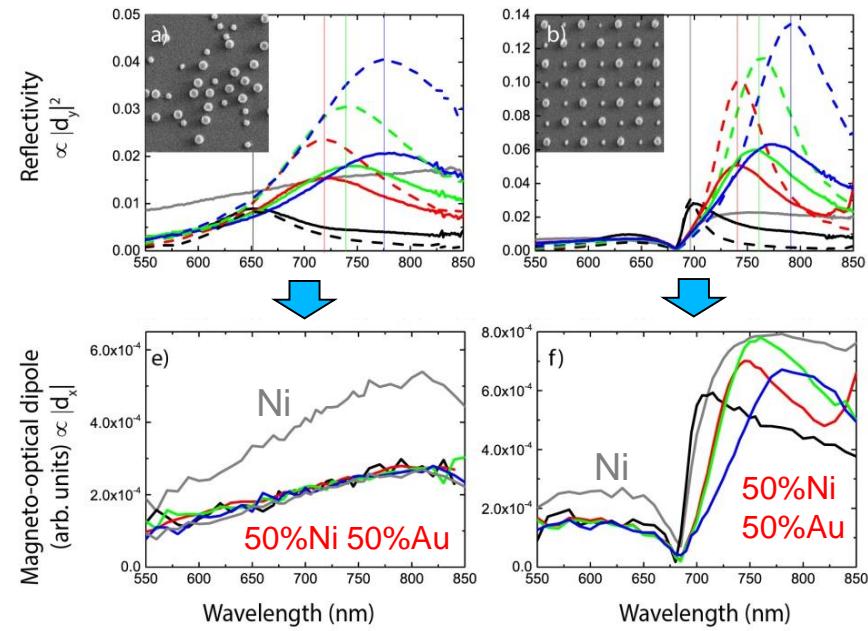
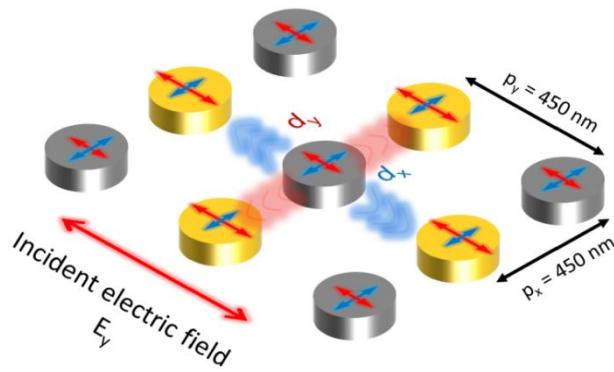
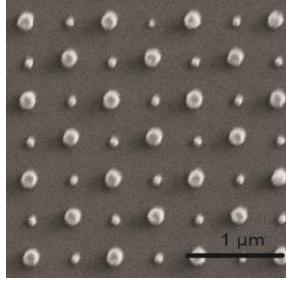
## Experiment



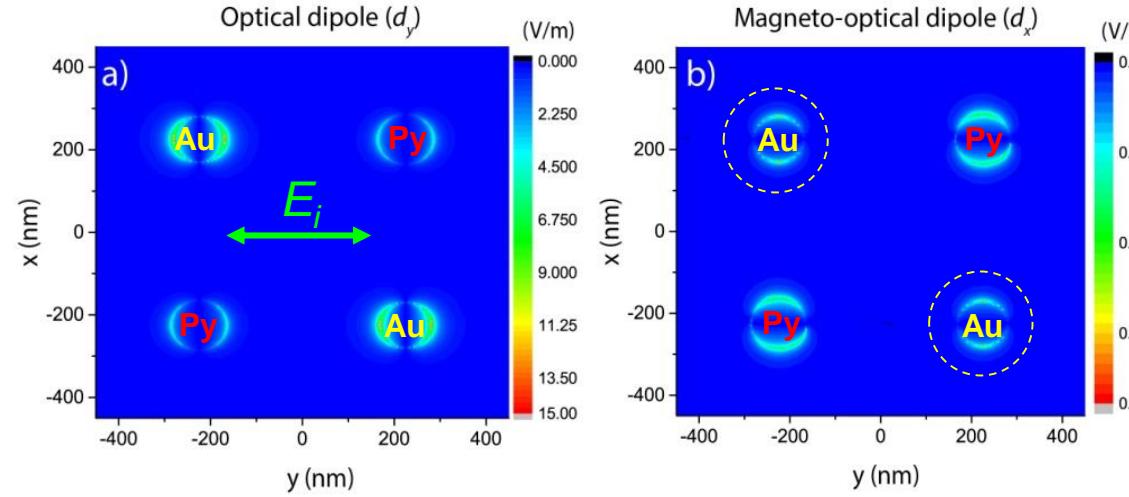
N. Maccaferri et al., Nano Lett. **16**, 2533 (2016)



# Checkerboard hybrid arrays of Py and Au nanoantennae



Efficient radiative far-field coupling between the magnetic and noble-metal components

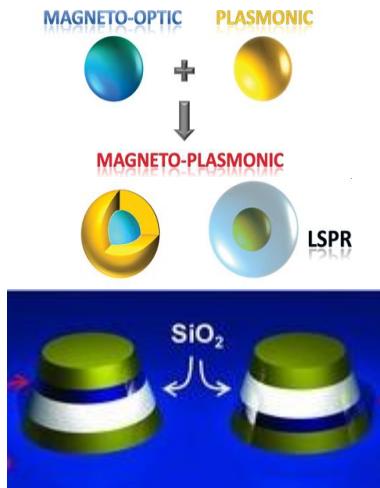


Integrating MO active and pure plasmonic nanostructures: combination of intense optical resonances with strong MO activity.

