# **Basic concepts on magnetization reversal (2)** Slow dynamics and thermal related processes

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#### Introduction: Application considerations



Thermal activation is crutial for nanoparticles (<25 nm) It is also relevant for thin films (domain nucleation and domain wall propagation)

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- I. Superparamagnetism
- II. Nucleation
- III. Domain wall propagation in disordered magnetic films
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#### Superparamagnetism: Energy barrier for macrospin





General case  

$$\Delta E = KV \left( 1 + \frac{H}{H_{SW}} \right)^{3/2}$$
Victoria PRL 63, 457 (1989)

#### Superparamagnetism: Thermodynamics of a macrospin



#### Superparamagnetism: Thermodynamics of a macrospin

Case with finite anistropy



#### Superparamagnetism: Thermodynamics of a macrospin



Occupancy probability for a Stoner-Wohlfarth model (H = 0)

#### Superparamagnetism: Temperature induced switching

Phenomenological: Arrhenius law

 $\Rightarrow$ Switching time  $\tau = \tau_0 \exp(\Delta E / kT)$ 

- $\Delta E$  calculated with the macrospin approch
- $au_0$  attempt time (~1 ns) : linked with magnetization dynamics



# **Superparamagnetism:** Temperature induced switching $\tau = \tau_0 \exp(\Delta E / kT)$

 $\tau > \tau_{measurement}$ Stability criterion :  $T_B = \frac{\pi v}{k_B} \ln \left( \frac{t}{\tau_0} \right)$ Blocking temperature  $\tau_0 = 0.1 ns$ lf 10 year **1s** 1min **1h** 1day **1year**  $\Delta E/kT$ 23 27 31 34 40 43 -

Hard drive applications

This problem drives an intense effort of reseach for high anisotropy materials. Best candidates are Pt-bases ordered alloys like **FePt and CoPt** ( $K \sim 10 MJ/m^3$  in bulk phase <->  $D_{limit} \sim 3 nm$ ) See e.g. Sun et al. Science 287, 1989 (2000) Warning: it is difficult to predict T<sub>B</sub> from volumic anisotropy measurements as in nanoparticles K is generally dominated by surface effects/low coordinated atoms See Jamet et al. PRL 86, 4676 (2001) Gambardella etal. Science 300, 1130 (2003)

#### Superparamagnetism: Characteristic time in experiments

Stability criterion :

 $au > au_{measurement}$ 



- Loop measurment in SQUID -> ~ 10min 1h
- ZFC-FC in squid -> ~ 1s
- magneto optical kerr effect (resistive coils) -> ~1s
- SP-STM / microSQUID : 100 ms
- ac susceptibility : 1ms 10s
- Moessbauer : 0.1 µs

In sweeping (field or temperature) experiments, charateristic time is ambiguous -> rather speak of sweeping rate

see e.g. Kurkijarvi PRB 6 832 (1972) (field sweep) Rohart et al PRB 74, 104408 (2006) (temperature sweep)

#### Superparamagnetism: Rate equation model



This equation can be used for any field orientation (if switching rates are known...)

#### Superparamagnetism: Hysteresis loop

Simulation of mean hysteresis loops with rate equations



Coercive field is not intrinsic -> depend on temperature AND sweeping rate



Scharrok JAP 76, 6413 (1994) IEEE Trans Mag 26, 193 (1999)

#### Superparamagnetism: experimental evidence

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#### Experimental Evidence of the Néel-Brown Model of Magnetization Reversal

W. Wernsdorfer,<sup>1,2</sup> E. Bonet Orozco,<sup>1,2</sup> K. Hasselbach,<sup>1</sup> A. Benoit,<sup>1</sup> B. Barbara,<sup>2</sup> N. Demoncy,<sup>3,4</sup> A. Loiseau,<sup>4</sup> H. Pascard,<sup>3</sup> and D. Mailly<sup>5</sup>

Presented are the first magnetization measurements of individual ferromagnetic nanoparticles (15-30 nm) at very low temperatures (0.1-6 K). The angular dependence of the hysteresis loop evidenced the single domain character of the particles. Waiting time, switching field, and telegraph noise measurements showed for the first time that the magnetization reversal of a well prepared ferromagnetic nanoparticle can be described by thermal activation over a single-energy barrier as originally proposed by Néel and Brown. The "activation volume" estimated by these measurements was close to the particle volume. [S0031-9007(97)02465-4]





