Low Dimensional Magnetism Workshop

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a

Magnetic moments: atoms vs. bulk

Magnetic moment of an atom: role of electron-electron and spin-orbit interactions

$$H = \sum_{i=1}^{Z} \frac{p_i^2}{2m} - \sum_{i=1}^{Z} \frac{Ze^2}{r_i^2} + \sum_{i < j} \frac{e^2}{\left|r_i - r_j\right|^2} + \sum_{i=1}^{Z} (\mathbf{l}_i \cdot \mathbf{s}_i)g(r_i) = H_C + V_{e-e} + V_{s.o.}$$





Hund's rules:

- **1)** Total spin $S = S_i s_i$ is maximized
- 2) Total orbital moment $L = S_i I_i$ is maximized
- 3) L and S couple parallel (J=|L+S|) if el. shell is more than half-filled,
 - L and S couple antiparallel (J=|L-S|) if el. shell is less than half-filled

see lecture 2 by J.M.D. Coey



Data from O. Eriksson et al., Phys. Rev. B 42, 2707 (1990).



Exchange-split electron band structure measured by UV photoemission



Himpsel et al., J. Magn. Magn. Mat. 200, 456 (1999).



Himpsel, Phys. Rev. Lett. 67, 2363 (1991)



bulk Fe DOS

6

5

4

3

2

0

2

3

4

5

-10

INTEGRATED DENSITY OF STATES (...)

INTEGRATED DENSITY OF STATES (...)



Moruzzi, Janak, and Williams, Calculated electronic properties of metals (Pergamon, 1978)

Sipr, Minar, and Ebert, Europhys. Lett., in press (2009)



Symmetry-dependent increase in topmost layer magnetization



S. Handschuh, PhD thesis, Uni Köln

1 ML Fe on W(110):

15 % increase in ground state (T=0) magnetic moment



FIG. 4. Magnetic moment per atom in the remanent state, in units of Bohr magnetons, μ/μ_B (+), vs *T* for the monolayer film of Figs. 1-3 in comparison with the mean hyperfine field $B_{\rm hf}$ (O) of a film W(110)/0.82/Ag, determined by CEMS. $B_{\rm hf}(0) = 11.86 \pm 0.18$ T is taken as the mean value between a $T^{3/2}$ and a linear extrapolation. $B_{\rm hf}$ and μ/μ_B are normalized at T = 220 K.

Elmers, Liu, and Gradmann, Phys. Rev. Lett. 1989





SP-KKR calculations, Mavropoulos, Lounis, Zeller, and Blügel, Appl. Phys. A 2006

Stoner criterion $Un(E_F) > 1$

Rectangular-shaped DOS

$$\int_{W} n(\varepsilon) d\varepsilon = const. \quad \Rightarrow n(E_F) \sim \frac{1}{W}$$



W :

 E_F

Ε

In transition metals:

$$n(E_F) \approx n_d(E_F) \sim \frac{1}{W_d}$$

Tight-binding:

$$W_d \approx 2\sqrt{N_{nn}}h_d(r_{nn})$$

nearest neighbors | lattice spacing hopping

$$W_d^{\text{ML}}$$
 : $W_d^{(001)}$: $W_d^{\text{fcc}} = 0.58$: 0.82 : 1
 n_d^{ML} : $n_d^{(001)}$: $n_d^{\text{fcc}} = 1.73$: 1.22 : 1
S. Blügel, FZ Jülich





$$h_{3d} < h_{4d} < h_{5d} \implies W_{3d} < W_{4d} < W_{5d} \implies n_{3d} > n_{4d} > n_{5d}$$



S. Blügel and P. Dederichs, FZ Jülich – Phys. Rev. Lett. 1992, Solid State Comm. 1994.

Nonzero magnetic moments in 4d metal clusters



Increase in total magnetization due to Pd deposition on a Fe film



Fig. 1. TOM during coverage of 17 atomic layers of Fe(110) on W(110) by Pd. Fe film prepared at elevated temperatures, hence with a smooth surface. R/H (see Eq. (10)) measured versus number of Pd layers D_{Pd} . Measurements were performed at 300 K in a field of 0.1 T. R/H approximately equals the excess moment $\Delta \mu_{surf}$ (Pd), which is given in units of Fe monolayer moment m_{ML} .