M. Kataia et al., Opt. Express 24, 3652 (2016)



## LSMs with hybrid nanostructures



Another common strategy to overcome the excess of damping is to develop hybrid structures consisting of noble metals and ferromagnets.

Banhí et. al Adv. Opt. Mat. **24**, OP36 (2012).

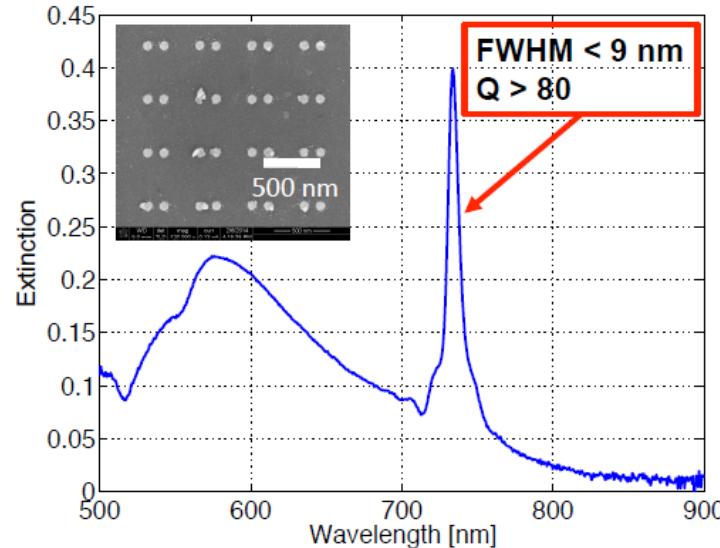


Mikko Kataja, Pourjamal Sara & Sebastiaan van Dijken

Aalto, Finland

Dimers

$E_x$





## Concluding remarks

- Concerted action of LSPRs (or SPPs) and MO-coupling can be exploited to achieve a controlled manipulation of the MO response (control Kerr rotation/ellipticity) beyond what is offered by intrinsic material properties.

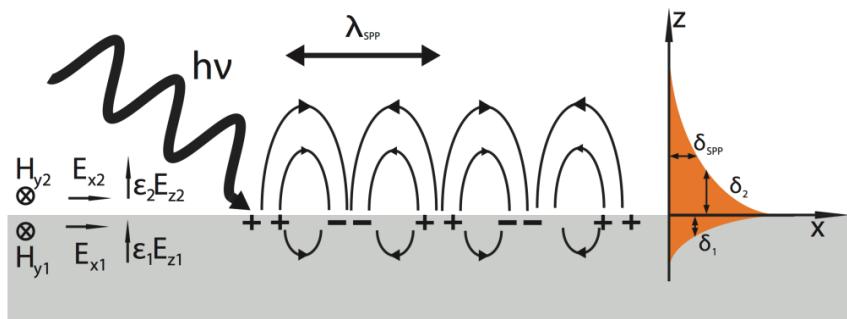
### Patterning magnetic nanostructures for resonant interaction with light: Magnetoplasmonic Crystals

- Magnetically tunable plasmonic crystal based on the excitation of Fano-like lattice surface modes in periodic arrays.
  - ✓ Highly tunable and amplified magneto-optical effects as compared to disordered systems.
- Two-dimensional magnetoplasmonic crystals supporting surface plasmon polariton modes and displaying a two-dimensional photonic band structure.
  - ✓ Design of metamaterials with tailored and enhanced magneto-optical response by engineering the plasmonic band structure via lattice engineering.



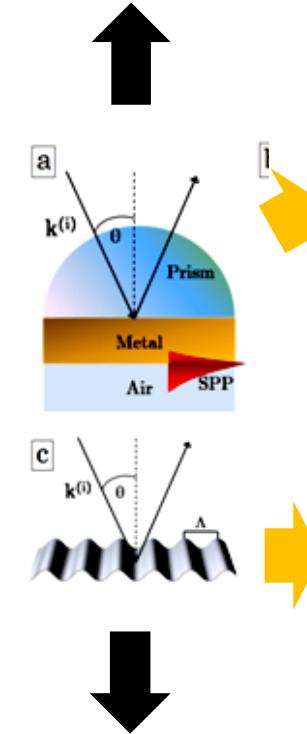
## Other directions explored: magneto-plasmonics with SPPs

SPPs are localized electromagnetic modes/charge density oscillations at the interface of two media with dielectric constants of opposite signs, e.g. a metal and a dielectric.,.

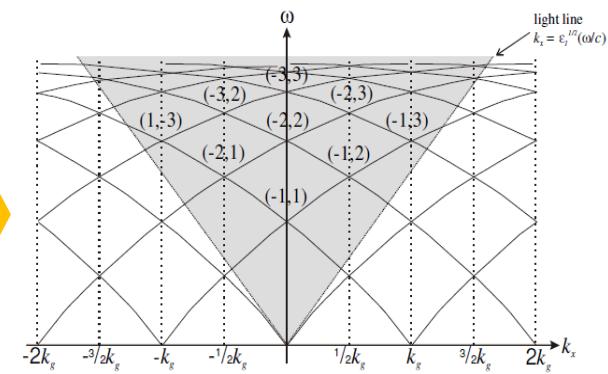
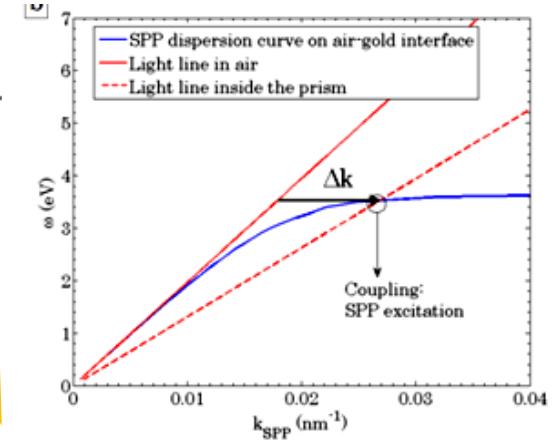


