# XMCD ....

Outlook of the lecture

- Magnetism in nutshell
- X-ray absorption spectroscopy XAS
- Magnetic XAS = XMCD (X-ray Magnetic Circular Dichroism)

# Magnetism in a nutshell

- "Rotating" charges produce magnetic field (angular momentum)
- There are two types spin (S) and orbital (L) magnetic moments



 $\langle m_L \rangle_z = \langle L_z \rangle \cdot \mu_B$   $\langle m_S \rangle_z = g \cdot \langle S_z \rangle \cdot \mu_B \approx 2 \cdot \langle S_z \rangle \cdot \mu_B$   $\mu_B = 9.274 \cdot 10^{-24} \text{ J/T}$ g = G - factor  $\mu_B$  = Bohr's Magneton

### orbital moment



- orbital moment has preferred axis in anisotropic crystal field
  - LS-coupling in 3d-shell orients the spin
- The small L is important for almost all properties, especially for technology
  - remnant field, easy and hard axis, coercivity ....

P. Bruno, Physical Review B 39 (1989) 865

### Some examples for "modern" magnetism applications!



Low weight and high field = forces Optimizing interaction strength between lattice and magnetic moments → orbital moments

Important to know:

What is the magnetism of each element? Nd? Fe? Co? Sm?.... Some examples for "modern" magnetism applications!



#### **NdFeB-Servo-Motor**

Optimizing interaction strength between lattice and magnetic moments
 ➔ orbital moments

permanent magnets, magnetostriction, spin wave damping, etc. etc.

### Why X-rays and magnetism?

- It is important to know spin and orbital moments
- for each element in the system separately
- contact areas are important → probing single atomic layers and separating them from others
- We know: X-rays provide significant spatial resolution on the atomic scale
- Your will see here how this is transferred to magnetism using X-ray Magnetic Circular Dichroism (XMCD)
- Or in other words: XMCD is able to transfer **ANY** X-ray technique in it's magnetic counterpart!

#### Now XAS

- X-ray absorption spectroscopy XAS
  - Dipole selection rules provide "wanted projections"
    - symmetry selective
  - Electric field vector can provide orbital occupation and orientation
- Further Examples:
  - Gas on a surface → Chemistry and binding orientation
  - Valence and Band structure determination (unoccupied of cause)

# Why XAS!

One famous example (also for magnetism):  $2p \rightarrow 3d$ 



- X-ray absorption spectroscopy (XAS)
  - dipole selection rules

m' = m + q $l' = l \pm 1$ 

- probing 3d magnetism
   2p → 3d
- probing 4f magnetism
   3d → 4f

Spin-Orbit-Splitting

### XAS: In resonance very strong effects



All is based on Fermi's Golden Rule!

• It provides the probability  $W_{ba} = \frac{d}{dt} |c_b^{(1)}(t)|^2$  to excite an electron from the initial state  $|\Psi_i\rangle$  to the final state  $|\Psi_f\rangle$ 



Based on time dependent pertbation theory

Time integral  $\rightarrow$  "Energy-Conserving- Deltafunction"

### What have we learned so far? XAS because ..

- it probes unoccupied states
- element specific due to energy position
- symmetry selective due to selection rules  $p \rightarrow d$

What else?

#### Good for chemistry and band structure determination

- Example: Mn  $L_{2,3}$  2p $\rightarrow$ 3d
  - different oxidization states
  - shape provides important information about the unoccupied density of states
  - some less clear chemical shift observable
    - reason: also the initial (here 2p) and the final states (here 3d) are shifted
  - details often complicated, due to electron-electron-interaction and so called *"multiplet effects"* (not discussed here)



### Hexadecane $C_{16}H_{34}$ on a Cu surface

• Molecular orientation on the surface

This also works nicely in anisotropic single crystals





Tilt angle determined by the angular dependency of the XAS spectra

#### XAS: How to measure X-ray Absorption Spectroscopy

#### Lambert-Beer-Law:

$$I(E_{phot}) = I_0 \cdot e^{-\mu(E) \cdot d}$$

$$\Leftrightarrow \mu(E) = \frac{1}{d} \cdot \ln \frac{I_0}{I(E_{phot})}$$

$$\xi = \frac{1}{\mu(E)}$$
 = attenuation length,

### i.e. the length for 1/e intensity

Example: Fe metal (calculation without resonances and spin –orbit-splitting)

> Hard to measure below 3-5keV, due to the very short attenuation length → Other techniques to measure the absorption