FIG. 2. Probability of not switching of magnetization as a function of the time at different applied fields at 4 K and for  $\theta \approx 12^{\circ}$ . Full lines are fits to the data with an exponential

FIG. 6. Telegraph noise measurements for three temperatures and  $\mu_0 H_y = 396.2 \text{ mT}.$ 

#### [Eq. (2).] $\Rightarrow$ Anisotropy precisely determined from astroid at 35 mK $\Rightarrow$ Volume determined by SEM imaging

#### $\Rightarrow$ Volume determined by SEM imaging

#### ⇒First perfect agreement with Néel-Brown model



In 3 D: (same Co cluster) E. Bonnet er al PRL 83, 4188 (1999)



3 nm Co cluster : M. Jamet PRL 86, 4676 (2001)

#### Superparamagnetism: experimental evidence



FIG. 4. Temperature dependence of the switching field measured in the  $H_y$ - $H_z$  plane in Fig. 3. An extrapolation of the switching fields to zero gives the blocking temperature  $T_B = 14$  K [22].

Jamet et al. PRL 86, 4676 (2001)



Fig. 1. Temperature dependance of the switching field of a 3 nm Co particle (a) measured with  $\tau_{mes} = 0.01$  s [2] and (b) calculated with  $\tau_{calc} = 30$  ns ( $\alpha = 0.1$ , calculation time step = 100 fs).



Fig. 2. Interpretation of  $\tau$  by an Arrhenius law: (a) determination of a mean  $\Delta E_b$  for different temperatures by fitting calculated astrolds with iso- $\Delta E_b$  curves, (b) fit of obtained results, for both calculated and experimental astrolds, with the petization Reversal. Slow Dynamics

Simulation of macrospin dynamics (Brown's model) Vouille et al. JMMM 272-276, e1237 (2004) (with exp. Data from Jamet et al.)

> S. ROHART : Basic Concepts on Magnetization Reversal : Slow Dynamics European School on Magnetization Reversal : Slow Dynamics Arrhenius law in order to determine τ<sub>0</sub>.

## Superparamagnetism:

#### Experimental observation in practical

- -> Single particle measurments are difficult
- -> Hysteresis loops are generally long to measure



#### Superparamagnetism: beyond macrospin?

Superparamagnetism and nucleation-propagation magnetization reversal

If  $L >> \delta$ : it is possible to nucleate and propagate a reversed domain

Braun PRL 1993 (same approach as Brown 1963)



$$\tau = \tau_0(H) \exp(A\sigma/kT)$$

 τ<sub>0</sub> -Strongly depends on H (<-> size of the critial nucleus to reverse magnetization)
 -Proportionnal to L (nucleation occurs in the particle – edges are neglected)



FIG. 2. The total switching rate is shown as a function of the external field *h* for particle diameters of (a) 100 Å, (b) 200 Å, and (c) 400 Å. For comparison, the dashed lines indicate the results of the Néel-Brown theory for an assumed particle aspect ratio ART-15Basic Concepts on Magnetization Reversal : Slow Dynamics European School on Magnetism - Targosite 2011

#### Superparamagnetism: beyond macrospin?

Superparamagnetism and nucleation-propagation magnetization reversal Experimental check :

Single particle measurement by spin polarized STM





Monte Carlo simulation  $\tau_0$  decrease with lenght, increase with the width  $\Rightarrow$ edge nucleation

Krause et al. PRL 103, 127202 (2009)

#### Superparamagnetism: beyond macrospin?

#### Superparamagnetism and spin waves

Atomic scale micromagnetic calculation on Co flat nanodots



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#### Nucleation processes: Droplet model

-> 2D problem : apply to thin films with weak disorder



$$\frac{dE}{dr}(r_c) = 0 \Longrightarrow r_c = \frac{\sigma}{2\mu_0 HM_s}$$
$$\Longrightarrow \Delta E = \frac{\pi \sigma^2 t}{2\mu_0 HM_s}$$

Energy :



Important process for thin films Energy barrier scales with 1/H

Nucleation rate  $R(H) = R_0 \exp(-\Delta E / kT)$ 

Barbara JMMM 129, 79 (1994) Vogel et al. CR Physique 7, 977 (2006)