**s ↔ p-polarization conversion!!**

$$k_x = \frac{\omega}{c} \left( \frac{\epsilon_1 \epsilon_2}{\epsilon_1 + \epsilon_2} \right)^{1/2} .$$



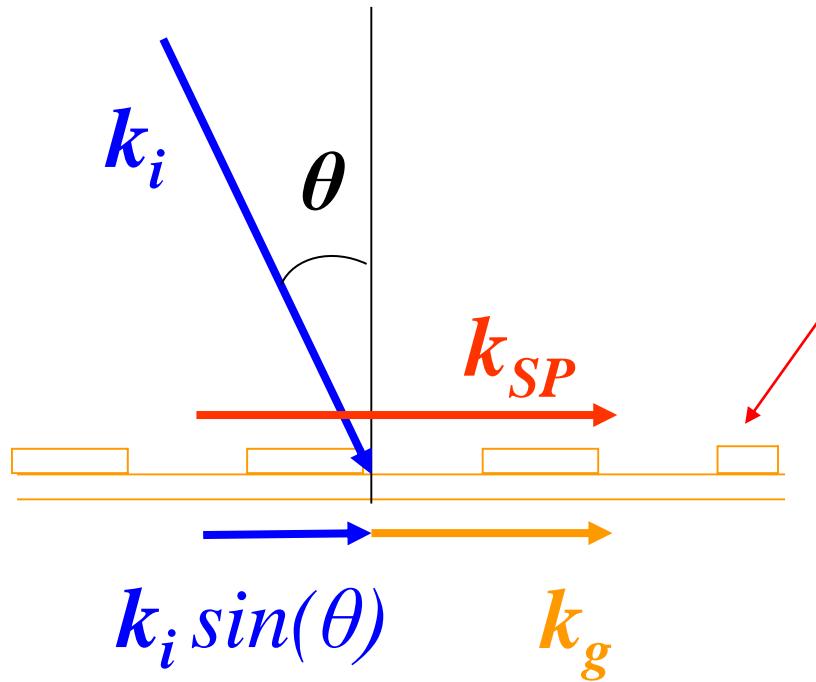
**p-polarization only**



$$k_{SPP} = k_{x,\text{photon}} \pm n k_{\text{grating}} = \frac{\omega}{c} \sin \theta_0 \pm n \frac{2\pi}{a}$$

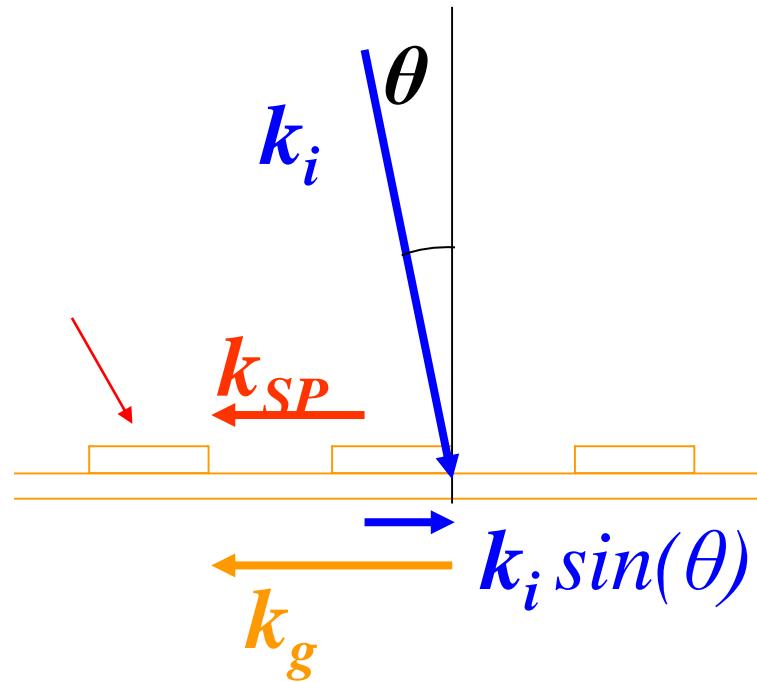


## SP resonance: coupling with a grating (conservation of momentum)



$$k_{SP} = k_i \sin(\theta) + k_g$$

+1 order coupling



$$k_{SP} = k_i \sin(\theta) - k_g$$

-1 order coupling



# Magntoplasmonic gratings: MOKE enhancement due to resonant coupling with SPPs

## Magnetic diffraction grating

Antidot array (square lattice):