L<sub>2,3</sub> edges

Length

3p or M<sub>23</sub> edges 2s or L<sub>1</sub> edge 100 100 104 Photon Energy (eV)

source: http://henke.lbl.gov/optical\_constants/

1s or

K edge

#### The absorption coefficient is often measured indirectly

• Example: Soft X-rays ~ 50-2000eV

**Idea:** Every additionally absorbed photon, for example due to the 2p→3d transition, produce additional electrons (Photo el., AUGER and secondaries) and **fluorescence photons** 

higher absorption  $\rightarrow$  more electrons (fluorescence photons)



#### **Total Fluorescence Yield (TFY)**



#### **Helical Undulator**

10<sup>8</sup> x more brilliance than x-ray tubes



#### **Global Synchrotron Density**



# For dynamic investigations $\rightarrow$ time structure of synchrotron radiation



### Now we go for Magnetism

- As magnetism is related to angular motion, why not using an "angular" probe?
- We will use circular polarized X-rays!

### XMCD: X-ray Magnetic Circular Dichroism

- In other words: Sample magnetization changes the absorption of X-rays
  - Sometimes a rather dramatic effect
- Pathway
  - What is XMCD?
  - How does it look like? Example: Fe Metal
  - How is it used? Quantitative! → sum rules
  - Can we understand this? Somehow!

Actually: First observed by Gisela Schütz in 1987 Director MPI for Intelligent Systems



## Again: How to get polarized X-rays?



2. Undulator



We also need "optical" components

approx. 1000 times higher brilliance

### How does it look exactly for soft x-rays

• typical setup for soft x-rays (100-2000eV)



Ultra-High-Vacuum! ≈10<sup>-10</sup> mBar





### X-ray magnetic circular dichroism: XMCD



#### Magneto-Optic-Effects: Origin (also for XMCD :=)

Start: Hunds rules Groundstate: Simplest example  $3d^1$ L = 2; S =  $\frac{1}{2}$  and J = L - S =  $\frac{3}{2}$ For T  $\rightarrow$  0 and B  $\rightarrow \infty$  only m<sub>J</sub> = -2 +  $\frac{1}{2}$  = - $\frac{3}{2}$  is occupied (saturated) Dipole-Selection-Rules:  $\Delta I = \pm 1 \rightarrow$  circular Pol.:  $\Delta m_J = \pm 1$ 



• This is a very general approach!

• Could be done in resonance or off resonance

Take home message: For circular polarization absorption is modified by magnetism!



Flipping the magnetization gives different excitation probabilities

### One example: SmCo<sub>5</sub> doped with some Fe



Schütz, Goering, Stoll, Int. J. Mat. Sci. 102 (2011) 773

- The magnetic moment of each element could be extracted separately
- Good for the understanding of magnetism in complex systems
- Sample has been modified to change the coercive behavior → Sm is responsible for that!



#### XMCD in 3d Transition Elements



Spin orbit splitting of 2p shell decreases from Cu to Ti Width increase → more unoccupied electrons

### Now it happens: Sum rules

#### VOLUME 70, NUMBER 5

PHYSICAL REVIEW LETTERS 1 Fi

pole  $[\sum_i \mathbf{s}_i - 3\hat{\mathbf{r}}_i(\hat{\mathbf{r}}_i \cdot \mathbf{s}_i)]_z$ ) that describe the magnetic field

generated by the valence electrons. Our results indicate that, besides  $\langle L_z \rangle$ , as described in Ref. [1], CMXD spec-

troscopy can provide an independent determination of the

ground-state expectation value of  $S_x$  [2]; this has been

tested using CMXD data, taken at the  $L_{2,3}$  edges of the

ferromagnetic metals Fe, Co, and Ni [3]. Furthermore,

valuable, site-specific information on the magnetic anisot-

1 FEBRUARY 1993 VO

#### X-Ray Circular Dichroism and Local Magnetic Fields

Paolo Carra,<sup>(1)</sup> B. T. Thole,<sup>(1),(2)</sup> Massimo Altarelli,<sup>(1)</sup> and Xindong Wang<sup>(3)</sup> <sup>(1)</sup>European Synchrotron Radiation Facility, BP 220, F-38043 Grenoble CEDEX, France <sup>(2)</sup>Department of Chemical Physics, Materials Science Center, University of Groningen, Nijenborgh 16, 9747 AG Groningen, The Netherlands <sup>(3)</sup>Ames Laboratory and Department of Physics and Astronomy, Iowa State University, Ames, Iowa 50011

(Received 13 July 1992) Sum rules are derived for the circular dichroic response of a core line (CMXD). They relate the in-

tensity of the CMXD signal to the ground-state expectation value of the magnetic field operators (orbital, spin, and magnetic dipole) of the valence electrons. The results obtained are discussed and tested for transition metals and rare earths.

