

# Simple concepts of magnetization reversal

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## II. Non-single-domain effects: Interactions, nanostructures and domain walls



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<http://perso.neel.cnrs.fr/olivier.fruchart/slides/>

# Was your head whirling?



Recas, Sep7th 2009

# Chamois, nearby Grenoble



June 1st, 2008

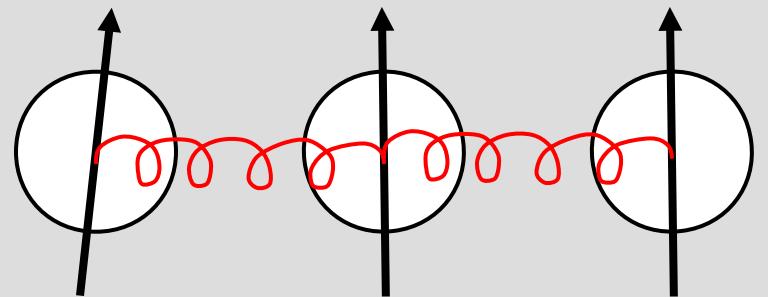
- **1. Dipolar energy**
- **2. Coercivity in patterned elements**
- **3. Manipulation of domain walls**
- **4. Interfacial effects**



## I.1. Dipolar energy

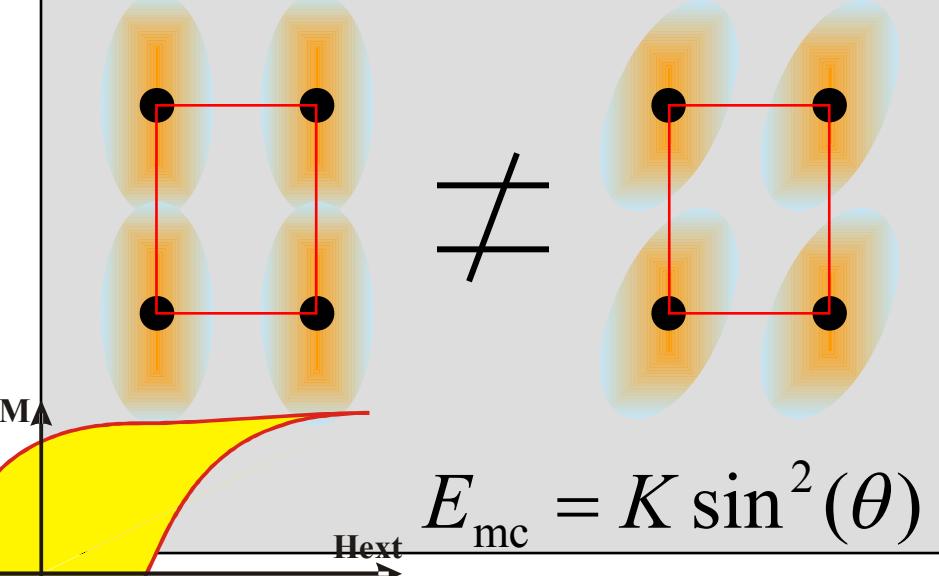
- 1. Treatment of dipolar energy
- 2. Some consequences of dipolar energy on hysteresis loops
- 3. Dipolar energy and collective effects in assemblies

## Exchange energy



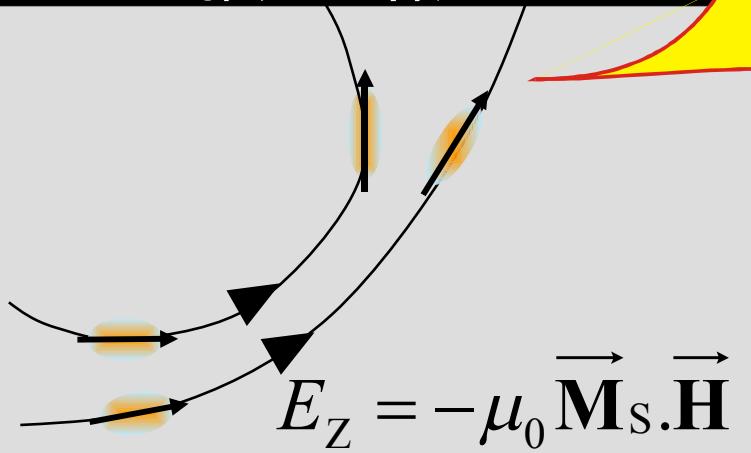
$$E_{\text{Ech}} = -J_{1,2} \vec{\mathbf{S}}_1 \cdot \vec{\mathbf{S}}_2 \\ = A(\nabla \theta)^2$$

## Magnetocrystalline anisotropy energy



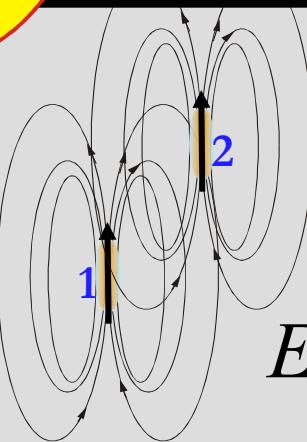
$$E_{\text{mc}} = K \sin^2(\theta)$$

## Zeeman energy (enthalpy)



$$E_Z = -\mu_0 \vec{\mathbf{M}}_S \cdot \vec{\mathbf{H}}$$

## Dipolar energy



$$E_d = -\frac{1}{2} \mu_0 \vec{\mathbf{M}}_S \cdot \vec{\mathbf{H}}_d$$

## Magnetization

Magnetization vector  $\mathbf{M}$

Can vary in time and space.

$$\mathbf{M} = \begin{pmatrix} M_x \\ M_y \\ M_z \end{pmatrix} = M_s \begin{pmatrix} m_x \\ m_y \\ m_z \end{pmatrix}$$

Modulus is constant

(hypothesis in micromagnetism)

$$m_x^2 + m_y^2 + m_z^2 = 1$$



Mean-field approach possible:  $M_s = M_s(T)$

Density of dipolar energy

$$E_d(\mathbf{r}) = -\frac{1}{2} \mu_0 \mathbf{M}(\mathbf{r}) \cdot \mathbf{H}_d(\mathbf{r})$$

By definition  $\text{div}(\mathbf{H}_d) = -\text{div}(\mathbf{M})$ . As  $\text{curl}(\mathbf{H}_d) = \mathbf{0}$  we have (analogy with electrostatics):

$$\mathbf{H}_d(\mathbf{r}) = -M_s \iiint_{\text{space}} \frac{\text{div}[\mathbf{m}(\mathbf{r}')].(\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^3 r'$$

$\rho(\mathbf{r}) = -M_s \text{div}[\mathbf{m}(\mathbf{r})]$  is called the **volume density of magnetic charges**

To lift the divergence that may arise at sample boundaries a volume integration around the boundaries yields:

$$\mathbf{H}_d(\mathbf{r}) = M_s \left( - \iiint_{\text{space}} \frac{\text{div}[\mathbf{m}(\mathbf{r}')].(\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^3 r' + \iint_{\text{sample}} \frac{[\mathbf{m}(\mathbf{r}') \cdot \mathbf{n}(\mathbf{r}')].(\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 r' \right)$$

$\sigma(\mathbf{r}) = M_s \mathbf{m}(\mathbf{r}) \cdot \mathbf{n}(\mathbf{r})$  is called the **surface density of magnetic charges**, where  $\mathbf{n}(\mathbf{r})$  is the outgoing unit vector at boundaries



Do not forget boundaries between samples with different  $M_s$

## Some ways to handle dipolar energy

Integrated dipolar energy:

$$\mathcal{E} = -\frac{1}{2} \mu_0 \iiint_{\text{sample}} \mathbf{M} \cdot \mathbf{H}_d \cdot dV$$

Notice: six-fold integral over space:  
non-linear, long-range, time-consuming.  
Bottle-neck of micromagnetic calculations

Usefull theorem for finite samples:

$$\mathcal{E} = -\frac{1}{2} \mu_0 \iiint_{\text{sample}} \mathbf{M} \cdot \mathbf{H}_d \cdot dV = \frac{1}{2} \mu_0 \iiint_{\text{space}} \mathbf{H}_d^2 \cdot dV$$

⇒  $\mathcal{E}$  is always positive

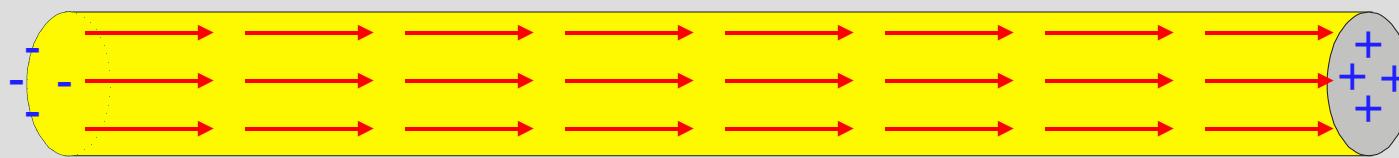
⇒ Significance of  $(BH_{\max})$  for permanent magnets

$$\begin{aligned} -\frac{1}{2} \mu_0 \iiint_{\text{sample}} (\mathbf{M} + \mathbf{H}_d) \cdot \mathbf{H}_d \cdot dV &= -\frac{1}{2} \mu_0 \iiint_{\text{sample}} \mathbf{B} \cdot \mathbf{H}_d \cdot dV \\ &= \frac{1}{2} \mu_0 \iiint_{\text{space} \setminus \text{sample}} \mathbf{H}_d^2 \cdot dV \end{aligned}$$

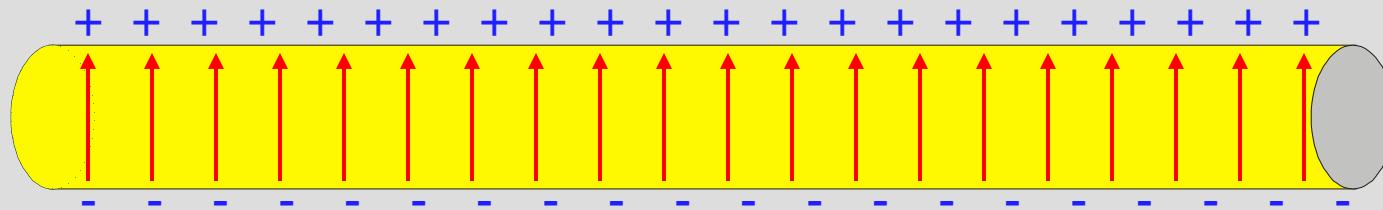
Cf: M. Coey

Energy available outside the sample, ie usefull for devices

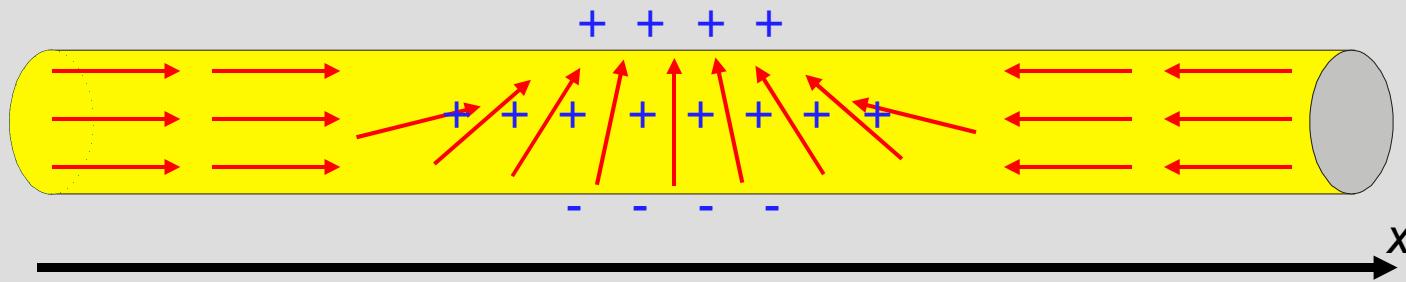
## Examples of magnetic charges



Notice: no charges  
and  $\epsilon=0$  for infinite  
cylinder



Charges on  
surfaces



Surface and  
volume charges

Assume uniform magnetization  $\mathbf{M}(r) \equiv \mathbf{M} = M_s(m_x\mathbf{x} + m_y\mathbf{y} + m_z\mathbf{z}) = M_s m_i \mathbf{u}_i$

$$\begin{aligned}\mathbf{H}_d(\mathbf{r}) &= M_s \iint_{\text{sample}} \frac{[\mathbf{m} \cdot \mathbf{n}(\mathbf{r}')].(\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 r' \\ &= M_s m_i \iint_{\text{sample}} \frac{n_i(\mathbf{r}').(\mathbf{r}' - \mathbf{r})}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 r',\end{aligned}$$

$$\begin{aligned}\mathcal{E}_d &= -\frac{1}{2} \mu_0 \iiint_{\text{sample}} \mathbf{H}_d(\mathbf{r}) \cdot \mathbf{M} d^3 \mathbf{r} \\ &= -\frac{1}{2} \mu_0 M_s^2 m_i \iiint_{\text{sample}} d^3 \mathbf{r} \iint_{\text{sample}} \frac{n_i(\mathbf{r}').[\mathbf{m} \cdot (\mathbf{r}' - \mathbf{r})]}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 \mathbf{r}' \\ &= -K_d m_i m_j \iiint_{\text{sample}} d^3 \mathbf{r} \iint_{\text{sample}} \frac{n_i(\mathbf{r}').(r_j' - r_j)}{4\pi \|\mathbf{r} - \mathbf{r}'\|^3} d^2 \mathbf{r}',\end{aligned}$$

$$\mathcal{E}_d = K_d V N_{ij} m_i m_j = K_d V \bar{\mathbf{m}} \cdot \bar{\mathbf{N}} \cdot \bar{\mathbf{m}}$$

See more detailed approach: M. Beleggia and M. De Graef, J. Magn. Magn. Mater. 263, L1-9 (2003)

$$\mathcal{E}_d = K_d N_{ij} m_i m_j = K_d {}^t \mathbf{m} \bar{\bar{\mathbf{N}}} \mathbf{m}$$

**N** is a positive second-order tensor

$$\langle \mathbf{H}_d(\mathbf{r}) \rangle = -M_s \bar{\bar{\mathbf{N}}} \cdot \mathbf{m}$$



... and can be defined and diagonalized  
for any sample shape

$$N = \begin{pmatrix} N_x & 0 & 0 \\ 0 & N_y & 0 \\ 0 & 0 & N_z \end{pmatrix}$$

$$\mathcal{E}_d = K_d (N_x m_x^2 + N_y m_y^2 + N_z m_z^2)$$

$$\langle H_{d,i}(\mathbf{r}) \rangle = -M_s N_i \quad \leftarrow \text{Valid along main axes only!}$$

$$N_x + N_y + N_z = 1$$

## What with ellipsoids???

Self-consistency: the magnetization must be at equilibrium and therefore fulfill  $\mathbf{m}/\mathbf{H}_{\text{eff}}$

→ Assuming  $\mathbf{H}_{\text{applied}}$  and  $\mathbf{H}_a$  are uniform, this requires  $\mathbf{H}_d(\mathbf{r})$  is uniform. This is satisfied only in volumes limited by polynomial surfaces of order 2 or less:  
slabs, cylinders, ellipsoids (+paraboloids and hyperboloids).

J. C. Maxwell, Clarendon 2, 66-73 (1872)

## Ellipsoids

$$N_x = \frac{1}{2}abc \int_0^{\infty} \left[ (a^2 + \eta)\sqrt{(a^2 + \eta)(b^2 + \eta)(c^2 + \eta)} \right]^{-1} d\eta$$

General ellipsoid:  
main axes (a,c,c)

$$N_x = \frac{\alpha^2}{1-\alpha^2} \left[ \frac{1}{\sqrt{1-\alpha^2}} \operatorname{Asinh} \left( \frac{\sqrt{1-\alpha^2}}{\alpha} \right) - 1 \right]$$

For prolate revolution ellipsoid:  
(a,c,c) with  $\alpha=c/a < 1$

$$N_x = \frac{\alpha^2}{\alpha^2 - 1} \left[ 1 - \frac{1}{\sqrt{\alpha^2 - 1}} \operatorname{Asin} \left( \frac{\sqrt{\alpha^2 - 1}}{\alpha} \right) \right]$$

For oblate revolution ellipsoid:  
(a,c,c) with  $\alpha=c/a > 1$

$$N_y = N_z = \frac{1}{2}(1 - N_x)$$

## Cylinders

$$N_x = 0; \quad N_y = c/(b+c); \quad N_z = b/(b+c) \quad \text{For a cylinder along } x$$

**J. A. Osborn, Phys. Rev. 67, 351 (1945).**

For prisms, see: **A. Aharoni, J. Appl. Phys. 83, 3432 (1998)**

More general forms, FFT approach: **M. Beleggia et al., J. Magn. Magn. Mater. 263, L1-9 (2003)**

## Magnetization loop of a macrospin along a hard axis

$$\epsilon = \sin^2(\theta) - 2h\cos(\theta - \theta_H)$$

Dipolar energy:  $H = h \cdot H_a$   
 $H_a = 2K / \mu_0 M_s$   
 $K = N_i K_d$

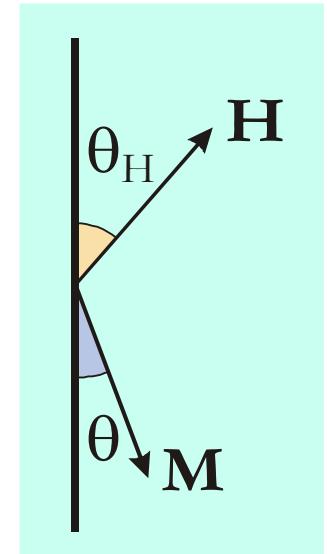
Hard axis:  $\theta_H = \pi/2$

$$\epsilon = \sin^2(\theta) - 2h \sin(\theta)$$

$$\frac{\partial \epsilon}{\partial \theta} = 2 \cos \theta (\sin \theta - h)$$

$$h = \sin \theta = \cos(\theta - \theta_H) = \mathbf{m} \cdot \mathbf{u}_h$$

Equilibrium position



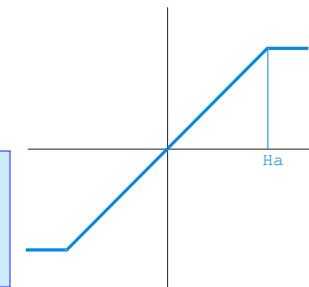
## Case of a bulk soft magnetic material

Hypotheses:

1. Use an ellipsoid, cylinder or slab along a main direction so that the demagnetizing field may be homogeneous.
2. Domains can be created to yield a uniform and effective magnetization  $\mathbf{M}_{\text{eff}}$

Density of energy:  $E_{\text{tot}} = E_d + E_Z$   
 $= \frac{1}{2} \mu_0 N \mathbf{M}_{\text{eff}}^2 - \mu_0 \mathbf{M}_{\text{eff}} H_{\text{ext}}$

Minimization:  $\frac{\partial E_{\text{tot}}}{\partial \mathbf{M}_{\text{eff}}} = \mu_0 N \mathbf{M}_{\text{eff}} - \mu_0 H_{\text{ext}} \rightarrow \mathbf{M}_{\text{eff}} = \frac{1}{N} \mu_0 H_{\text{ext}}$

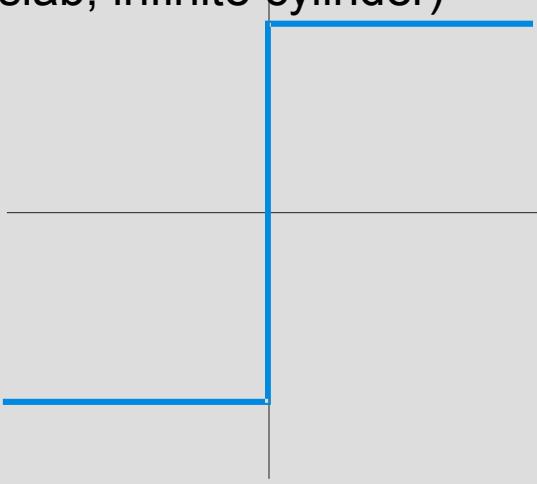


Conclusion for soft magnetic materials

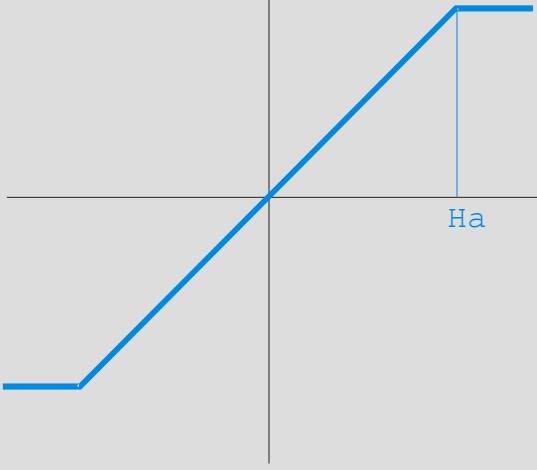
⇒ Susceptibility is constant and equal to  $1/N$