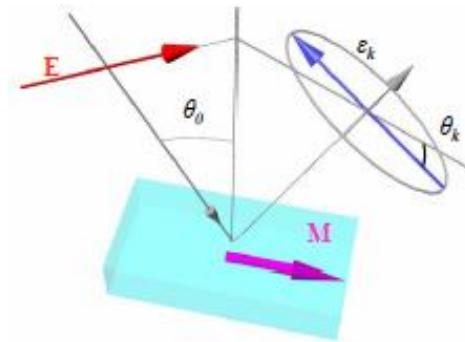
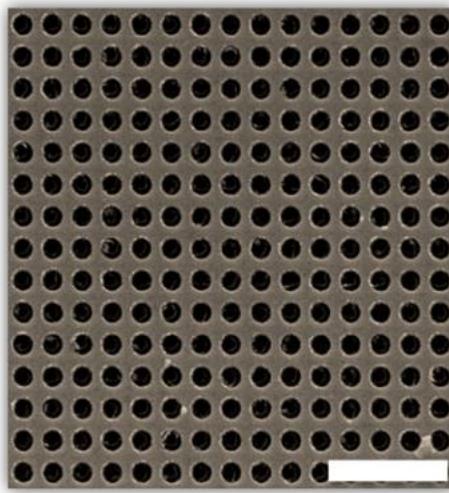
material **Py** ( $\text{Fe}_{20}\text{Ni}_{80}$ ), thickness = **80 nm**,

lattice parameter = **405 nm**,

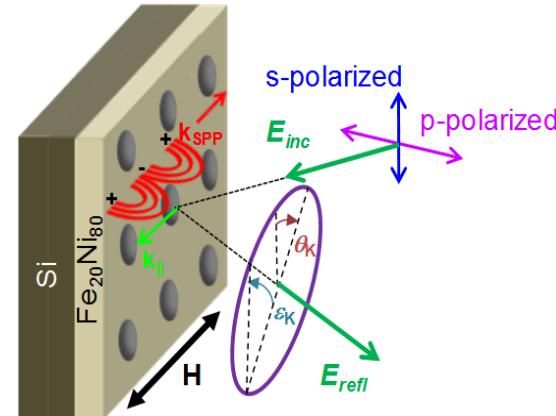
hole diameter = **265 nm**

by deep-UV photolithography

(Prof. A. Adeyeye, Singapore)



Longitudinal



N. Maccaferri et al., ACS Photonics 2, 1769 (2015)



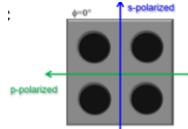
## SPP band structure: perturbative approach

$$k_{spp}(\lambda) = \frac{2\pi}{\lambda} \sqrt{\frac{\epsilon_d \cdot \epsilon_m}{\epsilon_d + \epsilon_m}}$$

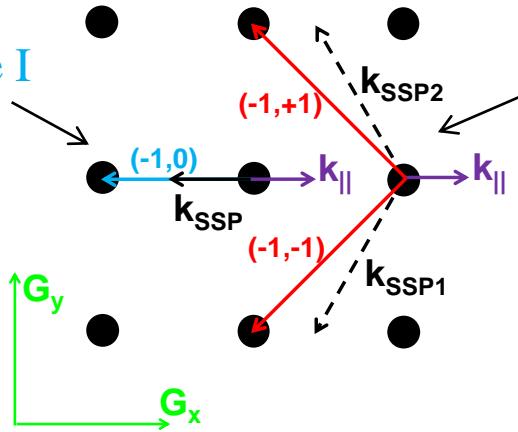
$$|\text{Re}(k_{spp}(\lambda))| = \left| k_{\parallel}(\lambda) + m \cdot \frac{2\pi}{a} i + n \cdot \frac{2\pi}{a} j \right|$$