PACS numbers: 78.70.Dm, 78.20.Ls

For circular dichroism in the x-ray region (CMXD), Thole *et al.* [1] have recently derived a new magnetooptical sum rule. It shows that, to a good approximation, the intensity of the CMXD signal, integrated over a complete core-level edge of a ferromagnet (or ferrimagnet), is proportional to the ground-state expectation value of the orbital angular momentum operator  $L_z$ . The derivation was carried out for electric dipole transitions in a local-

ized model, considering a single ion in crystal-field symmetry and including effects.

In this Letter we show that, within the work, another sum rule can be obtained. I CMXD signal, integrated over a single partr orbit-split core-level edge, to the ground-state value of the operators  $(L_z, \text{ total spin } S_z, \text{ and } S_z)$ 

$$\langle \Psi | r C_q^{(1)} | \Psi' j m \rangle = \sum_{\lambda \sigma} \langle \Psi | c_{jm}^{\dagger} | l_{\lambda \sigma} | \Psi' j m \rangle \langle c j n \rangle$$
$$= \sum_{\lambda \sigma} \langle \Psi | c_{jm}^{\dagger} | l_{\lambda \sigma} c_{jm} | \Psi' \rangle$$
$$\times \sum_{\gamma} (-)^{m-\gamma-1/2} \begin{bmatrix} 1/2 \\ \sigma \end{bmatrix}$$

The notation is as follows:  $c_{jm}^{\dagger}$  and  $l_{\lambda\sigma}^{\dagger}$  repr denotes a normalized spherical harmonic; [J] tion; and  $P_{cl} = \langle c || C^{(1)} || l \rangle R_{cl}$ . The total inte

694

$$I^{j} - \sum_{\Psi' m \lambda \sigma \lambda' \sigma'} \langle \Psi | c_{jm}^{\dagger} l_{\lambda \sigma} c_{jm} | \Psi' \rangle \langle \Psi' | c_{jm}^{\dagger} l_{\lambda \sigma}^{\dagger} c_{jm} | \Psi \rangle [j] \sum_{\gamma \gamma'} \begin{pmatrix} 1/2 & c & j \\ \sigma & \gamma & m \end{pmatrix} \begin{pmatrix} c & 1 & l \\ \gamma & q & \lambda \end{pmatrix} \begin{pmatrix} c & 1 & l \\ \gamma' & q & \lambda' \end{pmatrix} \begin{pmatrix} 1/2 & c & j \\ \sigma' & \gamma' & m \end{pmatrix} P_{cl}^{2}.$$

$$\tag{2}$$

In this expression, the final states can be removed by extending the set  $|\Psi'\rangle$  to the whole Hilbert space and using the closure relation. The added states give no contribution to  $I^{j}$ . Then, using a standard graphical notation for the angular factor [4], we have



#### VOLUME 70, NUMBER 5

#### PHYSICAL REVIEW LETTERS

1 FEBRUARY 1993

Transforming the diagonal matrix element by means of  $\{c_{jm}^{\dagger}, c_{jm}\} = 1$  and recoupling the angular part to obtain coupled tensor operators, one has the following:



with  $[a \cdots b] = (2a+1) \cdots (2b+1)$ . On the basis of expression (4) one can see that the total intensity  $I^{j}$  of the j edge is given by the ground-state expectation value of a linear combination of double tensors  $W^{(xy)x}$ , as defined by Judd [5]. of the triads  $(l \times l)$ , (1/2y l/2), and

We cant do this here in detail! This would take at least 3-4 times a 1.5h lecture!

 $\frac{(c+1)-2}{+1}\langle\Psi|S_{z}|\Psi\rangle$   $\frac{2}{-}\langle\Psi|T_{z}|\Psi\rangle\Big\{(P_{c}^{\pm})^{2}, \qquad (5)$ 

ion coefficient. artly filled spectator shell [1]; it can . In both cases only the *l* shell con-

tributes to  $\langle L_z \rangle$ ,  $\langle S_z \rangle$ , and  $\langle T_z \rangle$  (shell selectivity).

