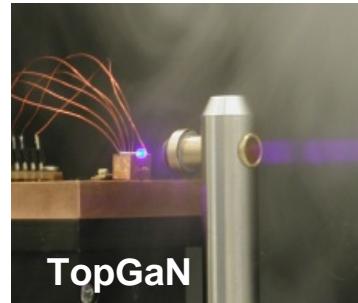


# Spintronics -- materials aspect

*Why to do not combine complementary resources of ferromagnets and semiconductors?*



- hybrid ferromagnetic-metal/semiconductor structures

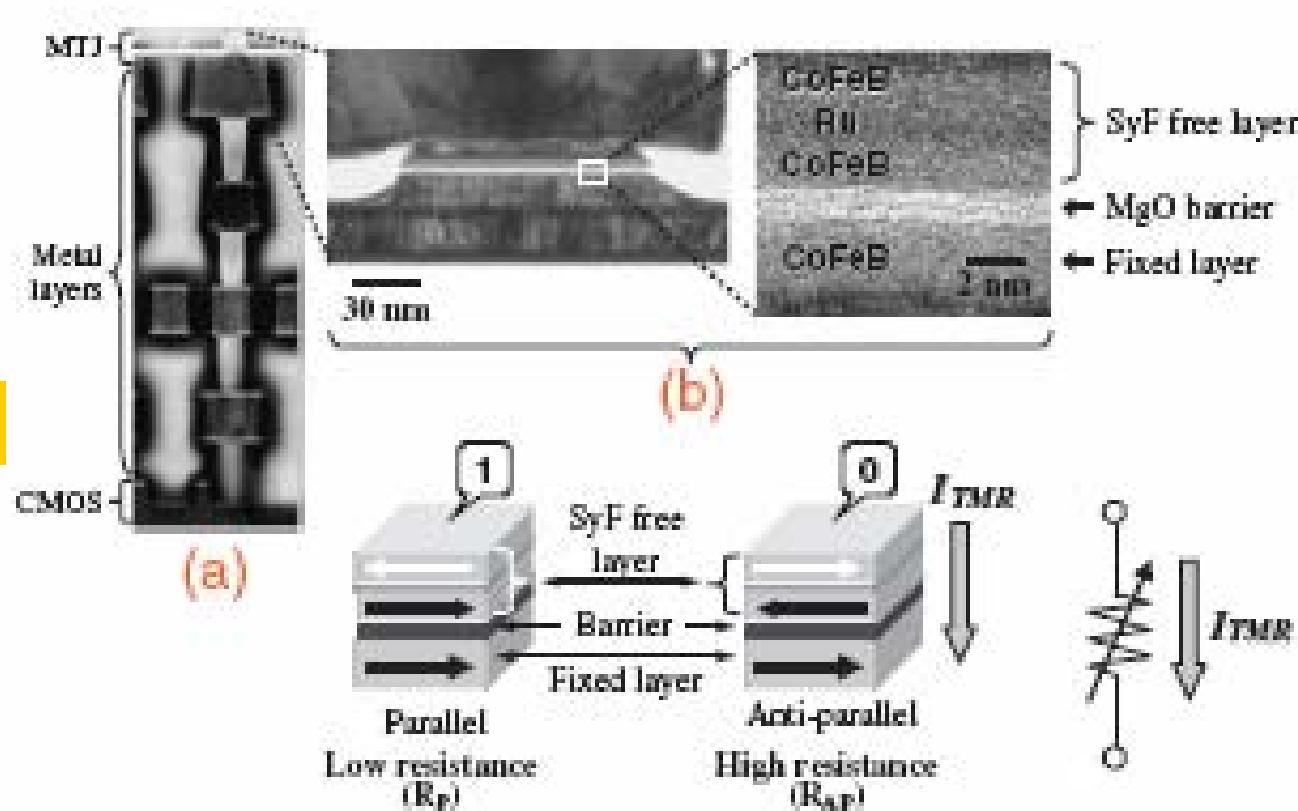
*cf. B. Dieny*

# Hybrid structures – an example

low-power hybrid logic

(distributed non-volatile memory)

spintronics



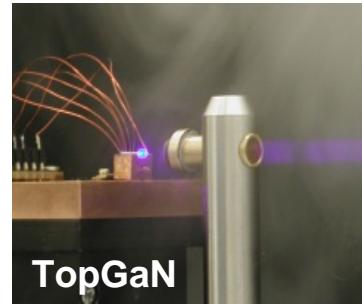
Adder: 34 MOSS + 4 MTJs

S. Matsunaga et al.. (Tohoku) APEX'08

cf. B. Dieny

# Spintronics -- materials aspect

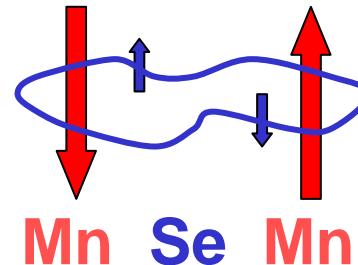
***Why to do not combine complementary resources of ferromagnets and semiconductors?***



- **ferromagnetic semiconductors – *multifunctional materials***

# Search for ferromagnetic semiconductors

- ***Antiferromagnetic superexchange dominates in magnetic insulators and semiconductors***  
→ no spontaneous magnetisation  
NiO, MnSe, EuTe, ...

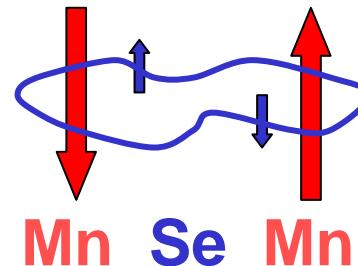


# Search for ferromagnetic semiconductors

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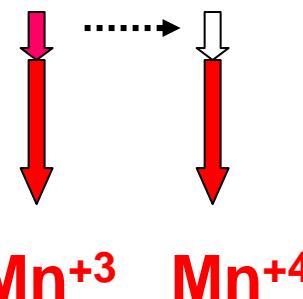
## Exceptions

- ferromagnetic superexchange dominates

EuO, ZnCr<sub>2</sub>Se<sub>4</sub>, ...  $T_C \approx 100$  K IBM, MIT, Tohoku, ... '60-'70

- double exchange (two charge states co-exist)

LaMnO<sub>3</sub> → La<sub>1-x</sub>Sr<sub>x</sub>MnO<sub>3</sub> (holes in d band)



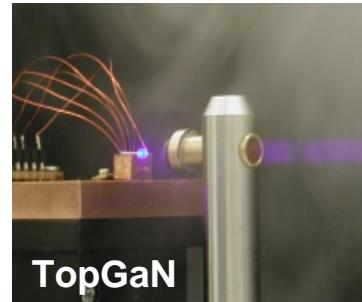
- ferrimagnets (two ions or two spin states co-exist)

Mn<sub>4</sub>N, NiO(Fe<sub>2</sub>O<sub>3</sub>), ...



# Spintronics -- materials aspect

***Why to do not combine complementary resources of ferromagnets and semiconductors?***

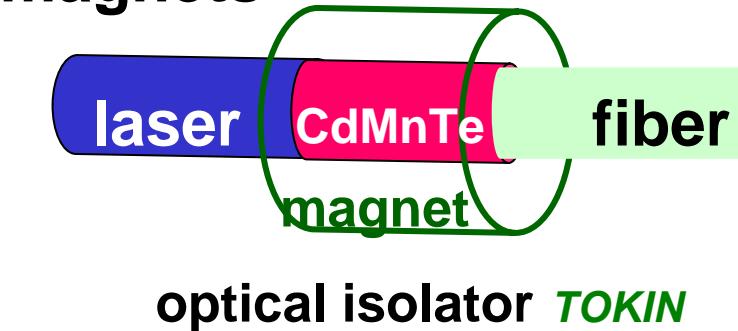
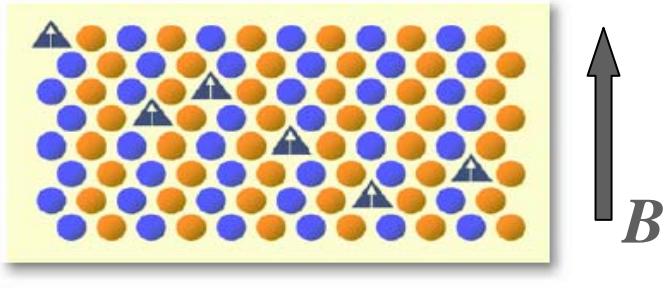
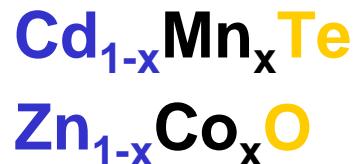


- **ferromagnetic semiconductors – *multifunctional materials***
  - **making good semiconductors of magnetic oxides**
  - **making good semiconductors magnetic**