$$k_{\parallel} = k_0 \sin \theta$$

$\phi = 0^\circ$

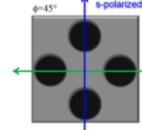


Type I

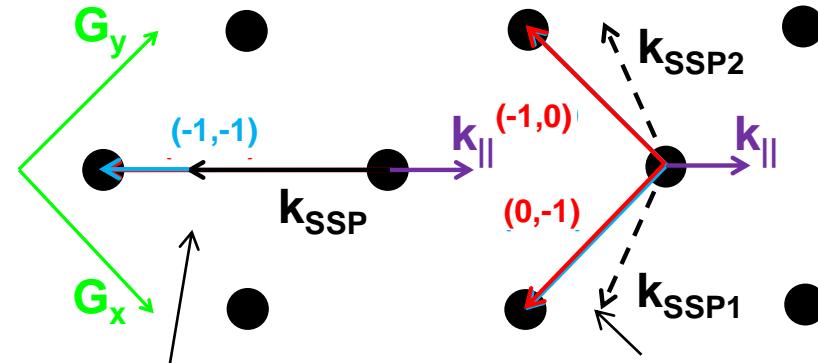


Type II

$\phi = 45^\circ$



Type I



Type II

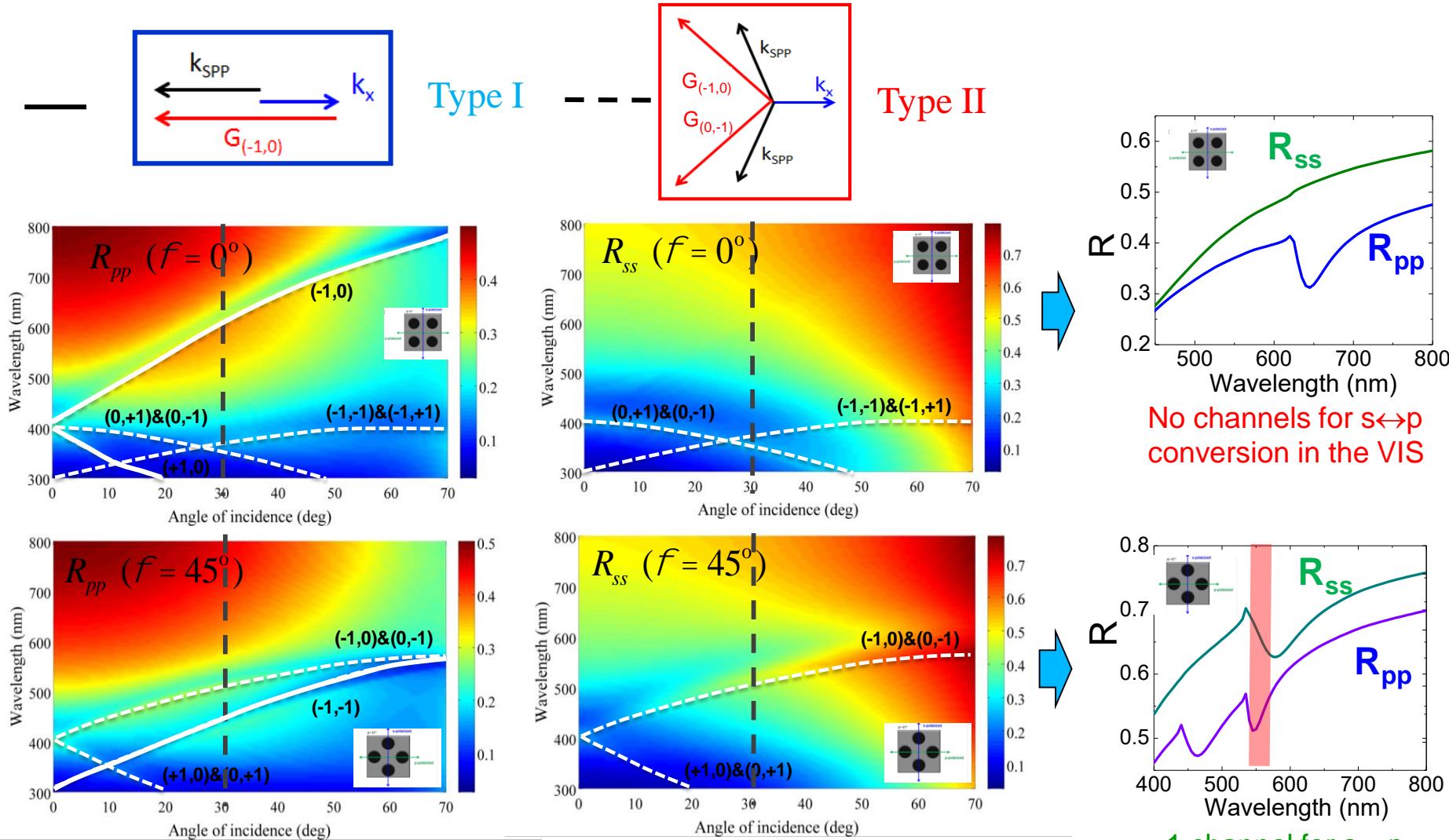
Key property

Type I:  
only p-pol

Type II:  
both p- and s-pol



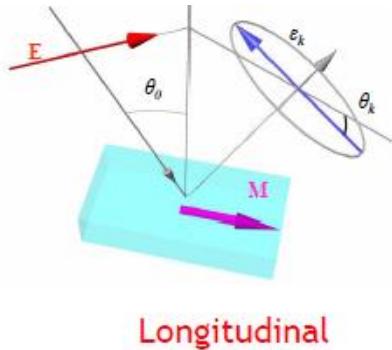
# Reflectivity maps: full calculations (antidots size and cross section)



"Generalized scattering-matrix approach for magneto-optics in periodically patterned multilayer systems"  
B. Caballero, A. García-Martín, and J. C. Cuevas, Phys. Rev. **B 85**, 245103 (2012)



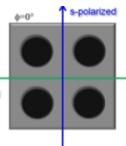
## MO activity enhancement mechanism (L-MOKE)



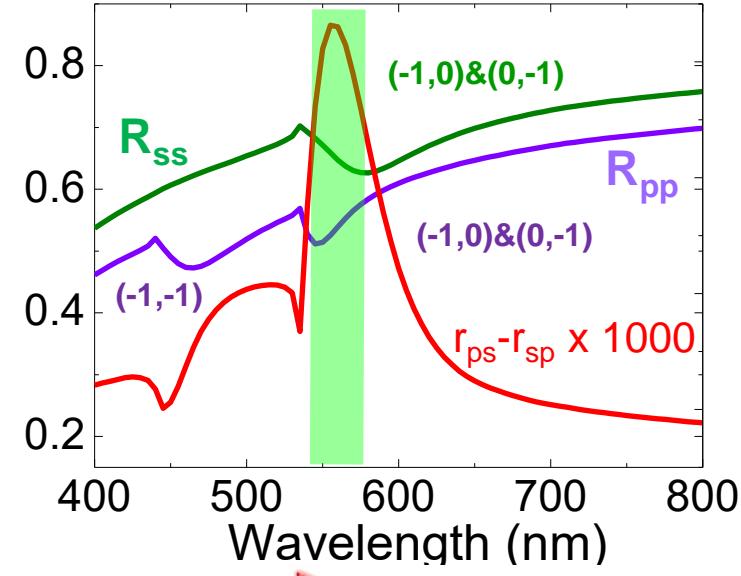
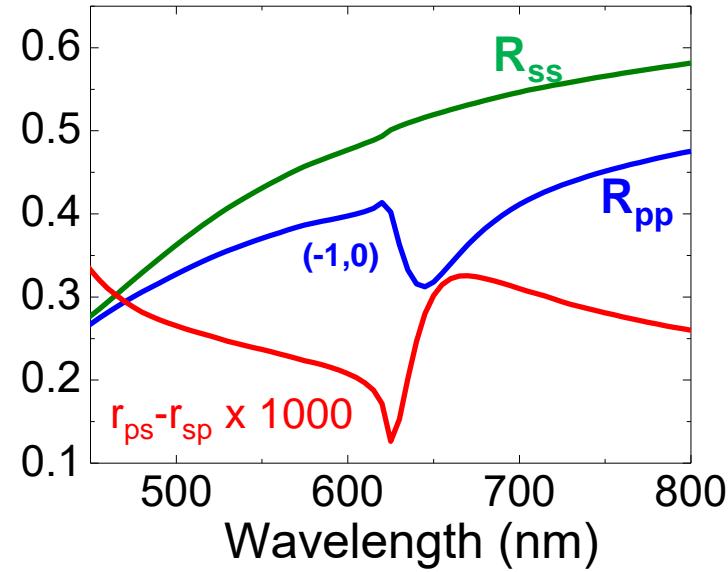
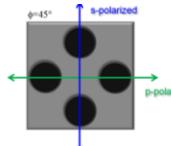
Longitudinal

