

Simple views on magnetization processes

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Dear Institute,

*I've always had a fascination with electromagnetism, and have pondered the theories of gravity. One thing I've come across in preliminary research is that **the current theories largely fail to include human element in**, as if we're just baseless objects trapped here without a role in the ultimate reason. (...)*

*Humans are magnets, too, as we possess iron. (...) If you take two magnets, they stick together when proper polars are placed near each other. What causes humans to act as the 2nd magnet in gravity is the iron found in humans. Earth, obviously the big magnet with the most iron, is able to control humans, the far smaller magnet with less iron. (...) **Ultimately there is one controlling magnet for the entire universe somewhere in space holding it all together, like Galileo said.***

*Calculations of Earth's maximum gravitation pull could be made by **testing individual boosters on humans and converting the thrust needed into some kind of formula which returns Earth's magnetic energical pull.** (...) While it doesn't conclude why other things on Earth are in the same situation as us, it is also based on magnetism and humans have to have their own role in the matter.*

***Further research into it needs to be done** as these are very preliminary original thoughts.*

Regards,

XXX YYY.

Manipulation of magnetic materials:

↪ Application of a magnetic field

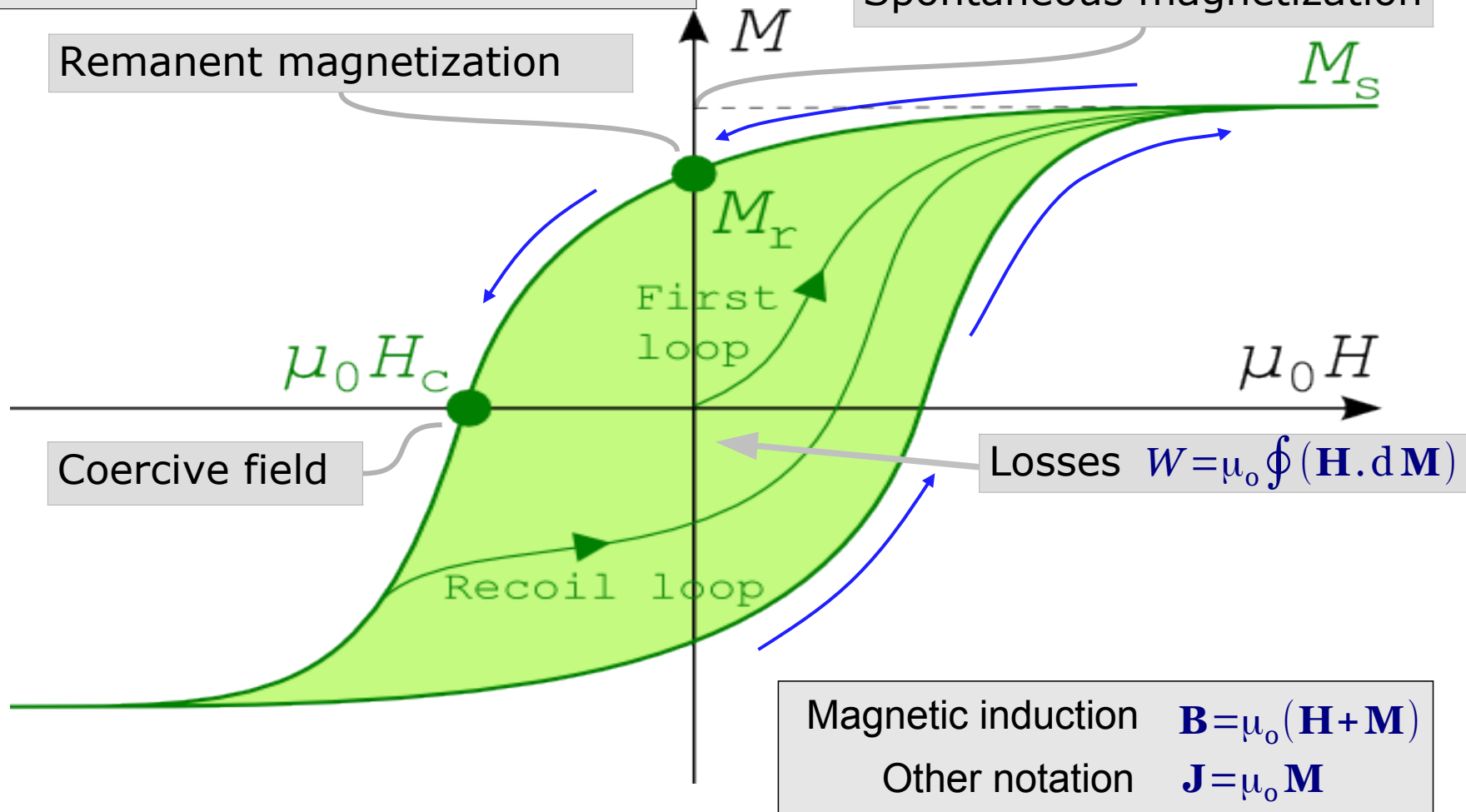
Zeeman energy: $E_Z = -\mu_0 \mathbf{H} \cdot \mathbf{M}$



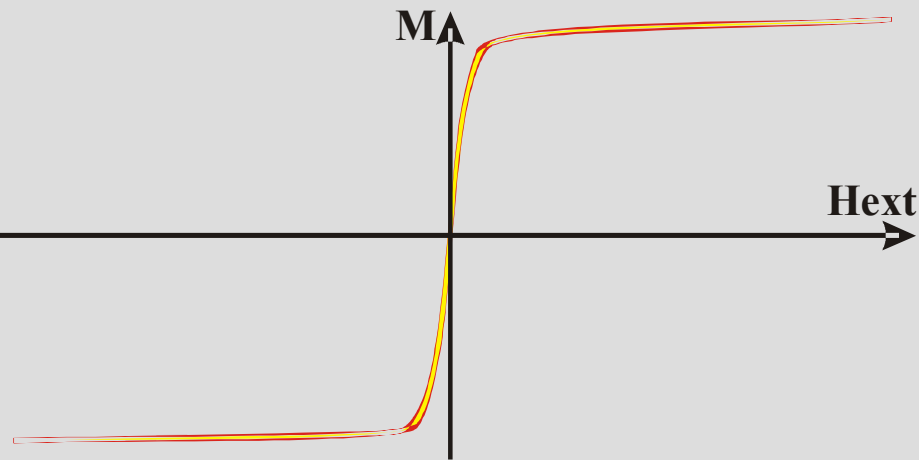
Spontaneous $\neq$ **S**aturation

Spontaneous magnetization

Remanent magnetization



Soft materials

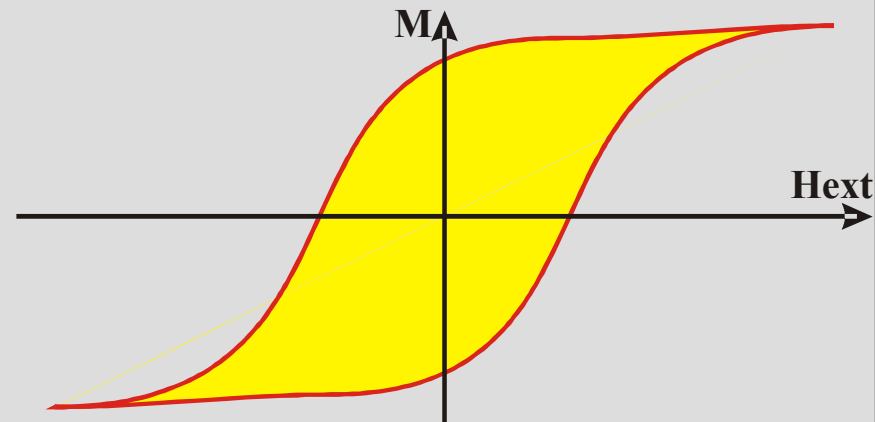


Transformers

Flux guides, sensors

Magnetic shielding

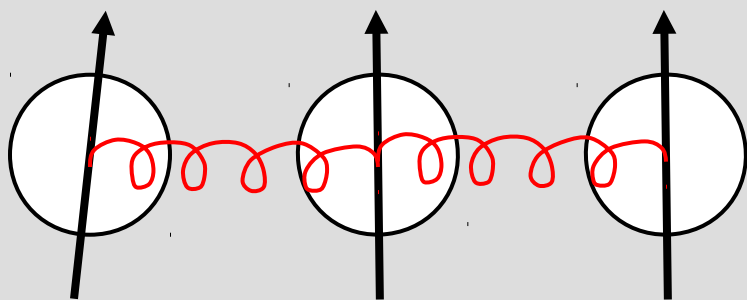
Hard materials



Permanent magnets, motors

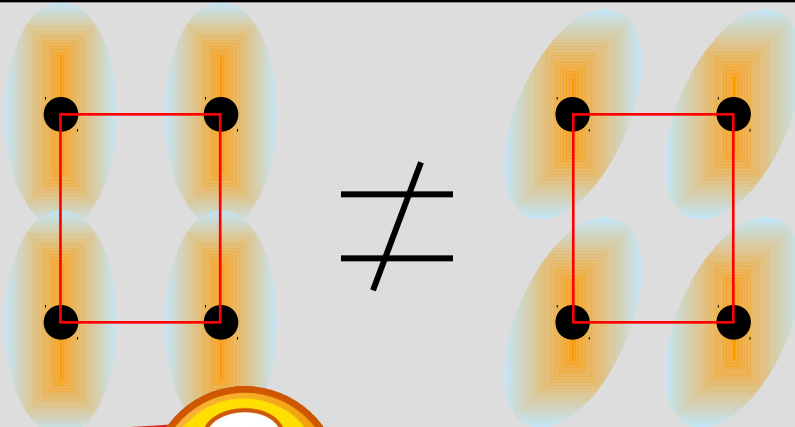
Magnetic recording

Exchange energy



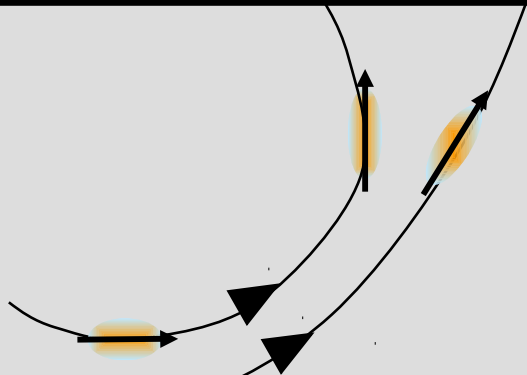
$$E_{\text{ex}} = A (\nabla \cdot \mathbf{m})^2$$

Magnetocrystalline anisotropy energy



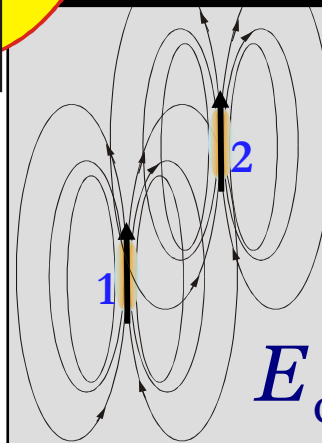
$$E_{\text{mc}} = K \sin^2 \theta$$

Zeeman energy ($\rightarrow$ enthalpy)



$$E_d = -\mu_0 \mathbf{M} \cdot \mathbf{H}$$

Magnetostatic energy



$$E_d = -\frac{1}{2} \mu_0 \mathbf{M} \cdot \mathbf{H}_d$$

Anisotropy exchange length

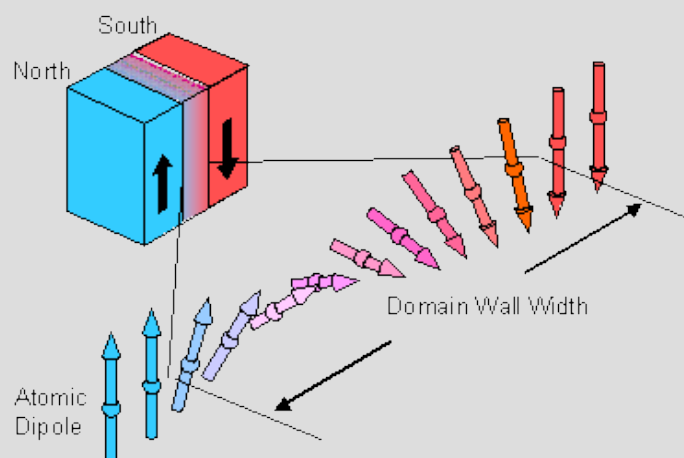
$$E = A (\partial_x \theta)^2 + K \sin^2 \theta$$

Exchange
→ J/m

Anisotropy
→ J/m³

Anisotropy exchange length: $\Delta_u = \sqrt{A/K}$

$\Delta_u \approx 1 \text{ nm} \rightarrow \Delta_u \geq 100 \text{ nm}$
Hard Soft



Often called *Bloch parameter* or *domain-wall width*

Dipolar exchange length

$$E = A (\partial_x \theta)^2 + K_d \sin^2 \theta$$

Exchange
→ J/m

Dipolar energy
→ J/m³

$$K_d = \frac{1}{2} \mu_0 M_s^2$$

Dipolar exchange length:

$$\Delta_d = \sqrt{A/K_d} = \sqrt{2A/\mu_0 M_s^2}$$

$$\Delta_d \approx 3 - 10 \text{ nm}$$

Single-domain critical size relevant for nanoparticles made of soft magnetic material



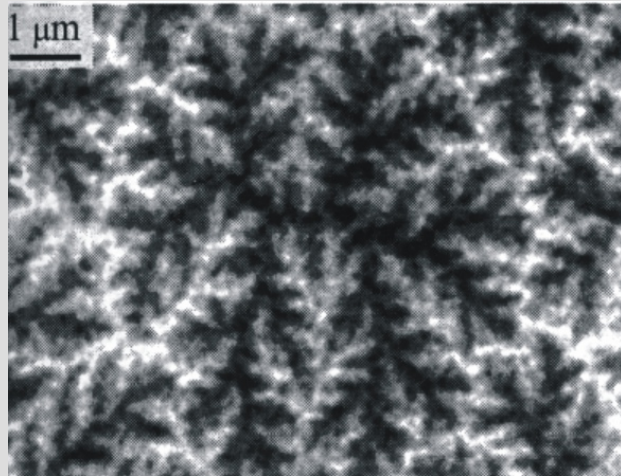
Often called *Exchange length*

Notice:

Other length scales: with field etc.