*R.R. Gałzka et al. (Warsaw) '77- ; H. Ohno et al. (IBM, Tohoku) '89 -*

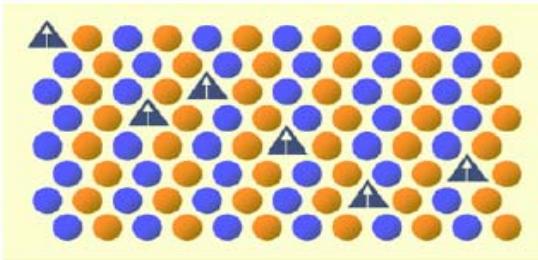
# Making DMS ferromagnetic

- Intrinsic DMS – random antiferromagnets

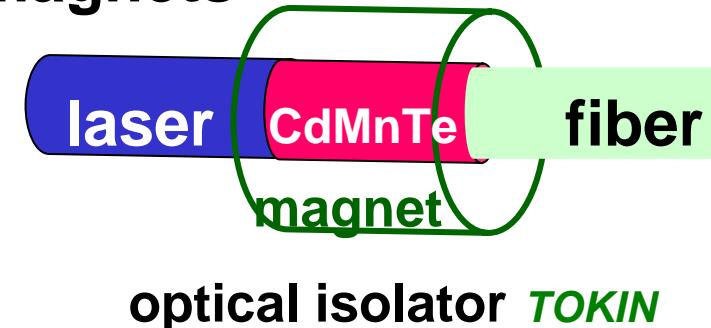


# Making DMS ferromagnetic

- Intrinsic DMS – random antiferromagnets



$B$



- p<sup>+</sup>-type DMS - ferromagnets

IV-VI: p-Pb<sub>1-x-y</sub>Mn<sub>x</sub>Sn<sub>y</sub>Te *Story et al. (Warsaw, MIT) PRL '86*

p-Ge<sub>1-x</sub>Mn<sub>x</sub>Te *Lechner et al. (Linz)*

III-V: In<sub>1-x</sub>Mn<sub>x</sub>As *Ohno et al. (IBM) PRL '92*

Ga<sub>1-x</sub>Mn<sub>x</sub>As *Ohno et al. (Tohoku) APL '96* T<sub>C</sub> ≈ 110 K for x = 0.05

II-VI: Cd<sub>1-x</sub>Mn<sub>x</sub>Te/Cd<sub>1-x-y</sub>Zn<sub>x</sub>Mg<sub>y</sub>Te:N QW *Haury et al. (Grenoble, Warsaw) PRL '97*

Zn<sub>1-x</sub>Mn<sub>x</sub>Te:N *Ferrand et al. (Grenoble, Linz, Warsaw) Physica B '99, PRB '01*

quantum nanostructures and ferromagnetism combined

# Transport in magnetic semiconductors and oxides

## Lecture 4

Tomasz Dietl

1. *Institute of Physics, Polish Academy of Sciences,  
Laboratory for Cryogenic and Spintronic Research*
2. *Institute of Theoretical Physics, Warsaw University*

support: *FunDMS – ERC Advanced Grant*  
*SemiSpinNet Maria Curie action*  
*SPINTRNA – ESF; Humboldt Foundation*



# Dual character of description of carriers in solids

## I. Carriers reside in c/v band

-- Boltzmann conductivity:

$$1/\tau = 1/\tau_{ii} + 1/\tau_{ph}(T) + \dots$$

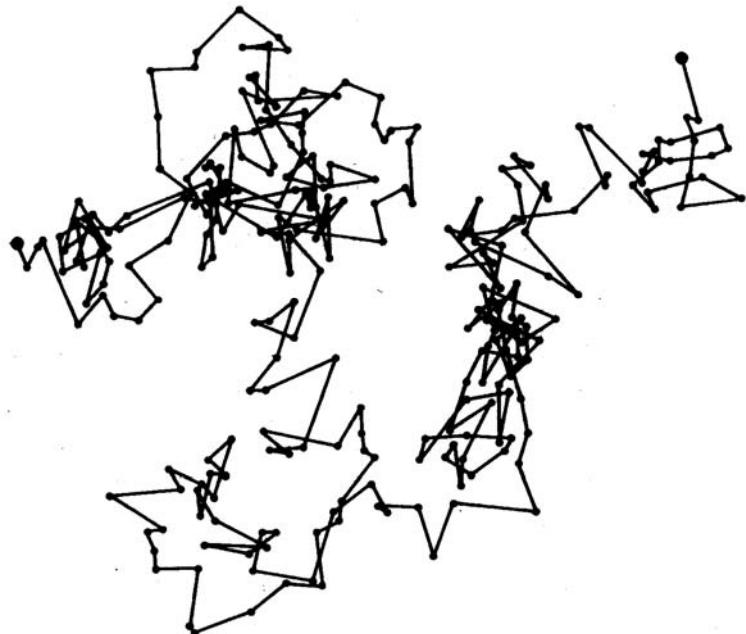
$$\sigma(T) \rightarrow \sigma_0 > 0; \rho(T) \rightarrow \rho_0 < \infty \text{ for } T \rightarrow 0$$

-- dielectric function

$$\epsilon(q) \rightarrow \infty \text{ for } q \rightarrow 0$$

-- electron-electron interaction  
unimportant

-- ....



## II. Carriers reside on impurities

-- phonon-assisted hopping

$$\sigma(T) \rightarrow 0; \rho(T) \rightarrow \infty \text{ for } T \rightarrow 0$$

-- dielectric function

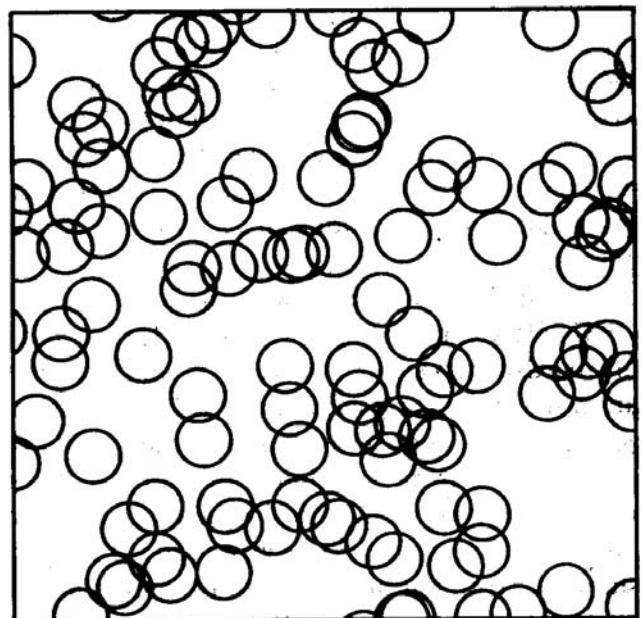
$$\epsilon(q) \rightarrow \epsilon_s < \infty \text{ for } q \rightarrow 0$$

-- electron-electron

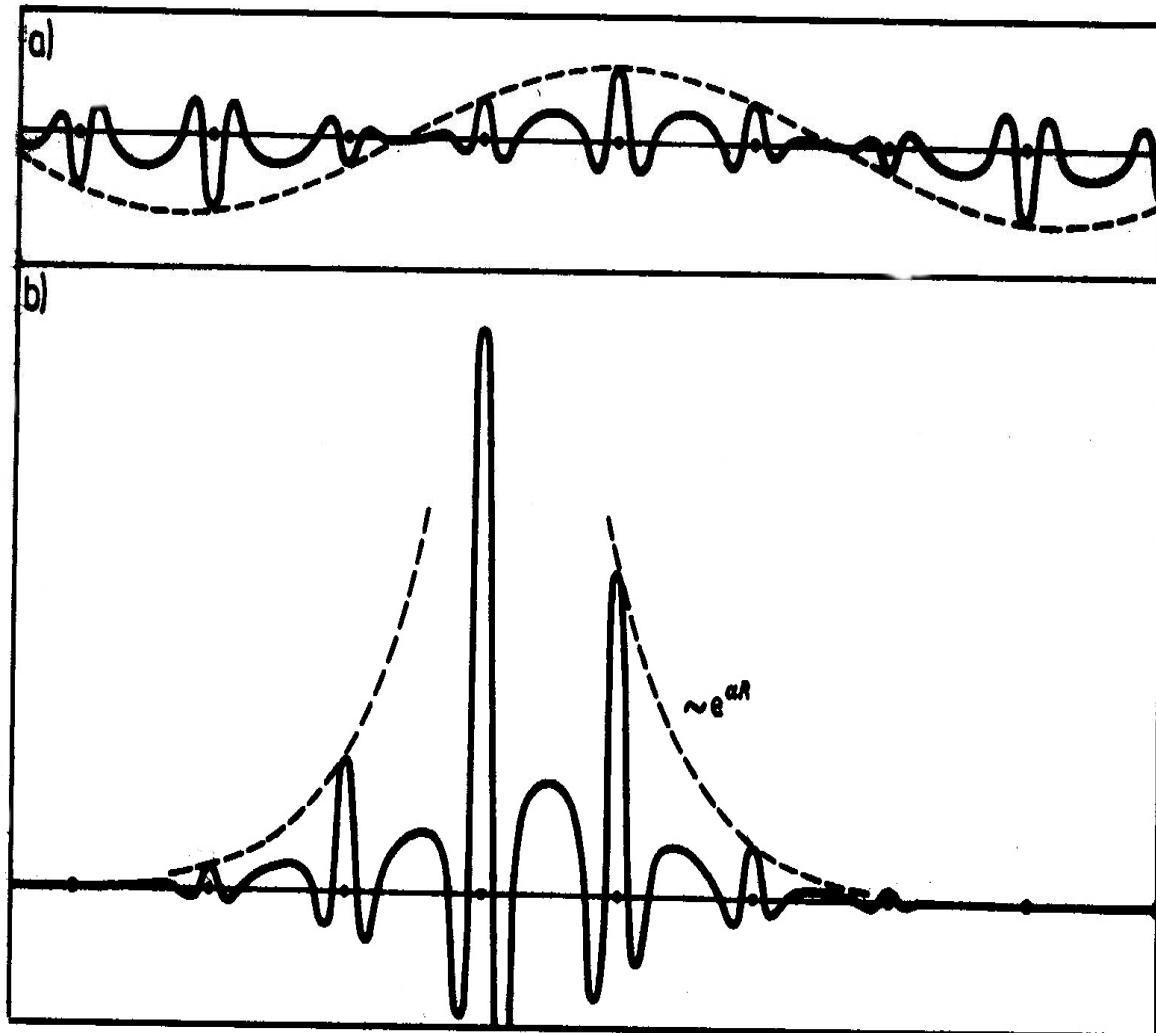
interaction important

(Coulomb gap in DOS, ...)