(L-MOKE and P-MOKE involve  $s \leftrightarrow p$  polarization conversion  
T-MOKE  $p \leftrightarrow p$ : no polarization conversion.)

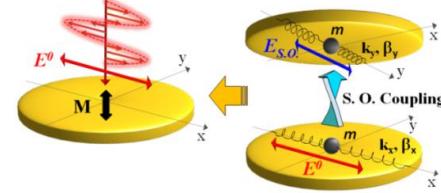
$$\phi = 0^\circ$$
$$\theta = 30^\circ$$



$$\phi = 45^\circ$$
$$\theta = 30^\circ$$

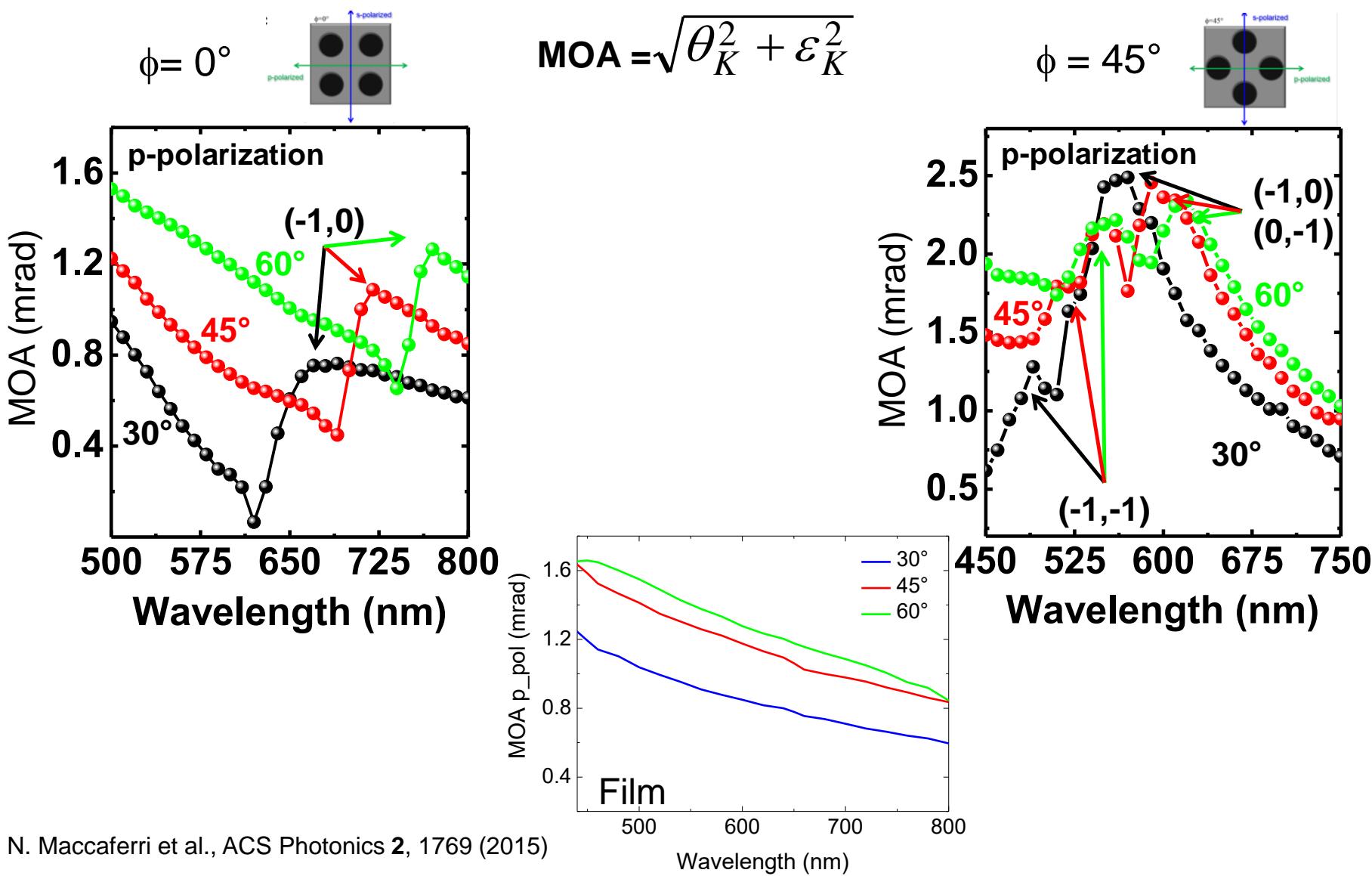


Plasmonic channel “open” for resonant MO induced polarization conversion.