Bulk material

Numerous and complex magnetic domains

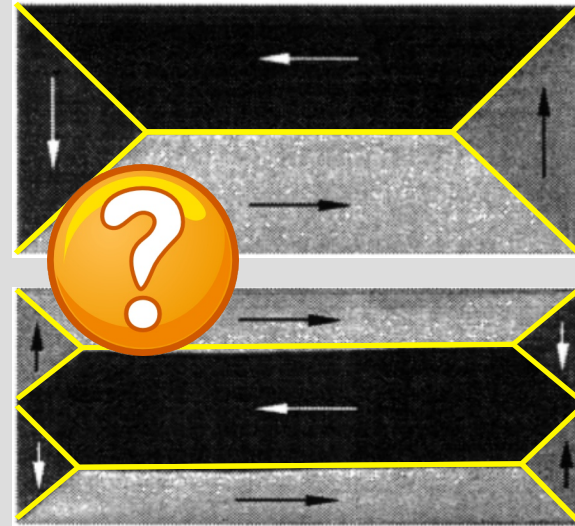


Co(1000) crystal – SEMPA

A. Hubert, *Magnetic domains*

Mesoscopic scale

Small number of domains, simple shape

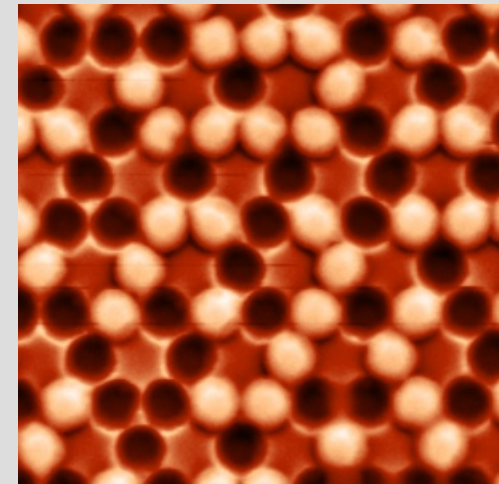


Microfabricated dots
Kerr magnetic imaging

A. Hubert, *Magnetic domains*

Nanometric scale

Magnetic single-domain



Nanofabricated dots
MFM

Sample courtesy:

N. Rougemaille, I. Chioar

Nanomagnetism ~ mesoscopic magnetism

Framework

Approximation: $\partial_r \mathbf{m} = \mathbf{0}$ (uniform magnetization)
(strong!)

$$\mathcal{E} = EV = V [K_{\text{eff}} \sin^2 \theta - \mu_0 M_s H \cos(\theta - \theta_H)]$$

$$K_{\text{eff}} = K_{\text{mc}} + K_d$$

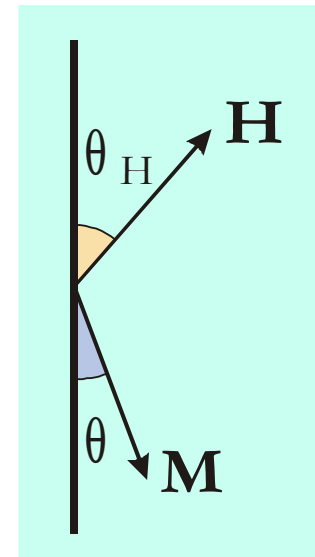
Dimensionless units:

$$e = \mathcal{E} / KV$$

$$h = H / H_a$$

$$H_a = 2K / \mu_0 M_s$$

$$e = \sin^2 \theta - 2h \cos(\theta - \theta_H)$$



L. Néel, *Compte rendu Acad. Sciences* 224, 1550 (1947)

E. C. Stoner and E. P. Wohlfarth, *Phil. Trans. Royal. Soc. London* A240, 599 (1948)

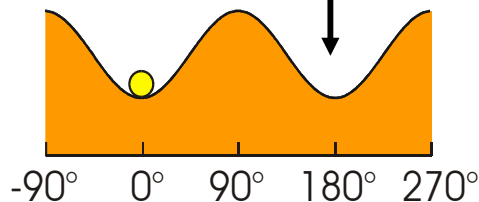
***IEEE Trans. Magn.* 27(4), 3469 (1991) : reprint**

Names used

- ➡ Uniform rotation / magnetization reversal
- ➡ Coherent rotation / magnetization reversal
- ➡ Macrospin etc.

Example for $\theta_H = 180^\circ \longrightarrow e = \sin^2 \theta + 2h \cos \theta$

$H > 0$



Equilibrium states

$$\partial_\theta e = 2 \sin \theta (\cos \theta - h)$$

$$\partial_\theta e = 0 \longrightarrow$$

$$\cos \theta_m = h$$

$$\theta \equiv 0 [\pi]$$

Stability

$$\partial_{\theta\theta} e = 2 \cos 2\theta - 2h \cos \theta$$

$$= 4 \cos^2 \theta - 2 - 2h \cos \theta$$

$$\partial_{\theta\theta} e(0) = 2(1-h)$$

$$\partial_{\theta\theta} e(\theta_m) = 2(h^2 - 1)$$

$$\partial_{\theta\theta} e(\pi) = 2(1+h)$$

Energy barrier

$$\Delta e = e(\theta_{\max}) - e(0)$$

$$= 1 - h^2 + 2h^2 - 2h$$

$$= (1-h)^2$$

Switching

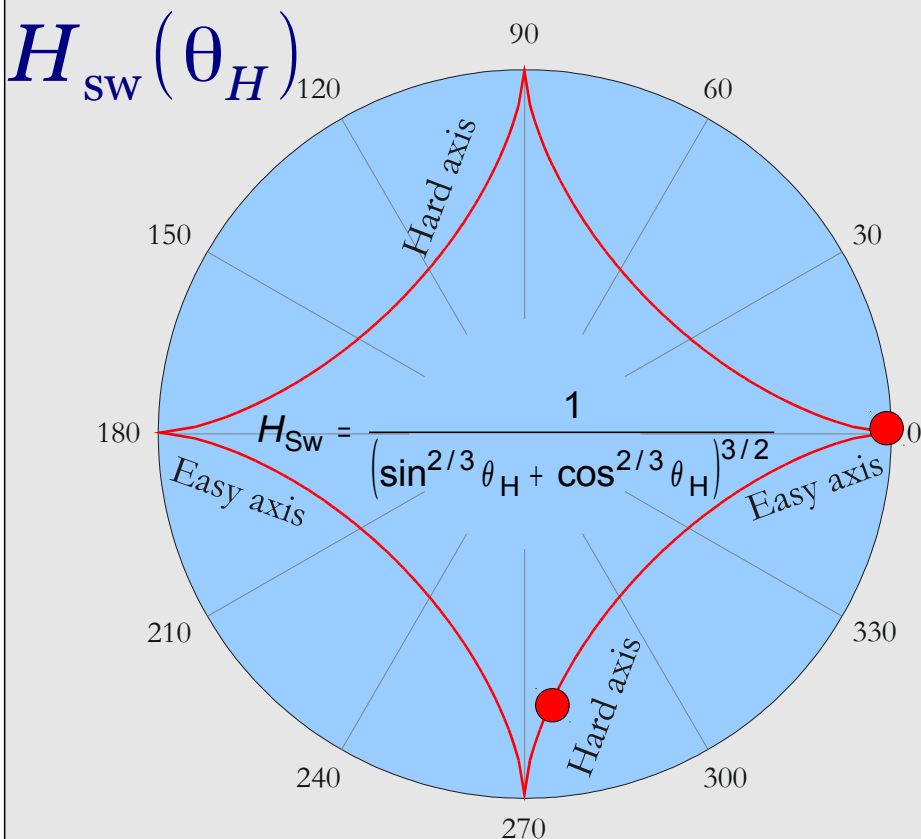
$$h = 1$$

$$H = H_a = 2K / \mu_0 M_S$$

$(1-h)^\alpha$ with exponent 1.5 in general

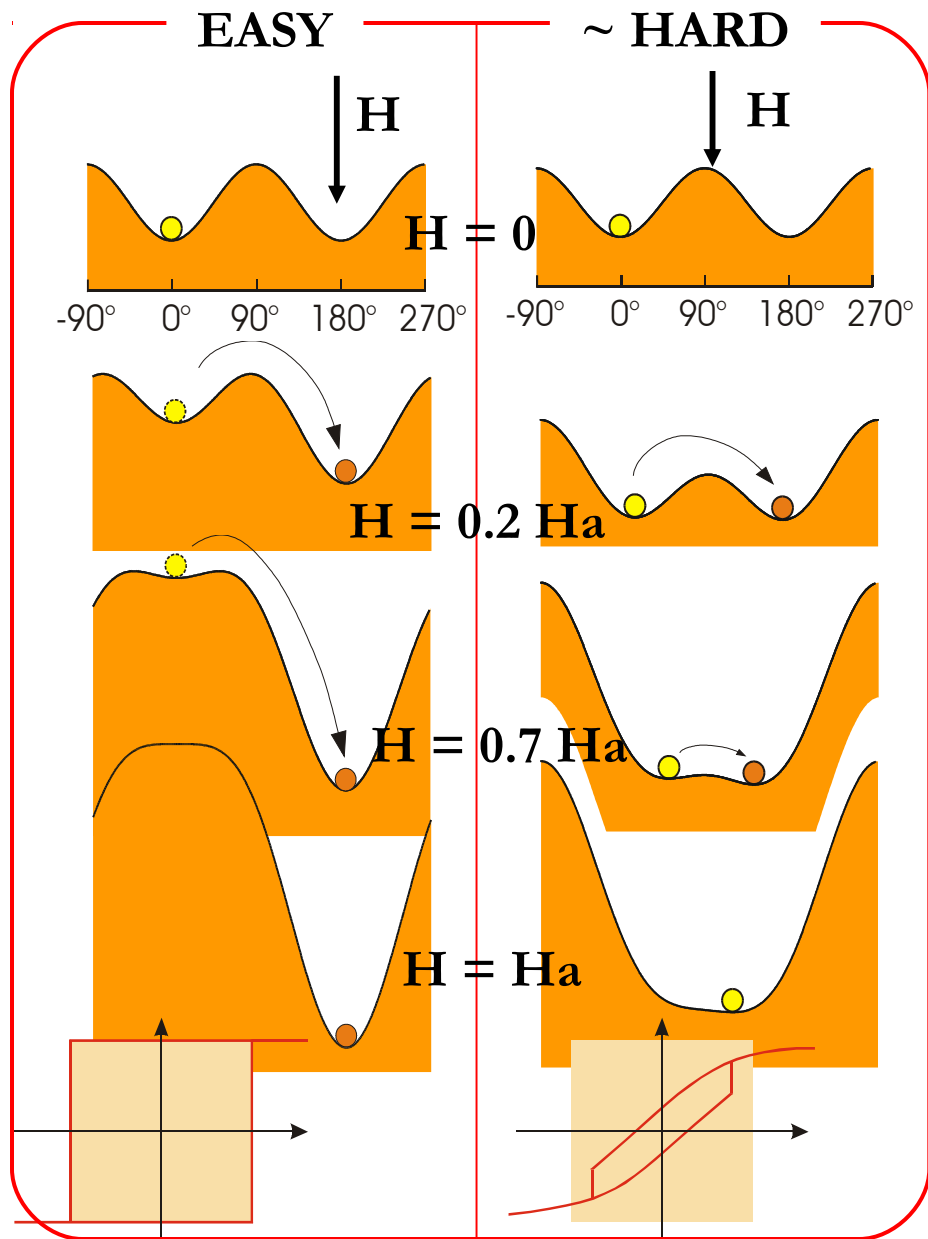


'Astroid' curve



➤ $H_{sw}(\theta)$ is a one signature of reversal modes

J. C. Slonczewski, Research Memo RM
003.111.224, IBM Research Center (1956)



Switching field = Reversal field

A value of field at which an irreversible (abrupt) jump of magnetization angle occurs.