-- ....



# Extended vs. localized states



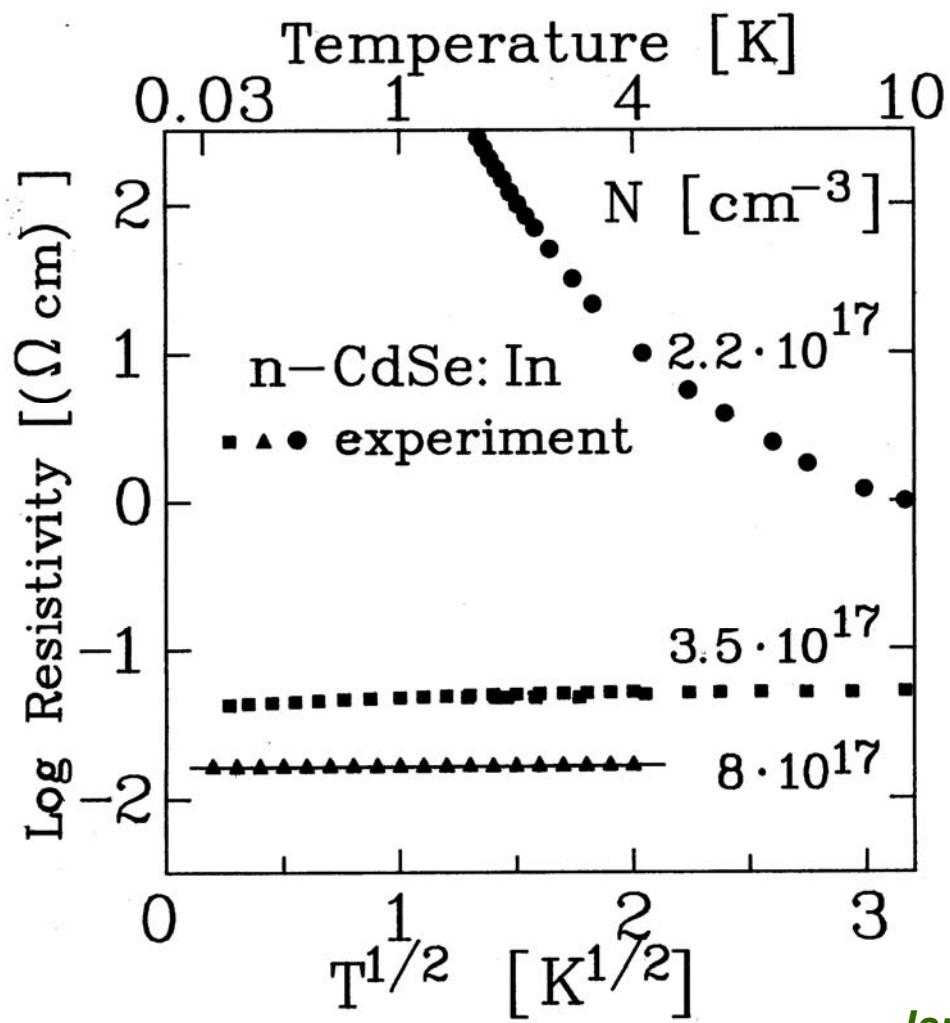
Sensitive to boundary conditions

Insensitive to boundary conditions

# Examples of metal-insulator transition (MIT)

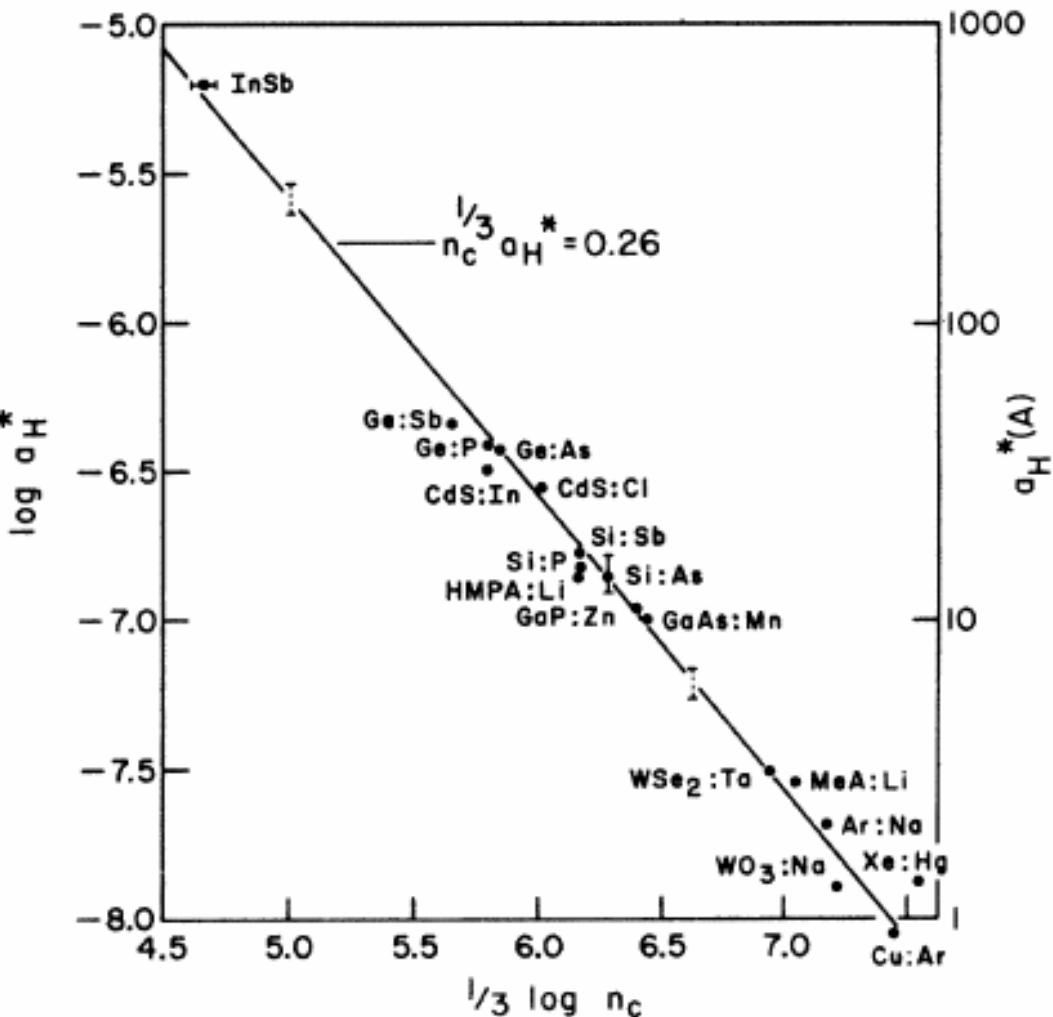
*cf. J. Spałek*

# MIT in doped semiconductors



Jaroszynski ... T.D.. '83

# MIT in various materials



MIT occurs for:  $n_c^{1/3} a_B^* \approx 0.25$

$$r_s/a_B^* = [3/(4\pi n_c)^{1/3}]/a_B \approx 2.5$$

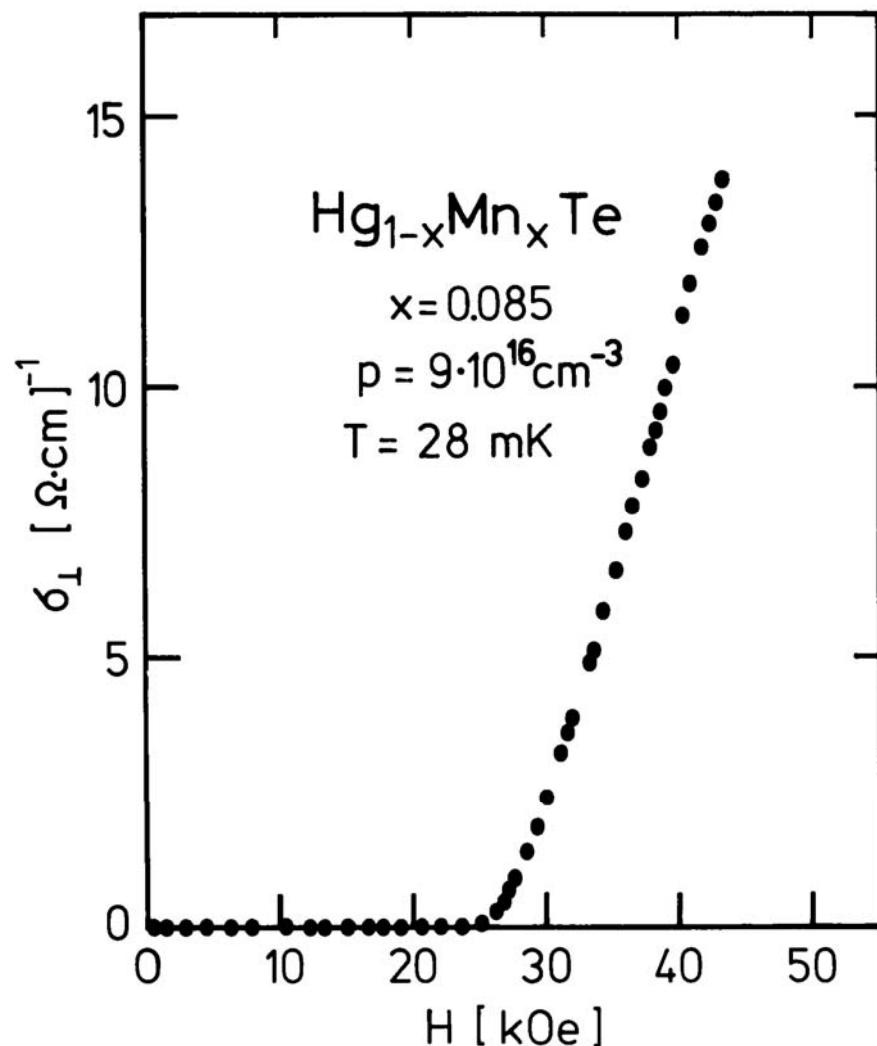
For hydrogenic-like donors:

$$a_B^* = a_B \varepsilon_s / (m^*/m_o)$$

More general:

$$a_B^* = \hbar / (2 E_I m^*)^{1/2}$$

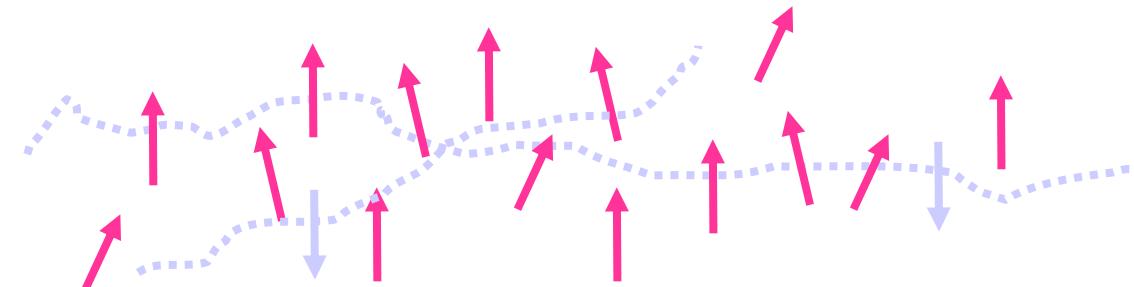
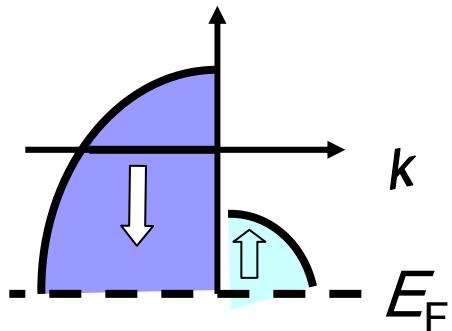
# MIT in p-(Hg,Mn)Te -- disorder (scattering by Mn spins) reduced by the magnetic field



Wojtowicz ... TD  
PRL'86

Spin/charge transport on the  
metallic side of the Anderson-  
Mott MIT

# p-d Zener model of hole-mediated ferromagnetism in DMS



*Driving force:*

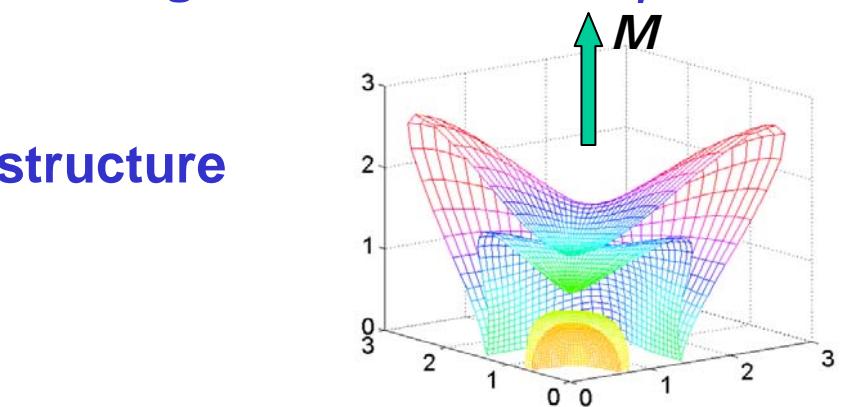
lowering of the hole energy due to redistribution between  
hole spin subbands split by p-d exchange interaction,  $\Delta \sim \beta M$

*Essential ingredient:*

Complexity of the valence band structure  
has to be taken into account

No adjustable parameters

$$T_C \sim \beta^2 \rho_{\text{DOS}}^{(s)}$$



T.D. et al., '97-  
MacDonald et al. (Austin/Prague) '99-

# p-d Zener model + Luttinger-Kohn $kp$ theory of carrier-mediated ferromagnetism in DMS

- p-d Zener model + 6x6 (or 8x8)  $kp$  theory describes **quantitatively or semi-quantitatively:**

- thermodynamic [ $T_C$ ,  $M(T,H)$ ]
- micromagnetic
  - (magnetic anisotropy, magnetic stiffness, magnetic domains)
- dc and ac charge and spin transport
  - (AHE, AMR, PHE,  $\sigma(\omega)$ , ESR)
- optical properties (MCD)

*Warsaw/Tohoku 1999-, Austin/Prague 2001-*

→ bases for magnetization manipulation

*Tohoku/ Warsaw/Grenoble/Wuerzburg/Orsay/Hitachi/Prague*

# a recent example

Vol 455 | 25 September 2008 | doi:10.1038/nature07318

nature

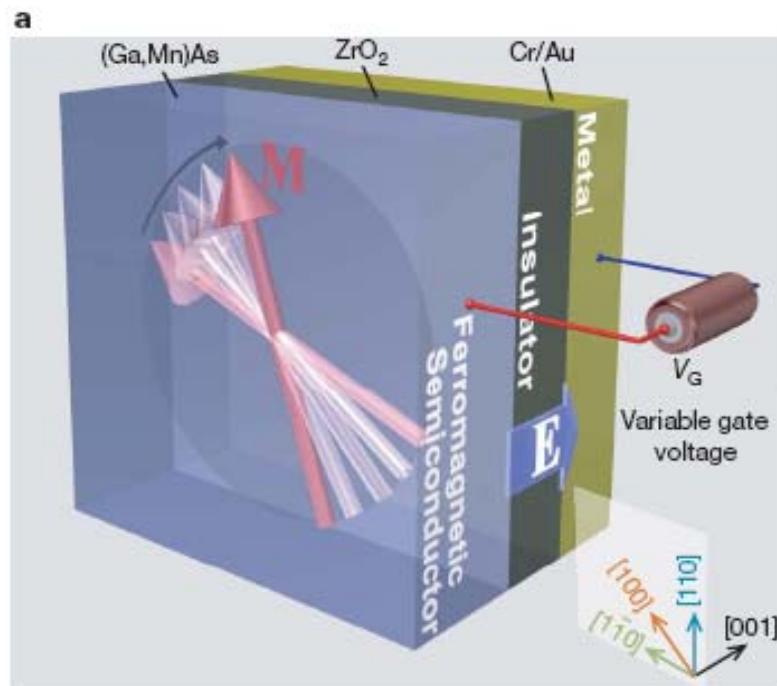
## Magnetization vector manipulation by electric fields

D. Chiba<sup>1,2</sup>, M. Sawicki<sup>2,3</sup>, Y. Nishitani<sup>2</sup>, Y. Nakatani<sup>4</sup>, F. Matsukura<sup>2,1</sup> & H. Ohno<sup>2,1</sup>

<sup>1</sup>Semiconductor Spintronics Project, Exploratory Research for Advanced Technology, Japan Science and Technology Agency, Sanban-cho 5, Chiyoda-ku, Tokyo 102-0075, Japan.

<sup>2</sup>Laboratory for Nanoelectronics and Spintronics, Research Institute of Electrical Communication, Tohoku University, Katahira 2-1-1, Aoba-ku, Sendai 980-8577, Japan. <sup>3</sup>Institute of Physics, Polish Academy of Sciences, Al. Lotników 32/46, PL-02668, Warszawa, Poland. <sup>4</sup>University of Electro-communications, Chofugaoka 1-5-1, Chofu, Tokyo 182-8585, Japan.