Gradmann, Dürkop, and Elmers, JMMM 165, 56 (1997).



Orbital moment



Electron hybridization reduces *m*_L

FIG. 2. Model state density for fcc Fe, Co, and Ni. Due to the spin-orbit coupling the degeneracy between the m_l and $-m_l$ states is lifted and an orbital moment develops. The correct number of valence electrons is obtained by adjusting the Fermi level as marked in the figure (Fe, Co, and Ni).

Eriksson et al., Phys. Rev. B 42, 2707 (1990).

	\mathbf{m}_{L} atom (μ_{B})	\mathbf{m}_{L} bulk (μ_{B})
Fe (-bcc)	2.0	0.09
Co (-hcp)	3.0	0.15
Ni (-fcc)	3.0	0.05

E.P. Wohlfart, in Ferromagnetic Materials, Vol. 1, E.P. Wohlfart ed., North Holland, Amsterdam (1980).

Cubic symmetry *d*-wavefunctions

$$\begin{split} \psi_{1} &\equiv d_{xz} = \sqrt{\frac{15}{4\pi}} \frac{xz}{r^{2}} = \frac{1}{\sqrt{2}} \left(-Y_{21} + Y_{2-1} \right) \\ \psi_{2} &\equiv d_{xy} = \sqrt{\frac{15}{4\pi}} \frac{xy}{r^{2}} = \frac{-i}{\sqrt{2}} \left(Y_{22} - Y_{2-2} \right) \\ \psi_{3} &\equiv d_{yz} = \sqrt{\frac{15}{4\pi}} \frac{yz}{r^{2}} = \frac{i}{\sqrt{2}} \left(Y_{21} + Y_{2-1} \right) \\ \psi_{4} &\equiv d_{3z^{2}-r^{2}} = \sqrt{\frac{5}{16\pi}} \frac{3z^{2} - r^{2}}{r^{2}} = Y_{20} \\ \psi_{5} &\equiv d_{x^{2}-y^{2}} = \sqrt{\frac{5}{16\pi}} \frac{x^{2} - y^{2}}{r^{2}} = \frac{1}{\sqrt{2}} \left(Y_{22} + Y_{2-2} \right) \end{split}$$

$$\boldsymbol{m}_{L} = -\boldsymbol{\mu}_{B}\boldsymbol{L}$$
$$\boldsymbol{H}_{Zeeman} = -\boldsymbol{m}_{L} \cdot \boldsymbol{B} = \boldsymbol{\mu}_{B}\boldsymbol{L}_{z}\boldsymbol{B}$$

Electrons described by real 3*d* wavefunctions have zero orbital moment:

$$\left\langle \psi_{5} \left| \mathbf{L}_{z} \left| \psi_{5} \right\rangle = \frac{1}{2} \left(\left\langle +2 \right| + \left\langle -2 \right| \right) \mathbf{L}_{z} \left(\left| +2 \right\rangle + \left| -2 \right\rangle \right) = \frac{1}{2} \left(+2 -2 \right) = 0$$



In the presence of a cubic crystal field larger than the s.o. or Zeeman field:

$$t_{2g} \text{ subspace:} \\ \left\langle L_z \right\rangle_{ij} = \begin{pmatrix} 0 & 0 & -i \\ 0 & 0 & 0 \\ i & 0 & 0 \end{pmatrix} \xrightarrow{\text{diagonalize}} \begin{pmatrix} -1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

e_g subspace:

$$\left\langle L_z \right\rangle_{ij} = \begin{pmatrix} 0 & 0 \\ 0 & 0 \end{pmatrix}$$

eigenvectors

$$t_1 = \frac{1}{\sqrt{2}} (\psi_1 - i\psi_3) = Y_{2-1}$$

 $t_2 = \frac{1}{\sqrt{2}} (-i\psi_1 + \psi_3) = Y_{21}$
 $t_3 = \psi_2 = \frac{-i}{\sqrt{2}} (Y_{22} - Y_{2-2})$ **Rotition**