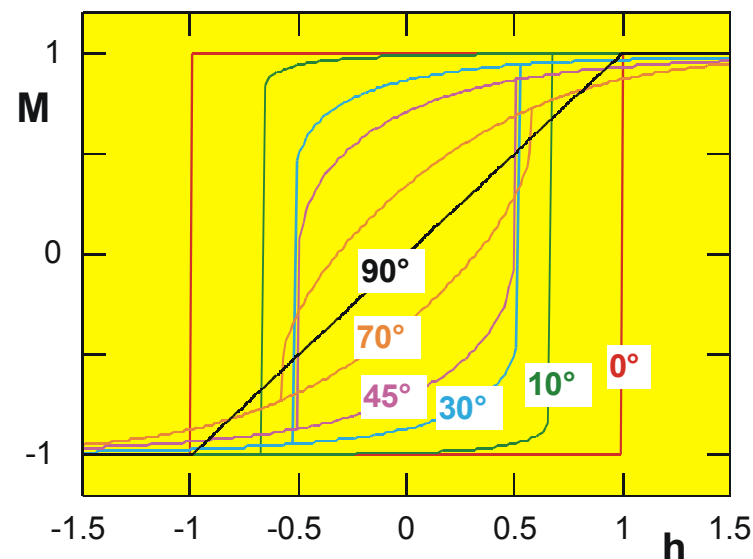
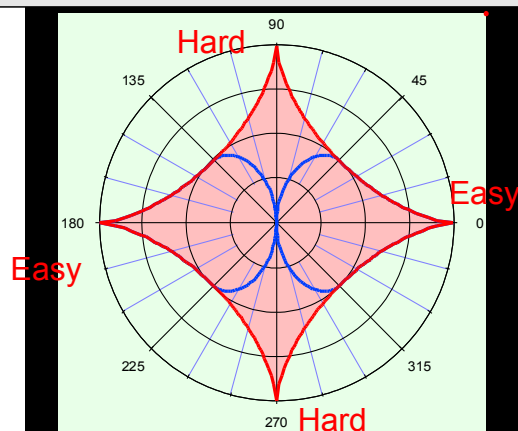
Can be measured only in single particles.

Coercive field

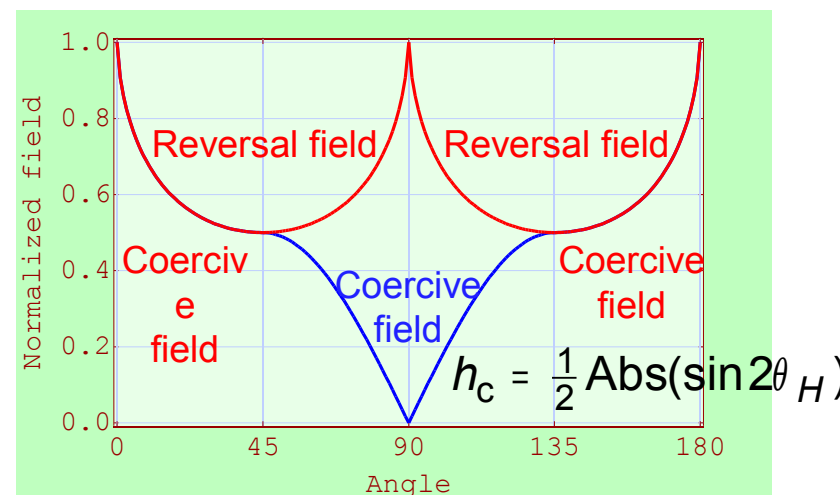
The value of field at which $\mathbf{M} \cdot \mathbf{H} = 0$ ($\theta = \theta_H \pm \pi/2$)

A quantity that can be measured in real materials (large number of 'particles').

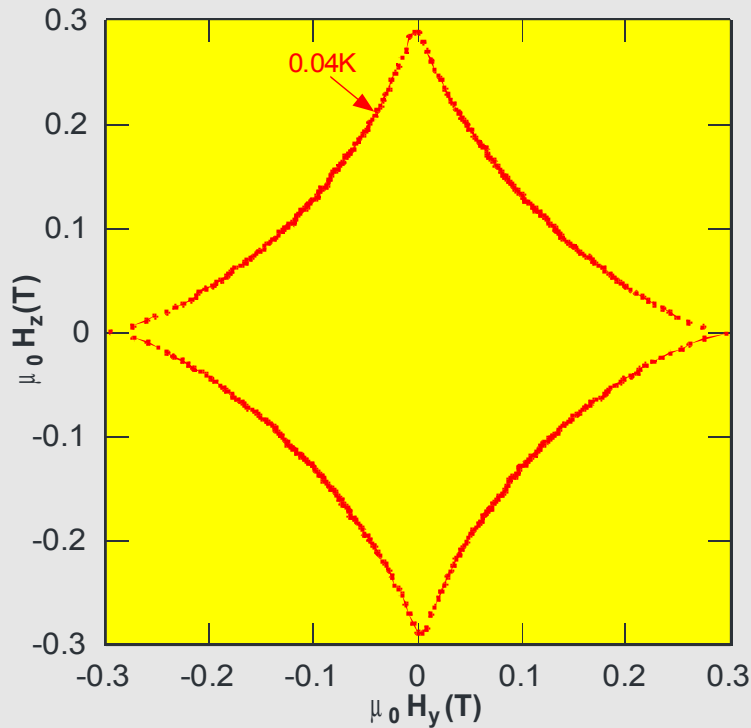
May be or may not be a measure of the mean switching field at the microscopic level



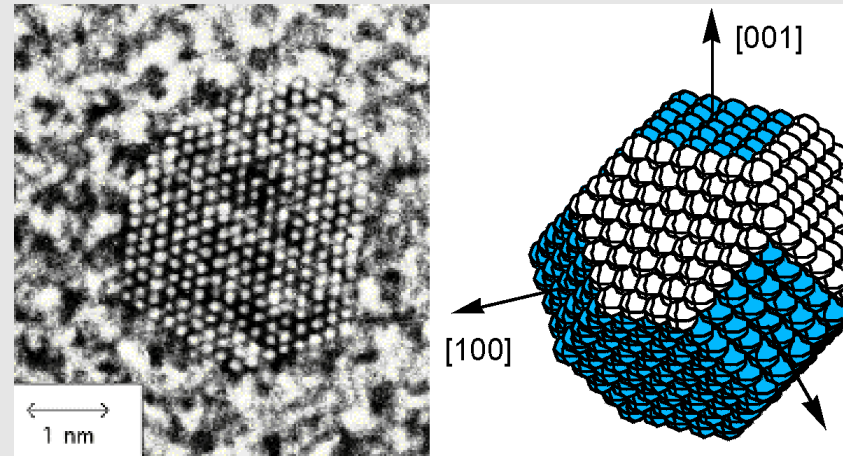
$$h_{Sw} = \frac{1}{(\sin^{2/3} \theta_H + \cos^{2/3} \theta_H)^{3/2}}$$



Experimental evidence

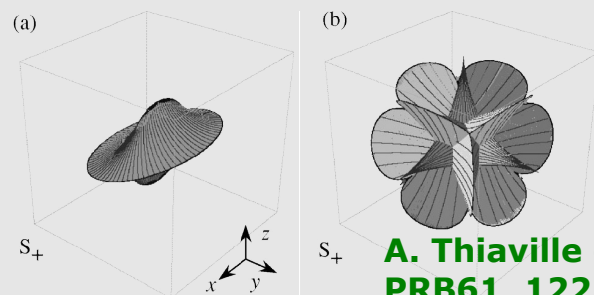


**First evidence: W. Wernsdorfer et al.,
Phys. Rev. Lett. 78, 1791 (1997)**

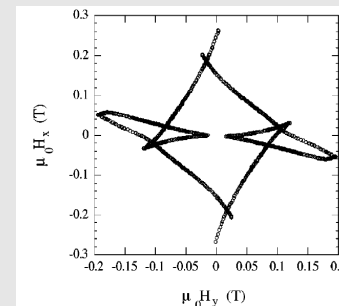


M. Jamet et al., Phys. Rev. Lett., 86, 4676 (2001)

Extensions: 3D, arbitrary anisotropy etc.



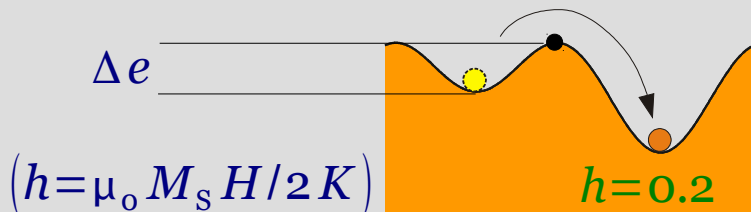
**A. Thiaville et al.,
PRB61, 12221 (2000)**



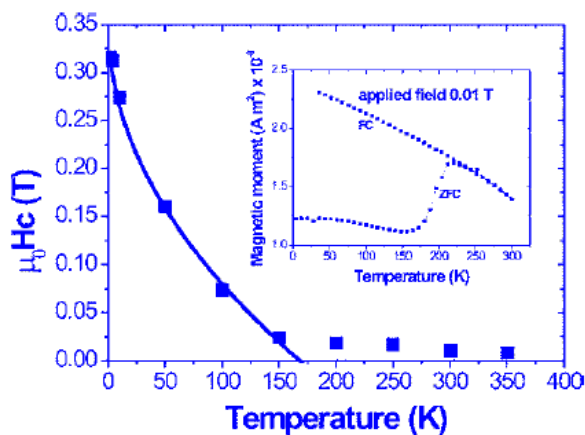
**M. Jamet et al., PRB69,
024401 (2004)**

Barrier height

$$\Delta e = e(\theta_{\max}) - e(0) = (1-h)^2$$



J. Appl. Phys. **99**, 08Q514 (2006)



Thermal activation

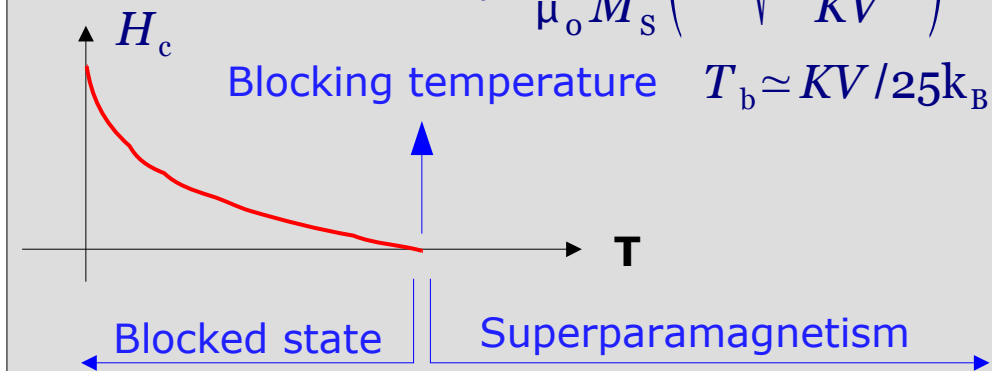
Brown, Phys.Rev.130, 1677 (1963)

$$\tau = \tau_0 \exp\left(\frac{\Delta \mathcal{E}}{k_B T}\right) \quad \Rightarrow \quad \Delta \mathcal{E} = k_B T \ln(\tau / \tau_0)$$

$$\tau_0 \approx 10^{-10} \text{ s}$$

Lab measurement: $\tau \approx 1 \text{ s} \Rightarrow \Delta \mathcal{E} \approx 25 k_B T$

$$\Rightarrow H_c = \frac{2K}{\mu_0 M_s} \left(1 - \sqrt{\frac{25 k_B T}{KV}}\right)$$



E. F. Kneller, J. Wijn (ed.) Handbuch der Physik XIII/2: Ferromagnetismus, Springer, 438 (1966)

M. P. Sharrock, J. Appl. Phys. 76, 6413-6418 (1994)

Notice, for magnetic recording : $\tau \approx 10^9 \text{ s}$ $KV_b \approx 40 - 60 k_B T$

Formalism

C. P. Bean & J. D. Livingston, J. Appl. Phys. 30, S120 (1959)

Energy

$$E = KV.f(\theta, \varphi) - \mu_0 \mu H$$

Partition function

$$Z = \sum \exp(-\beta E)$$

Average moment

$$\langle \mu \rangle = \frac{1}{\beta \mu_0 Z} \frac{\partial Z}{\partial H}$$

Isotropic case

$$Z = \int_{-M}^M \exp(-\beta E) d\mu$$

Note: equivalent to integration over solid angle

$$\langle \mu \rangle = M [\coth(x) - 1/x]$$

Langevin function

Note:

Use the moment M of the particle, not spin $1/2$.