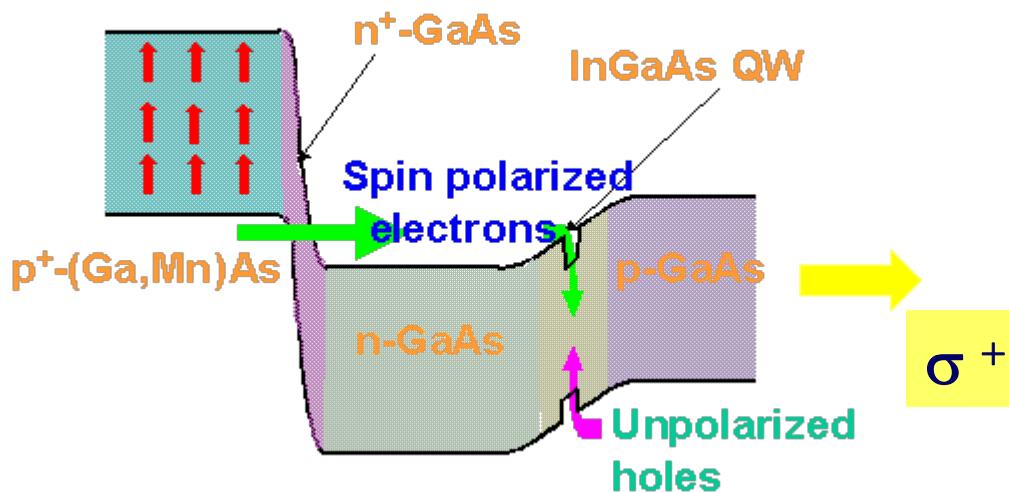
515



# Spin Esaki-Zener Diode

How to change *spin polarization of holes* into  
*spin polarized electrons*

## Spin Esaki-Zener diode



Recent experimental results:

Polarization of electrons  $P_j$  up to 70%

*Tohoku, St. Barbara, IMEC, Regensburg,...*

# Description of spin transport effects in ferromagnetic structures

- two spin channels characterized by  $f_{\uparrow}$  and  $f_{\downarrow}$ 
  - **spin diffusion equation**
  - **continuity conditions**
  - **boundary conditions**

*Aronov et al. '76-- ; Silsbee et al. '80-- ; Fert et al. '93-- , Schmidt et al. '00—*

*cf. B. Dieny*

**spin accumulation, resistance mismatch, ...**

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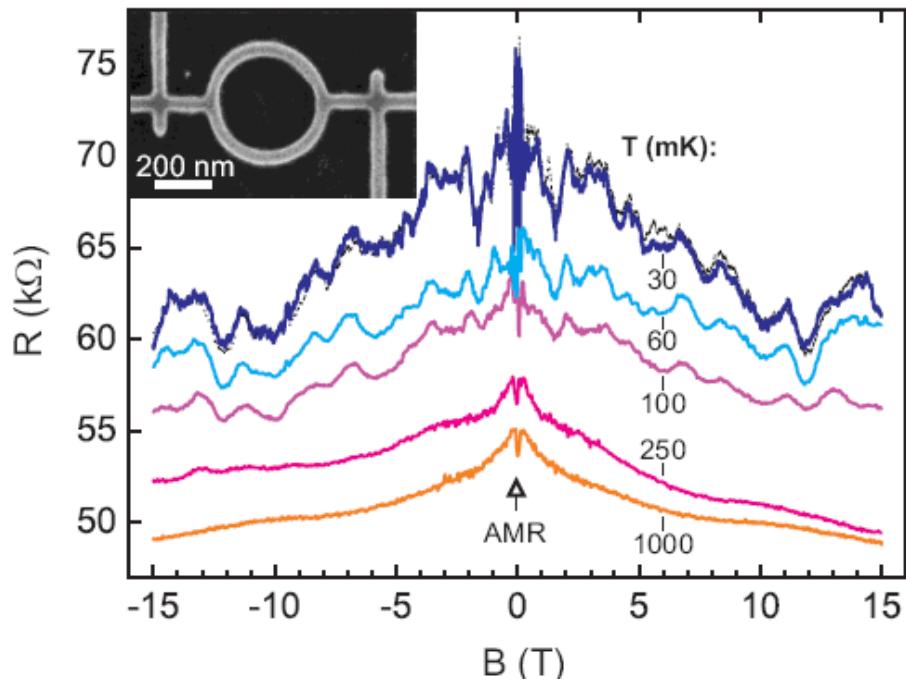
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*cf. B. Dieny*

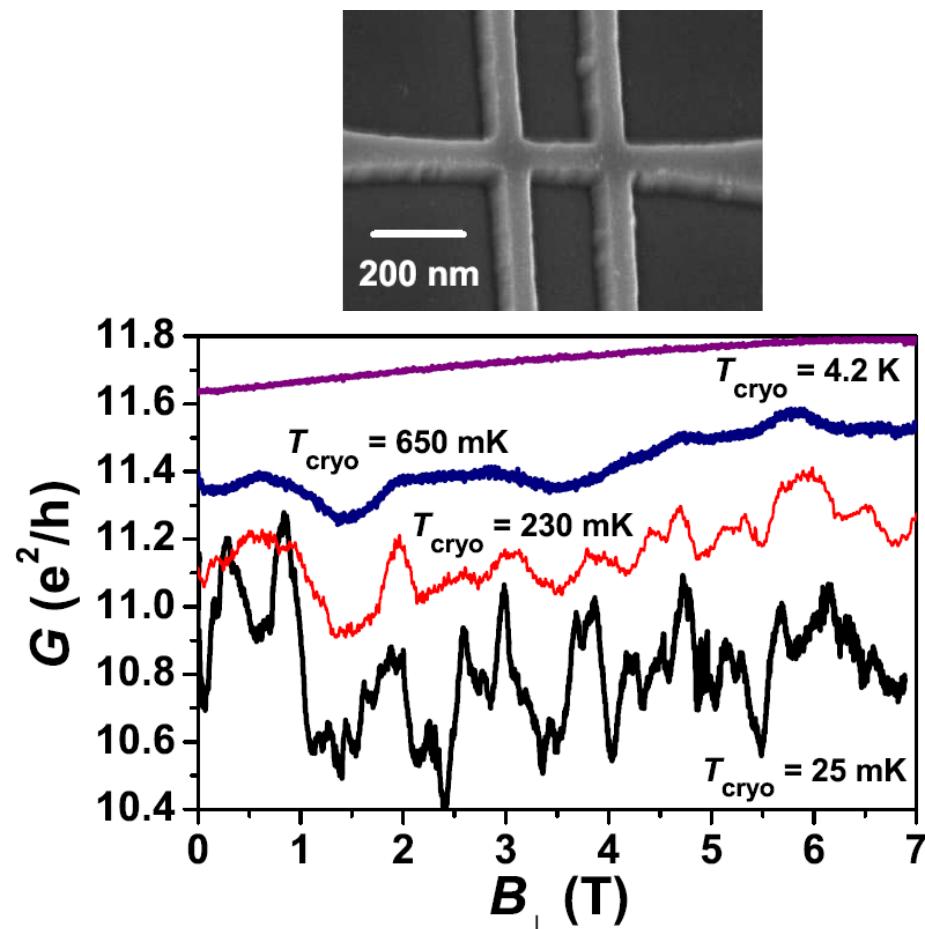
→ spin accumulation, resistance mismatch, ...

-- Implicit assumption:  $L_s \gg L_\phi$   
is it valid in (Ga,Mn)As?

# (Ga,Mn)As: universal conductance fluctuations



Wagner et al. (Regensburg) PRL '06



Vila et al. (Marcoussis, Grenoble)  
PRL '07

$L_{\phi}(T) \approx 100$  nm at 4 K from WLR and UCF

# Description of spin transport in modulated structures of (Ga,Mn)As

- in **(Ga,Mn)As type materials:**
  - four channels strongly mixed by spin-orbit interaction

$$L_s \leq L_\varphi(T) \approx 30 \text{ nm at 4 K from WLR and UCF}$$

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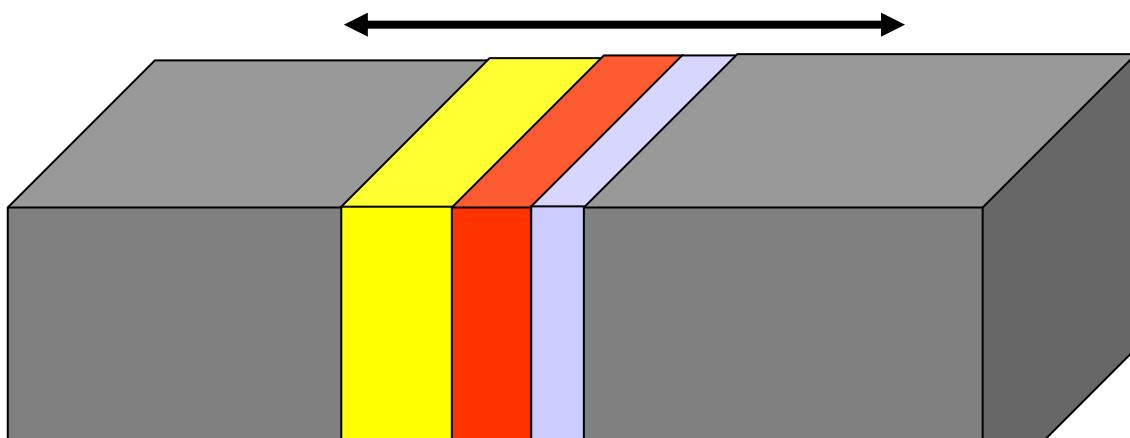
$$L_s \leq L_\varphi(T) \approx 30 \text{ nm at 4 K from WLR and UCF}$$

→ quantum Landauer-Büttiker formalism

*implementation for semiconductor layered structures, see A. Di Carlo, SST'03*

- uniform and infinite in 2D ( $k_x, k_y$  good quantum numbers)
- modulation in 1D
- simulation length  $L \approx L_\varphi$

$$L = L_\varphi$$



# Description of semiconductor band structure

***kp* method:** RTD *Petukhov et al., PRL'02*  
TMR *Brey, APL'04, Jeffres '06*  
DWR *Nguyen et al., PRL'06*

# Description of semiconductor band structure

***kp* method:** RTD *Petukhov et al., PRL'02*  
TMR *Brey, APL'04, Jeffres '06*  
DWR *Nguyen et al., PRL'06*

Standard *kp* formalism disregards effects  
important for spin transport and spin tunneling:

- Rashba and Dresselhaus terms
- spin filtering at interfaces cf. Fe/MgO *cf. A. Bonanni*
- spin-mixing conductance *Brataas et al. '01*
- band extrema away from the center of the Brillouin zone

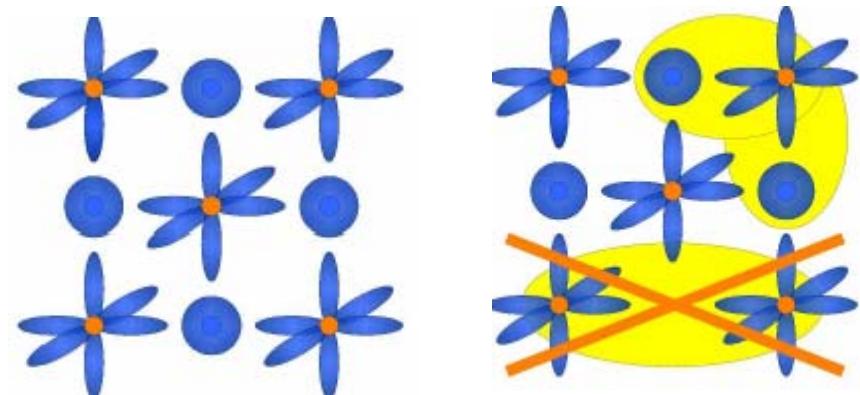
These can be taken into account within  
empirical tight-binding approach

# Tight-binding model

## GaAs: $sp^3d^5s^*$ :

- nn coupling
- Ga and As atoms: 20 orbitals
- parametrization:

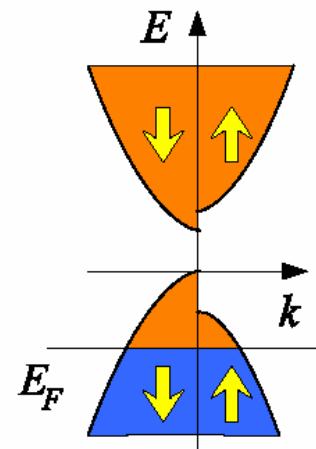
*M.-J. Jancu et al., PRB'98*



## (Ga,Mn)As: GaAs + spin splitting

- VCA, MFA
- $\Delta_c = \alpha N_o \times \langle S_z \rangle$ ,  $\Delta_v = \beta N_o \times \langle S_z \rangle$ ,  
 $\alpha N_o = 0.2 \text{ eV}$ ,  $\beta N_o = -1.2 \text{ eV}$

**no adjustable parameters**



# Landauer-Büttiker + tight-binding model for (Ga,Mn)As-based structures -- summary

- The model describes
  - magnitude and anisotropy of  $P_j$  and TMR
  - decay of  $P_j$  and TMR with  $V$
  - crystalline anisotropy of  $P_j$  and TMR

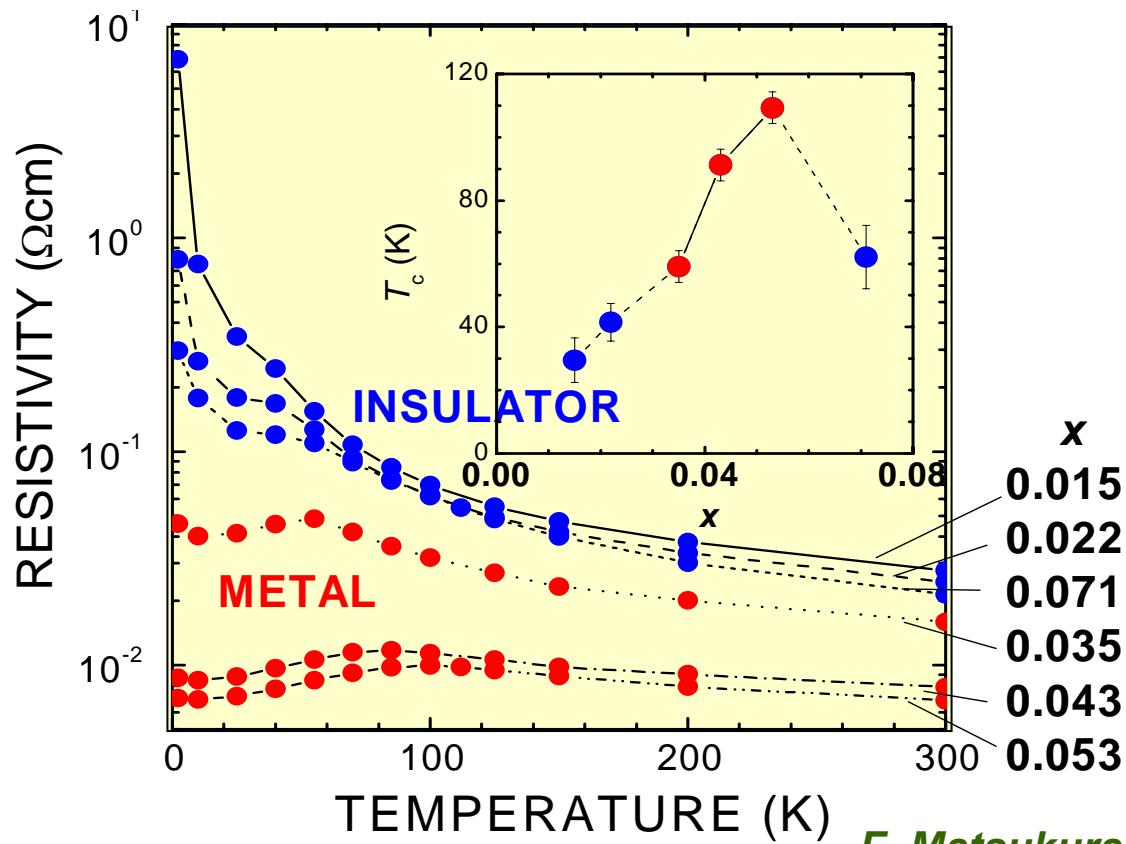
*P. Sankowski... T.D., PRB'05, 07*

- LLG eq. + adiabatic spin torque describes:
  - current-induced domain-wall velocity
- The model does *not* describe:
  - domain-wall resistance → disorder essential

*R. Oszwaldowski ... T.D. PRB'06*

# Spin/charge transport near the Anderson-Mott MIT

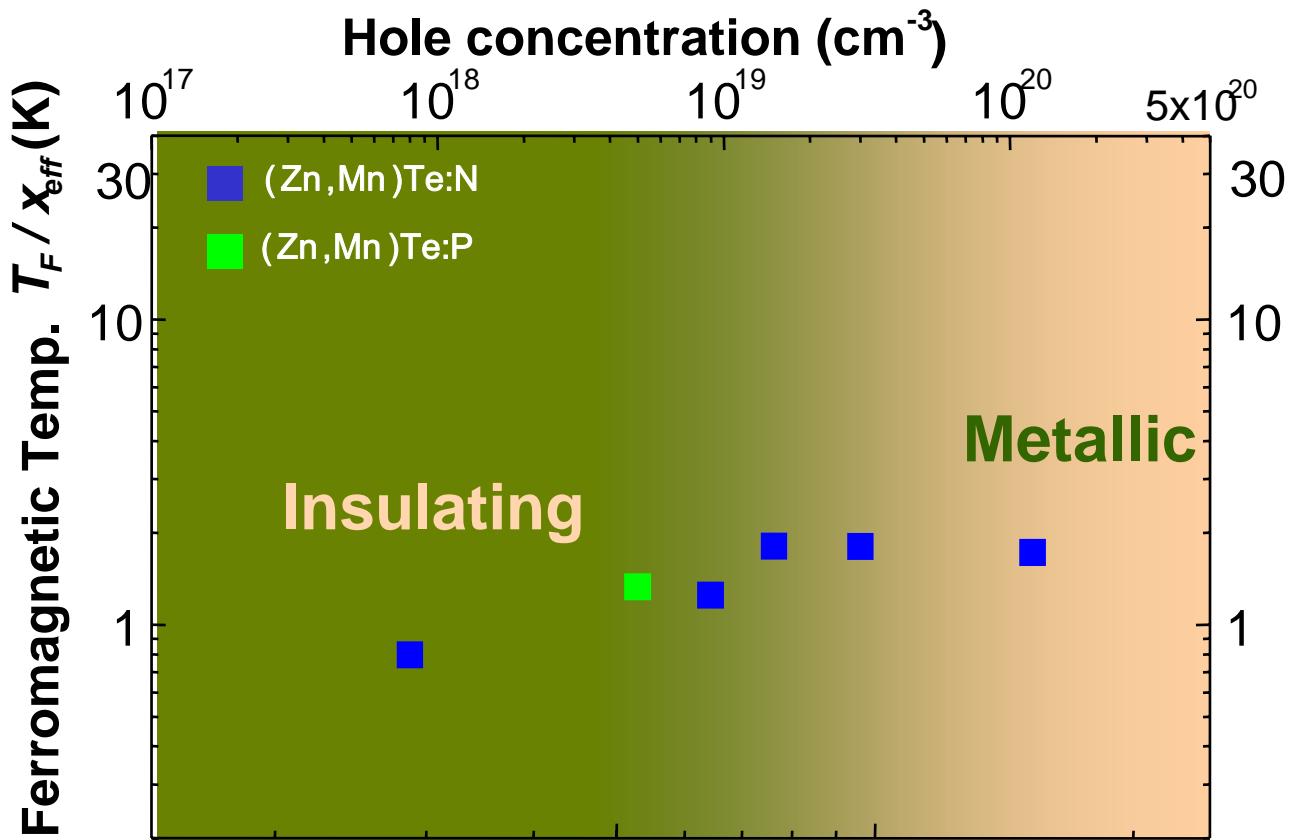
# $\text{Ga}_{1-x}\text{Mn}_x\text{As}$ : resistance vs. temperature and Curie temperature vs. $x$