**Ideally soft**

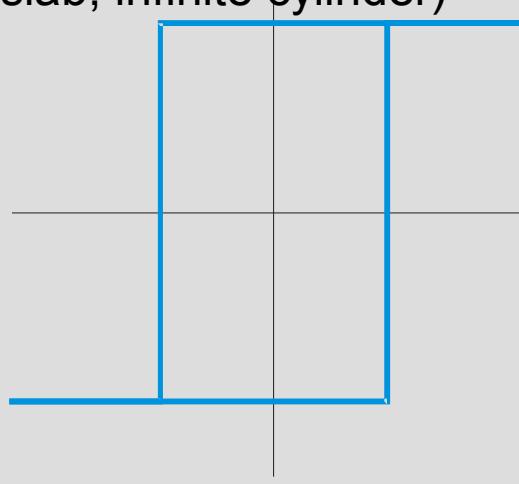
N=0 (slab, infinite cylinder)



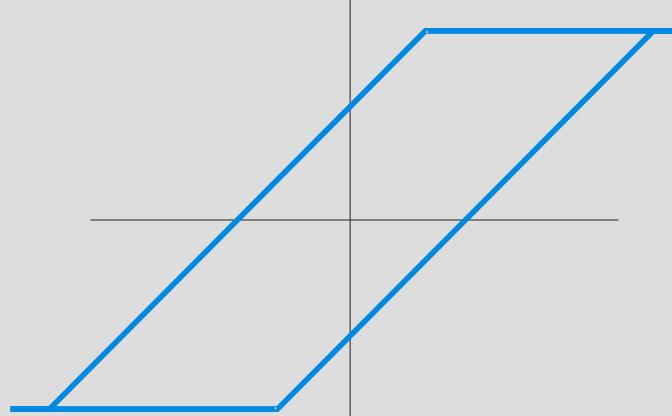
N>0 (here N=1: slab, perpendicular)

**Easy axis, coercitive**

N=0 (slab, infinite cylinder)



N>0 (here N=1: slab, perpendicular)

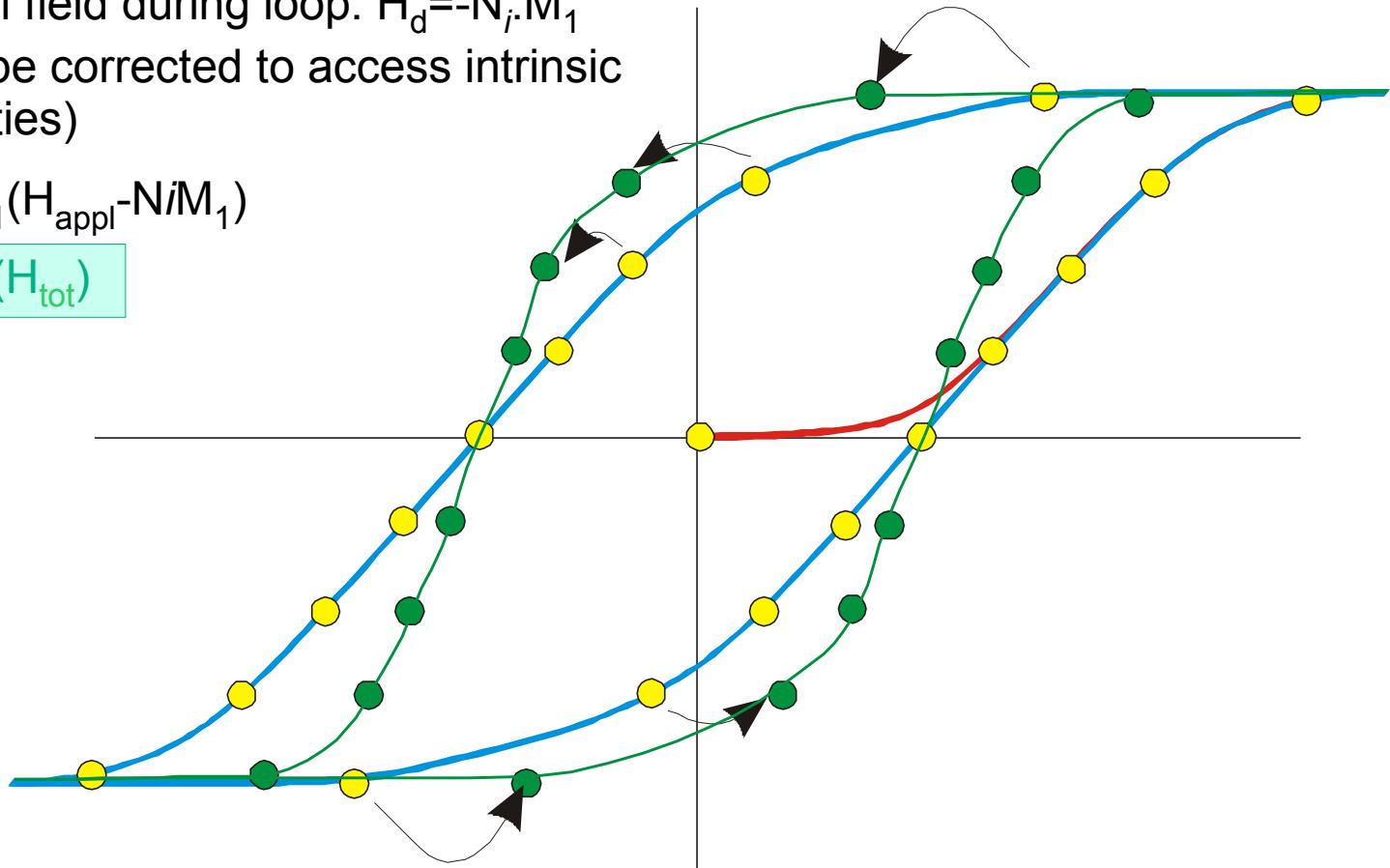


1. Measure a hysteresis loop  $M_1(H_{\text{appl}})$

2. Internal field during loop:  $H_d = -N_i \cdot M_1$   
(must be corrected to access intrinsic properties)

3. Plot  $M_1(H_{\text{appl}} - N_i M_1)$

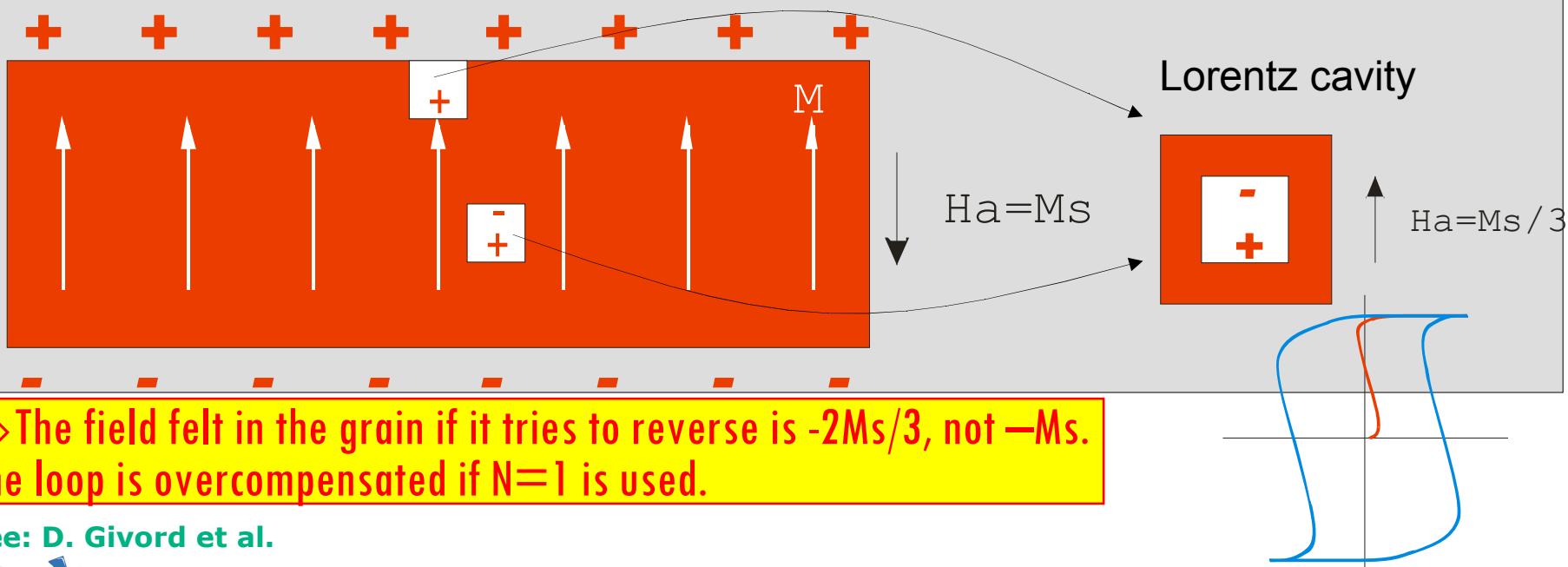
→  $M_2(H_{\text{tot}})$



## Specific aspects in hard magnetic materials

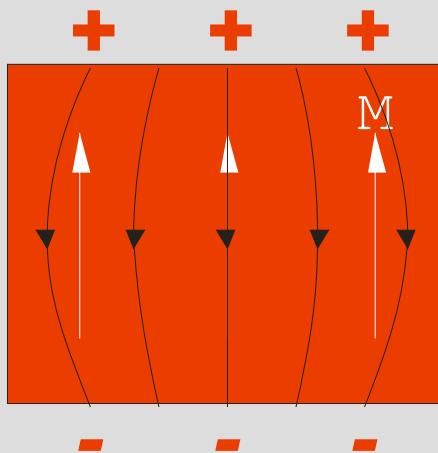
1. The concept of effective magnetization fails, because grains are either up or down.
2. Individual grains have a shape, implying a demagnetizing field that must be taken into account
3. In heteromaterials (ex: hard-soft; magnetic/non-magnetic etc.) the magnetization of both phases has to be taken into account. Depends also on grain size...

## Example with cubic grains



See: D. Givord et al.

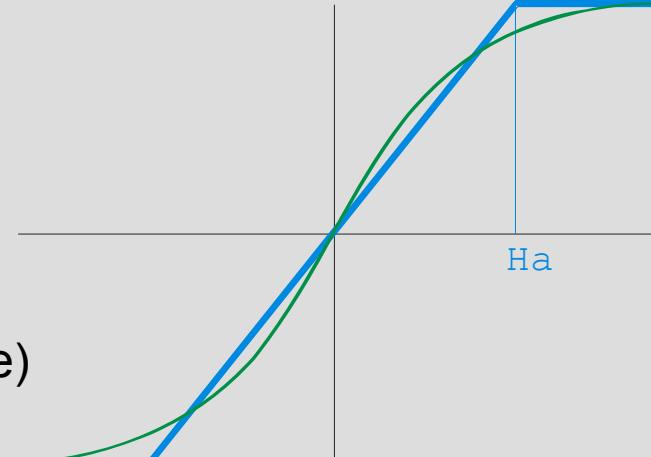
## Specific aspects to systems with non-ellipsoidal shapes



Cf: O. Chubykalo

In a non-ellipsoidal (or cylindrical, slab) system the demagnetizing field is not homogeneous in magnitude nor direction

1. Initial slope higher than  $1/N$   
(demag field smaller than average)
2. Late slope smaller than  $1/N$   
(demag field larger than average)



Demagnetizing energy (thus area above loop) is identical  $E_d = \int_0^{M_s} \mu_0 H_{\text{ext}} dM = \frac{1}{2} \mu_0 N M_s^2$

→ In a non-ellipsoidal sample (or cylinder, slab) the loop is overcompensated at low magnetization and undercompensated at high field, even for soft magnetic materials.  
→ This effect adds up to the previous effect of grain shape

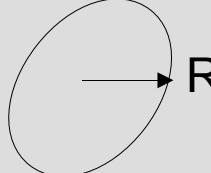
P. O. Jubert, O. Fruchart et al., *Europhys. Lett.* 63, 102-108 (2003)

## Upper bound for dipolar fields in 2D

Estimation of an upper range of dipolar field in a 2D system

$$\|\mathbf{H}_d(R)\| \leq \oint \frac{2\pi r dr}{r^3} \quad \text{Integration}$$

Local dipole:  $1/r^3$

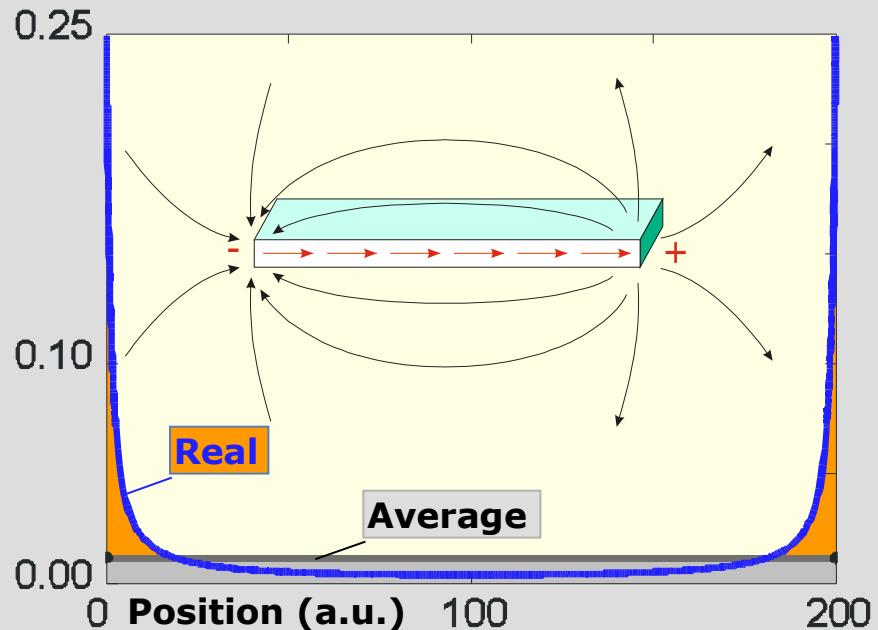


$$\|\mathbf{H}_d(R)\| \leq \text{Cte} + 1/R$$

Convergence with finite radius  
(typically thickness)

## Non-homogeneity of dipolar fields in 2D

Example: flat stripe with thickness/height = 0.0125



- ⇒ Dipolar fields are weak and short-ranged in 2D or even lower-dimensionality systems
- ⇒ Dipolar fields can be highly non-homogeneous in anisotropic systems like 2D
- ⇒ Consequences on dot's non-homogenous state,  
magnetization reversal, collective effects etc.

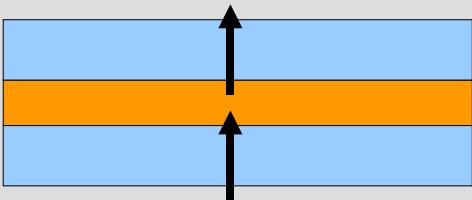


## Stacked dots : dipolar

In-plane magnetization



Out-of-plane magnetization



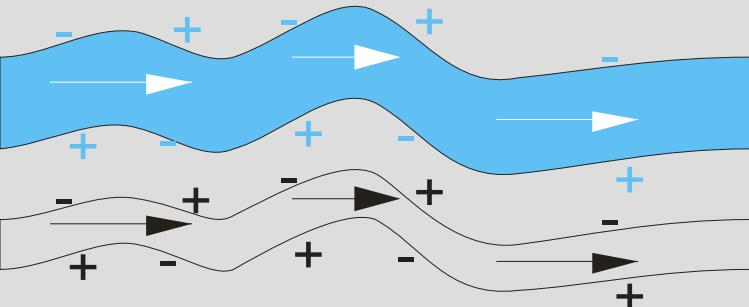
### Hint:

An upper bound for the dipolar coupling is the self demagnetizing field

**Notice:** similar situation as for RKKY coupling

## Stacked dots : orange-peel coupling

In-plane magnetization



Always parallel coupling

L. Néel, C. R. Acad. Sci. 255, 1676 (1962)

(valid only for thick films)

J. C. S. Kools et al., J. Appl. Phys. 85, 4466 (1999)

(valid for any films)

Out-of-plane magnetization

May be parallel or antiparallel

J. Moritz et al., Europhys. Lett. 65, 123 (2004)

## Models for arrays of single-domain planar rectangular dots

**E. Y. Tsymbal, Theory of magnetostatic coupling in thin-film rectangular magnetic elements, Appl. Phys. Lett. 77, 2740 (2000)**

**R. Álvarez-SÁnchez et al., Analytical model for shape anisotropy in thin-film nanostructured arrays: Interaction effects, J. Magn. Magn. Mater. 307, 171-177 (2006)**

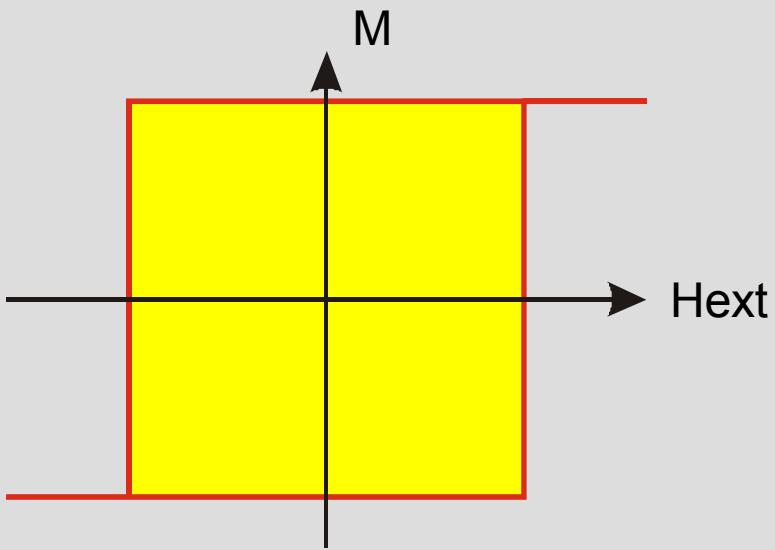
## Models for arrays of elements of arbitrary shapes

**M. Beleggia and M. De Graef, On the computation of the demagnetization tensor field for an arbitrary particle shape using a Fourier space approach, J. Magn. Magn. Mater. 263, L1-9 (2003)**

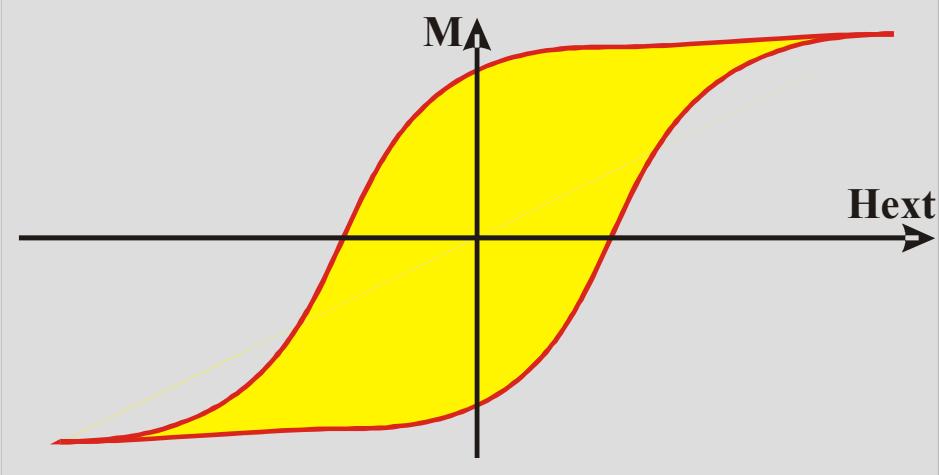
**E.Y. Vedmedenko, N. Mikuszeit, H. P. Oepen and R. Wiesendanger, Multipolar Ordering and Magnetization Reversal in Two-Dimensional Nanomagnet Arrays, Phys. Rev. Lett. 95, 207202 (2005)**

**N. Mikuszeit, E. Y. Vedmedenko & H. P. Oepen, Multipole interaction of polarized single-domain particles, J. Phys. Condens. Matter 16, 9037-9045 (2005)**