$$x = \beta \mu_0 M H$$

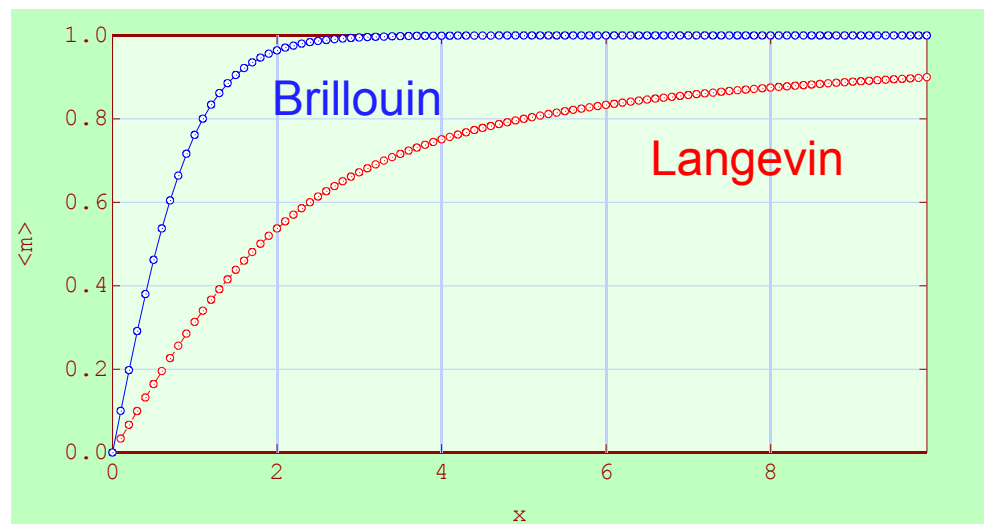


Infinite anisotropy

$$Z = \exp(\beta \mu_0 M H) + \exp(-\beta \mu_0 M H)$$

$$\langle \mu \rangle = M \tanh(x)$$

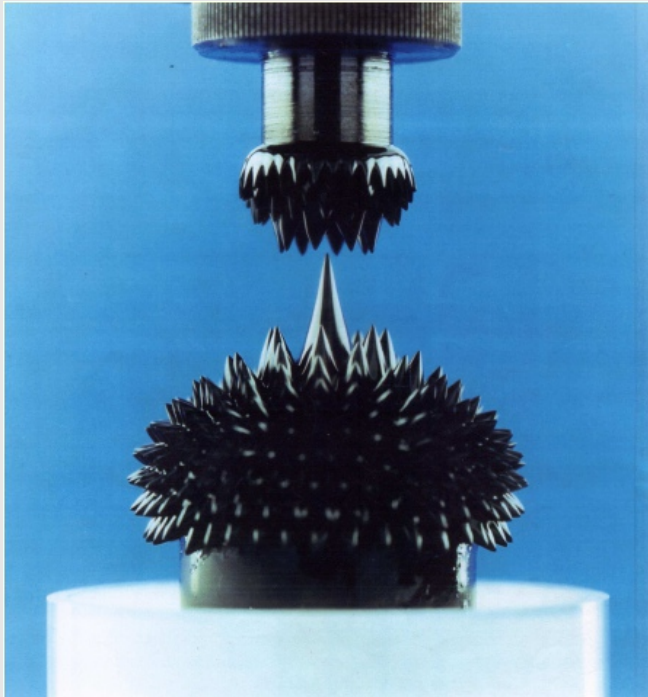
Brillouin $1/2$ function



Ferrofluids

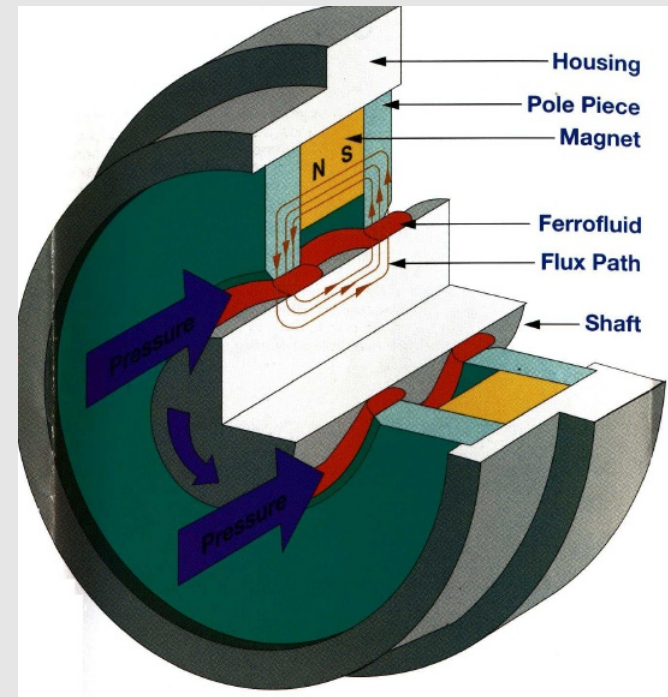
⇒ Principle

Surfactant-coated nanoparticles,
preferably superparamagnetic
→ Avoid agglomeration of the particles
→ Fluid and polarizable



⇒ Example of use

Seals for rotating parts



**R. E. Rosensweig, Magnetic fluid seals,
US patent 3,260,584 (1971)**

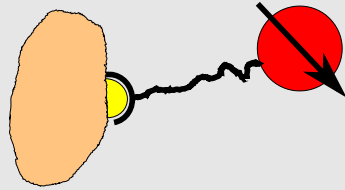
<http://esm.neel.cnrs.fr/2007-cluj/slides/vekas-slides.pdf>

Health and biology

Beads = coated nanoparticles,
preferably superparamagnetic
→ Avoid agglomeration of the particles

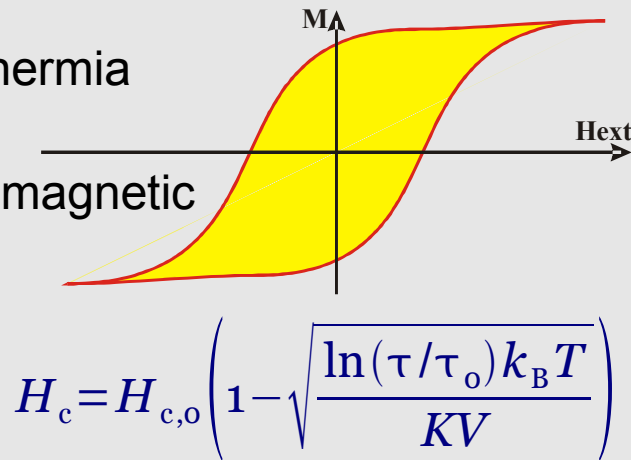
⇒ Cell sorting

$$\mathbf{F} = \nabla \mu \cdot \mathbf{B}$$

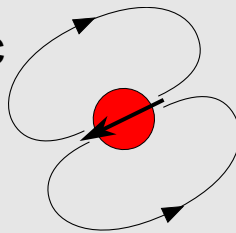


⇒ Hyperthermia

Use ac magnetic
field



⇒ Contrast agent in Magnetic
Resonance Imaging (MRI)



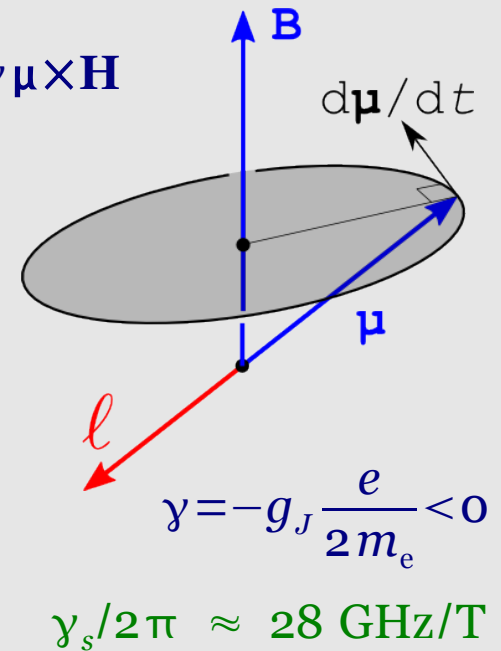
RAM (radar absorbing materials)

⇒ Principle

Absorbs energy at a well-defined
frequency (ferromagnetic
resonance)

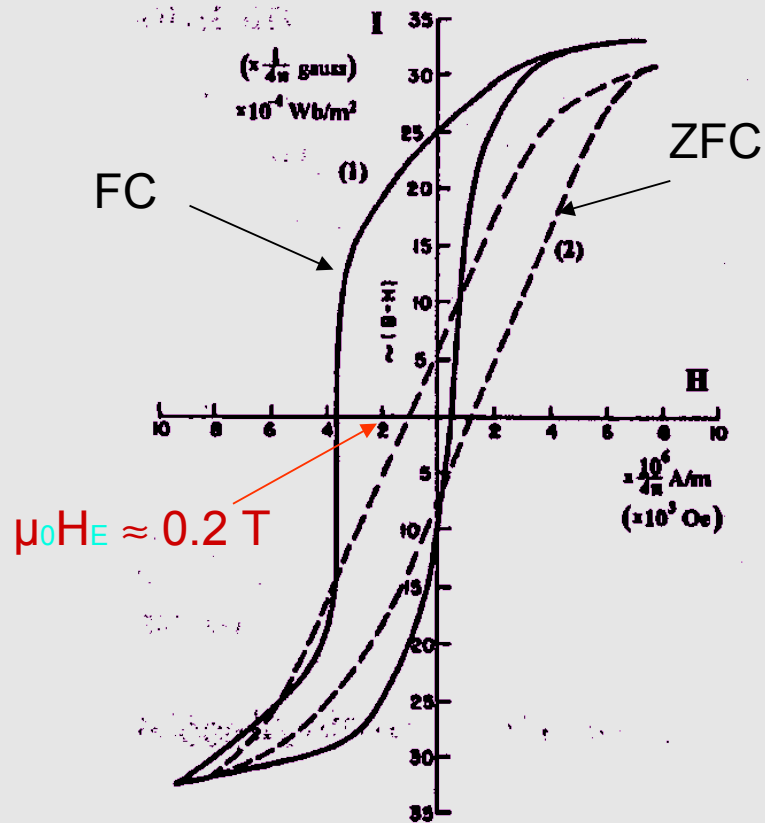
$$\Rightarrow \frac{d\ell}{dt} = \Gamma = \mu_0 \mu \times \mathbf{H} = \mu_0 \gamma \ell \times \mathbf{H}$$

$$\Rightarrow \frac{d\mu}{dt} = \mu_0 \gamma \mu \times \mathbf{H}$$



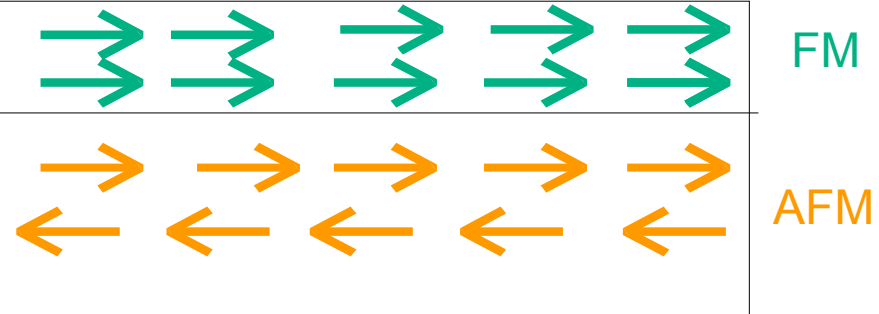
Seminal studies

Oxidized Co nanoparticles



Meiklejohn and Bean,

Phys. Rev. 102, 1413 (1956),
 Phys. Rev. 105, 904, (1957)



Field-cooled hysteresis loops:

- Increased coercivity
- Loop shifted along field axis

Exchange bias

J. Nogués and Ivan K. Schuller
 J. Magn. Magn. Mater. 192 (1999) 203

Exchange anisotropy—a review

A E Berkowitz and K Takano
 J. Magn. Magn. Mater. 200 (1999)

Increase coercivity of layers

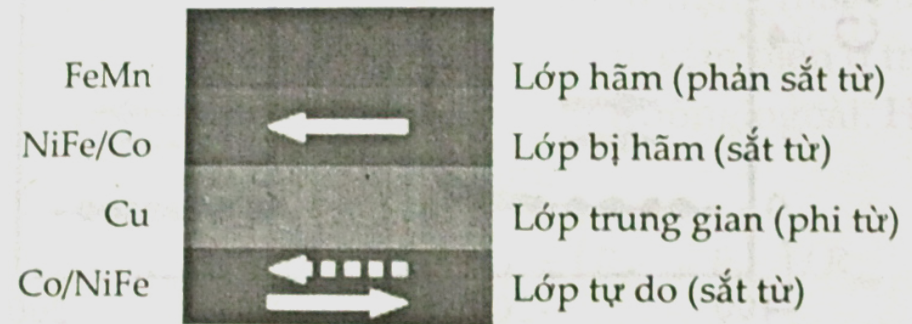


Crude approximation for thin layers:

$$H_{F-AF} \approx H_F \left(1 + \frac{K_{AF} t_{AF}}{K_F t_F} \right)$$

Application

Concept of spin-valve in magneto-resistive elements



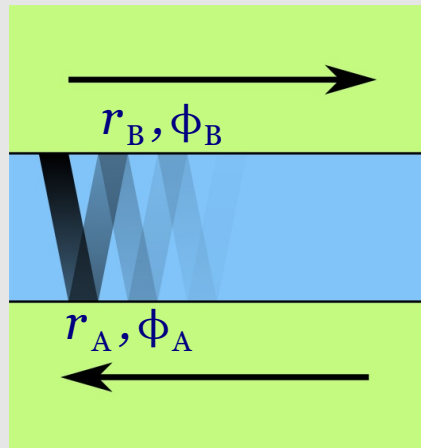
B. Diény et al., Phys. Rev. B 43, 1297 (1991)

- ⇒ Sensors
- ⇒ Memory cells
- ⇒ Etc.