unperturbed Schroedinger equation: $H_0 |\psi_{gnd}^0\rangle = E_{gnd}^0 |\psi_{gnd}^0\rangle$ small perturbation: $(H_0 + \lambda V) |\psi\rangle = E |\psi\rangle$ $E = E^{(0)} + \lambda E^{(1)} + \lambda^2 E^{(2)} + \dots$ $|\psi\rangle = |\psi^{(0)}\rangle + \lambda |\psi^{(1)}\rangle + \lambda^2 |\psi^{(2)}\rangle + \dots$ $E^{(1)} = \left\langle \psi_{gnd}^{(0)} \left| V \right| \psi_{gnd}^{(0)} \right\rangle$ $\left| \psi^{(1)} \right\rangle = \sum_{\text{exc}\neq\text{gnd}} \frac{\left\langle \psi_{exc}^{(0)} \left| V \right| \psi_{gnd}^{(0)} \right\rangle}{E_{exc}^{(0)} - E_{ond}^{(0)}} \left| \psi_{exc}^{(0)} \right\rangle$ $E^{(2)} = \sum_{\text{exc}\neq\text{gnd}} \frac{\left| \left\langle \psi_{exc}^{(0)} \middle| V \middle| \psi_{gnd}^{(0)} \right\rangle \right|^2}{E_{exc}^{(0)} - E_{ond}^{(0)}}$



Tetragonal distorted d⁹ state (Cu²⁺, 10 Dq=2 eV, $D_s=0.1 eV$, $D_t=0$)



Unperturbed ground state has d_{x2-y2} symmetry, i.e., <L> = 0, however

$$\lambda \mathbf{L} \cdot \mathbf{S} = \lambda \left(\mathbf{L}_{\mathbf{z}} \mathbf{S}_{\mathbf{z}} + \mathbf{L}_{+} \mathbf{S}_{-} + \mathbf{L}_{-} \mathbf{S}_{+} \right)$$

mixes excited states into d_{x2-y2} inducing nonzero <L> ~ $\lambda/\Delta E$

Orbital moment in low-dimensional metal films



Directional quenching of orbital moment in a free-standing metal layer:



Orbital moment in low-dimensional metal films



VOLUME 75, NUMBER 20 PHYSICAL REVIEW LETTERS 13 N
 Microscopic Origin of Magnetic Anisotropy in Au/Co/Au Probed with X-Ray Magnetic Circular Dichroism
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enhanced orbital magnetic moment from 3D to 2D and 1D



P. Gambardella et al., Phys. Rev. Lett. 93, 077203 (2004).

Orbital moment and magnetocrystalline anisotropy in 3d metals



see, e.g., P. Bruno, PRB **39**, 865 (1989); H. A. Dürr et al., *Science* **277**, 213 (1997).



Magnetocrystalline anisotropy

$$E_a = E(\mathbf{M} \parallel \hat{z}) - E(\mathbf{M} \perp \hat{z})$$

Can be defined as: magnetic anisotropy energy per atom (eV/atom) magnetic anisotropy energy per unit volume (MJ/m³, erg/cm³)

 $\alpha_1 = \cos \theta$ $\alpha_2 = \sin\theta\cos\phi$ $\alpha_3 = \sin\theta\sin\phi$ cubic system: $F(\mathbf{M}) = K_0 + K_1(\alpha_1^2 \alpha_2^2 + \alpha_1^2 \alpha_3^2 + \alpha_2^2 \alpha_3^2) + K_2 \alpha_1^2 \alpha_2^2 \alpha_3^2 + \dots$ $= K_0 + \frac{K_1}{64} \{ (3 - 4\cos 2\theta + \cos 4\theta)(1 - \cos 4\phi) + 8(1 - \cos 4\theta) \} + \frac{K_2}{256} (1 - \cos 2\theta - 2\cos 4\theta + \cos 6\theta)(1 - \cos 4\phi) + \dots$

uniaxial system:

$$F(\mathbf{M}) = K_0 + K_1 \sin^2 \theta + K_2 \sin^4 \theta + \dots$$

Fe bcc

easy axis: (100)

Co hcp

easy axis: (0001)

Ni fcc

easy axis: (111)