*F. Matsukura et al. (Tohoku) PRB'98*

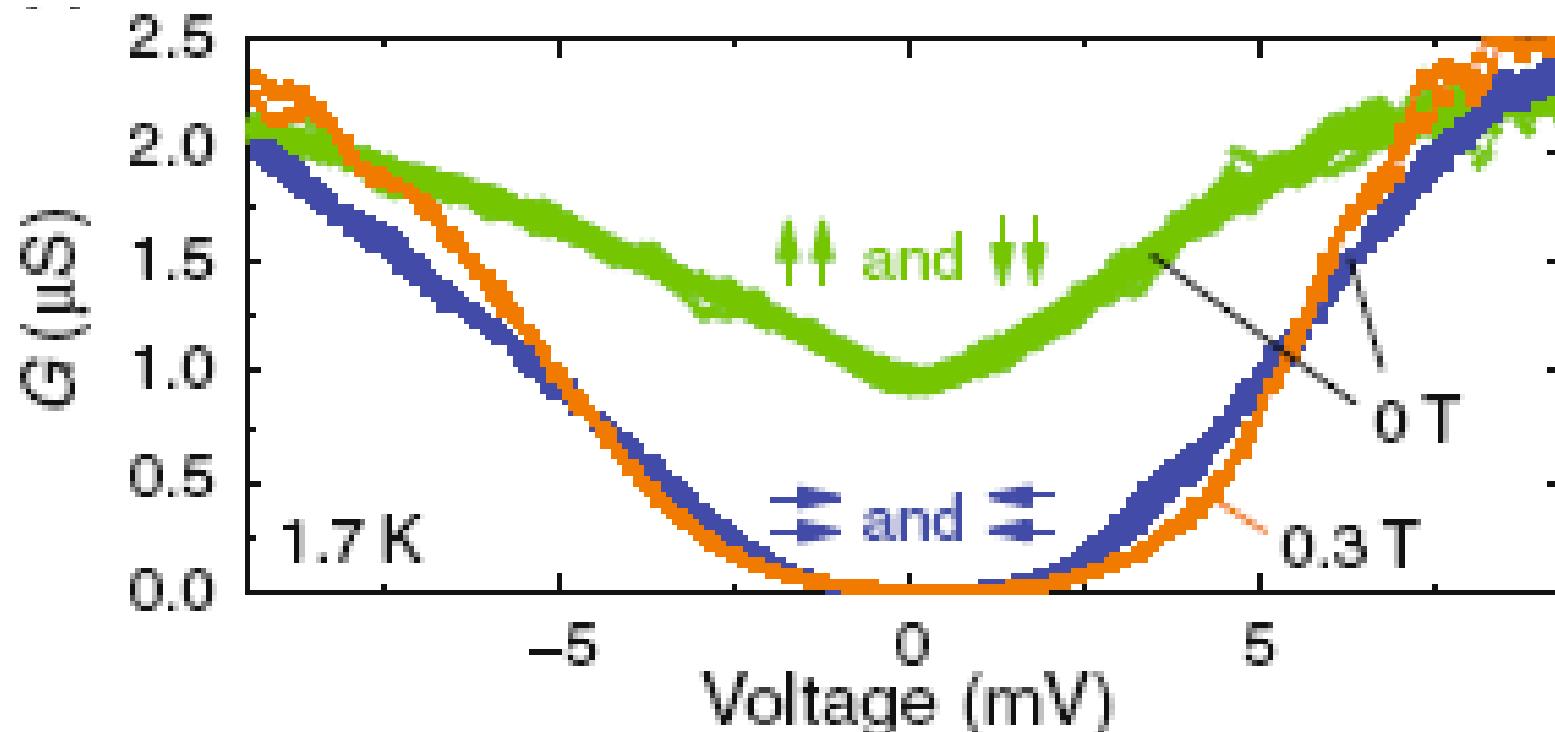
- ferromagnetism on both sides of metal-insulator transitions
- ferromagnetism disappears in the absence of holes

# Ferromagnetic temperature in p-(Zn,Mn)Te



- ferromagnetism disappears in the absence of holes
- ferromagnetism on both sides of metal-insulator transition

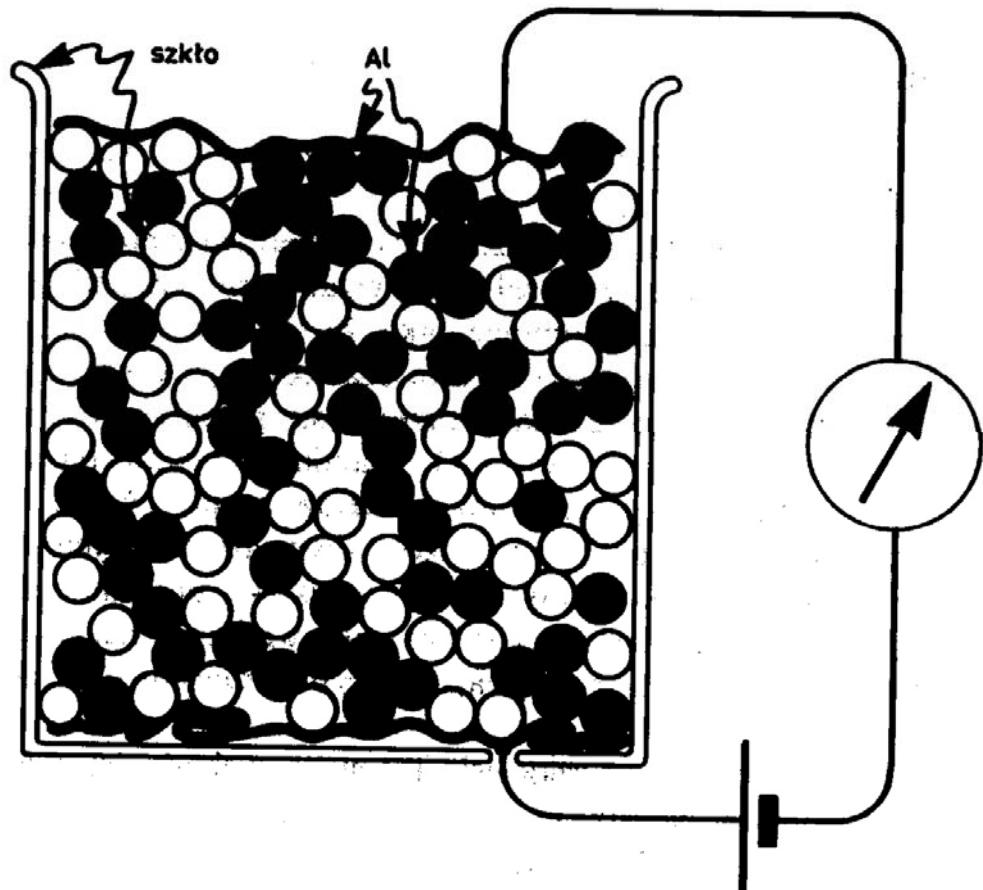
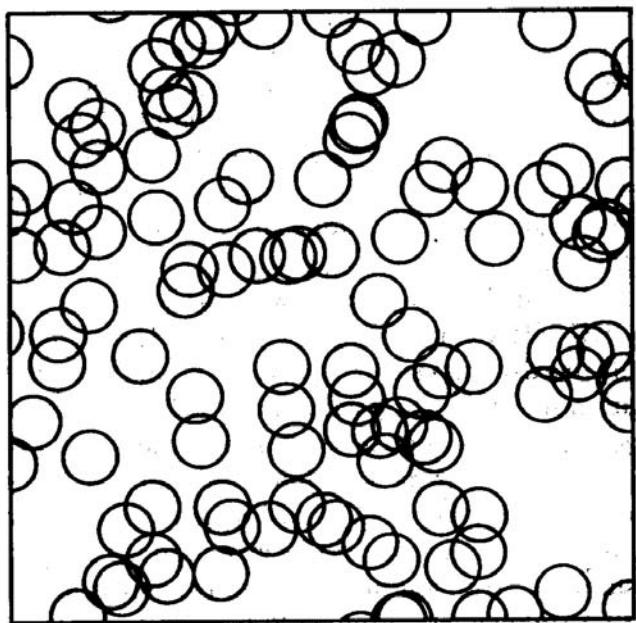
# Conductance vs. bias in a TMR structure of (Ga,Mn)As - evidence for a Coulomb gap and TAMR



Pappert et al. (Wuerzburg) PRL'06

# (Classical) percolation theory of MIT

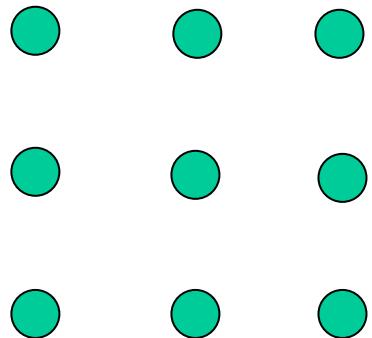
# Conductive/nonconductive composites



# (Quantum) Anderson localization

# Particle/wave propagation in solids

## Crystals (periodic potential)



Classical particles: channeling  
(e.g., Rutherford back scattering of  $\alpha$  particles)