The physics

Spin-dependent quantum confinement in the spacer layer



Forth & back
phase shift
 $\Delta\phi = q t + \phi_A + \phi_B$

Spin-independent

$$q = k^+ - k^-$$

Spin-dependent

$$r_A, \phi_A, r_B, \phi_B$$

Figures

Constructive and destructive interferences

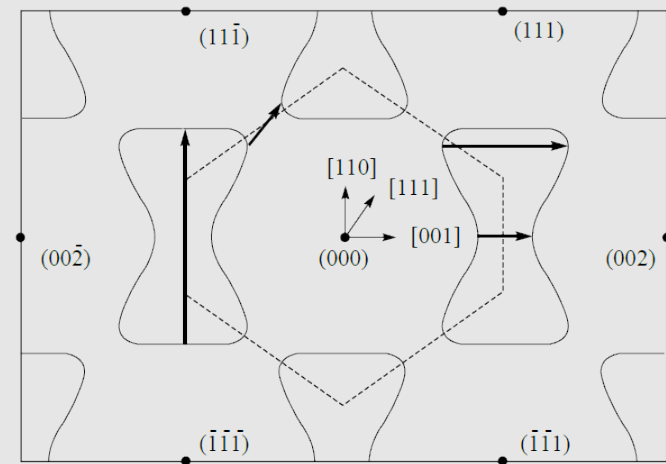
⇒ Maxima and minima of $n(\epsilon)$

Coupling strength:

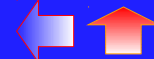
$$E_s = J(t) \cos \theta \quad \text{in } J/\text{m}^2$$

$$\theta = \langle m_1, m_2 \rangle$$

$$\text{with: } J(t) = \frac{A}{t^2} \sin(q_\alpha t + \Psi)$$



P. Bruno, J. Phys. Condens. Matter 11, 9403 (1999)



Ti 	V 		Cr 		Mn 	Fe 	Co 	Ni 	Cu 		
No Coupling	9	3	7	7		Ferro-Magnet	Ferro-Magnet	Ferro-Magnet	8	3	
	0.1	9	.24	18					0.3	10	
2.89	2.62		2.50		2.24	2.48	2.50	2.49	2.56		
Zr 	Nb 		Mo 		Tc 	Ru 	Rh 	Pd 	Ag 		
No Coupling	9.5	2.5	5.2	3		3	3	7.9	3	No Coupling	No Coupling
	.02	*	.12	11		5	11	1.6	9		
3.17	2.86		2.72		2.71	2.65	2.69	2.75	2.89		
Hf 	Ta 		W 		Re 	Os 	Ir 	Pt 	Au 		
No Coupling	7	2	5.5	3	4.2	3.5		4	3	No Coupling	No Coupling
	.01	*	.03	*	.41	10		1.85	9		
3.13	2.86		2.74		2.74	2.68	2.71	2.77	2.88		

fcc bcc
 hcp complex cubic

Element	
A_1 (Å)	ΔA_1 (Å)
J_1 (erg/cm ²)	P (Å)
r_{ws} (Å)	

$$J(t) = \frac{A}{t^2} \sin\left(\frac{2\pi t}{P} + \Psi\right)$$

Illustration of coupling strength

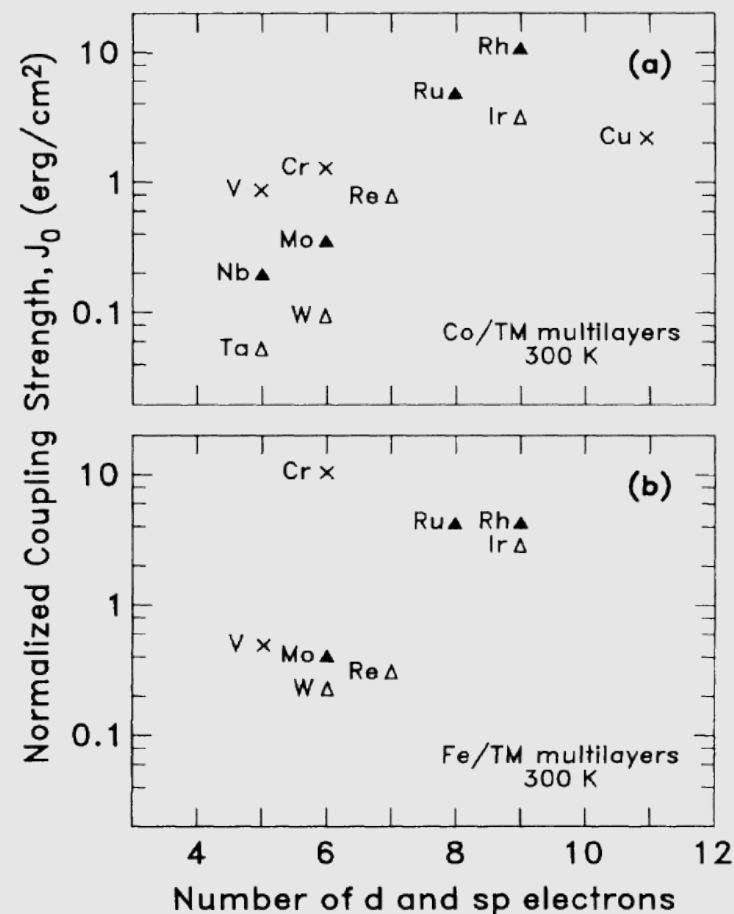
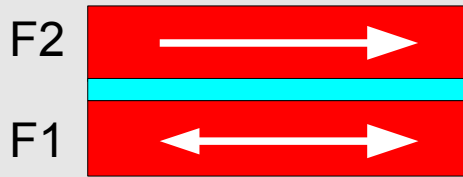


FIG. 3. Dependence of the normalized exchange coupling constant on the 3d, 4d and 5d transition metals in (a) Co/TM and (b) Fe/TM multilayers.

Note: $J(t)$ extrapolated for $t=3\text{\AA}$

S. S. P. Parkin, Phys. Rev. Lett. 67, 3598 (1991)

Synthetic Ferrimagnets (SyF) — Crude description



Hypothesis:

- ⇒ Two layers rigidly coupled
- ⇒ Reversal modes unchanged
- ⇒ Neglect dipolar coupling

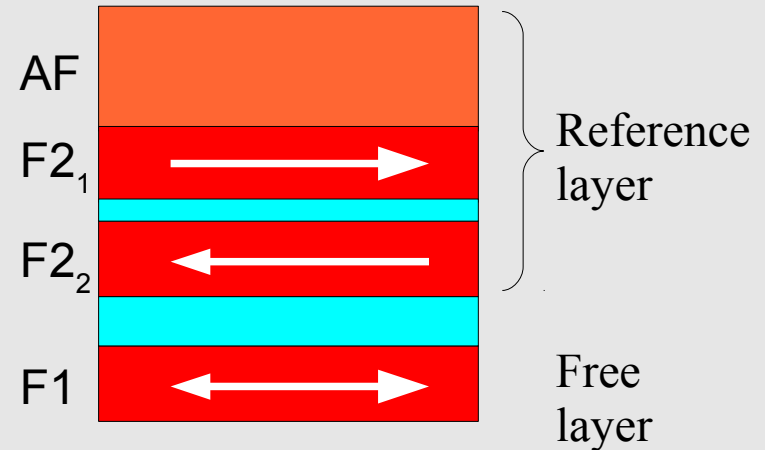


$$M = \frac{|e_1 M_1 - e_2 M_2|}{e_1 + e_2} \quad K = \frac{e_1 K_1 + e_2 K_2}{e_1 + e_2}$$

$$H_c = \frac{e_1 M_1 H_{c,1} + e_2 M_2 H_{c,2}}{|e_1 M_1 - e_2 M_2|}$$

What use?

- ⇒ Increase coercivity of pinned layers
- ⇒ Decrease intra- and inter- dot dipolar coupling



Practical aspects

- ⇒ Ru spacer layer (largest effect)
- ⇒ Control thickness within a few Angströms !

Basics of precessional switching

Magnetization dynamics:

Landau-Lifshitz-Gilbert equation:

$$\frac{d\mathbf{M}}{dt} = -\gamma_0 [\mathbf{M} \times \mathbf{H}_{eff}] + \frac{\alpha}{M_s} \left[\mathbf{M} \times \frac{d\mathbf{M}}{dt} \right]$$

γ_0 Gyromagnetic factor

$$\gamma_0 = \mu_0 \gamma \quad \gamma = \frac{gq}{2m}$$

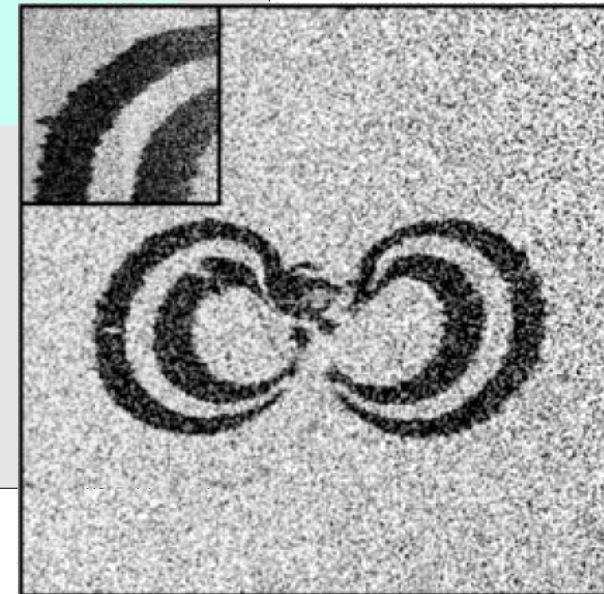
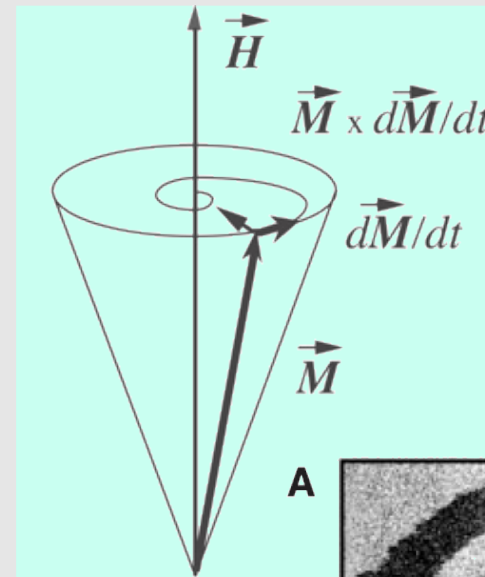
$$\gamma / 2\pi = 28 \text{ GHz/T}$$

$\mathbf{H}_{eff}$ Effective field
(including applied)

$$\mu_0 \mathbf{H}_{eff} = - \frac{\partial \mathbf{E}_{mag}}{\partial \mathbf{M}}$$

α Damping coefficient ($10^{-3} \rightarrow 10^{-1}$)

Démonstration: 1999



150 μm

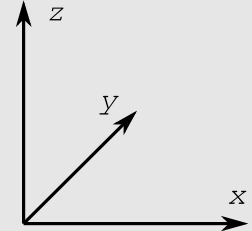
C. Back et al., Science 285, 864 (1999)

Precessional trajectory using energy conservation

(1) $E = \frac{1}{2} \mu_0 M_s^2 N_z m_z^2 - K m_x^2 - \mu_0 M_s H m_y$ In-plane uniaxial anisotropy along x

(2) $m_x^2 + m_y^2 + m_z^2 = 1$

Starting condition: $m_x = +1$



(1) $\Rightarrow e = E/K_d = N_z m_z^2 - h_K m_x^2 - 2h m_y$ with : $e(t=0) = -h_K$

Using (2) $\Rightarrow m_x^2 = 1 - \frac{2h}{N_z + h_K} m_y - \frac{N_z}{N_z + h_K} m_y^2$

Can be rewritten:

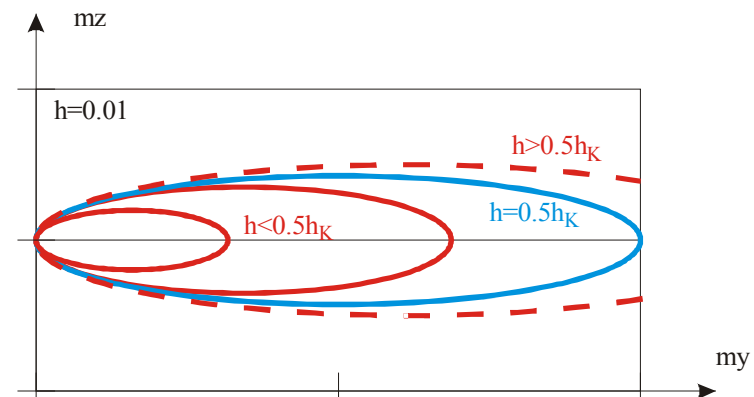
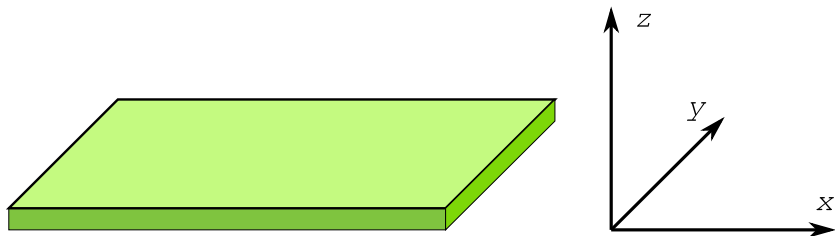
$$m_x^2 + \frac{(m_y + h/N_z)^2}{1 + h_K/N_z} = 1 + \frac{h^2}{N_z(N_z + h_K)}$$