#### **Nucleation processes:**

#### Magnetization reversal in constant magnetic field

-> Nucleation rate vs. Domain expansion :

$$\frac{dN}{dt} = (N_0 - N)R \Rightarrow N = N_0 (1 - \exp(-Rt)) \text{ Domain nucleation} \qquad \begin{array}{l} N_0 & \text{Nucleation site density} \\ N & \text{Nucleated domaines} \\ R & \text{Nucleation rate} \end{array}$$

 $S_N(t) = \pi (r_c + v_0 t)^2$  Surface of the domain nucleated at t=0  $v_0$  Domain wall velocity



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#### **Nucleation processes:**

#### Magnetization reversal in constant magnetic field



Fig. 4. Magnetization versus reduced time  $t_R$  for a GdFe sample ( $k \approx 2000$ ) and a TbCo one ( $k \approx 0$ ), corresponding domain structure observed by Kerr effect.

Labrune et al. JMMM 80, 211 (1989)

#### Nucleation processes: Coercive field and droplet model



Au/Co/Au films and nanostructures Raquet et al. PRB 54, 4128 (1996)

## **Nucleation processes:**

## Droplet model in reduced dimensions

 $\Rightarrow$ Confined droplet model (circular dot)



JP. Adam PhD thesis, Orsay 2008 (unpublished) See also 3D theory : Hinzke and Nowak PRB 58 265 (1998) S. ROHART : Basic Concepts on Magnetization Reversal : Slow Dynamics European School on Magnetism - Targosite 2011

#### **Nucleation processes:**

#### Coalescence between nucleated domains



Pt/Co(0.5 nm)/Pt Time between frame : 400 s Nucleation field : 5 Oe Propagation field : 3Oe (to reduce DW velocity) ⇒The experiment validates the picture of nucleation/propagation

⇒Coalescence between domains is difficult

 $\Rightarrow$ Nucleation of 360° domain walls

Dipolar repulsion between domains



 $\Rightarrow$ Saturation may be difficult to reach  $\Rightarrow$ Poison for magnetization reversal

Bauer et al. PRL 94, 207211 (2005)

See also : Schrefl, et al. J. Appl. Phys. 87, 5517 (2000) (in plane magnetization) Hehn et al. APL 92, 072501 (2008) (in MRAM nanoelements)

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Domain wall is not extended as a straight line (minimisation of length) but also feels some weak defects.

 $\Rightarrow Competition between elasticity$ and pinningDriving force : H $Elasticity : <math>\varepsilon = \sigma t = 4t\sqrt{AK}$ Pinning :  $f_{pin}$ (roughness, thickness variation...)

From Creep to viscous motion



**Propagation and roughness** 



→ Velocity with universal behavior on 10 orders of magnitude.

## **Domain wall motion in disordered films** Elastic energy



#### ➔ Roughness and fluctuation ⇔ Elastic energy cost



**<u>Pinning energy</u>** :  $E_{pinning} = -f_{pin}\sqrt{n_i\xi L}\xi = -\sqrt{\xi^2}L\Delta$ 

Competition between pinning and elasticity



Scaling law – Renormalization group theory

For  $L > L_c > n_c$ 

 $v = v_c \cdot (\frac{L}{L_c})^{\zeta}$  Scaling law for fluctuations

 $\zeta$ = 2/3 : universal exponent (for a 1D interface in motion in a 2D medium with weak disorder)

 $E_{elastic} = \frac{\varepsilon v_c^2}{L} \left(\frac{L}{L_c}\right)^{2\zeta} E_c = E_{pinning}(L_c) = E_{elastic}(L_c)$   $E_{pinning} = E_c \cdot \left(\frac{L}{L_c}\right)^{2\zeta-1}$   $Critical \ volume : V_c = L_c v_c t$   $E_{zeeman} = M_s \ tvL \ H = M_s \ V_c \ H \left(\frac{L}{L_c}\right)^{\zeta+1}$ 