On the basis of our findings, one can view CMXD spectroscopy as a probe of the magnetic field of the valence electrons. The probe is *shell specific*; furthermore, the orbital and spin contributions can be separated: (i) Adding the two partners of a spin-orbit-split edge and normalizing to the unpolarized x-ray-absorption spectroscopy spectrum, one has

$$\rho = \int_{j_{+}+j_{-}} d\omega (\mu^{+} - \mu^{-}) \Big/ \int_{j_{+}+j_{-}} d\omega (\mu^{+} + \mu^{-} + \mu^{0}) = \frac{1}{2} \frac{l(l+1) + 2 - c(c+1)}{l(l+1)(4l+2-n)} \langle L_{z} \rangle, \tag{6}$$

yielding the ground-state expectation value of the orbital angular momentum per hole [1,6]. (ii) The ground-state expectation value of the spin-dependent part of the local magnetic field per hole is given by

$$\delta = \frac{\int_{j_+} d\omega (\mu^+ - \mu^-) - [(c+1)/c] \int_{j_-} d\omega (\mu^+ - \mu^-)}{\int_{j_++j_-} d\omega (\mu^+ + \mu^- + \mu^0)}$$
  
=  $\frac{l(l+1) - 2 - c(c+1)}{3c(4l+2-n)} \langle S_z \rangle + \frac{l(l+1)[l(l+1) + 2c(c+1) + 4] - 3(c-1)^2(c+2)^2}{6lc(l+1)(4l+2-n)} \langle T_z \rangle.$  (7)

To obtain expressions (6) and (7) we neglected relativistic corrections to the radial part and set  $P_{cl}^+ = P_{cl}^-$ ; this approxi-

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T. Thole, P. Carra et al. : PRL 86 (1992) 1943 ; PRL 70 (1993) 694



Röntgenenergie E,

### XMCD is famous because its quantitative: Sum-Rules



Theoretical prediction: T. Thole, P. Carra *et al.* : PRL **86** (1992) 1943 ; PRL **70** (1993) 694

Exp. verification and rough procedure: C.T. Chen et al, PRL 75 (1995) 152

## Data measurement and analysis: Co thin film!

Measure sample current  ${\rm I}_1$  and incoming intensity  $~{\rm I}_0$  for north and south field

4,5 -Co 2p > 3d140 Co 2p > 3d 130 L<sub>2,3</sub> South L<sub>2.3</sub> 120 4,0 North 110 100 I<sub>0</sub>,I<sub>1</sub> current (pA) 3.5 -90 1<sup>1</sup>0 80 -70 3,0 60 50 40 -2,5 30 only north 20 -2,0 10 -0 -770 780 790 800 810 820 740 750 760 770 780 790 800 810 820 830 Energy (eV) Energy (eV)

**Step 1:** Divide them  $I_1/I_0$ 

north and south means field orientation with respect to the photon beam!

**Step 2:** Remove "offset" by a simple factor

Important: Make sure that pre- and Post-Edge region (without XMCD) are equal



Here the factor is 1.04

**Step 3:** Subtract background by a linear approximation Important: Exactly the same for north and south spectra



**Step 4:** Devide by post edge value to normalize

Important: Exactly the same value for north and south spectra



Now the data is so called edge normalized!

**Step 5:** Plot together with difference XMCD= North-South



**Step 6:** For **sum rule** analysis remove non resonant background and calculate the "non magnetic" average. This does not change XMCD signal



**Step 7:** Calculate the integrals for XAS (= nonmagnetic) and XMCD



### Data measurement and analysis Step 8: Sum Rules Calculation: Use values in formula



XAS = 13.77= XMCD (L<sub>3</sub>)= -3.684 = XMCD (L<sub>2</sub>)= 2.515 =  $1-n_{34}$ (Co)=2.49

$$\langle L_z \rangle = -\frac{4}{3} \cdot \frac{-3.64 + 2.515}{2 \cdot 13.77} \cdot 2.49 = 0.14$$

$$\langle S_z \rangle + 7 \cdot \langle T_z \rangle = -\frac{-3.64 - 2 \cdot 2.515}{2 \cdot 13.77} \cdot 2.49 = 0.785$$

#### **Step 9:** Correct for finite degree of circular polarization

Depends on Energy, setup, beamline, source as bending or undulator etc. → usually ask the beamline responsible

In our case here 84%!

Using the g-factor of 2 for the spin and transfer from angular momenta to magnetic moments

$$\langle m_L \rangle_z = \frac{\langle L_z \rangle}{0.84} \cdot \mu_B = \frac{0.14}{0.84} \ \mu_B = \underbrace{0.17 \ \mu_B}_{======} \qquad \langle m_S \rangle_z = 2 \cdot \frac{\langle S_z \rangle}{0.84} \cdot \mu_B = 2 \cdot \frac{0.785}{0.84} \cdot \mu_B = 1.87 \ \mu_B$$

The deviation here is because of Tz!