Using (2) $\Rightarrow m_z^2 = \frac{2h}{N_z + h_K} m_y - \frac{h_K}{N_z + h_K} m_y^2$

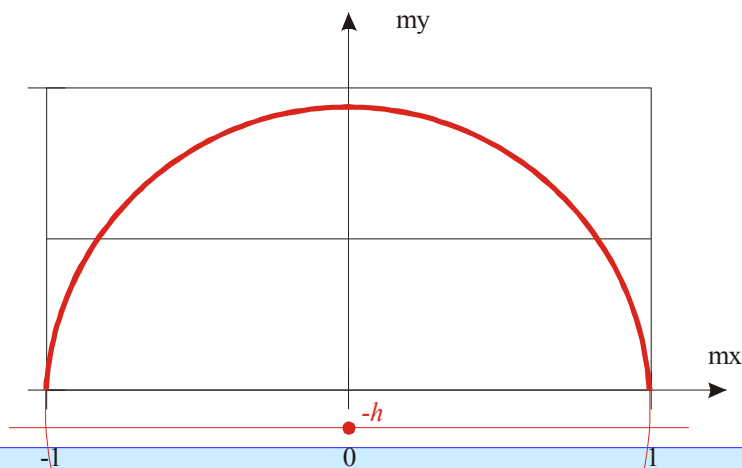
Can be rewritten:

$$\left(\frac{m_z^2}{\frac{h_K}{N_z + h_K}} \right) + \left(m_y - \frac{h}{h_K} \right)^2 = \left(\frac{h}{h_K} \right)^2$$

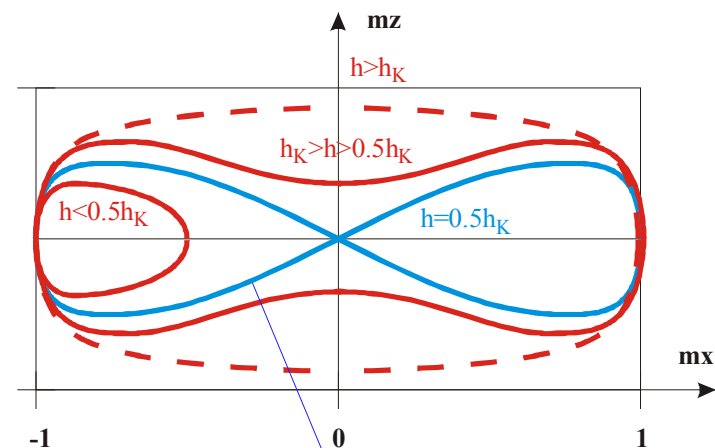
Magnetization trajectories



$$\left(\frac{m_z^2}{\frac{h_K}{N_z + h_K}} \right) + \left(m_y - \frac{h}{h_K} \right)^2 = \left(\frac{h}{h_K} \right)^2$$



$$m_x^2 + \frac{(m_y + h/N_z)^2}{1 + h_K/N_z} = 1 + \frac{h^2}{N_z(N_z + h_K)}$$

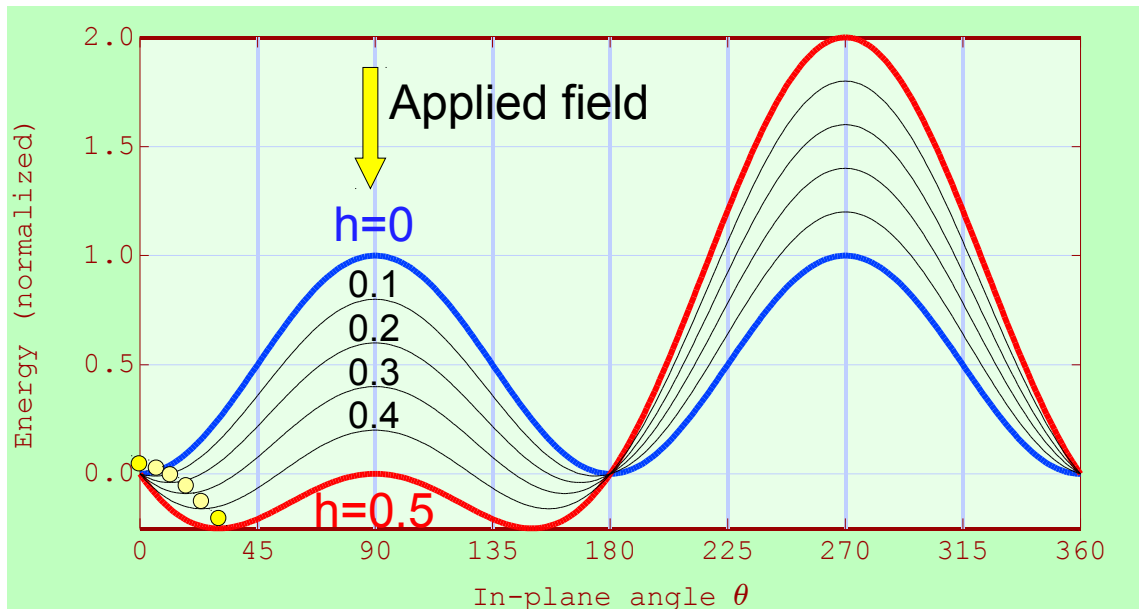


$$\omega \approx 0.847 \gamma_0 \sqrt{M_s(H - H_K)/2}$$

Stoner-Wohlfarth versus precessional switching

Stoner-Wohlfarth model: describes processes where the system follows quasistatically energy minima, e.g. with slow field variation

Precessional switching: occurs at short time scales, e.g. when the field is varied rapidly



Relevant time scales

Precession period

$$2\pi / \gamma = 35 \text{ ps.T}$$

➡ 25 - 500 ps

Precession damping

$$1/(2\pi \alpha) \text{ per period}$$

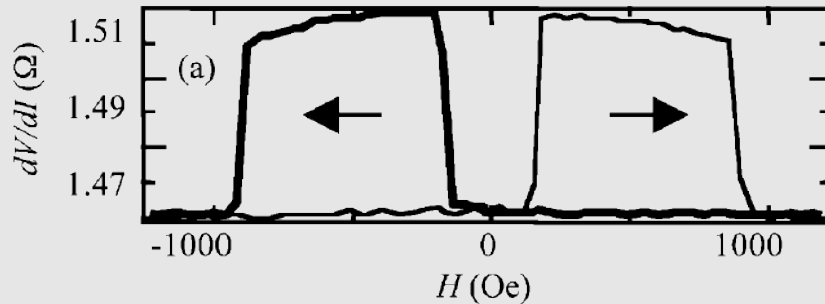
$$(\alpha = 0.01 - 0.5)$$

Notice ➡ Magnetization reversal allowed for $h > 0.5h_K$ (more efficient than classical reversal)

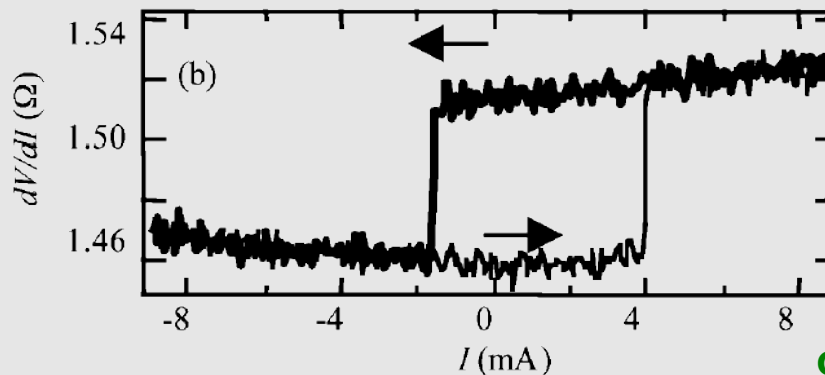
Facts

Can be viewed as the reverse of GMR effect

J. C. Slonczewski (1996)
L. Berger (1996)



Conventional hysteresis loop



Current-induced magnetization reversal

Group Myers et Ralph, Cornell University (2000)

Related physics

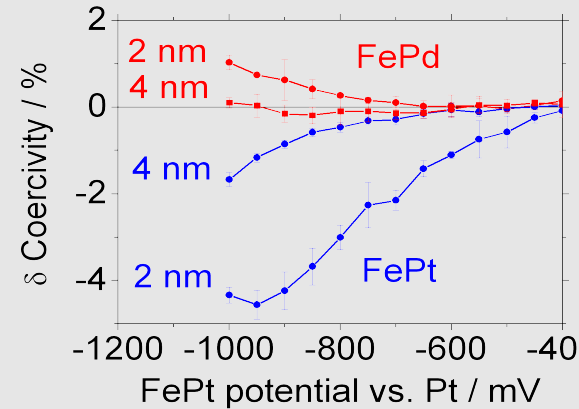
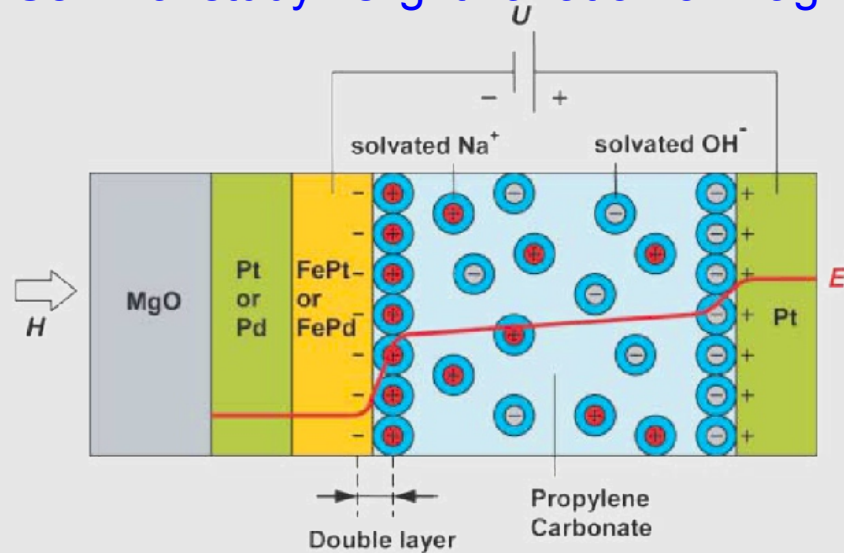
- ↻ Pure spin current
- ↻ Spin injection (eg in semiconductor)
- ↻ Non-local reversal

Motivations for technology

- ↻ Simplified architectures (MRAMs etc.)
- ↻ Fully electronic read/write
- ↻ Domain wall motion (memory, logic)
- ↻ Agile GHz oscillators

Facts

Seminal study : slight variation of magnetic anisotropy



M. Weisheit et al., Science 315, 349 (2007)

Recent

⇒ Magnetization switching with pulse of E-field

Y. Shiota et al., Nature Mater.11, 39 (2012)

⇒ E-field-induced ferromagnetic resonance

T. Nozaki et al., Nature Phys. 8, 491 (2012)

Motivations for technology

- ⇒ Drastically reduce Joule heating
- ⇒ Gateable properties

Principle

Combined heating
+ inverse Faraday effect

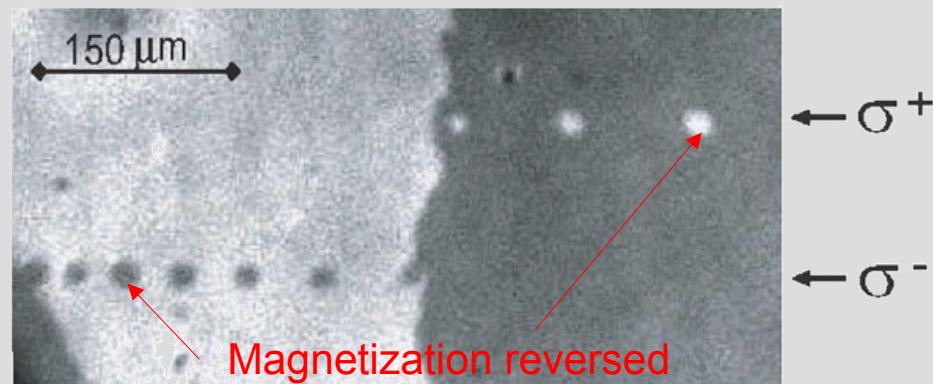
Magneto-optical
material. $T_c=500K$



Ti:S laser:

$\lambda=800\text{nm}$; $\Delta\tau=40\text{fs}$.