## Expected hysteresis loop for macrospins

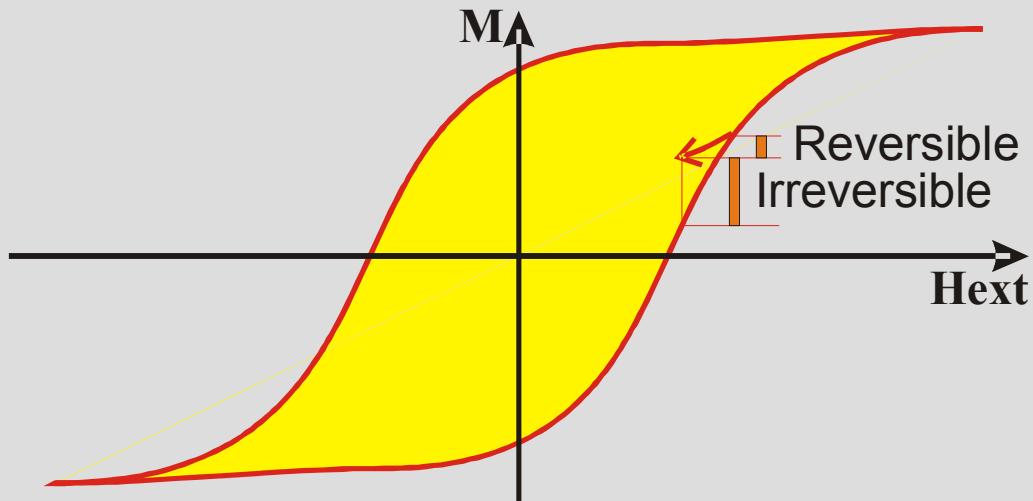


## Hysteresis for assemblies of dots

**Possible effects that may arise**

- Distribution of coercive fields
- (Dipolar) interactions
- The loops of the macrospins are slanted

## Distribution of properties

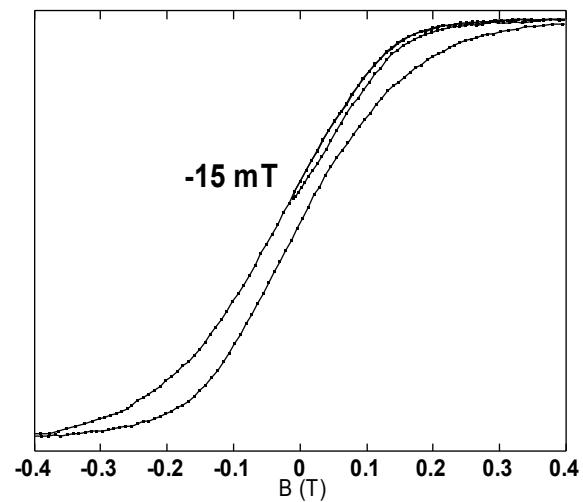


$$\rho(H_r) = \left. \frac{dm}{dH} \right|_{\text{irreversible}}$$

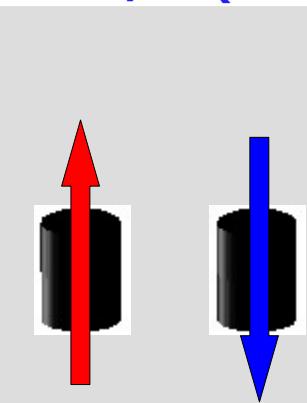
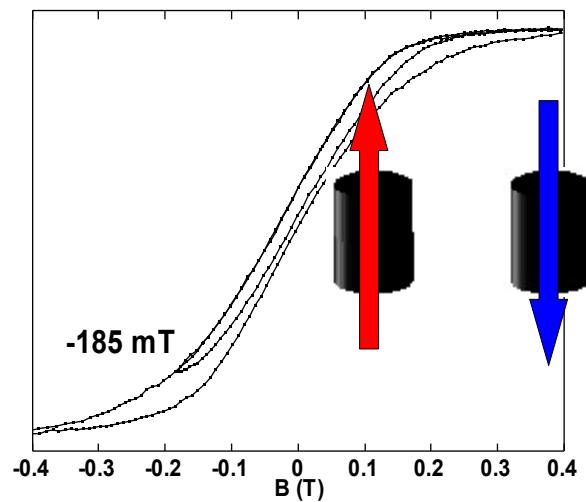
**$H_c(T)$  for a given population of the distribution can be studied at a given stage of the reversal (10%, 20% etc.)**

**Effect of distributions and dipolar interactions are sometimes difficult to disentangle**

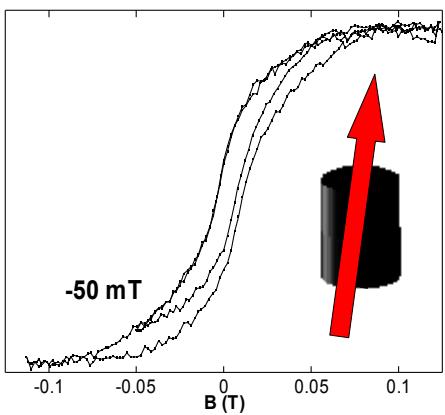
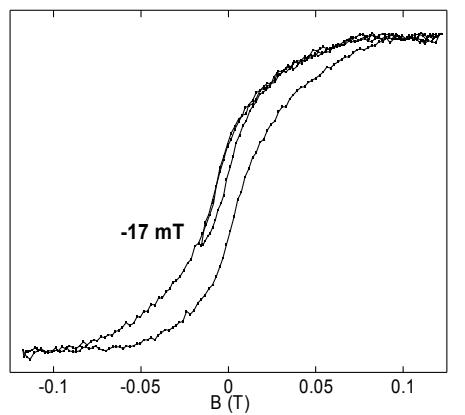
## Minor loops: negative interactions



**Example: dipolar interactions in arrays of Co/Au(111) pillars**



## Minor loops: negligible interactions



- Faster than Henkel and Preisach
- Other applications: characterization of exchange bias

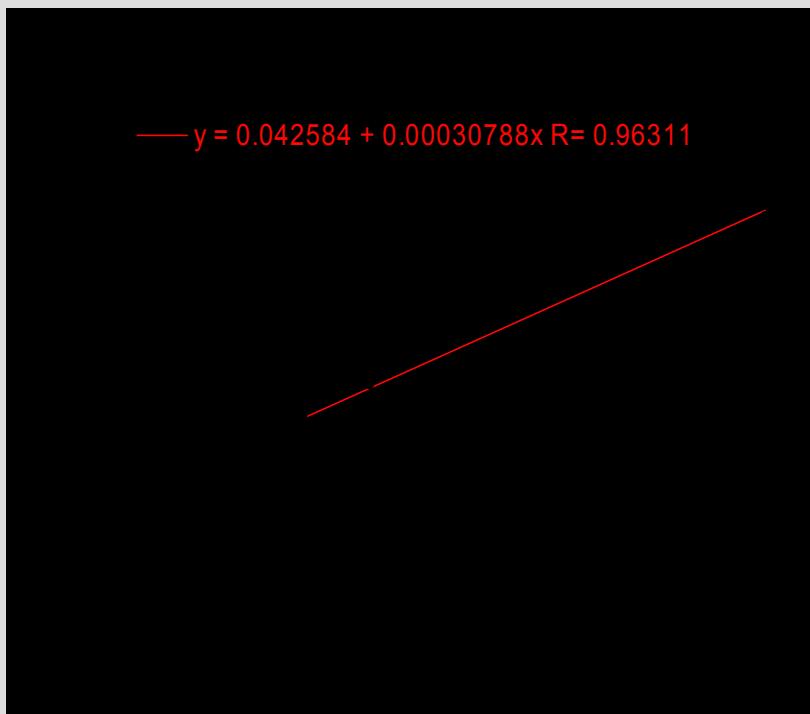
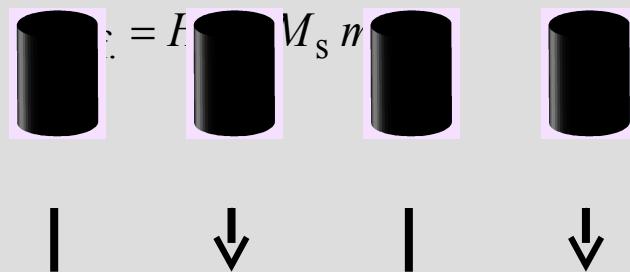
O. Fruchart et al., unpublished

## Superparamagnetic regime: plot of inverse susceptibility

- Brillouin 1/2 function

$$m = B_{1/2}(\mu_0 \mu_{\text{Co}} N H_{\text{eff.}} / kT)$$

- Effective field



- First order expansion:  
susceptibility

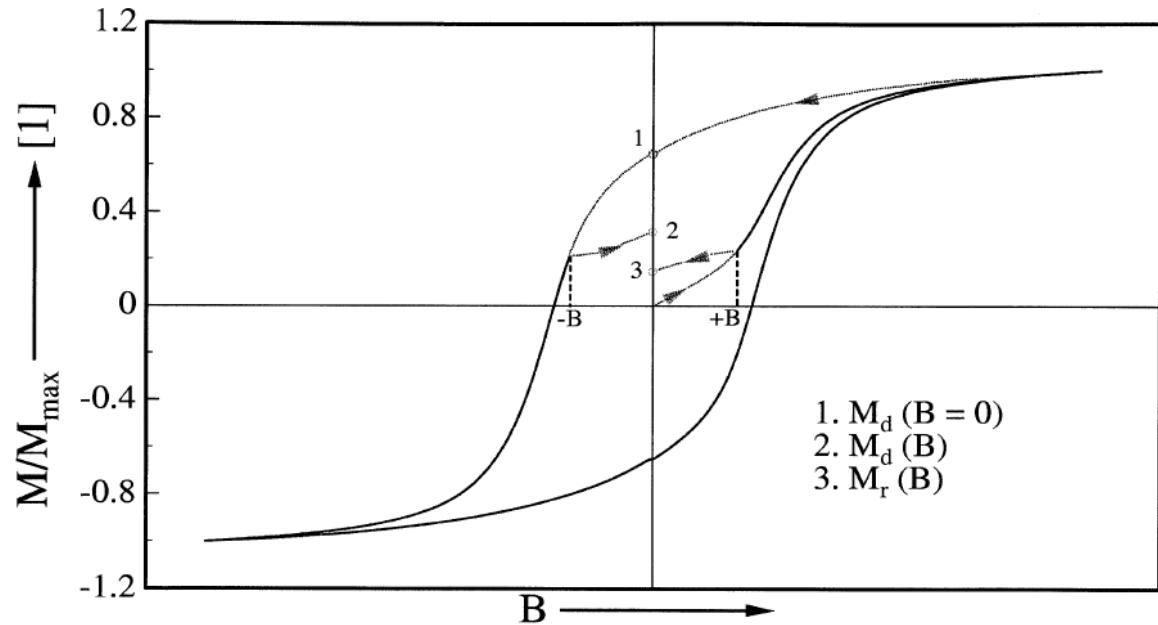
$$\frac{d(\mu_0 H)}{dm} = \frac{1}{\chi} = -\mu_0 M_S r + \frac{k}{\mu_{\text{Co}} N} T$$

*a* + *b* . *T*

O. Fruchart et al., PRL 23, 2769 (1999)

- No need of hysteresis
- Analogy with Curie-Weiss law

## Henkel plots



O. Henkel,  
Phys. Stat. Sol. 7, 919 (1964)

S. Thamm et al.,  
JMMM184, 245 (1998)

Fig. 1. Explanation of how to measure the two different remanent magnetisations  $M_r$  and  $M_d$ .

### Measure of dipolar interactions

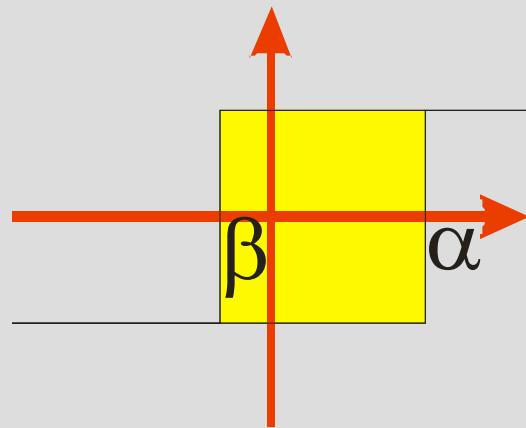
$$\Delta M_H(x) = M_d(x) - [1 - 2M_r(x)]$$

- The analysis of interactions on qualitative
- Long experiments (ac demagnetization)

## Preisach model

G. Biroci et al., Il Nuov. Cim. VII, 829 (1958)

I. D. Mayergoyz, Mathematical models of hysteresis, Springer (1991)

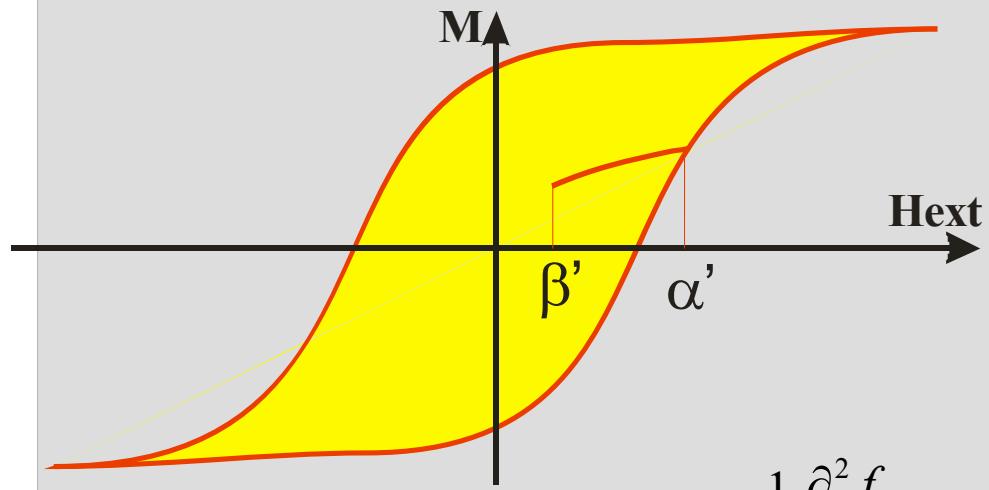


↳ Distribution function

$$\mu(\alpha, \beta) \text{ with } \alpha > \beta$$

↳ No true link between real particles and  $\mu$

## Solving



$$\mu(\alpha', \beta') = \frac{1}{2} \frac{\partial^2 f_{\alpha', \beta'}}{\partial \alpha' \partial \beta'}$$

- Long experiments (1D set of hysteresis curves)
- Better suited to bulk materials with strong interactions

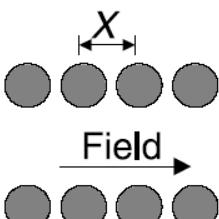
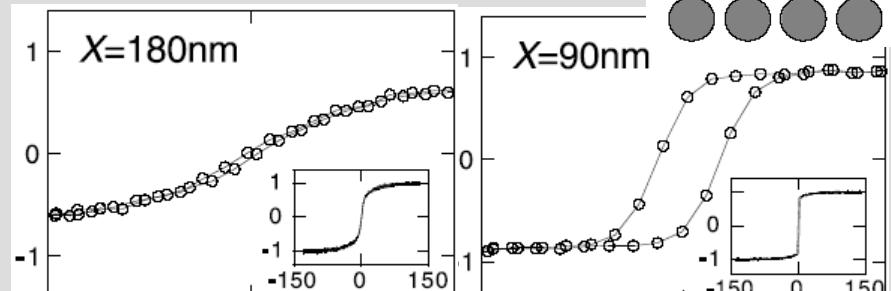
## Interactions between (suparamagnetic) particles

**S. Bedanta & W. Kleemann,**  
**Supermagnetism, J. Phys. D: Appl. Phys.,**  
**013001 (2009)**

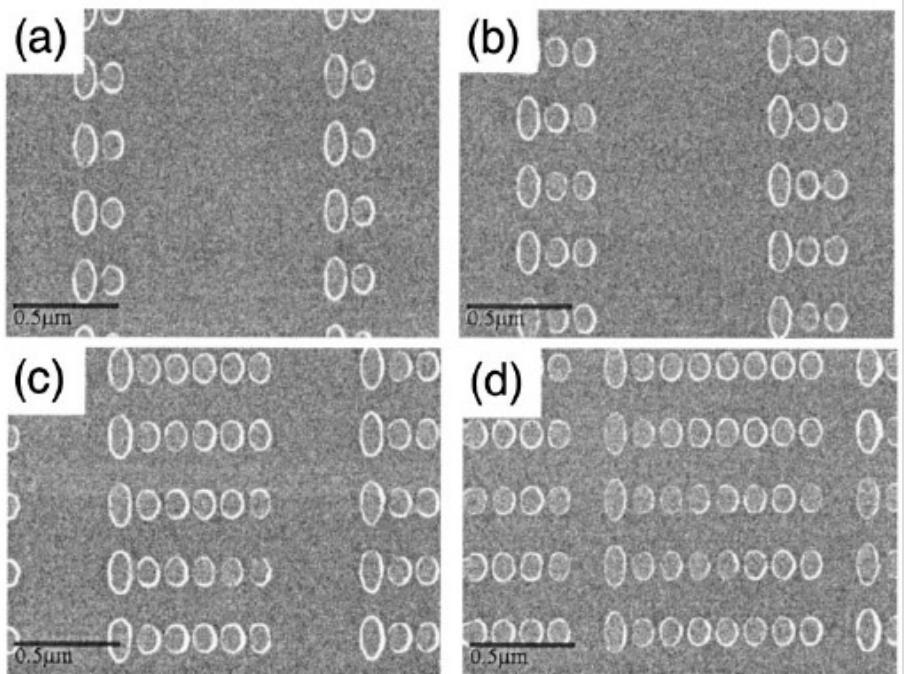
Cf O. Chubykalo:

'Negative' or 'Positive' interactions?  
 Smaller or larger energy barriers?

### Archetype for ferro coupling



### Archetype for AF coupling



R. P. Cowburn, PRB65, 092409 (2002)

### Conclusion:

Interactions may decrease or increase the switching field, as well as increase energy barriers

## II.2. Coercivity in patterned elements

- 1. Near-single domain structures
- 2. Flux-closure domains
- 3. Conclusion on characteristic length scales

## Configurational anisotropy: deviations from single-domain

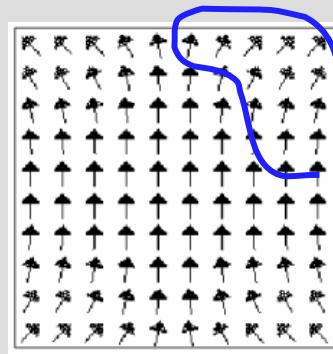
Strictly speaking, ‘shape anisotropy’ is of second order:

$$E_d = \frac{1}{2} \mu_0 (N_x M_x^2 + N_y M_y^2 + N_z M_z^2)$$

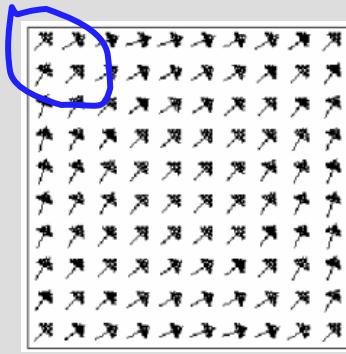
**2D:**  $E_{\text{tot}} = V K_d \sin^2 \theta$

In real samples magnetization is never perfectly uniform: competition between exchange and dipolar

Num.Calc. (100nm)



Flower state  
 $c/a > 2.7$



Leaf state  
 $c/a < 2.7$

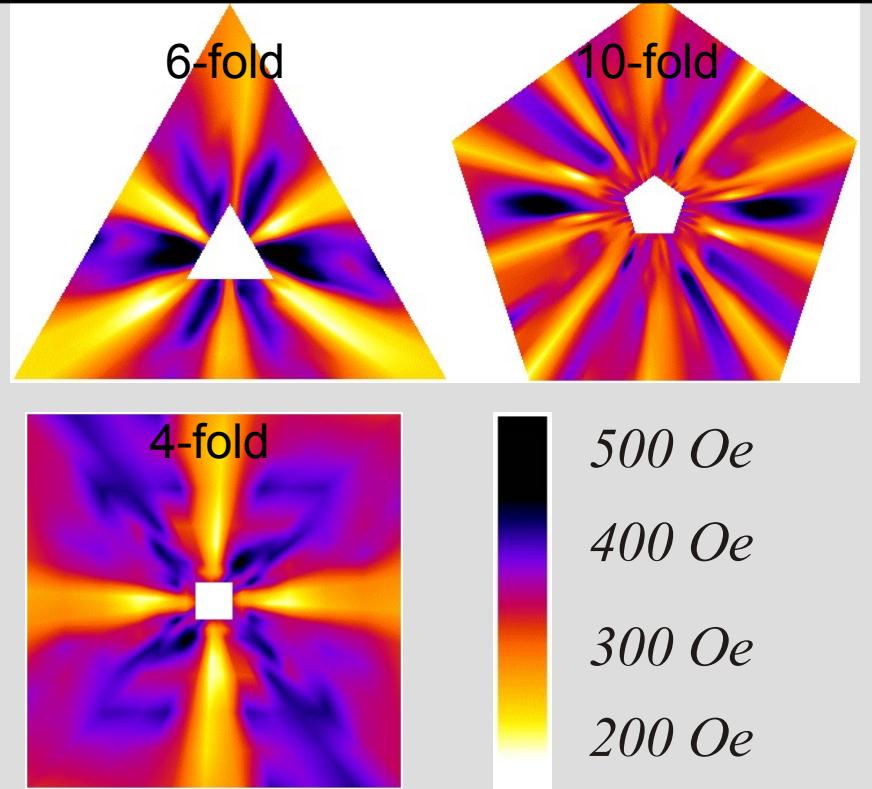
Configurational anisotropy may be used to stabilize configurations against switching