## **Domain wall motion in disordered films** Activation energy and regime of motion

Thermally activated regime in creep regime

 $\Delta E = -M_S V_c H + E_C \cdot \left(\frac{L}{L_c}\right)^{2\zeta - 1}$  $E_{activation} = E_{Zeeman} + E_{pinning}$ Activation energy as a function of external field  $\Delta E = E_C \left(\frac{H_{crit}}{H}\right)^{\frac{2\zeta-1}{2-\zeta} \Rightarrow \frac{1}{4}} \quad \text{With } \zeta = 2/3 \qquad v = v_0 \exp\left[-\frac{E_C}{k_B T} \left(\frac{H_{crit}}{H}\right)^{1/4}\right]$ v In the vicinity of the depinning field LOW  $H_{crit} = E_C / M_S V_C$ DEPINNIN  $E_{pinning}(L_C) = E_{Zeeman}(L_C)$  $V = (H - H_{crit})^{\beta}$ CREEP Η Flow regime  $v = \mu H$ T=0



Unpublished results 3.0 See also S. Lemerle et al, PRL.80, 849 (1998)

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2.0

2.5

1.5

## **Domain wall motion in disordered films** ex: Pt/Co/Pt ultrathin films



#### Mobilité/ champ critique/ champ de Walker



Mouvement visqueux observé = régime précessionnel



## → Paramètre d'amortissement de Gilbert $\alpha$ ~0.25 compatible avec résultats FMR et valeurs utilisées pour des simulations numériques

P. J. Metaxas, Phys. Rev. Lett. 99 217208 (2007)

Divergence of energy barrier

Evidence of energy barrier for H /H<sub>crit</sub> <<1



$$\Delta E = E_{C} \left(\frac{H_{crit}}{H}\right)^{\frac{1}{4}}$$

H= 2 Oe ( $0.01 H_{crit}$ ) Dt = 200 secondes H = 4 Oe ( $0.02 H_{crit}$ ) Dt =1 seconde

 $\rightarrow$ L<sub>jump</sub> is defined at the energy barrier

$$\Delta E = E_C \cdot \left(\frac{L}{L_C}\right)^{1/3} + M_S t H v_C L_C \left(\frac{L}{L_C}\right)^{5/3}$$

Jump length

$$L_{jump} = E_L \frac{1}{H^{4/3}}$$

Barkhausen jumps with 1/H<sup>4/3</sup> jump length
 Motion through avalanche processes

V. Repain et al., EuroPhysicsLett 68 (2004) 10213

#### **Roughness analysis**



Correlation on a given length L

$$C^{2}(L) = \left\langle \left[ \nu(x) - \nu(x+L) \right]^{2} \right\rangle_{L} \propto \left( \frac{L}{L_{C}} \right)^{4/3}$$

Critial exponent is independent of H (for H<0.9H<sub>c</sub>) Sligh increase of  $L_c$  for  $H/H_c>0.2$ 

A. Mougin et al. unpublished results

## **Domain wall motion in disordered films** Creep in confined geometry



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#### **Domain wall motion in disordered films** Magnetization reversal with strong pining



Epitaxial FePt(40nm)/Pt film : presence of micromacle than pins the domain walls.

Domain wall propagation is channeled between micromacles : fast fractal-like domain growth.

Saturation needs to overcome strong pinning barriers :

 $\Rightarrow$ Slow high field saturation

0.5

M/Ms

0.5

-0,5

 $\Rightarrow$ Thermal activation (slow dynamics)





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Attane et al. PRL 93, 257203 (2004)

#### Conclusion

#### Take home message

When dealing with long time scales, thermal activation plays an essential role.
Many properties (like coercive field) depend on the time scale (field sweeping time, waiting time)...

#### To go further

•Toward quantum fluctuations : already observed in molecular magnets

-> quantum fluctuation and tunneling of a domain wall is still a challenge...

Wernsdorfer and Sessoli Science 284, 133 (1999)

Gunther and Barbara Quantum Tunneling of Magnetization-QTM'94 (Kluwer, Netherlands,

1995)

•Magnetization reversal under spin polarized current

-> Creep law with a different driving force (spin transfert torque) Yamanouchi et al. Nature 428, 539 (2004)

#### Some readings

- •Skomski and Coey *Permanent magnetism* (Taylor & Francis Group 1999)
- •Aharoni Introduction to the theory of ferromagnetism (Oxford 1996)
- •Skomski Nanomagnetics J. Phys. Cond. Mat. 15, R841 (2003)
- •Fiorani Surface effects in Magnetic Nanoparticles (Springer 2005)
- •P. Metaxas, PhD thesis (Creep), Orsay, 2009 : http://trove.nla.gov.au/work/39007513