Local reversal with controlled power



C. D. Stanciu et al., Phys. Rev. Lett. 99, 047601 (2007)

Physics

- ↪ Ultra-fast magnetization process ($<1\text{ps}$)
- ↪ Exchange-related precession for RE — 3d alloys

Technology

- ↪ Ultrafast writing
- ↪ Heat-assisted writing

Still other means

- ↪ Strain (or sound waves)
- ↪ Heat
- ↪ ...



Anisotropy exchange length

$$E = A \left(\partial_x \theta \right)^2 + K \sin^2 \theta$$

Exchange $\rightarrow$ J/m
Anisotropy $\rightarrow$ J/m³

Anisotropy exchange length:

$$\Delta_u = \sqrt{A/K}$$

$$\Delta_u \approx 1 \text{ nm} \rightarrow \Delta_u \geq 100 \text{ nm}$$

Hard Soft

Relevant for Bloch domain walls



Often called *Bloch parameter*
or *domain-wall width*

Dipolar exchange length

$$E = A \left(\partial_x \theta \right)^2 + K_d \sin^2 \theta$$

Exchange $\rightarrow$ J/m
Dipolar energy $\rightarrow$ J/m³

$$K_d = \frac{1}{2} \mu_0 M_s^2$$

Dipolar exchange length:

$$\Delta_d = \sqrt{A/K_d}$$

$$= \sqrt{2A/\mu_0 M_s^2}$$

$$\Delta_d \approx 3 - 10 \text{ nm}$$

Single-domain critical size
relevant for nanoparticles
made of soft magnetic material

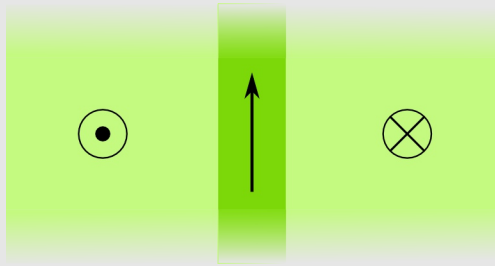


Often called *Exchange length*

Notice:

Other length scales: with field etc.

Bloch domain wall in the bulk (2D)



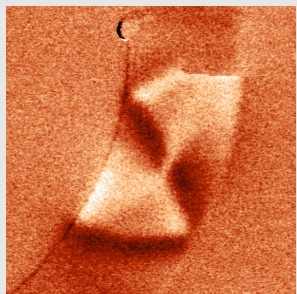
- ⇒ No magnetostatic energy
- ⇒ Width $\Delta_u = \sqrt{A/K}$
- ⇒ Areal energy $\gamma_w = 4\sqrt{AK}$



Other angles & anisotropy

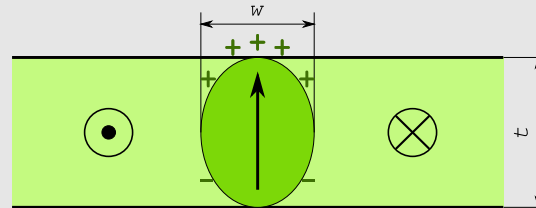
F. Bloch, Z. Phys. 74, 295 (1932)

Constrained walls (eg : in stripes)



Permalloy (15nm)
Stripe 500nm

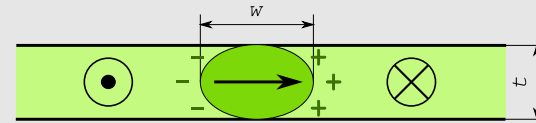
Domain walls in thin films (2D → 1D)



Bloch wall

$$t \gtrsim w$$

300x800nm



Néel wall

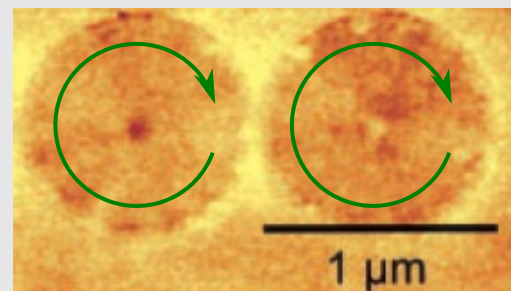
$$t \lesssim w$$

1000x2000nm

- ⇒ Contains magnetostatic energy
- ⇒ No exact analytics

L. Néel, C. R. Acad. Sciences 241, 533 (1956)

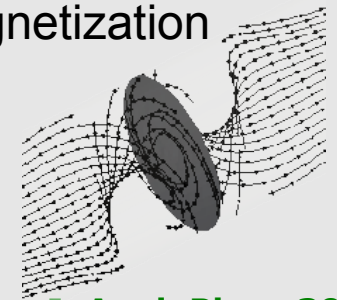
Magnetic vortex (1D → 0D)



T. Shinjo et al.,
Science 289, 930 (2000)

Bloch point (0D)

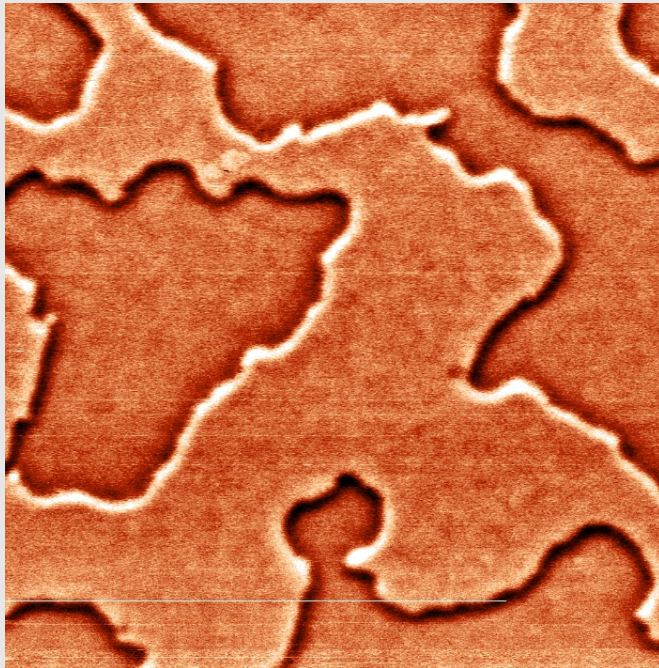
- ⇒ Point with vanishing magnetization



W. Döring, J. Appl. Phys. 39,
1006 (1968)

Magnetic history

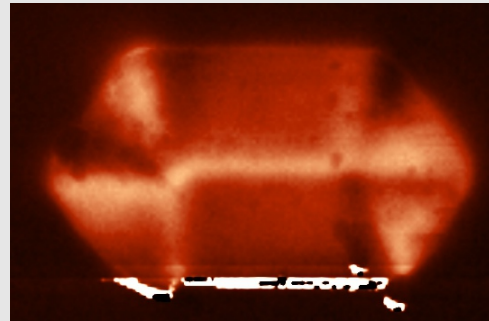
- ⇒ Non-magnetized sample (virgin state)
- ⇒ Demagnetized sample



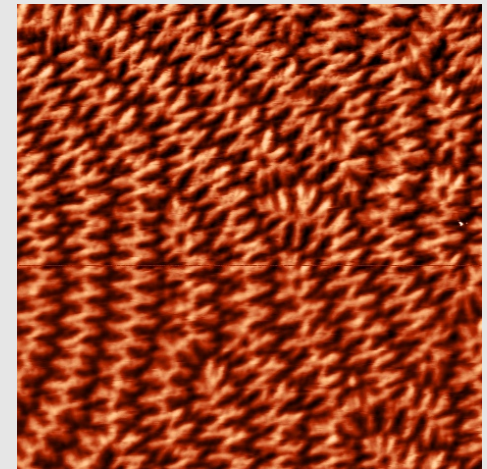
4nm FePt film
MFM, $1.5\mu\text{m}$
Perpendicular magnetization
Sample courtesy : A. Marty

Magnetostatics

- ⇒ Ground-state driven by decrease of magnetostatic energy (flux closure)



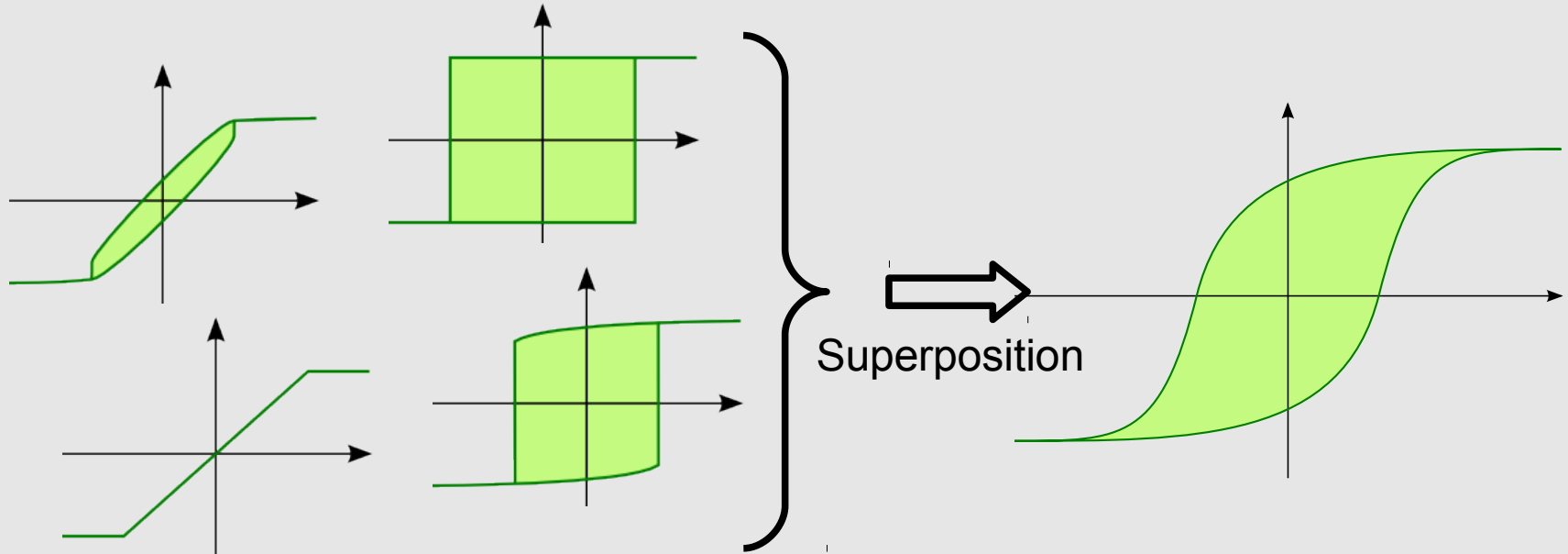
Fe self-assembled dot
MFM, $1.5\mu\text{m}$



NdFeB film with low H_c
MFM, $15\mu\text{m}$
Sample courtesy : N. Dempsey

Physics : coercivity determined dual grains

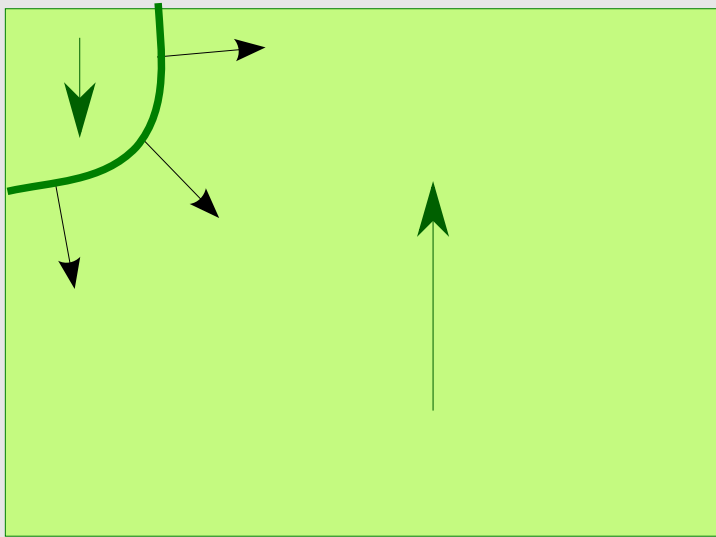
⇒ Different loops with distribution



⇒ Practical Victorino FRANCO

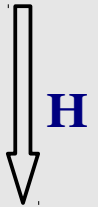
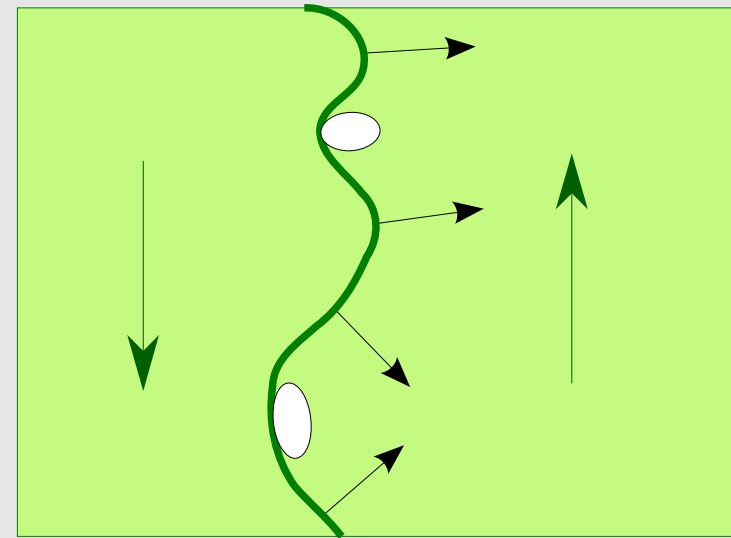
⇒ Next lecture : learn from loops