Higher order contributions to the anisotropy

M. A. Schabes et al., JAP 64, 1347 (1988)

R.P. Cowburn et al., APL 72, 2041 (1998)

## Polar plot of experimental configurational anisotropy with various symmetry

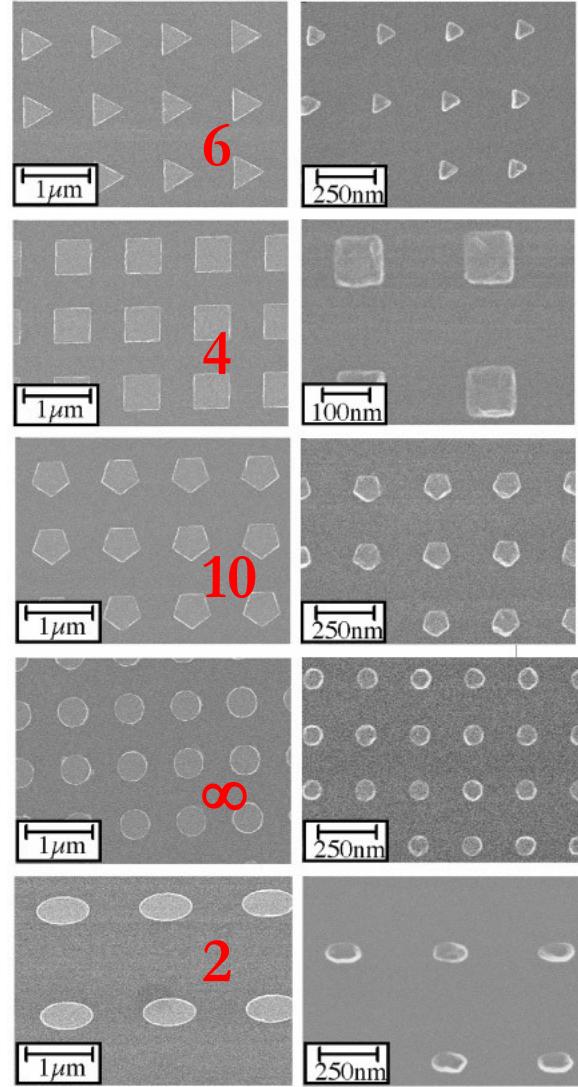


**Color code:** strength of anisotropy in a given direction

**Radius:** size of measured pattern

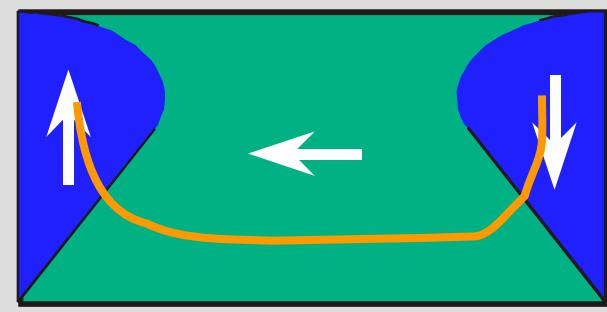
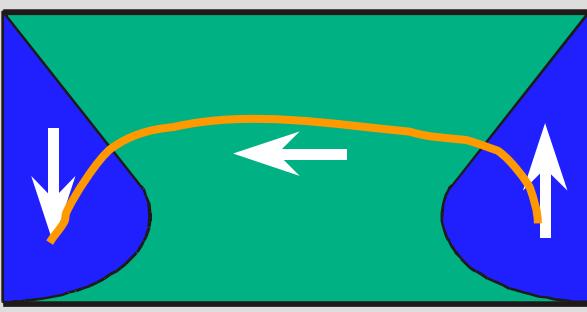
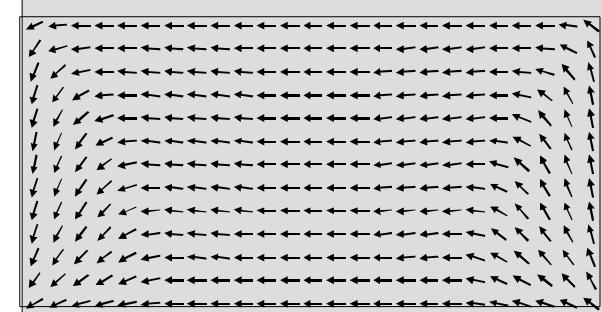
**Direction:** direction of measurement

R.P. Cowburn, J.Phys.D:Appl.Phys.33, R1-R16 (2000)

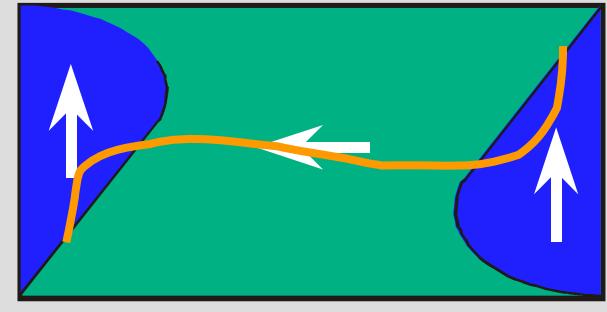
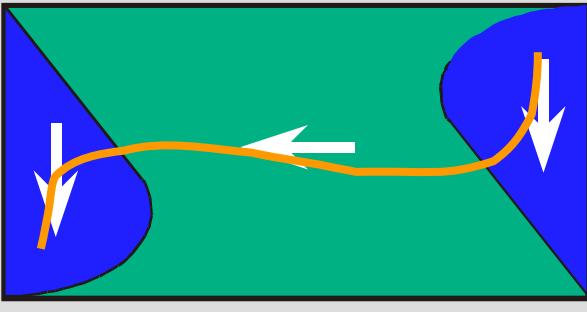
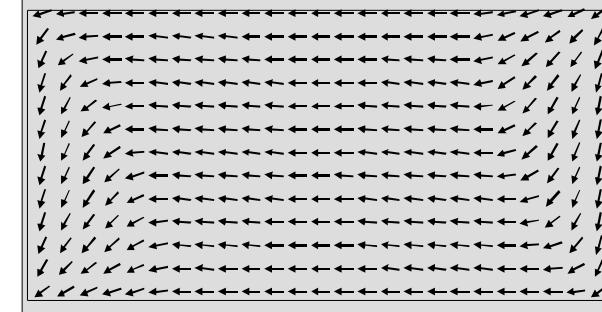




'C' state



'S' state

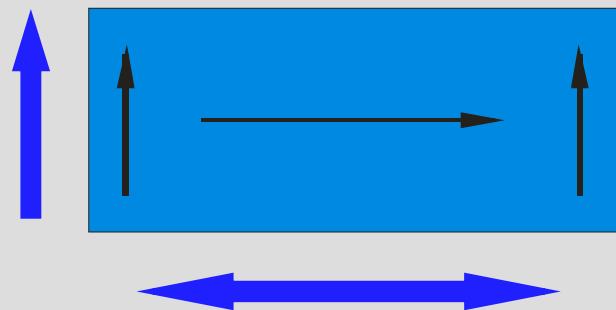


➡ At least 8 nearly-equivalent ground-states for a rectangular dot  
➡ Issue for the reproducibility of magnetization reversal

# NON-SINGLE DOMAIN EFFECTS – C and S states (2/2)

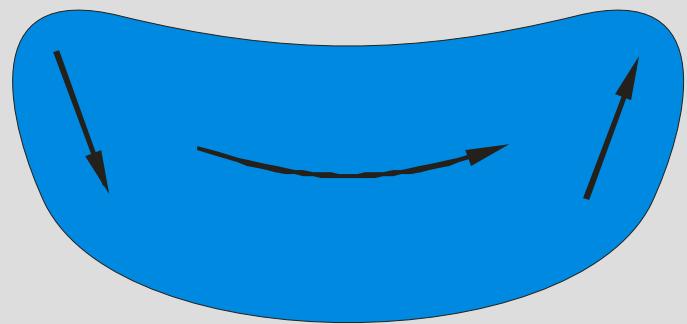
## Preparation of 'S' state

Transverse field to keep end domains aligned parallel to each other



Longitudinal field to reverse the magnetization

## Preparation of 'C' state



End domains aligned mainly antiparallel owing to a dipolar shape effect

## Purpose

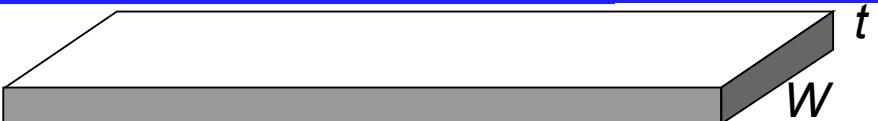
☞ Avoid the formation of  $180^\circ$  domain walls during magnetization reversal

# NON-SINGLE DOMAIN EFFECTS – Coercivity of stripes

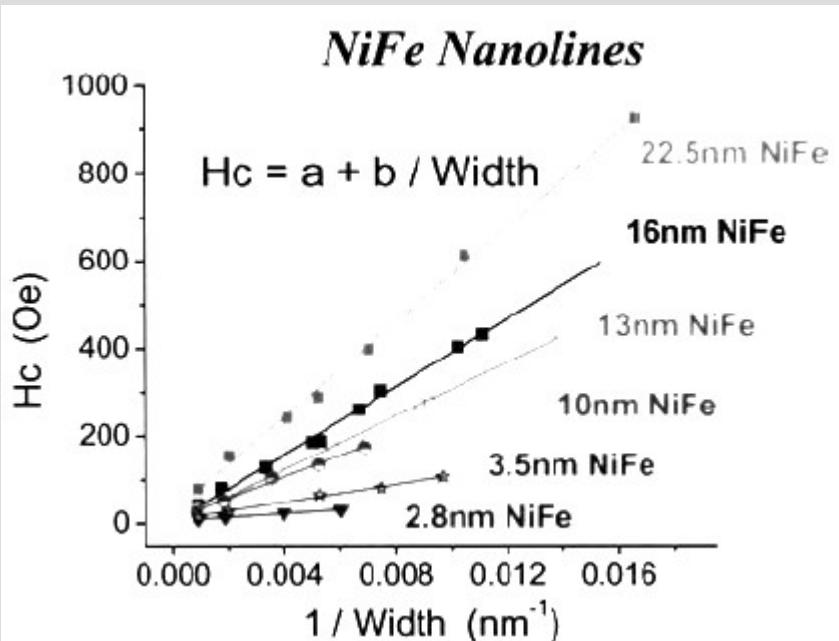


Hypotheses  $\Rightarrow$  Soft magnetic material

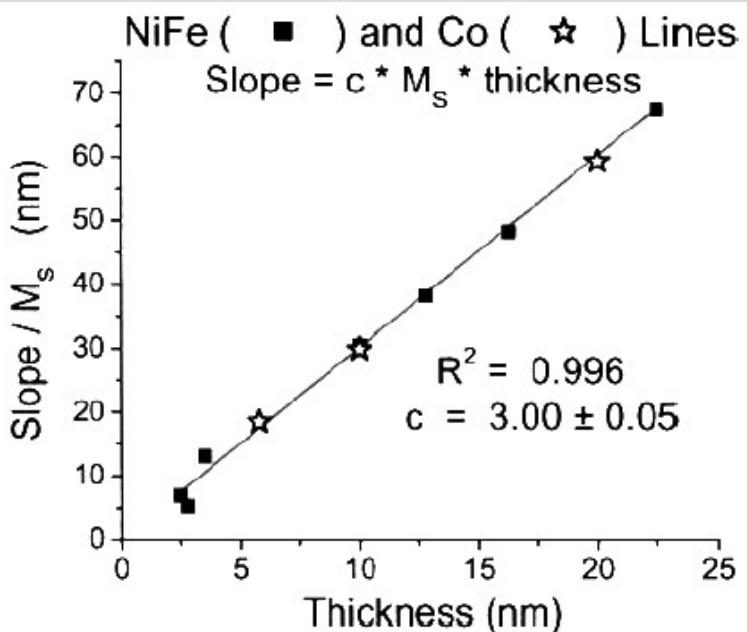
$\Rightarrow$  Not too small neither too large nanostructures



$H_c \sim 1/\text{Width}$



$H_c \sim M_s * \text{Thickness}$



$$H_c = a + 3M_s \frac{t}{W}$$



$\sim$  lateral demagnetizing coefficient of the stripe

W. C. Uhlig & J. Shi,  
Appl. Phys. Lett. 84, 759 (2004)

Magnetization is pinned at sharp ends

Experiments Permalloy (soft)

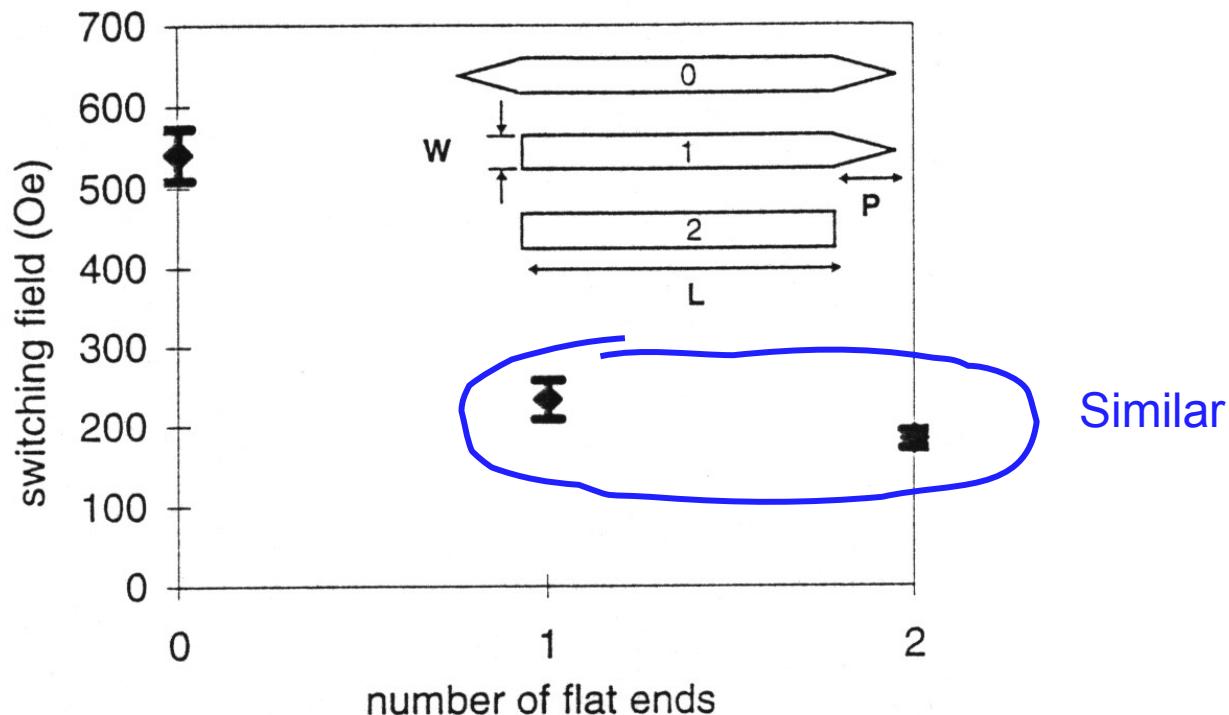


Fig. 8 Dependence of switching field of acicular elements on the **number of flat ends**. Element geometry is also shown:  $L=2.5\ \mu\text{m}$ ,  $W=200\ \text{nm}$ ,  $P=500\ \text{nm}$ .

K.J. Kirk et al., J. Magn. Soc. Jap., 21 (7), (1997)

## Magnetization is pinned at sharp ends

### Numerical micromagnetic calculation

J.G. Zhu

6672 J. Appl. Phys., Vol. 87, No. 9, 1 May 2000

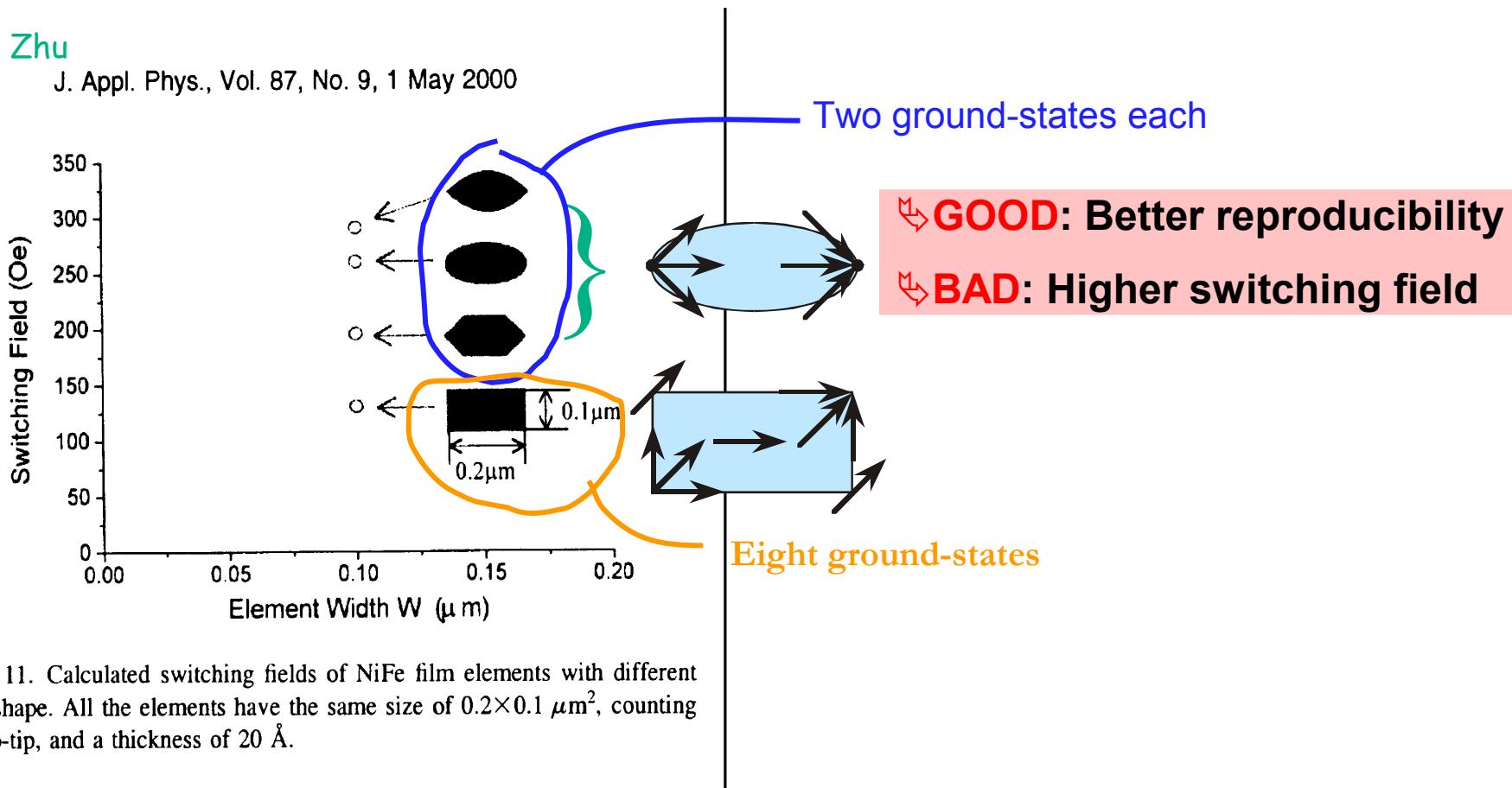


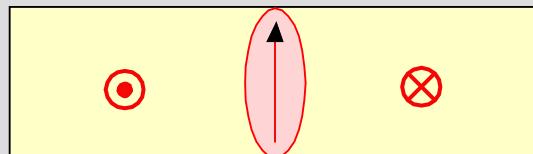
FIG. 11. Calculated switching fields of NiFe film elements with different end shape. All the elements have the same size of  $0.2 \times 0.1 \mu\text{m}^2$ , counting tip-to-tip, and a thickness of 20 Å.