Element	exp. (XMCD)		theo.	
	m <sub>s</sub> (μ <sub>B</sub> )	m <sub>ι</sub> (μ <sub>в</sub> )	m <sub>s</sub> (μ <sub>B</sub> )	m <sub>l</sub> (μ <sub>B</sub> )
Fe Chen PRL 75	1.98	0.085	2.19	≈ 0.059
CO Chen PRL 75	1.55	0.153	1.57	≈ 0.087
Ni Dhesi PRB 60	0.58	0.07	0.58	≈ 0.06

Sum-Rules Hands On

• Try to estimate the areas using a rule and a pen.



 $\langle L_{\underline{i}} \rangle = -\frac{4}{3} \cdot -$ 

 $(10 - n_{3d}) \cdot \mu_B$ 

Estimating area by FWHM x Height or as you want



Typical pitfall: Offset corrected with wrong factor



Best visible in a finite slope in the XMCD integral If present → better factor

### Why using a single factor for Offset correction?

Electron current depends on B-field dependent proportionality.

#### Could be asymmetric



$$I(E_{phot}, B) = f(B) \cdot \mu(E_{phot}, B)$$

$$\mu(E_{phot}, B^{+}) = \mu_{0}(E_{phot}) + \mu_{c}(E_{phot}, |B|)$$

$$\mu(E_{phot}, B^{-}) = \mu_{0}(E_{phot}) - \mu_{c}(E_{phot}, |B|)$$

$$\Delta I(E_{phot}; B) = f(B^{+}) \cdot [\mu_{0}(E_{phot}) + \mu_{c}(E_{phot}, |B|)] - f(B^{-}) \cdot [\mu_{0}(E_{phot}) - \mu_{c}(E_{phot}, |B|)]$$

$$= [f(B^{+}) - f(B^{-})] \cdot \mu_{0}(E_{phot}) + [f(B^{+}) + f(B^{-})] \cdot \mu_{c}(E_{phot}, |B|)$$
if  $f(B^{+}) = f(B^{-}) = f(B)$ :
$$\Delta I(E_{phot}; B) = 2 \cdot f(B) \cdot \mu_{c}(E_{phot}, |B|)$$

if  $f(B^+) \neq f(B^-)$  choose k as  $= f(B^+) = k \cdot f(B^-)$ 

As  $\mu_0$  is not a straight line, a line offset subtraction is wrong!

E. Goering et al., J.Sync.Rad. 8 (2001) 434-436 and J. Appl. Phys. 88 (2000) 5920

### Sum Rules: In general for all edges!



d

7/3

2

From Schütz, Stoll, and Goering Handbook of Magnetism (Wiley) based on T. Thole, P. Carra *et al.* : PRL **86** (1992) 1943 ; PRL **70** (1993) 694

What is this  $T_z$ ? perturbation theory provides:  $T_z \approx -\frac{2}{7} \cdot \mathbf{Q} \cdot \hat{\mathbf{S}}$ 

G. van der Laan, J. Phys.: Condens. Matter **10** (1998) 3239

Q: quadrupolar charge distribution traceless tensor 2<sup>nd</sup> order



Is important in less than cubic systems, with oriented crystals, in 4f metals, and in ultra thin films and interfaces

Something more about Tz: König and Stöhr, PRL **75** (1995) 3748; Buck and Fähnle, JMMM **166** (1997) 297

### Further "Problems"

 For the light 3d transition metals, its hard to separate P<sub>3/2</sub> and P<sub>1/2</sub> excitations → excitations "mix"

see: E. Goering, Phil. Mag. 85 (2005) 2897-2911 and references therein

• In 4f systems, as supermagnets, the spin-sum-rule is not "simply" valid anymore (orbital works fine)

see: Y. Teramura et al, J.Phys.Soc **65** (1996) 3056 and T. Jo, J.El.Spec.Rel.Phenom, **86** (1997) 73

• Actually, we are working on this at the moment, and it looks to be solvable, at least in a practical way.

2013 we could inaugurate our "new" 7T XMCD system!



### XMCD at the "recent" limit: 0.2ML paramagnetic Ni on Graphen



*In-situ prepared* Ni nanostructures(3nm height) :0.2 ML nominal (@ 200 K) onGraphen/Ir Moiré-template

Cooperation with group of M. Fonin, Univ.- Konstanz



Sicot et. al.: APPLIED PHYSICS LETTERS **96**, 093115 2010

### Questions:

1: Can we distinguish between pinned and rotatable moments?

2: Do we get a XMCD signal for a sample with permanent magnetic moments but disordered?

3: What do we get, if we have the same magnetic atoms, but half the amount? As Fe-XMCD for Fe → FeCo alloy



X-ray magnetic circular dichroism: XMCD