Coercivity determined by nucleation



- ⇒ Physics has some similarity with that of grains
- ⇒ Concept of nucleation volume

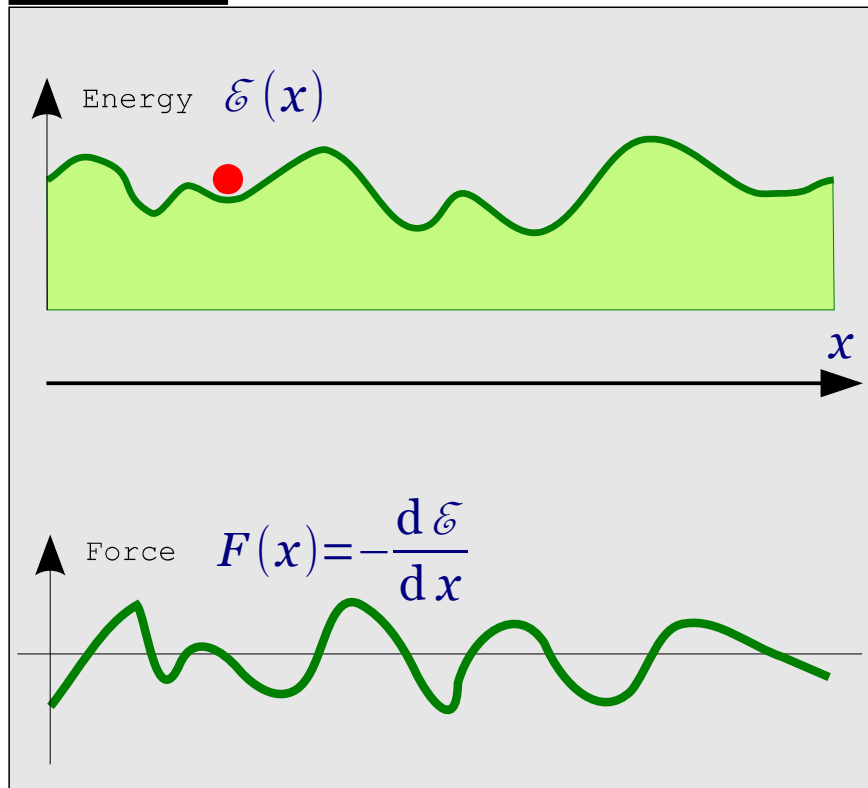
Coercivity determined by propagation



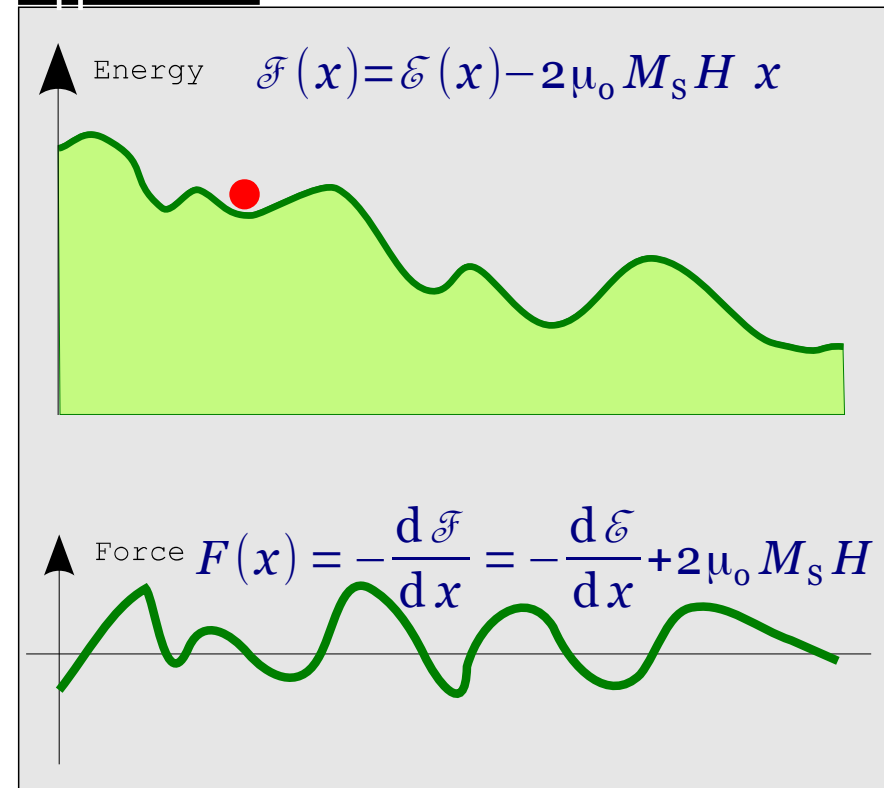
- ⇒ Physics of surface/string in heterogeneous landscape
- ⇒ Modeling necessary

Hypothesis : translational invariance along the wall $\rightarrow$ 1d model (variable x)

Zero field



Applied field



Propagation field : $H_p = \frac{1}{2\mu_0 M_s} \text{Max} \left(\frac{d\varepsilon}{dx} \right) \rightarrow \text{Search for : } \frac{d^2\varepsilon}{dx^2} = 0$

E. Kondorski, On the nature of coercive force and irreversible changes in magnetisation, Phys. Z. Sowjetunion 11, 597 (1937)

Reduction in Coercive Force Caused by a Certain Type of Imperfection

A. AHARONI

Department of Electronics, The Weizmann Institute of Science, Rehovot, Israel

(Received February 1, 1960)

As a first approach to the study of the dependence of the coercive force on imperfections in materials which have high magnetocrystalline anisotropy, the following one-dimensional model is treated. A material which is infinite in all directions has an infinite slab of finite width in which the anisotropy is 0. The coercive force is calculated as a function of the slab width. It is found that for relatively small widths there is a considerable reduction in the coercive force with respect to perfect material, but reduction saturates rapidly so that it is never by more than a factor of 4.

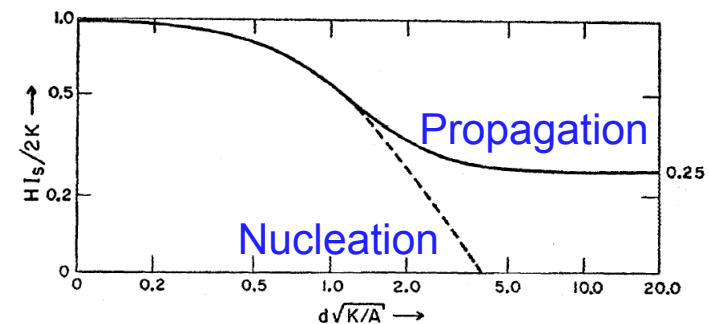
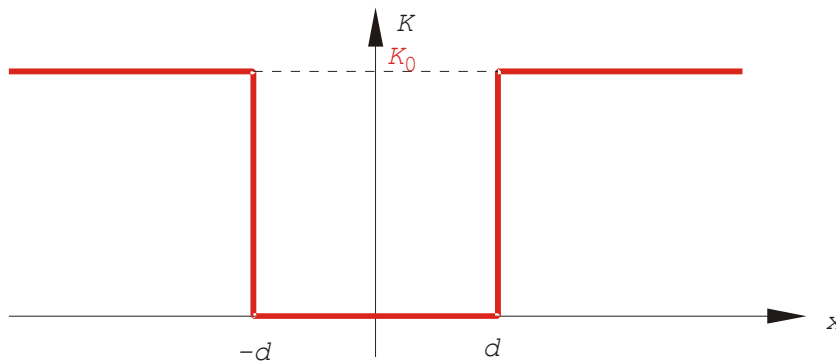


FIG. 1. The nucleation field (dashed) and coercive force (full curve) in terms of the coercive force of perfect material, $HI_s/2K$, as functions of the defect size, d .

See practical : <http://magnetism.eu/esm/2009/slides/fruchart-tutorial.pdf>

Brown's paradox

In most systems $H_c \ll \frac{2K}{\mu_0 M_s}$

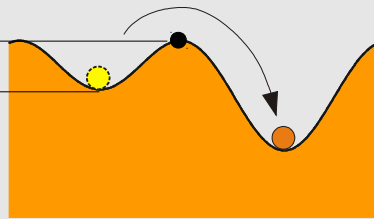


Micromagnetic analytics or simulations

- ⇒ Link H_c with microstructure
- ⇒ Issue : microscopic knowledge

Reminder : single-domain

Δe



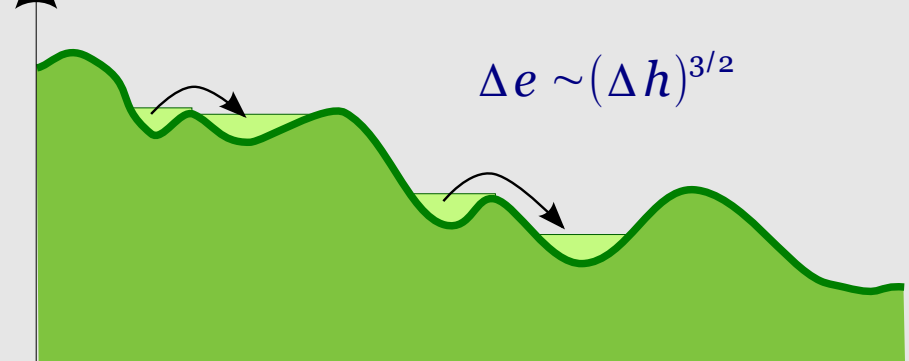
$$\Delta e \sim (\Delta h)^2 \quad \text{for } \theta_H = 0^\circ$$

$$\Delta e \sim (\Delta h)^{3/2} \quad \text{for } \theta_H \neq 0^\circ$$

with: $\Delta h = h_c(T=0 \text{ K}) - h$

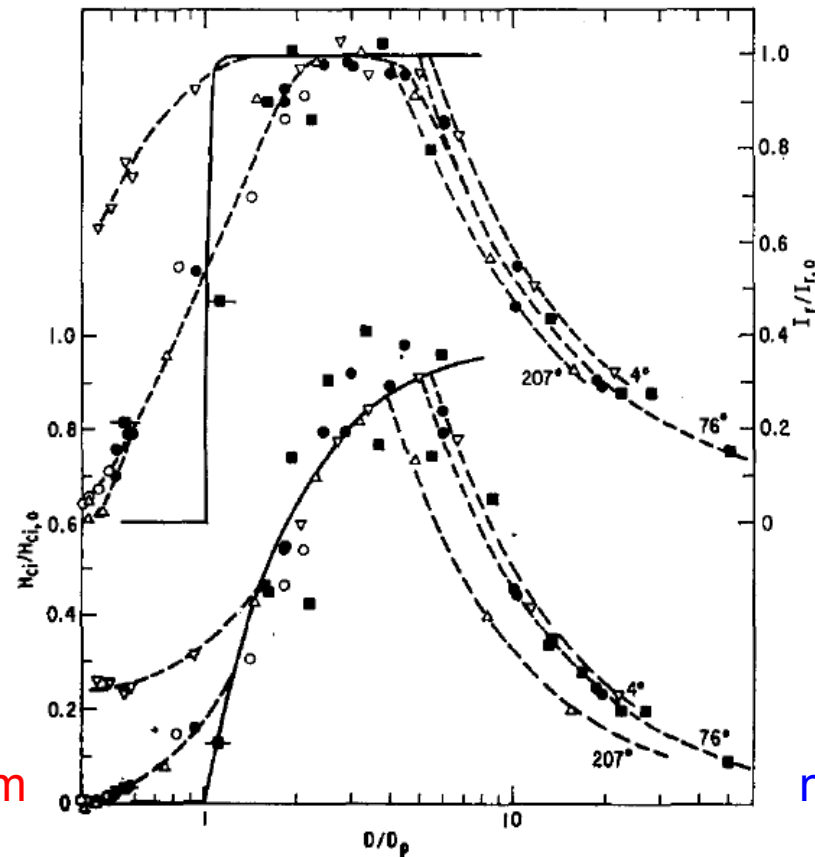
Kondorski model (1d)

Energy



⇒ Notice : other exponents for other situations and model

Thermally-activated DW motion:
→ Creep regime



Towards
superparamagnetism

Towards
nucleation-propagation
and multidomain

FIG. 1. Particle size dependence of essentially spherical, randomly oriented, iron particles. Calculated curve given by solid line. Diameters $D = \hat{d}_v$. Data at 76°K obtained from electron microscopic examination ■, calculated from I_r/I_s vs temperature ○, and from smoothed data of H_{ci} vs D ●.

E. F. Kneller & F. E. Luborsky,
Particle size dependence of coercivity and remanence of single-domain particles,
J. Appl. Phys. 34, 656 (1963)



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- [3] **R. Skomski, Nanomagnetism**, J. Phys.: Cond. Mat. 15, R841–896 (2003).
- [4] **O. Fruchart, A. Thiaville, Magnetism in reduced dimensions**, C. R. Physique 6, 921 (2005) [Topical issue, Spintronics].
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