 $K_1 = 4.8 \times 10^4 J/m^3$ $= 2.4 \ \mu eV/atom$

 $K_1 = 4.1 \times 10^5 \ J \ / \ m^3$ $= 45 \ \mu eV \ / \ atom$

<111> 500 Easy <111> Medium Magnetization (emu/cm³) <110> 400 300 ∞ 0 <100>200 100 0 100 500 600 Magnetic field (Oe)

 $K_1 = -5.5 \times 10^3 \ J \ / m^3$ = -0.3 \ \mu eV \ \ atom

Magnetic anisotropy energy, angular dependence



 Table 1: Typical ground-state energies E in eV/atom for 3d metal films

	E (eV/atom)
cohesive energy	5.5
local moment formation	1.0
alloy formation	0.5
magnetic order	0.2
structural relaxation	0.05
magnetic anisotropy	0.0001÷0.002

Courtesy G. Bihlmayer, FZ Jülich

Temperature dependence of magnetic anisotropy energy constants





Laboratoire d'Électrostatique et de Physique du Métal, Grenoble.

The magnetocristalline energy term depends on the symmetry of the crystal which defines the interaction directions between neighbour atoms. In a classic pair model the energy of a pair of atoms is supposed to depend only on the angle between their spins and the interatomic axis:

$$E_{ij} = l(\cos^2 \varphi_{ij} - 1/3) + q(\cos^4 \varphi_{ij} + ...)$$

For a solid with cubic simmetry, summing E_{ij} over nearest neighbours cancels out the cos² term this is not true anymore in the case of a surface, where the anisotropy energy per unit area becomes (neglecting the higher order terms):

$$K = \frac{1}{2} \sum_{i,j} l \cos^2 \varphi_{ij}$$



W. J. M. de Jonge et al., in Ultrathin Magnetic Structures I, J. A. C. Bland and B. Heinrich eds., Springer (1994)

Chappert and Bruno, J. Appl. Phys. 64, 5736 (1988)





Orientation and shape of Co magnetic domains

 $20\ \mu m$ S. Rusponi, P.G., L. Claude, H. Brune, F. Nolting, unpublished

PHYSICAL REVIEW B

VOLUME 42, NUMBER 17

15 DECEMBER 1990-I

Molecular-beam-epitaxial growth and magnetic properties of Co-Pt superlattices oriented along the [001], [110], and [111] axes of Pt

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Co/Pt superlattices grown by MBE with [001], [110], [111] orientation:

"Epitaxy along these different orientations can clearly induce defect structures and local lattice distortions that may result in different values of the magnetocrystalline anisotropy."



Spin-orbit interaction, orbital moment anisotropy, and MCA

 $H_{so} = \xi \mathbf{S} \cdot \mathbf{L}$

$$E_a = E_{so}(\hat{\mathbf{S}}_z) - E_{so}(\hat{\mathbf{S}}_x)$$



Orbital moment and magnetocrystalline anisotropy

... a long story

1930s – Bloch and Gentile, Van Vleck

1940s – H. Brooks

Crystal field theory (see, e.g., Molecular Magnetism by O. Kahn)

1990s – transition metal films

P. Bruno, PRB 39, 865 (1989)

G. van der Laan, JPCM 10, 3239 (1998).



the magnetic anisotropy: Angular dependence - atomic symmetry Magnitude - 3d bandwidth - orbital moment - spin-orbit coupling *K* depends on the atomic coordination: $K_{\rm Co_1/Pt}$ = 200 $K_{\rm Co \ bulk}$

Factors that determine







STM of individual Co atoms on Pt(111) (image size 85 x 85 Å²)



Science 300, 1130 (2003); Surf. Sci. 603, 1830 (2009).



2nd order perturbation theory:

P. Bruno, PRB 39, 865 (1989) G. van der Laan, JPCM 10, 3239 (1998).

$$K \sim \frac{\xi_{\rm s.o.}}{4} \left< \Delta L \right>$$

More on local atomic environment effects in metals

0.4 ML Co T = 130 K $T_{ann} = 300$ K Monolayer experiment 1.0 area Co islands perimeter 0.8 perimeter & area Size about [.n.] X [a.u.] 0.4 1000 atoms 0.2 0.0 50 100 150 200 250 300 0 *T* [K] 250 Å 0.2 ML Pt core and 0.2 ML Co shell 1.0 0.8 χ [a.u.]