Essentially Equivalent Topological Properties

## Bloch versus Néel wall

Crude model: wall is a uniformly-magnetized cylinder with an ellipsoid base

Bloch wall



$$E_d = K_d \frac{W}{2t}$$

Thickness t

Néel wall



$$E_d = K_d \frac{t}{2W}$$

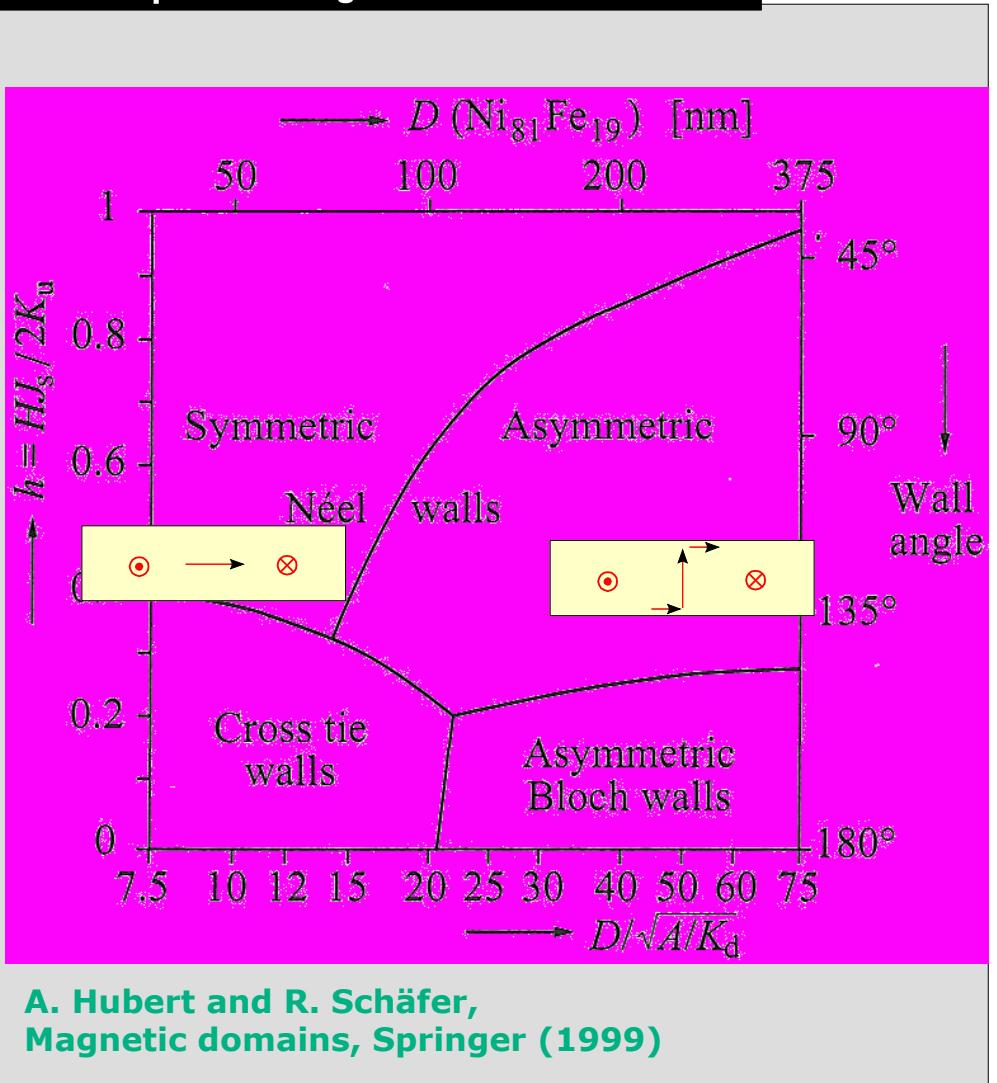
Wall width W

L. Néel, Énergie des parois de Bloch dans les couches minces,  
C. R. Acad. Sci. 241, 533-536 (1955)

### Conclusion

- ⇒ At low thickness (roughly  $t \approx W$ ) Bloch domain walls are expected to turn their magnetization in-plane > Néel wall
- ⇒ Model needs to be refined
- ⇒ Domain walls not changed for films with perpendicular magnetization

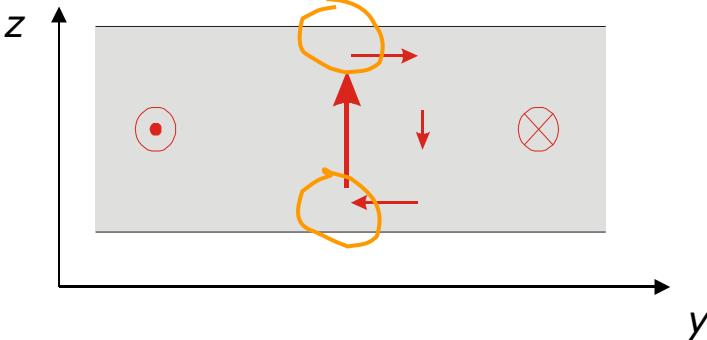
## Refined phase diagram of domain walls



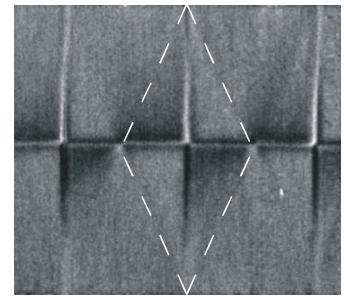
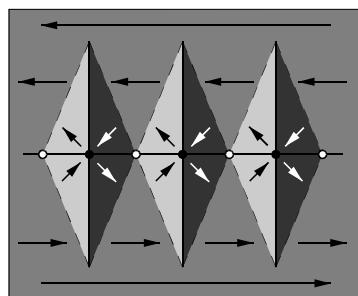
Néel caps occur atop Bloch walls to reduce surface and volume magnetic charges

$$\mathbf{M} \cdot \mathbf{n} = 0$$

$$-\operatorname{div} \mathbf{M} = -\frac{\partial M_x}{\partial x} - \frac{\partial M_y}{\partial y} - \frac{\partial M_z}{\partial z}$$

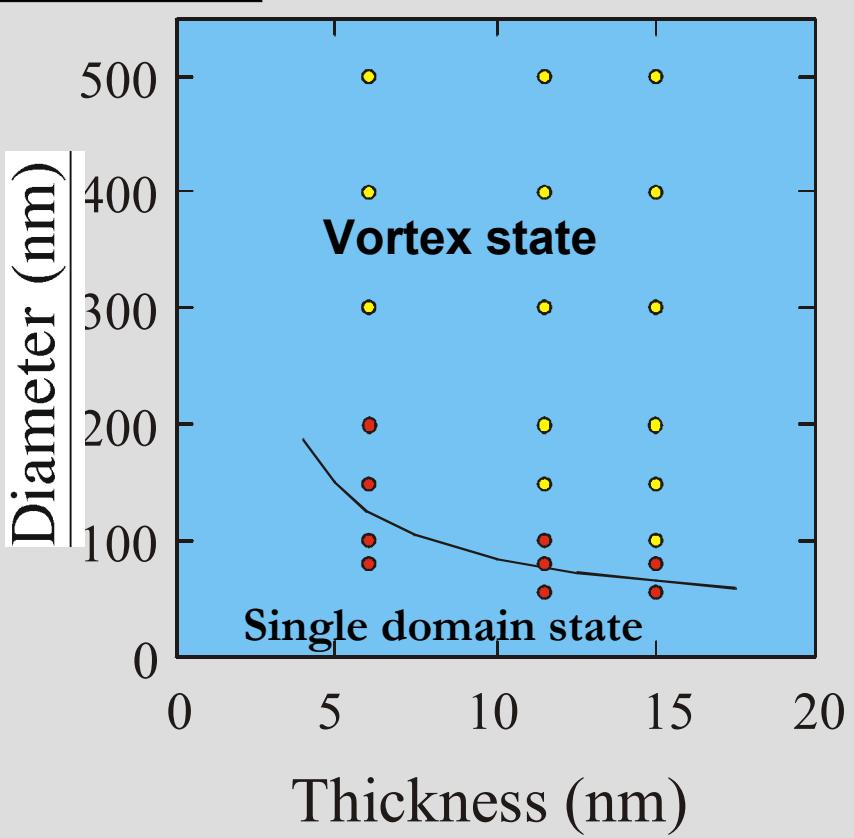


From Néel walls to cross-tie walls



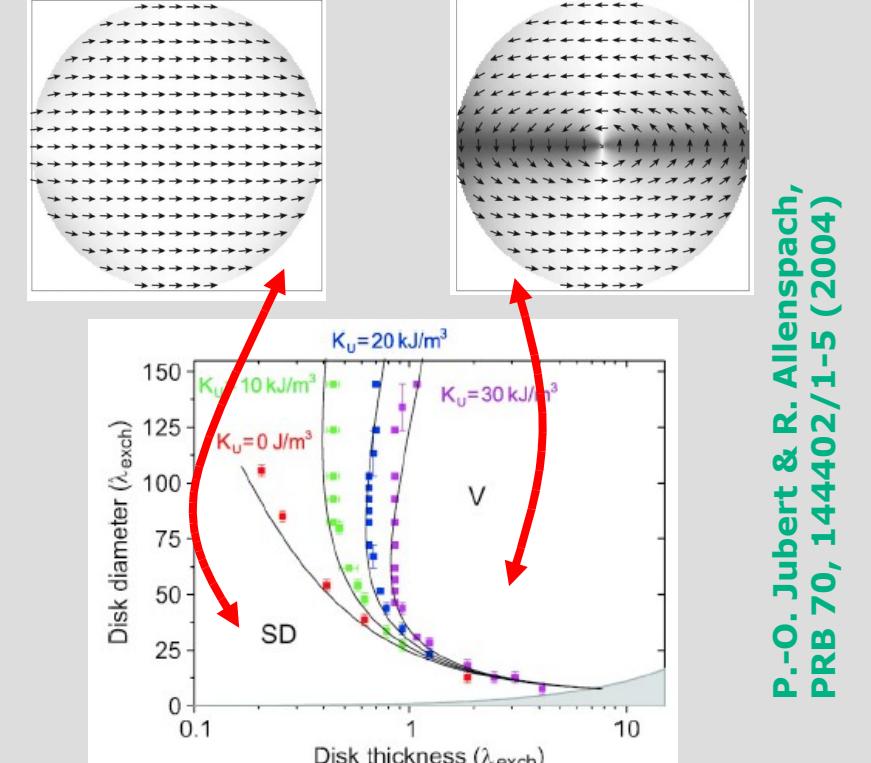


## Experiments



R.P. Cowburn,  
J.Phys.D:Appl.Phys.33, R1–R16 (2000)

## Theory / Simulation



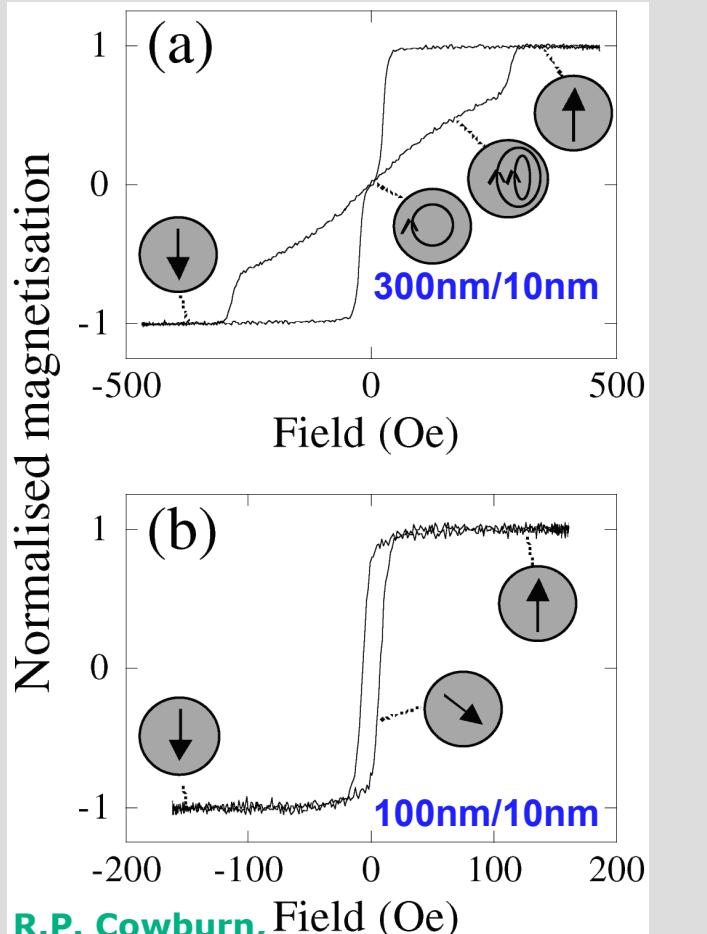
Zero-field  
cross-over

$$t \cdot D \approx 20 \lambda_{\text{exch}}^2$$



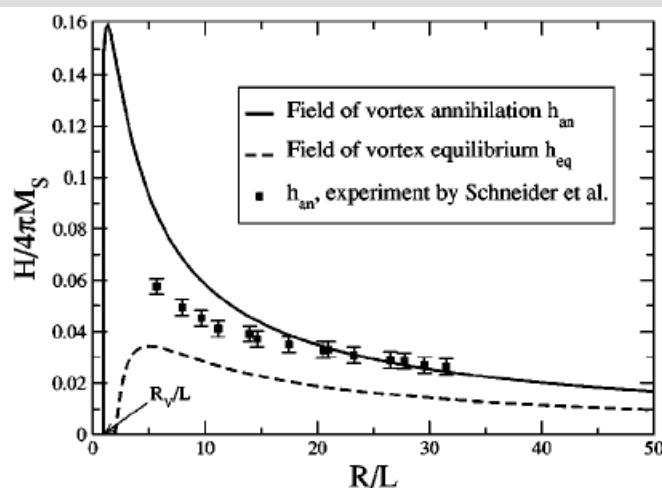
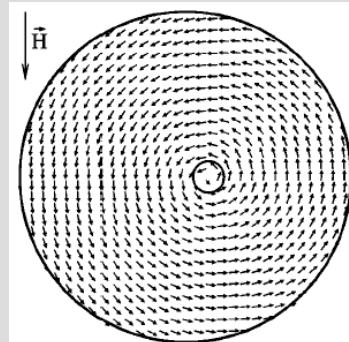
- ➡ Vortex state (flux-closure) dominates at large thickness and/or diameter
- ➡ The size limit for single-domain is much larger than the exchange length
- ➡ Experimentally the vortex may be difficult to reach close to the transition (hysteresis)

## Experiments



## Theory / Simulations

Displaced vortex  
model



Calculation of the equilibrium line and  
the annihilation line

K. Y. Guslienko & K. L. Metlov,  
PRB 63, 100403(R) (2001)

Typical loops for flux-closure states

Energy of the vortex state can be computed from the anhysteretic above-loop area.

**Hypothesis****Van den Berg model**

Infinitely soft material ( $K=0$ )  $\ell_{mc} = 0$       2D geometry (neglect thickness)

Zero external magnetic field  $\ell_Z = 0$       Size  $>>$  all magnetic length scales (wall width)

$$\ell_{ex} \longrightarrow 0$$

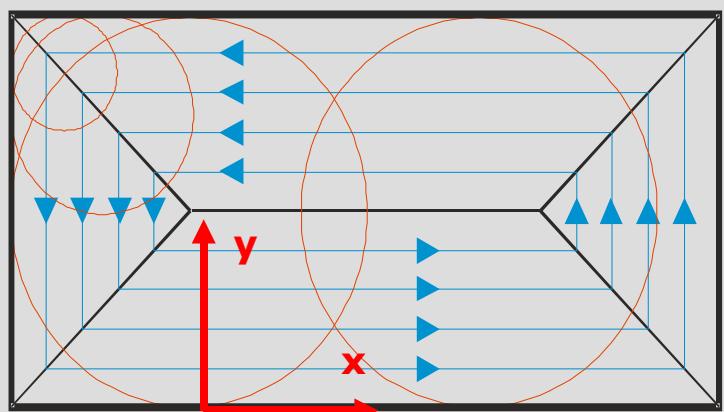
**Solution**

Looking for a solution with :  $\ell_d = 0$

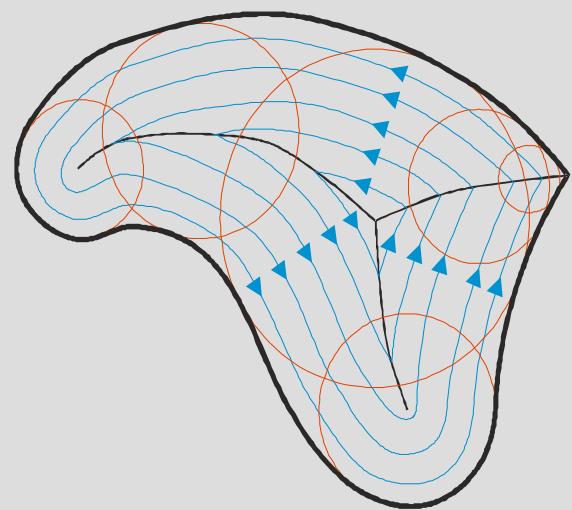
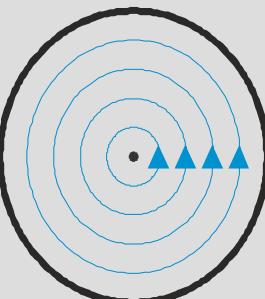
$-\text{div}\mathbf{M} = 0$  (no volume charges)

$\mathbf{M} \cdot \mathbf{n} = 0$  (no surface charges)

**« Flux closure »**



$$\text{div}\mathbf{M} = \frac{\partial M_x}{\partial x} + \frac{\partial M_y}{\partial y}$$

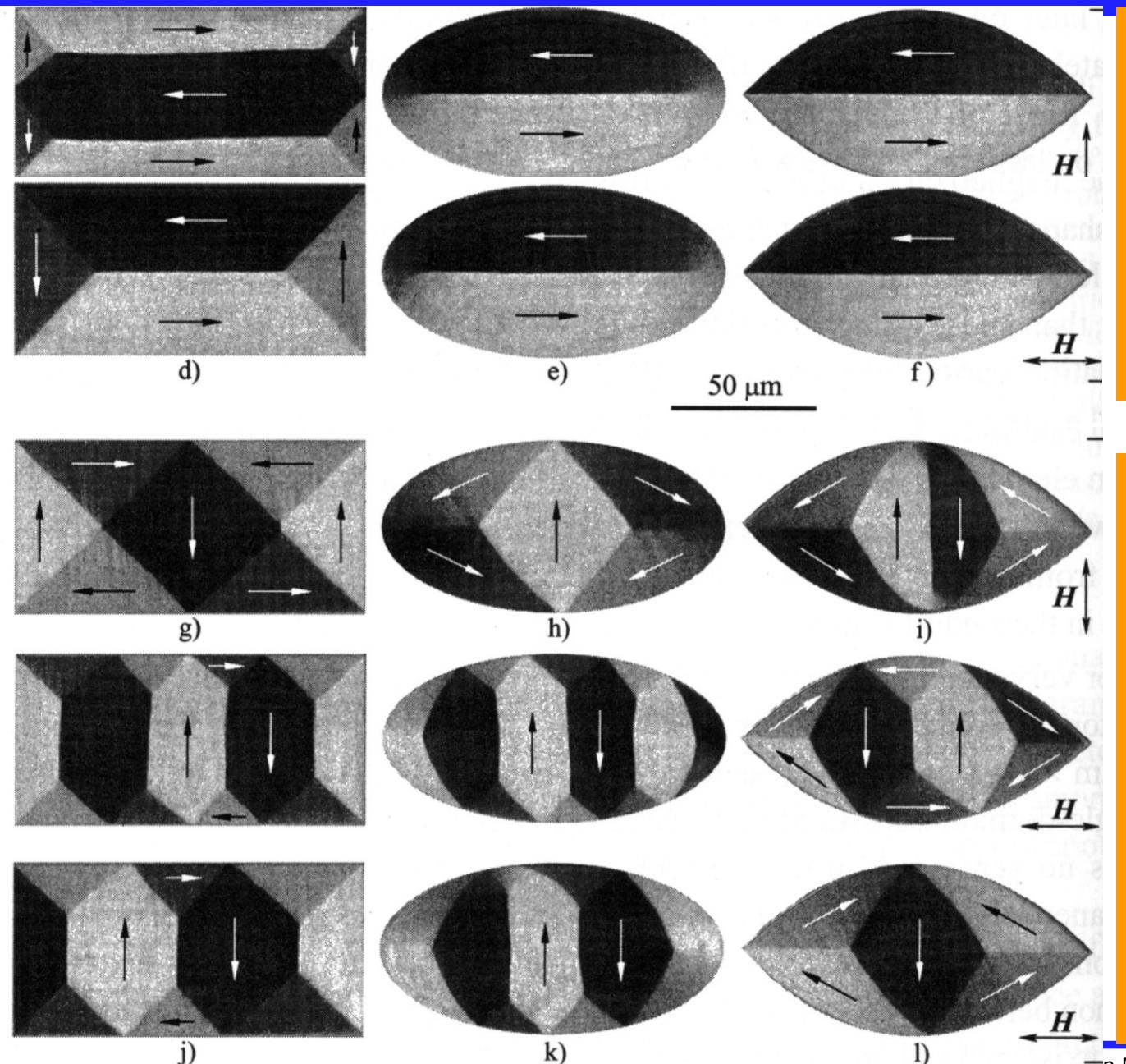


**H. A. M. Van den Berg, J. Magn. Magn. Mater. 44, 207 (1984)**

## Sandpiles for simulating flux-closure patterns



# NON-SINGLE DOMAIN EFFECTS – Van den Berg model and anisotropy



Easy axis of **weak** magnetocrystalline anisotropy

Easy axis of **weak** magnetocrystalline anisotropy

- Large dots** 
- many degrees of freedom
  - many possible states
  - history is important
  - even slight perturbations can influence the dot (anisotropy, defects, etc.).