## Experimental MO-activity

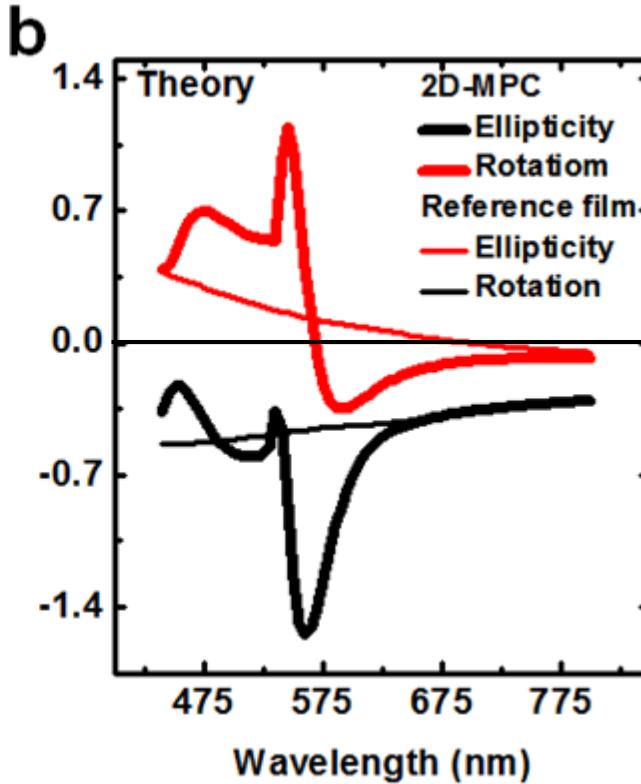
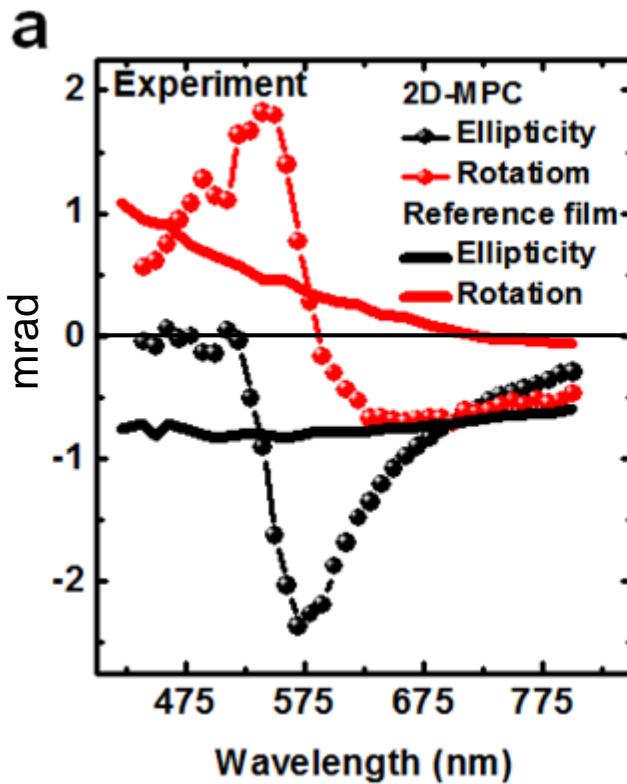
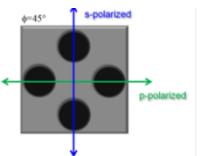


N. Maccaferri et al., ACS Photonics **2**, 1769 (2015)



## Rotation and ellipticity

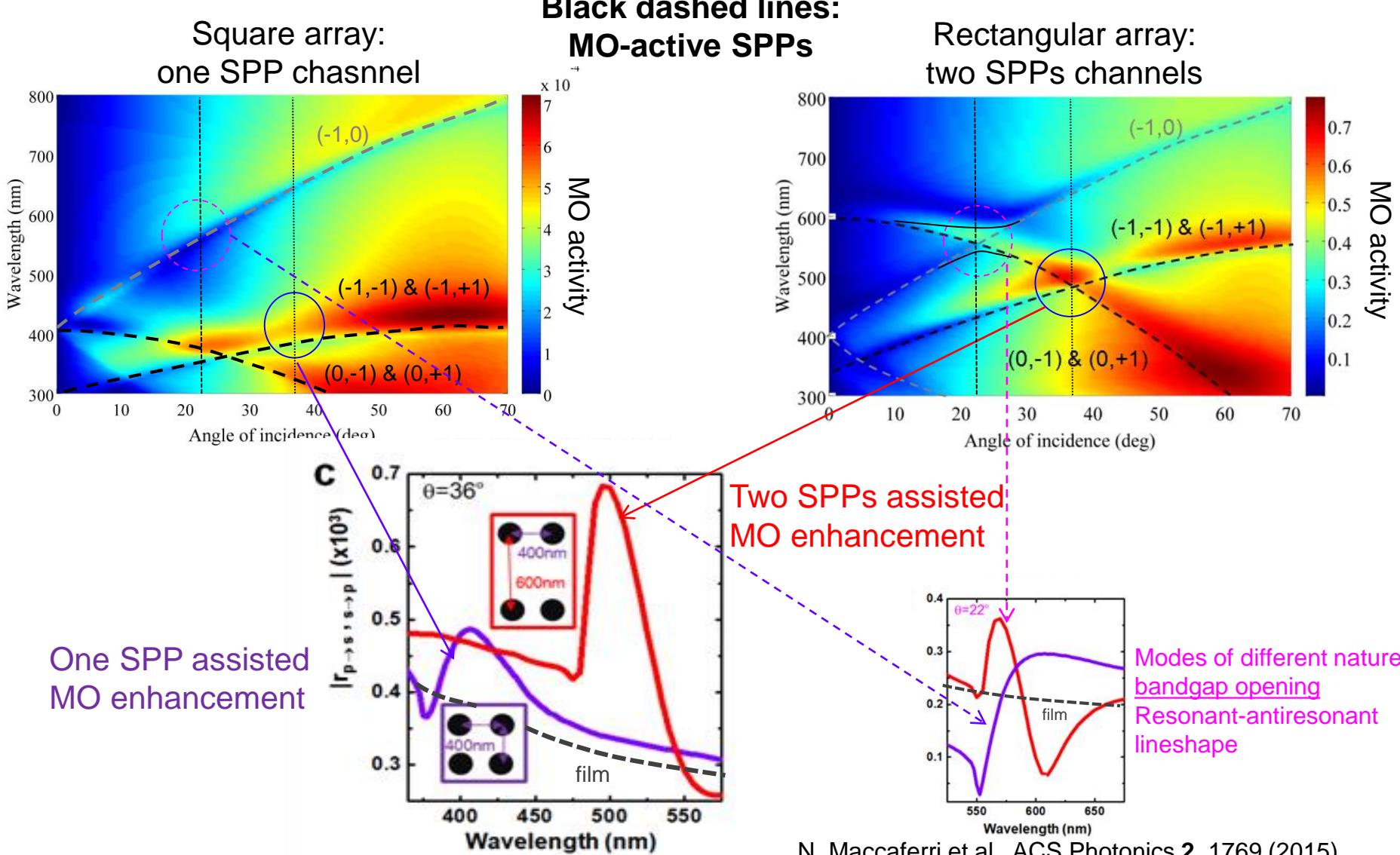
$$\begin{aligned}\phi &= 45^\circ \\ \theta &= 30^\circ\end{aligned}$$