0.6

0.4

0.2

0.0

0

50

100

perimeter & area

200

250

150

T [K]

Compared to pure Co islands: 1) same total MAE 2) reduced magnetic moment S. Rusponi et al., Nature Mat. 2, 546 (2003).

200 Å

Co Pt

4Å-

2Å-

0Å-





Single molecule magnets

Single-molecule magnets (SMMs)





"Mn₁₂ acetate"

Sessoli et al., Nature 1993

"Tb double-decker"

Ishikawa et al., JACS 2003

$[\mathrm{Mn}_{12}\mathrm{O}_{12}(\mathrm{CH}_{3}\mathrm{COO})_{16}(\mathrm{H}_{2}\mathrm{O})_{4}]\!\cdot\!2\mathrm{CH}_{3}\mathrm{COOH}\!\cdot\!4\mathrm{H}_{2}\mathrm{O}$



Total spin: S=8x(2)+4x(-3/2)=10

Spin Hamiltonian: $H = -DS_z^2 - AS_z^4 - g\mu_B S_z B_z$

Relatively large single molecule moment, 20 μ_{B} Relatively small number of quantum levels

Magnetic relaxation at high temperature

Thermal activation (over the barrier)



 $U=DS^{2} + AS^{4} = 6 \text{ meV}$ and $v_{0} = 0.5 \times 10^{7} \text{ Hz}$

Arrhenius law





Classicaly :

Calculated field required to reverse the magnetization \approx 12 T

Quantum tunneling between resonant spin states Mn₁₂ Molecular clusters





- ✓ smalles magnets
- ✓ identical quantum objects
- ✓ cheap to make

X low T_B

- X not easy to manipulate/assemble
- X write?



Figure 1 Representative examples of the peripheral functionalization of the outer organic shell of the $[Mn_{12}O_{12}(CH_3COO)_{16}(H_2O)_4]$ SMM (centre). Different functionalizations used to graft the SMM to surfaces are displayed: **a**, $[Mn_{12}O_{12}(C(CH_3)_3COO)_{16}(H_2O)_4]$. **b**, $[Mn_{12}O_{12}(p-CH_3S-C_6H_4-COO)_{16}(H_2O)_4]$. **c**, $[Mn_{12}O_{12}(O_2CC_6H_5)_8(1,8-dicarboxyl-10-(4-acetylsulphanylmethyl-phenyl)$ $anthracene-1,8-dicarboxylic acid)_4(H_2O)_4]$. **d**, $[Mn_{12}O_{12}(CH_3OS(CH_2)_{15}COO)_{16}(H_2O)_4]$. **e**, $[Mn_{12}O_{12}((CH_3)_3NCH_2COO)_{16}(H_2O)_4]^{16+}$. All structures are determined by X-ray crystallography, except **d**, which is a model structure. Solvent molecules have been omitted.

Surface functionalization of SMM?



Figure 3. Constant-current STM image of Au-bound Mn_{12} clusters (setpoint = 5 pA, bias = 1.3 V, scan size = 100 nm, scan rate = 3 Hz). The inset shows three isolated molecules (setpoint = 10 pA, bias = 0.8 V, scan size = 30 nm, scan rate = 3 Hz).

Cornia et al., Angew. Chem. 2003

Bogani and Wernsdorfer, Materials Naturals 2007

SMM deposition in UHV



Electronic Structure of Surface-supported Bis(phthalocyaninato) terbium(III) Single Molecular Magnets

Lucia Vitali,*,† Stefano Fabris,‡ Adriano Mosca Conte,‡ Susan Brink,§ Mario Ruben,§ Stefano Baroni,‡ and Klaus Kern^{†,II}

Perhaps, but not yet (ferro)magnetic !

2D spin networks

* + *





2D self-assembled supramolecular networks

terephthalic acid (TPA)







Fe : TPA ≈ 1:1

M. Lingenfelder et al., Chem. Eur. J. **10** (2004) 1913, P.G. et al. Nat. Mater. **8**, 189 (2009)