## Generalization for non-zero field

The domains with magnetization parallel  
to the applied field are favored

P. Bryant et al., *Appl. Phys. Lett.* 54, 78 (1989)

See further extension to  
field arbitrarily-close  
to the saturation field:

A. DeSimone, R. V. Kohn, S. Müller, F. Otto & R. Schäfer, Two-dimensional modeling of soft ferromagnetic films, *Proc. Roy. Soc. Lond. A* 457, 2983-2991 (2001)

A. DeSimone, R. V. Kohn, S. Müller & F. Otto, A reduced theory for thin-film micromagnetics, *Comm. Pure Appl. Math.* 55, 1408-1460 (2002)

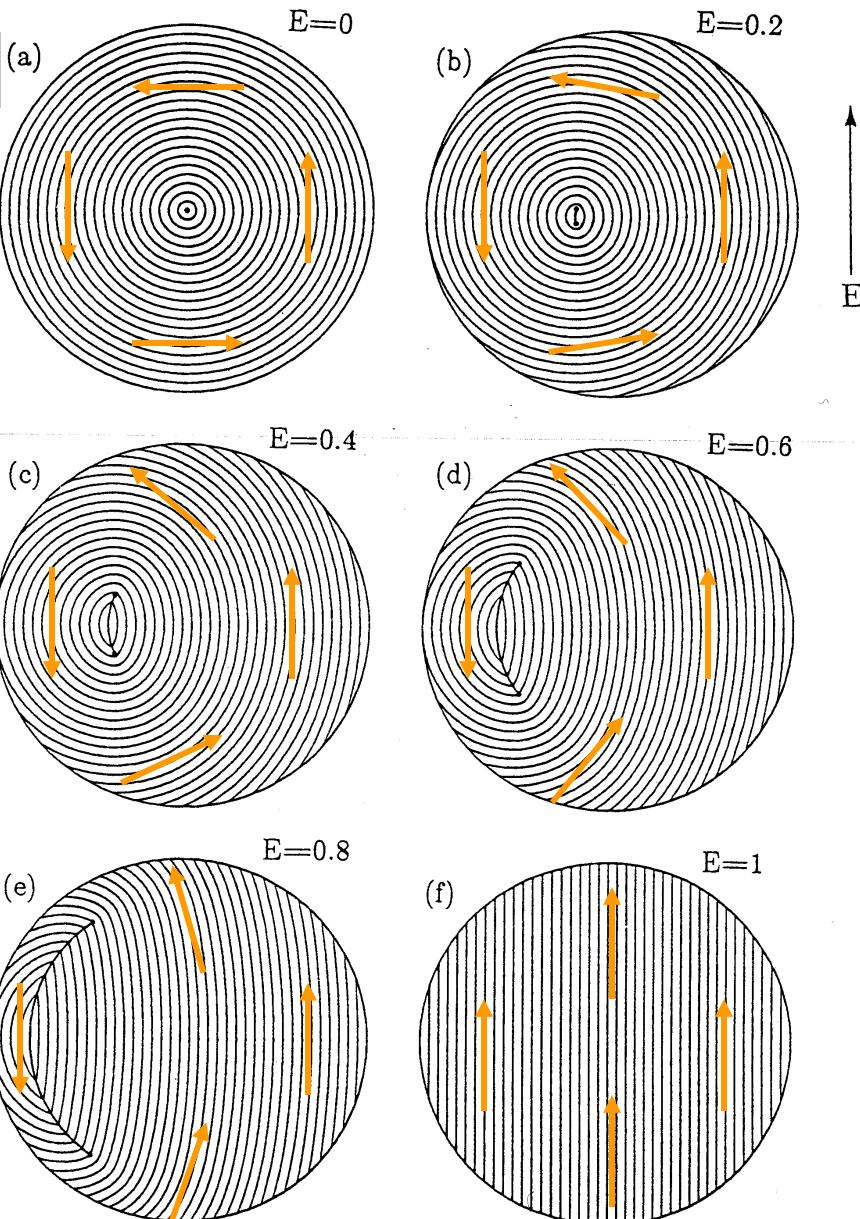


Figure 3

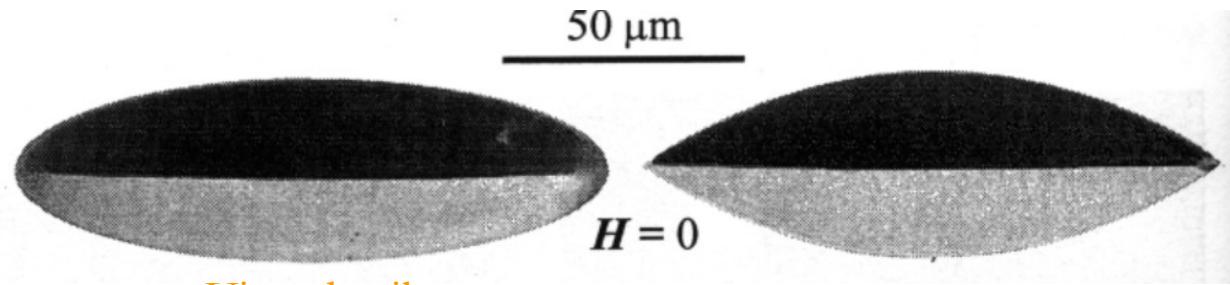
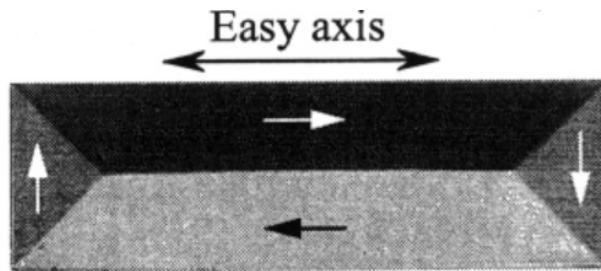
# NON-SINGLE DOMAIN EFFECTS – Van den Berg model in field (2/3)

In the following, many pictures taken from Hubert's book

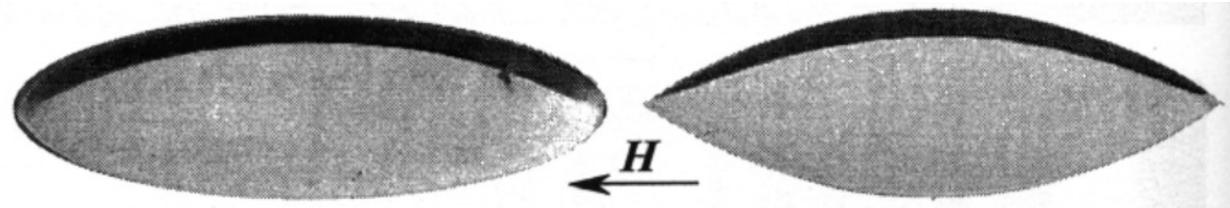
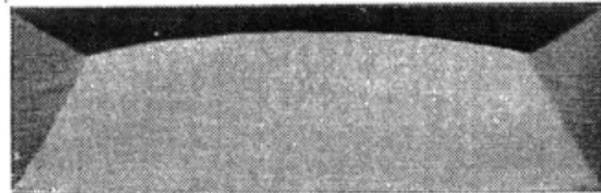
Zero field : agreement with Van den Berg's model

Material : Ni<sub>80</sub>Fe<sub>20</sub>

'Permalloy', Py.

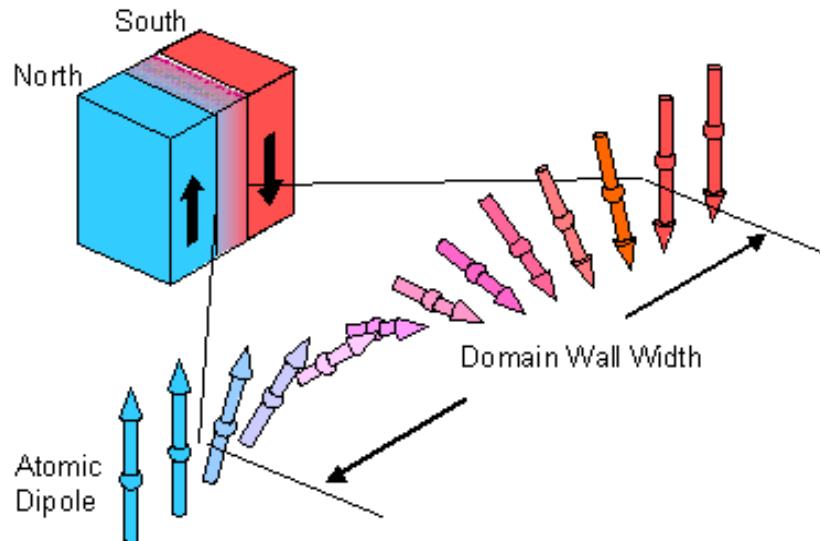


Longitudinal applied field



The domains with magnetization parallel to the applied field are favored

## Typical length scale:

Bloch wall width  $\lambda_B$ 

$$e = A(d\theta / dx)^2 + K \sin^2 \theta$$

Exchange  
→  $J/m$

Anisotropy  
→  $J/m^3$

## Numerical values

$$\lambda_B = \pi \sqrt{A / K}$$

$$\lambda_B = 2 - 3 \text{ nm} \longrightarrow \lambda_B \geq 100 \text{ nm}$$

Hard

Soft



$\Delta = \sqrt{A/K}$  is often called the Bloch wall parameter. Notice also that several definitions of Bloch wall width have been proposed, e.g. with  $\pi$  or 2 as prefactor

**Typical length scale:****Exchange length**  $\lambda_{\text{ex}}$ 

$$e = A(d\theta/dx)^2 + K_d \sin^2 \theta$$

Exchange  
J/mDipolar energy  
J/m<sup>3</sup>

$$\begin{aligned}\lambda_{\text{ex}} &= \sqrt{A/K_d} \\ &= \sqrt{2A/\mu_0 M_s^2}\end{aligned}$$

$$\lambda_{\text{ex}} = 3 - 10 \text{ nm}$$

Critical size relevant for nanoparticules made of soft magnetic material

$$D_c \approx \pi \sqrt{3} \lambda_{\text{ex}}$$

Generalization for various shapes

$$D_c \approx \pi \sqrt{6A/(N\mu_0)M_s^2}$$

**Quality factor Q**

$$e = -K \sin^2 \theta + K_d \sin^2 \theta$$

m.c.  
J/mDipolar energy  
J/m<sup>3</sup>

$$Q = K / K_d$$

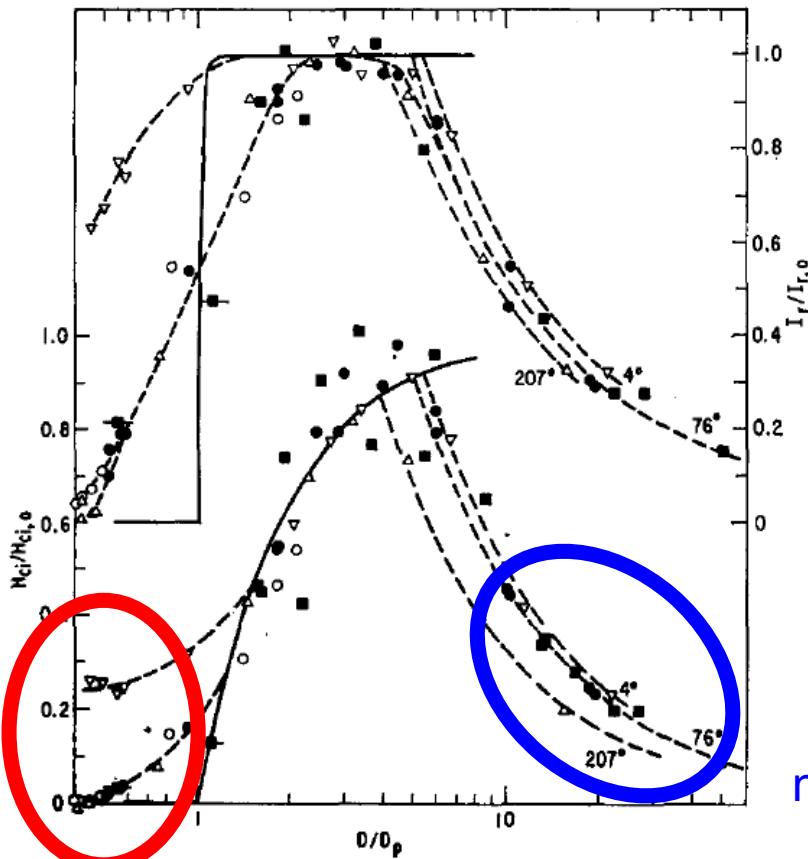
Relevant e.g. for stripe domains in thin films with perpendicular magnetocrystalline anisotropy

**Critical size for hard magnets**

$$D_c \approx 6E_w / K_d \approx 2.5Q\lambda_B$$

$$E_w \approx 4\sqrt{AK} \text{ for hard magnetic materials}$$

**Notice:****Other length scales: with field etc.**



Towards  
suparamagnetism

Towards  
nucleation-propagation  
and multidomain

FIG. 1. Particle size dependence of essentially spherical, randomly oriented, iron particles. Calculated curve given by solid line. Diameters  $D = \hat{d}_v$ . Data at 76°K obtained from electron microscopic examination ■, calculated from  $I_r/I_r$  vs temperature O, and from smoothed data of  $H_{ci}$  vs  $D$  ●.

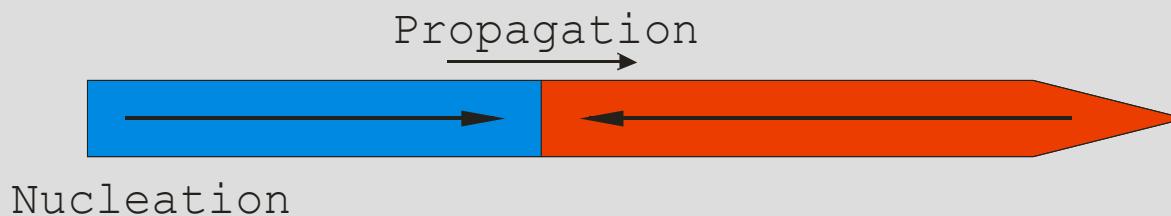
E. F. Kneller & F. E. Luborsky,  
*Particle size dependence of coercivity and remanence of single-domain particles*,  
*J. Appl. Phys.* **34**, 656 (1963)



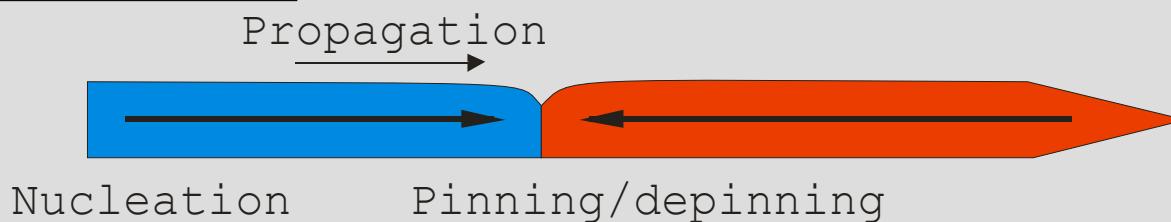
## II.3. Manipulating domain walls

- 1. Details and use of domain walls in stripes
- 2. Magnetization processes inside domain walls

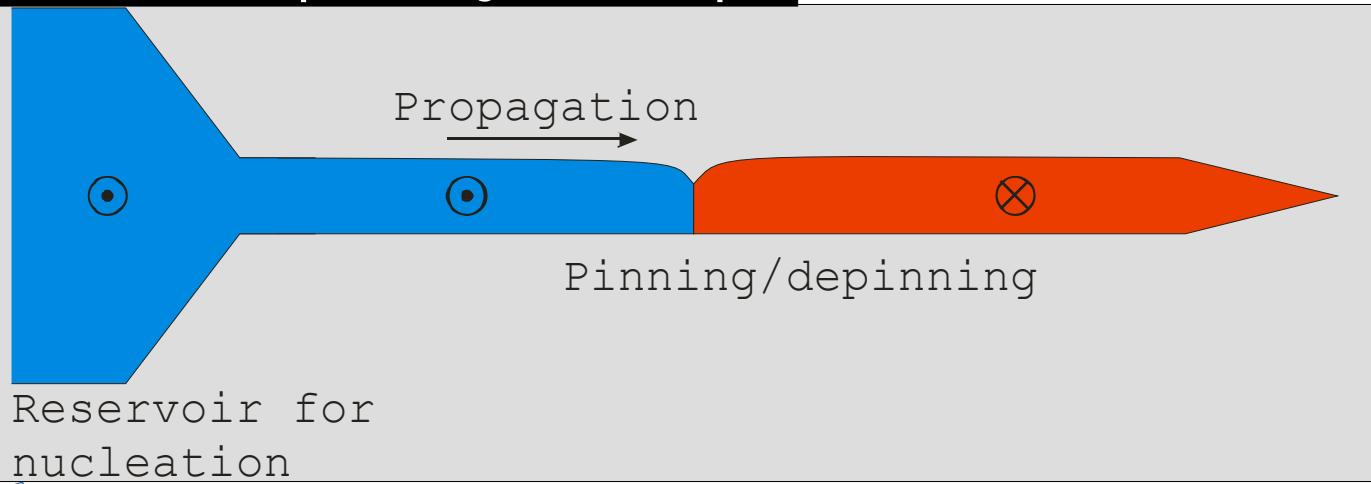
## Nucleation in in-plane magnetized stripes



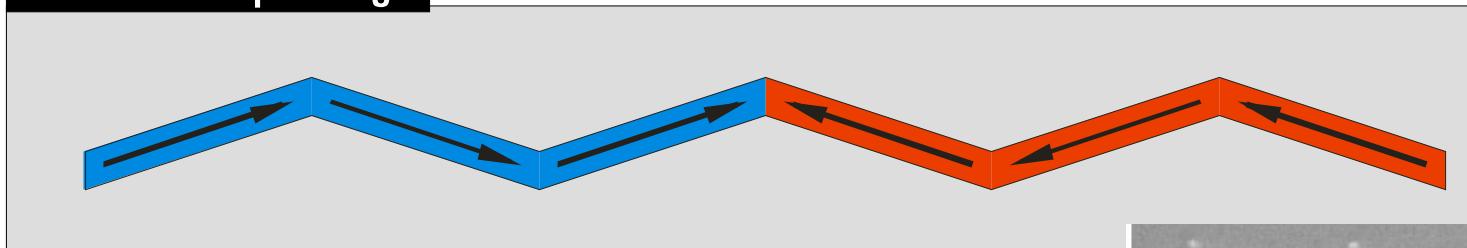
## Pinning in stripes: notches



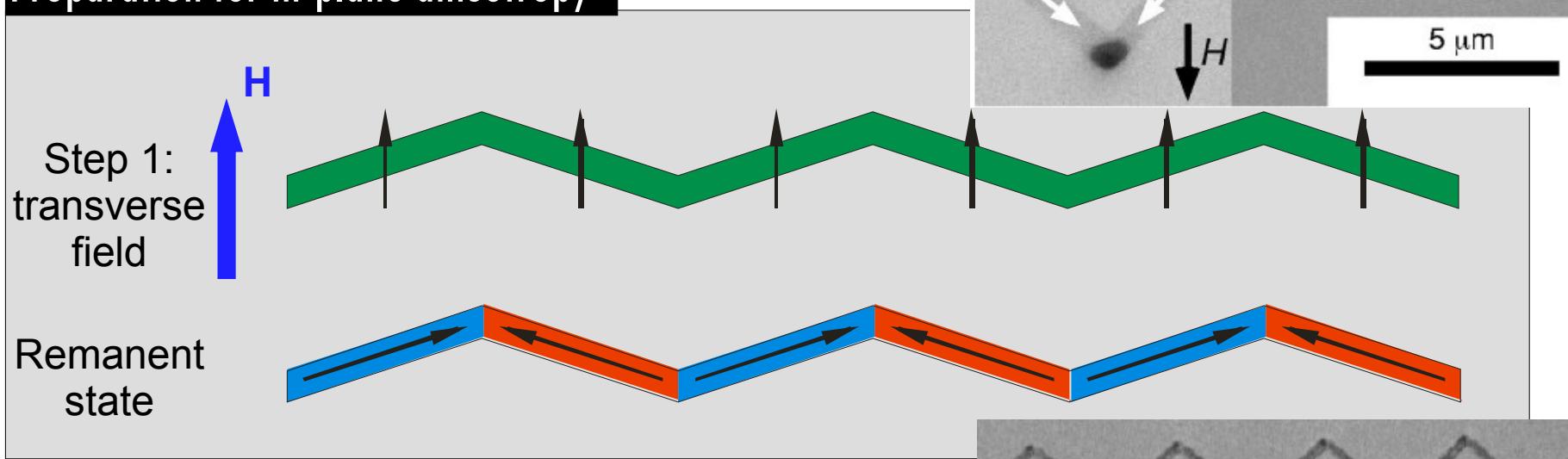
## Nucleation in out-of-plane magnetized stripes