N. Maccaferri et al., ACS Photonics 2, 1769 (2015)



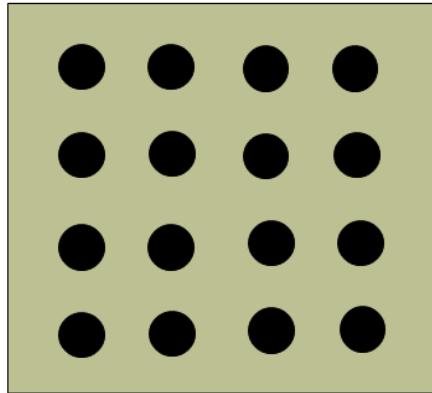
# SPP band structure engineering



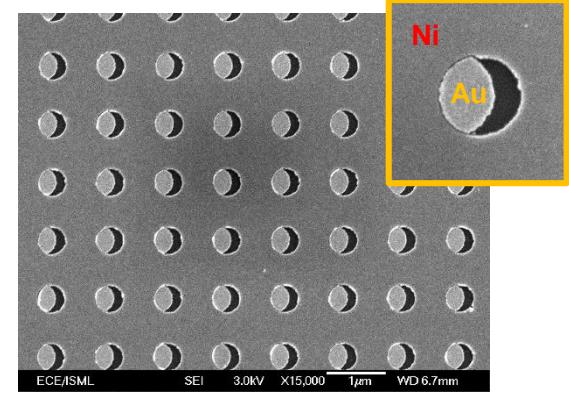
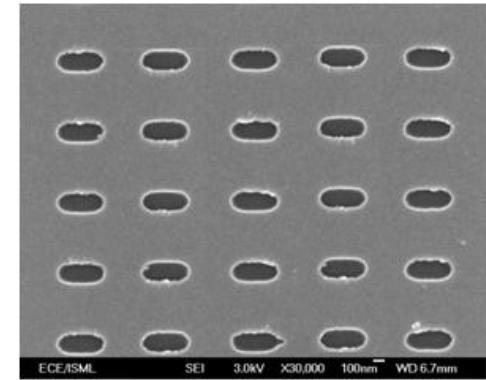
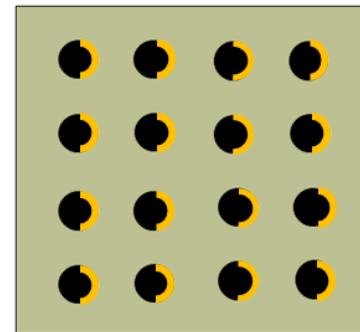
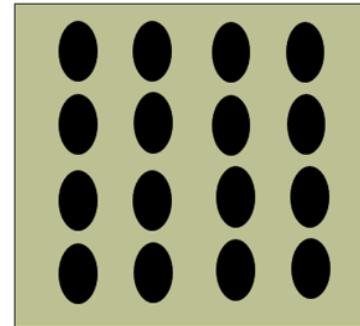
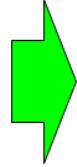
N. Maccaferri et al., ACS Photonics 2, 1769 (2015)



**SPPs**



Where to go?



**Zhou Xue & Adekulne O. Adeyeye**

National University of Singapore

P. VAVASSORI

European School on Magnetism (ESM-2018), Krakow 17-28 September 2018

**ikerbasque**  
Basque Foundation for Science



## Concluding remarks

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- Magnetically tunable plasmonic crystal based on the excitation of Fano-like lattice surface modes in periodic arrays.
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  - ✓ Design of metamaterials with tailored and enhanced magneto-optical response by engineering the plasmonic band structure via lattice engineering.