## Geometrical pinning

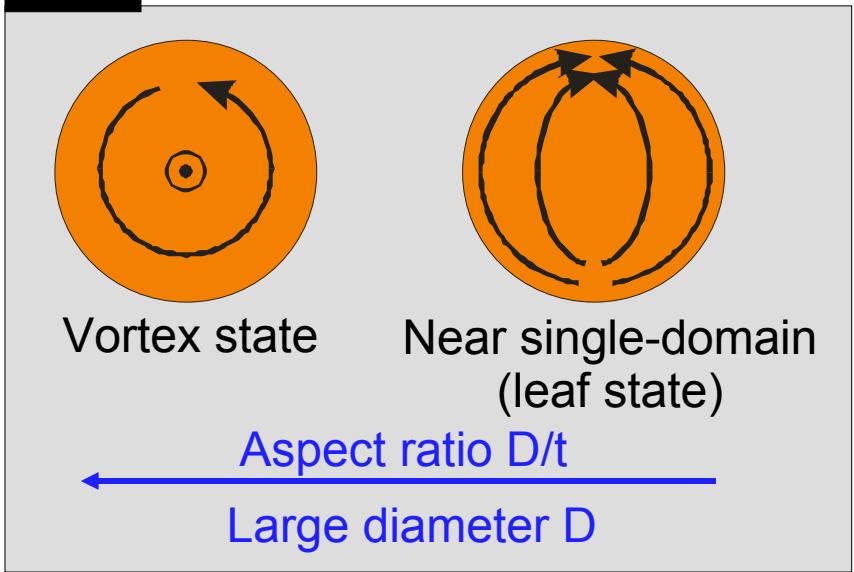


## Preparation for in-plane anisotropy

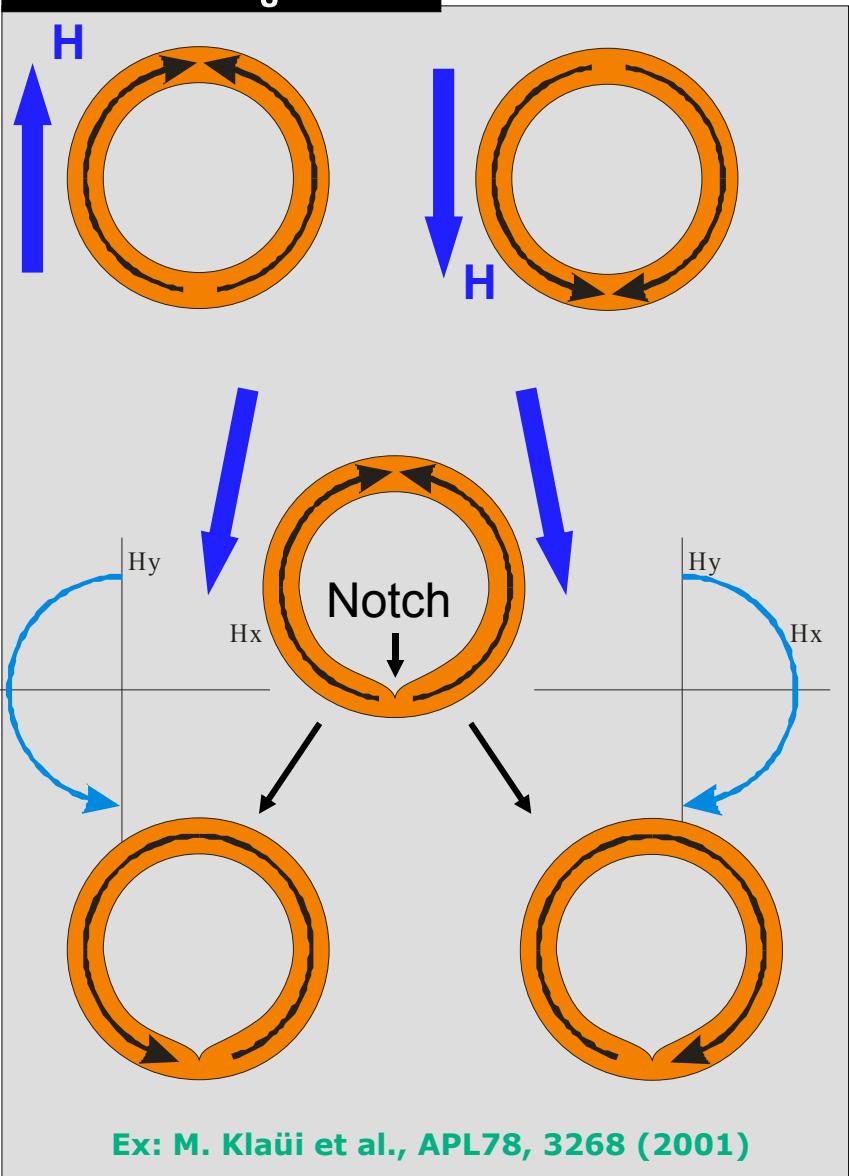


T. Taniyama et al., APL76, 613 (2000)

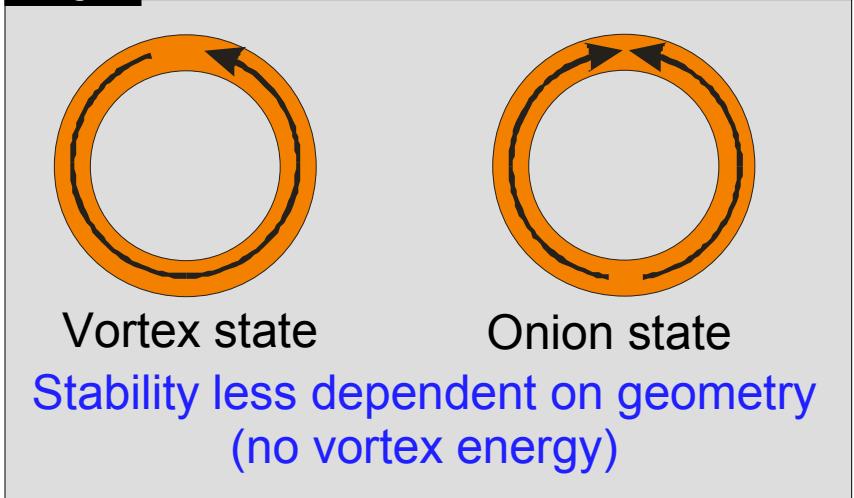
## Disks



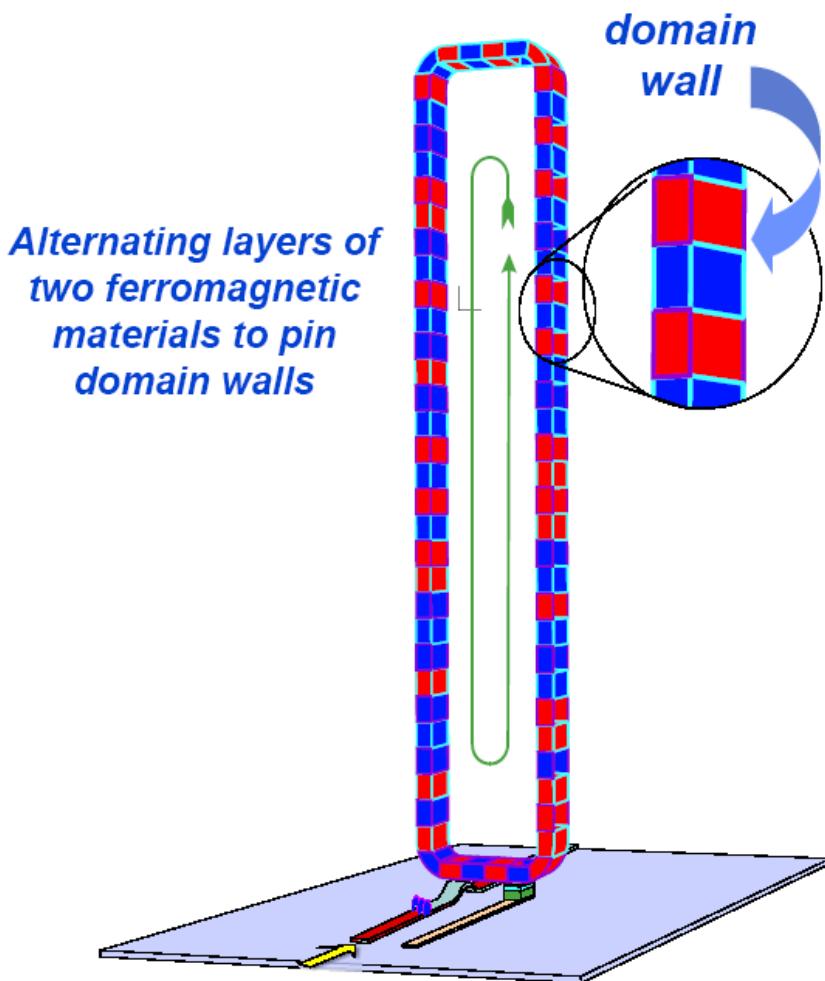
## Control of ring states



## Rings



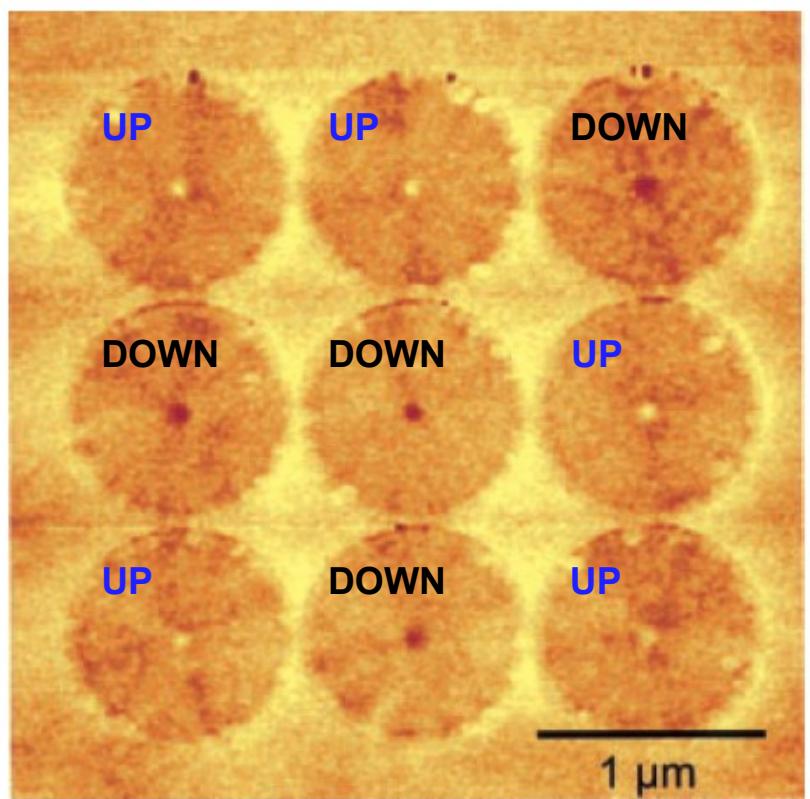
## Magnetic Race-Track Memory: Domain-Wall Magnetic Shift Register



S. S. P. Parkin, IBM-Almaden  
U.S. patents 6834005, 6898132, 6920062

D. A. Allwood, G. Xiong, C. C. Faulkner, D. Atkinson,  
D. Petit & R. P. Cowburn,  
Magnetic domain-wall logic, Science 309, 1688 (2005)

## Closure domains (flat)



**Fig. 2.** MFM image of an array of permalloy dots 1  $\mu\text{m}$  in diameter and 50 nm thick.

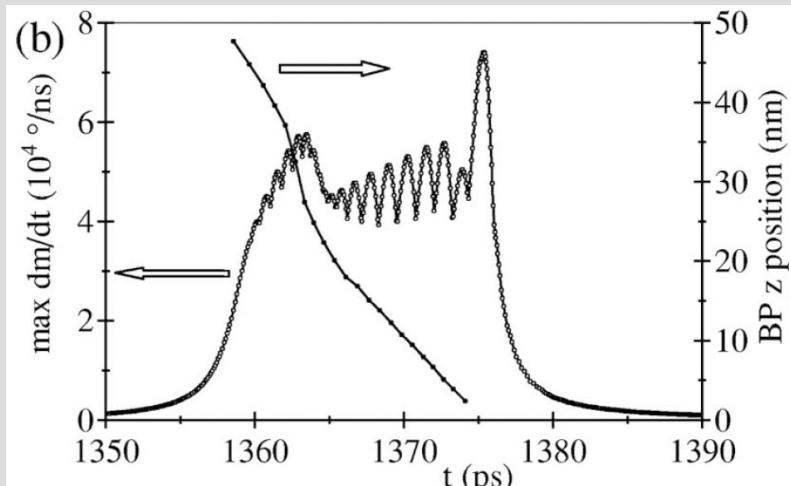
The central magnetic vortex  
can be magnetized up or down using  
a perpendicular field

T. Shinjo et al., *Science* **289**, 930 (2000)  
T. Okuno et al., *JMMM* **240**, 1 (2002)

## Theory and simulation

## Micromagnetic simulation

A. Thiaville et al., *Phys. Rev. B* **67**, 094410 (2003)



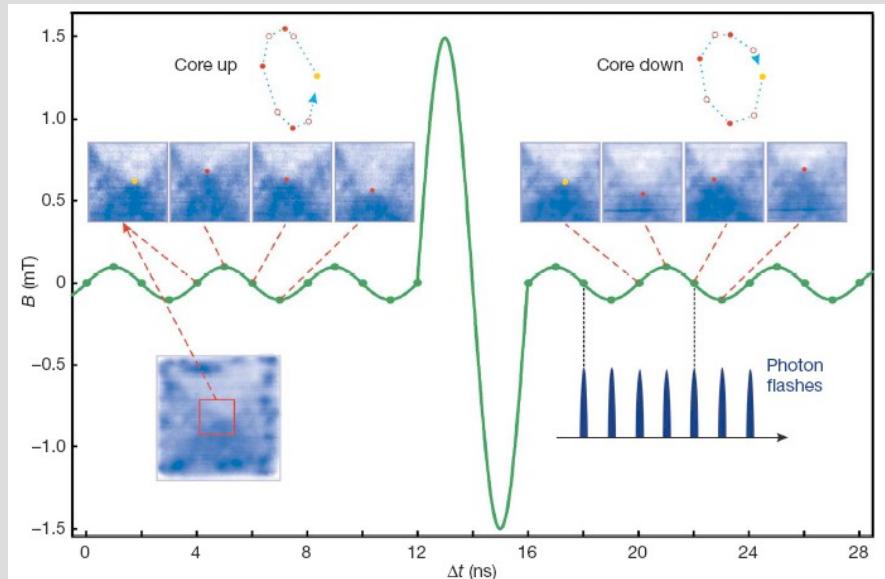
Require a Bloch point:  
Not well described in micromagnetism

First theoretical insight in Bloch points

W. Döring, *J. Appl. Phys.* **39**, 1006 (1968)

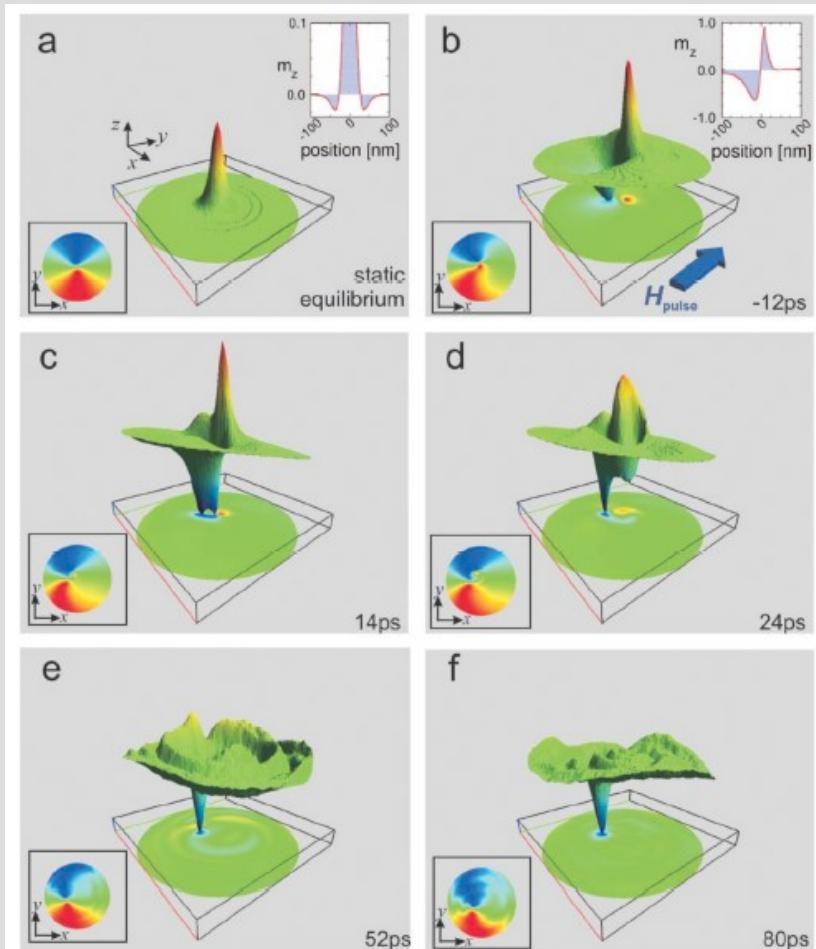
## Magnetic vortex core reversal by excitation with short bursts of an alternating field

B. Van Waeyenberg et al.,  
Nature 444, 461 (2007)



Resonant phenomenon

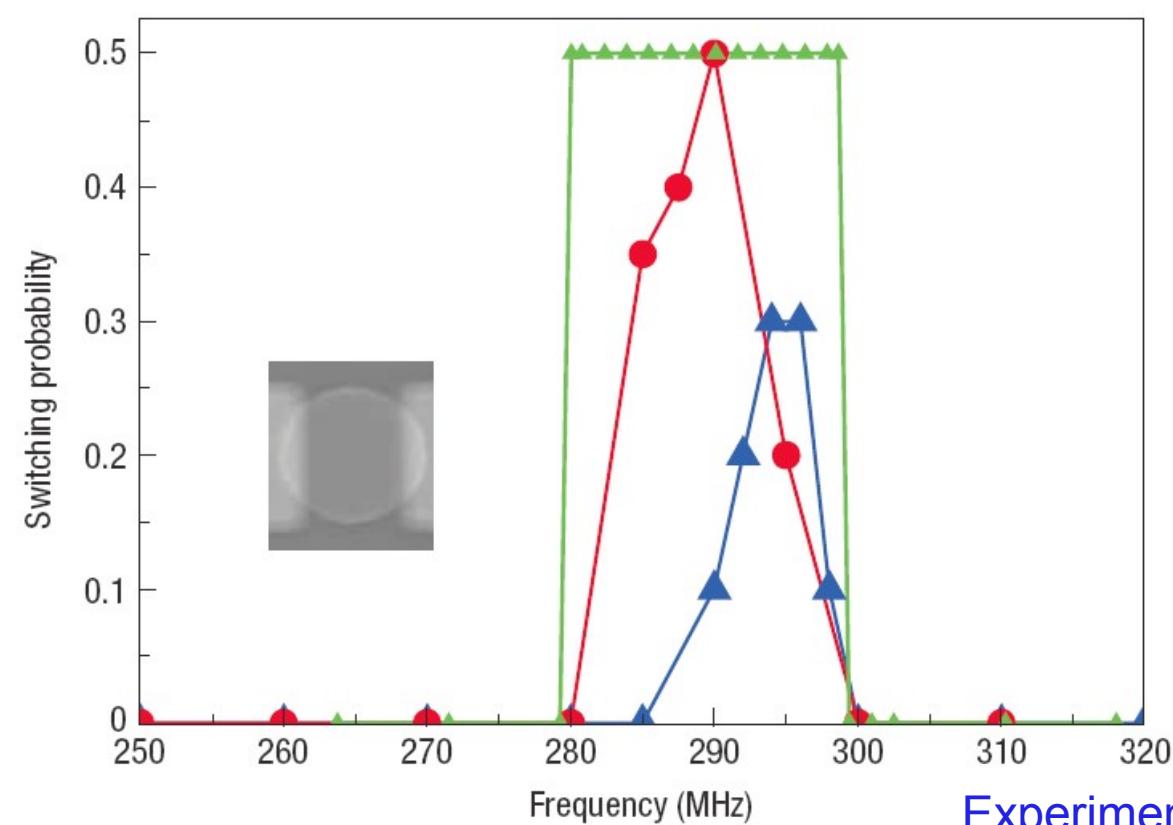
R. Hertel et al.,  
Phys. Rev. Lett. 98, 117201 (2007)



Non-resonant phenomenon

## Electrical switching of the vortex core in a magnetic disk

K. Yamada et al., Nat. Mater. 6 (2007)

Experiment  $2.4 \times 10^{11} \text{ A/m}^2$ Experiment  $3.5 \times 10^{11} \text{ A/m}^2$ Simulation  $3.88 \times 10^{11} \text{ A/m}^2$ 

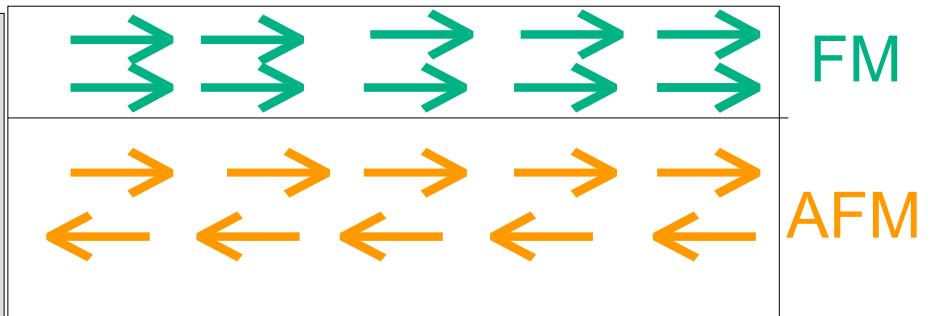
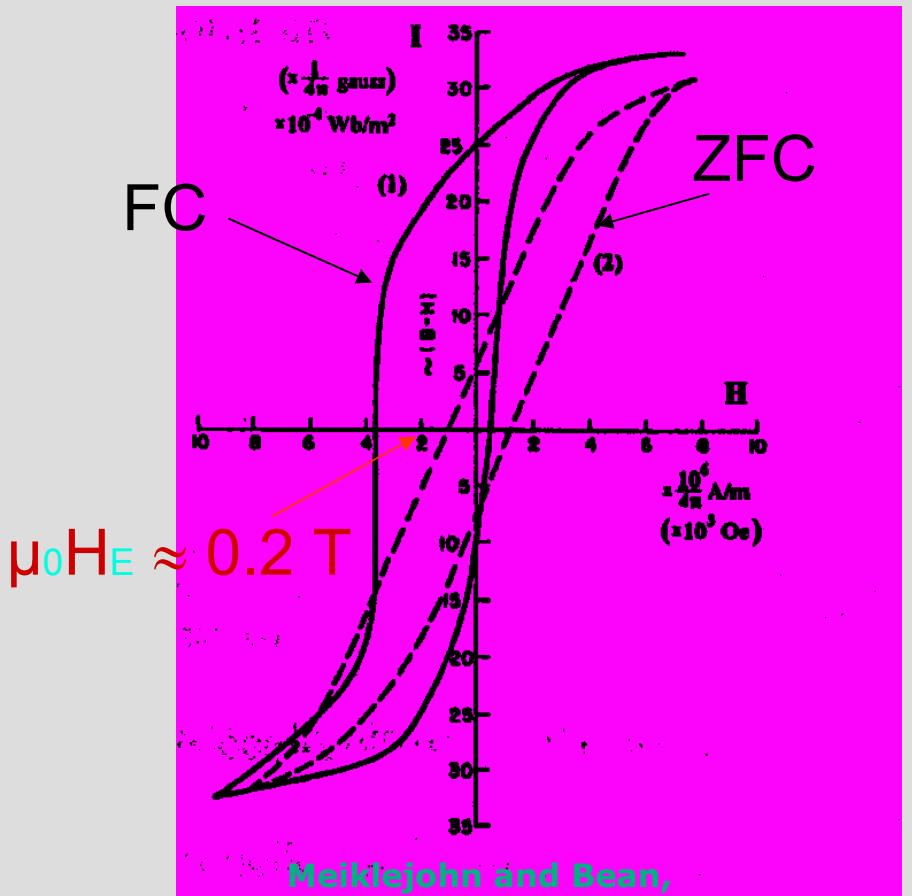
(resonant phenomenon)



## II.4. Interfacial effects on magnetization reversal

## Seminal studies

Oxidized Co nanoparticles

**Field-cooled hysteresis loops:**

- **Increased coercivity**
- **Shifted in field**

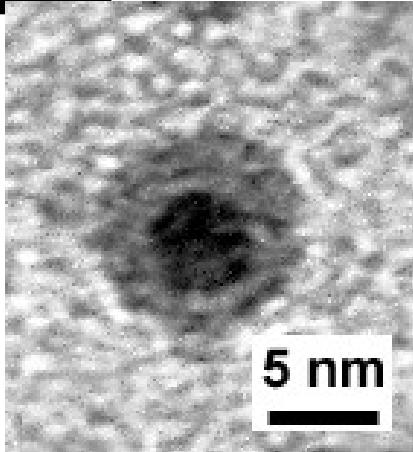
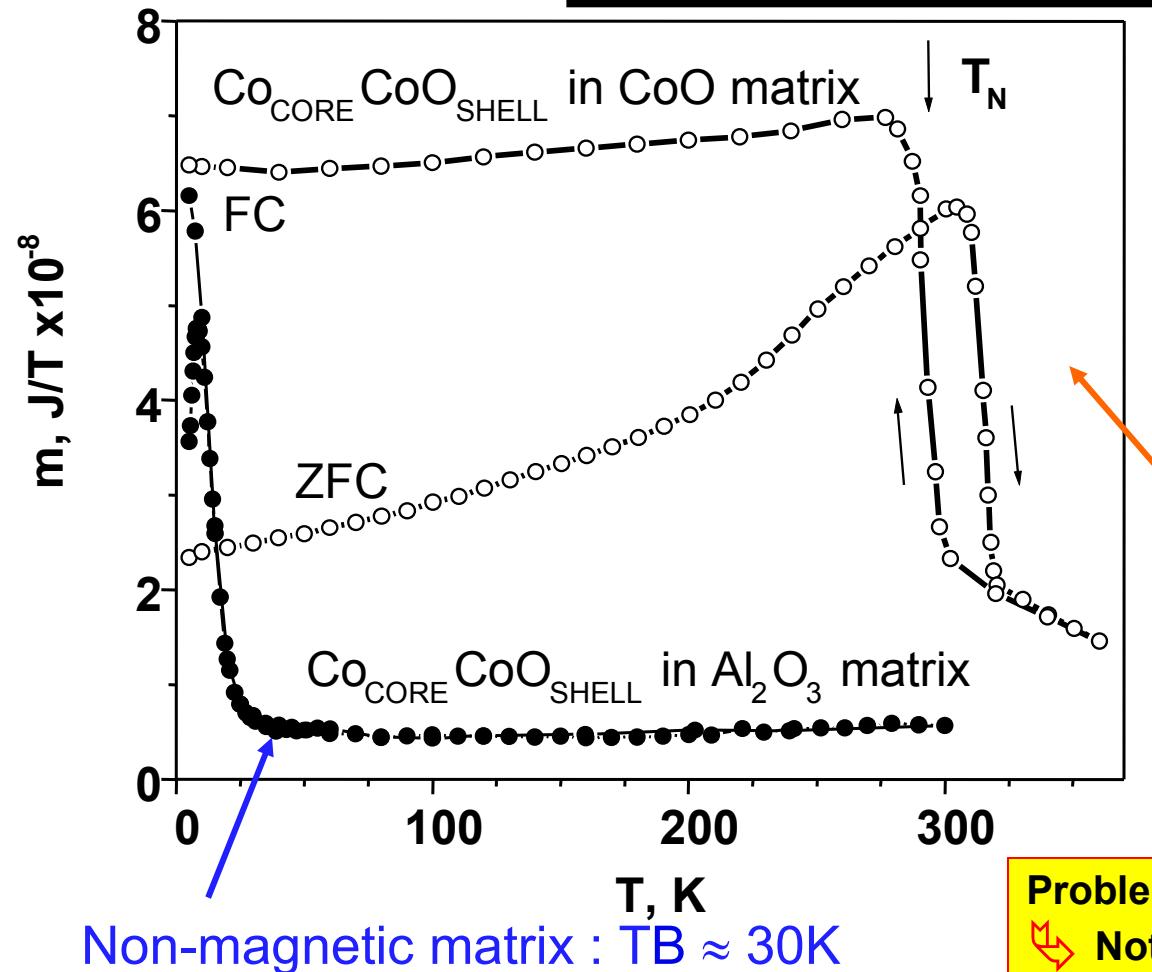
**Exchange bias**

**J. Nogués and Ivan K. Schuller**  
**J. Magn. Magn. Mater. 192 (1999) 203**

**Exchange anisotropy—a review**

**A E Berkowitz and K Takano**  
**J. Magn. Magn. Mater. 200 (1999)**

## Dependence of the blocking temperature on the nature of the matrix



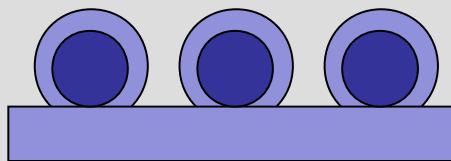
AFM matrix  
 $T_B \approx T_N \text{ CoO}$

V.Skumryev, et al.,  
Nature 423, 850 (2003)

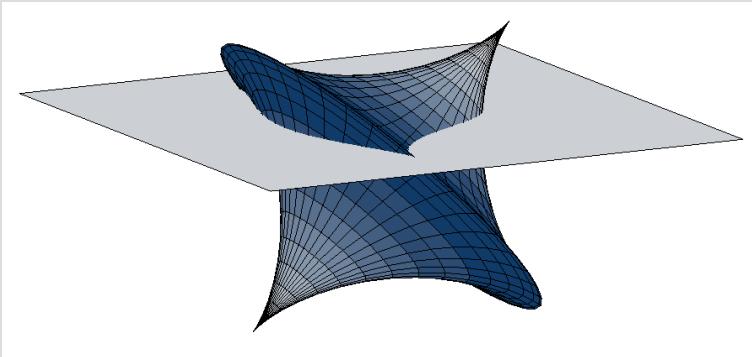
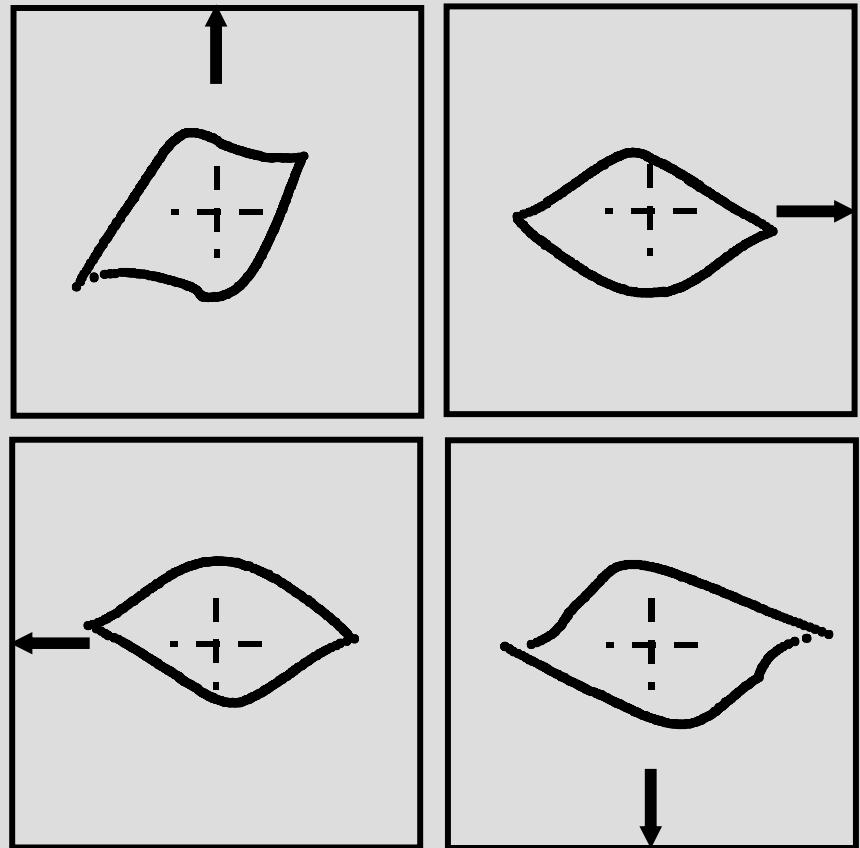
Problems remain:

- ➡ Not all features understood
- ➡ Very sensitive on fabrication

## Astroids of single particles with Ferro/Antiferro exchange

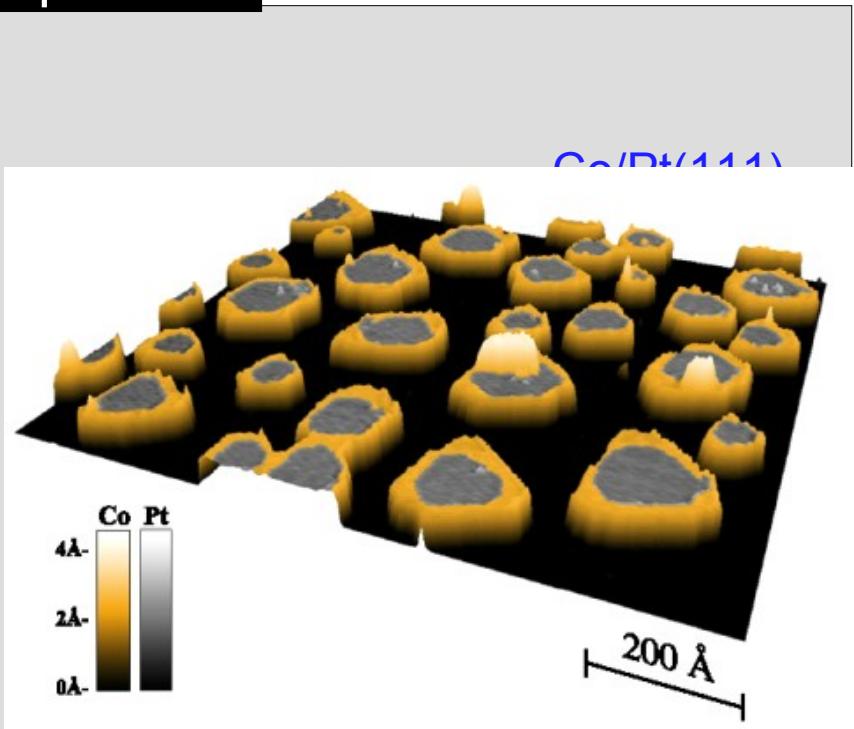


Core-shell CoO cluster on CoO



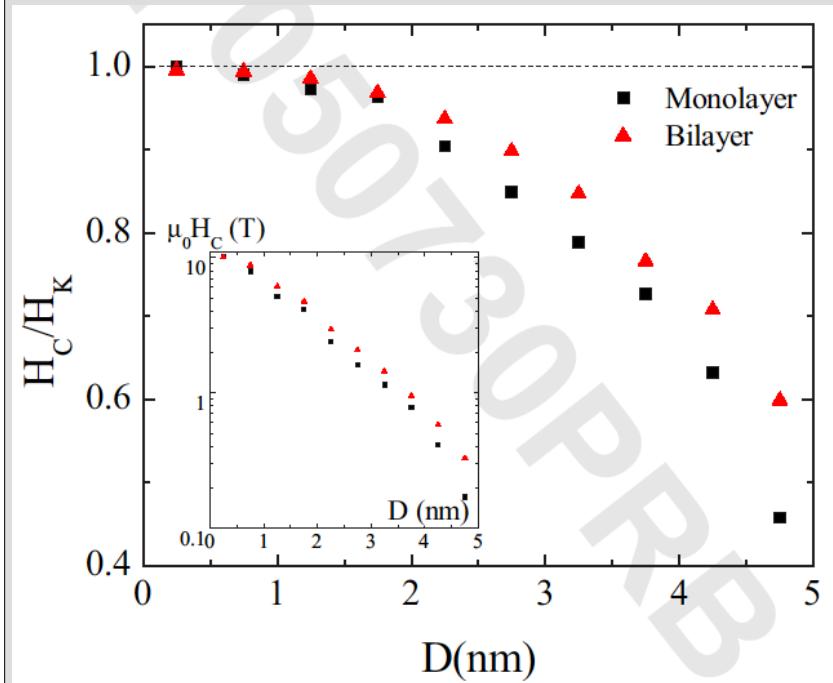
A. Brenac et al., CEA-Grenoble,  
W. Wernsdorfer, Institut Néel

## Experiments



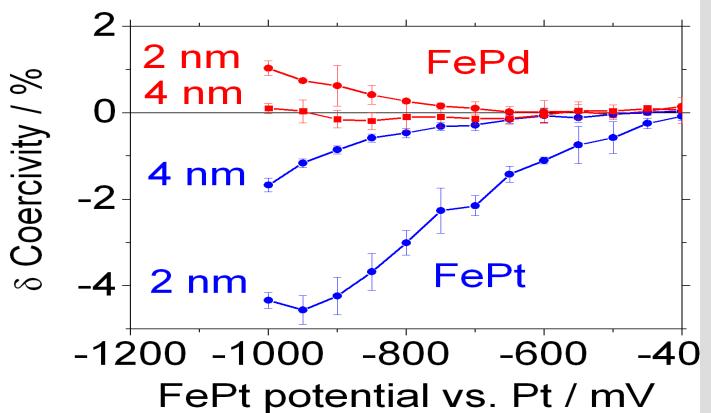
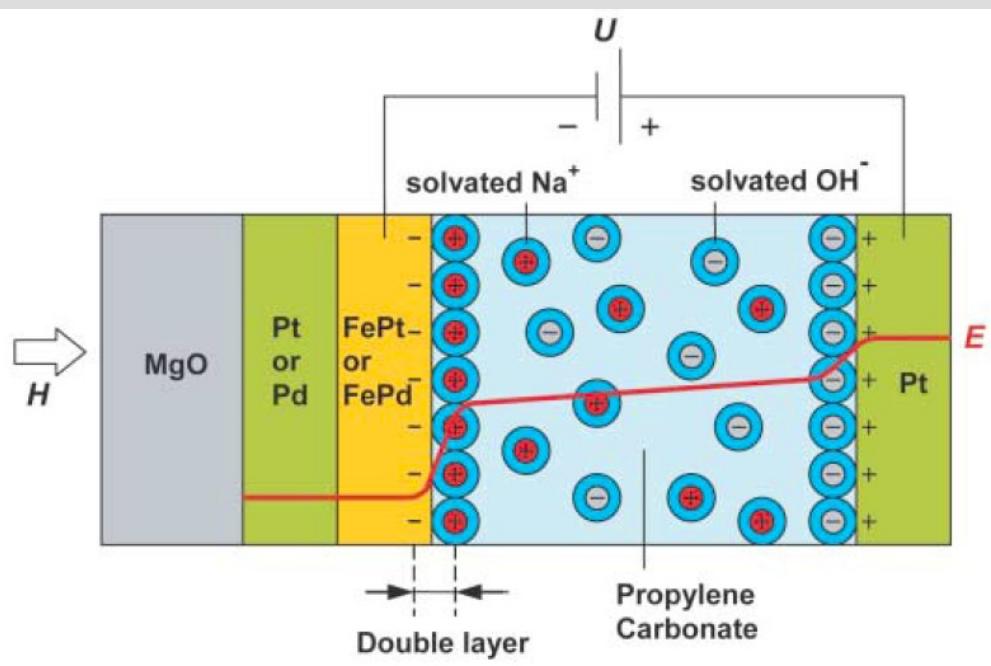
**S. Rusponi et al., Nature Mater. (2003):**  
« The remarkable difference between surface  
and step atoms in the magnetic anisotropy  
of two-dimensional nanostructures”

## Simulation/Theory



**S. Rohart, PhD Thesis (2005)**  
**S. Rohart, A. Thiaville, unpublished**

## Electric modification of intrinsic properties



M. Weisheit et al., Science 315, 349 (2007)

See also: magnetic semiconductors, multiferroics etc.

## SOME READING

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- [2] R. Skomski, Simple models of Magnetism, Oxford (2008).
- [3] R. Skomski, *Nanomagnetics*, J. Phys.: Cond. Mat. **15**, R841–896 (2003).
- [4] O. Fruchart, A. Thiaville, *Magnetism in reduced dimensions*, C. R. Physique **6**, 921 (2005) [Topical issue, Spintronics].
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<http://perso.neel.cnrs.fr/olivier.fruchart/slides/>
- [7] G. Chaboussant, Nanostructures magnétiques, Techniques de l'Ingénieur, revue 10-9 (RE51) (2005)
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