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## Crystals (periodic potential)



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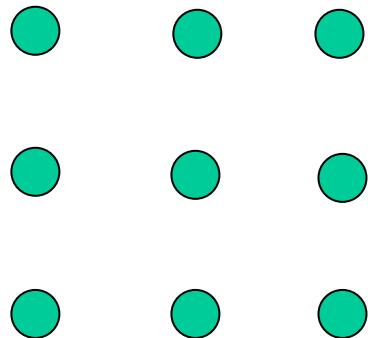


**Quantum particles:** (electrons, photons,...)  
*Energy bands:* quasi-free (ballistic) propagation  
*Energy gaps:* regions of evanescent waves

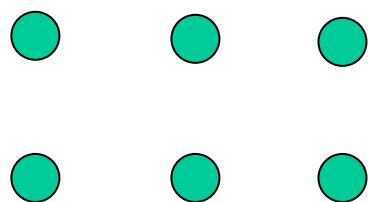


# Particle/wave propagation in solids

## Crystals (periodic potential)

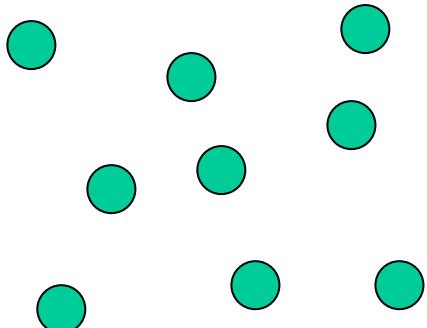


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## Disordered solids



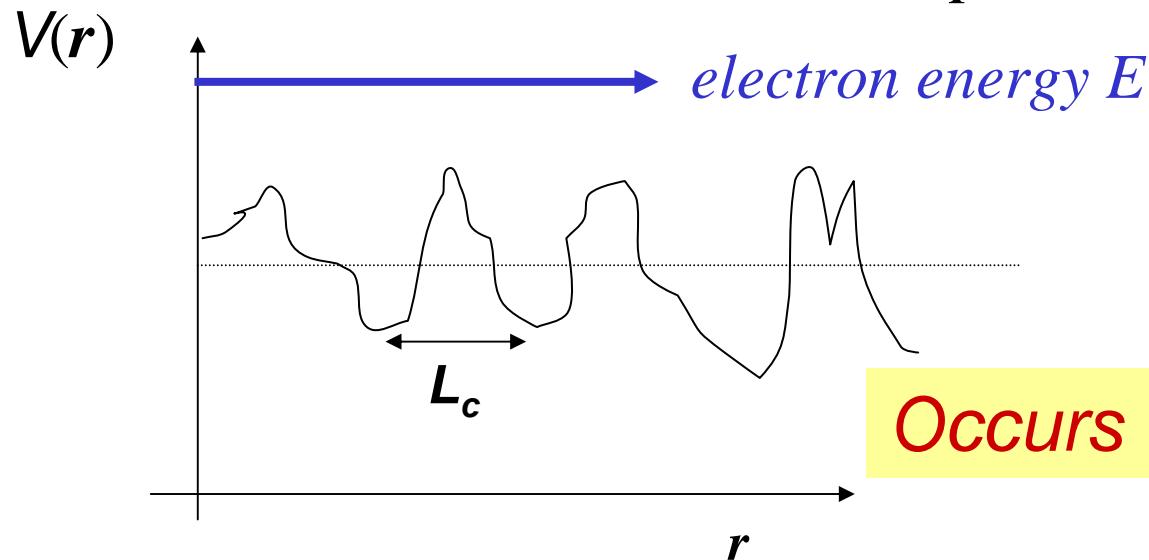
**Classical particles:**  
diffusion above percolation threshold

$$(\langle r^2(t) \rangle)^{1/2} = \sqrt{2 t D d} \rightarrow \infty \text{ for } t \rightarrow \infty$$

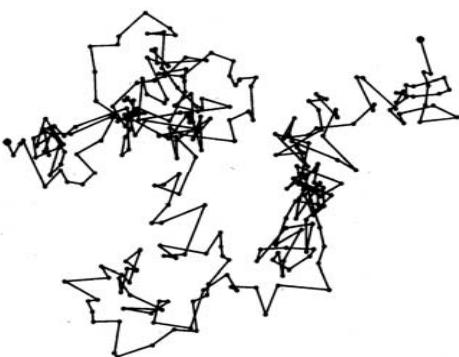
# Anderson localization

## Quantum localization by scattering

1. Contradicts classical percolation picture



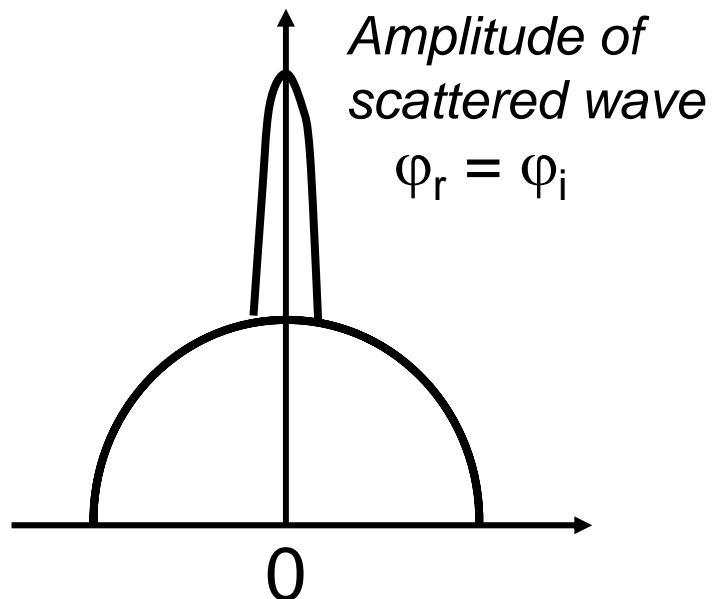
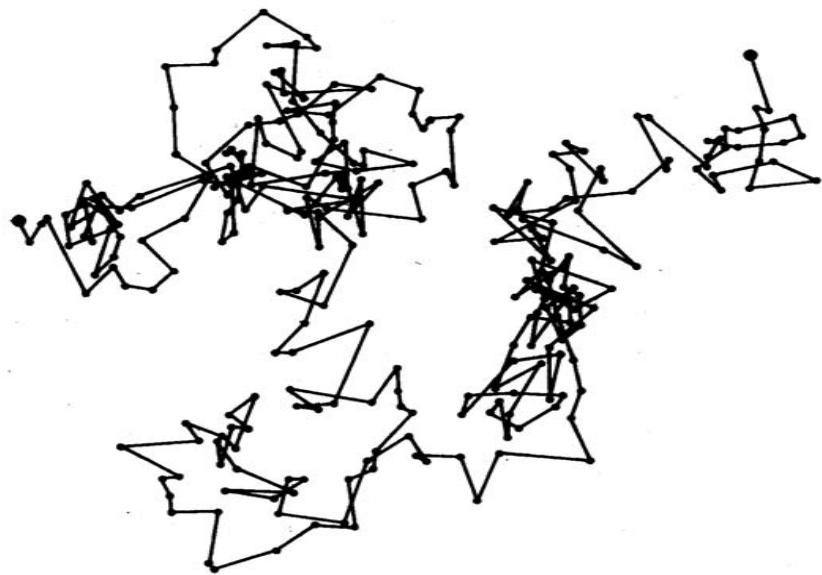
2. Contradicts classical diffusion equation



$$(\langle r^2(t) \rangle)^{1/2} = \sqrt{2tDd} \rightarrow \infty \text{ for } t \rightarrow \infty$$

Cannot be described by CPA,...

# Enhanced backscattering

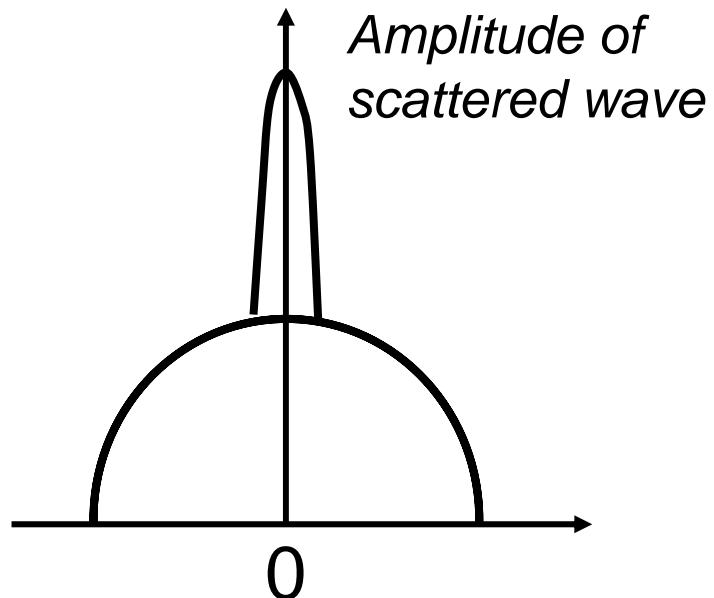
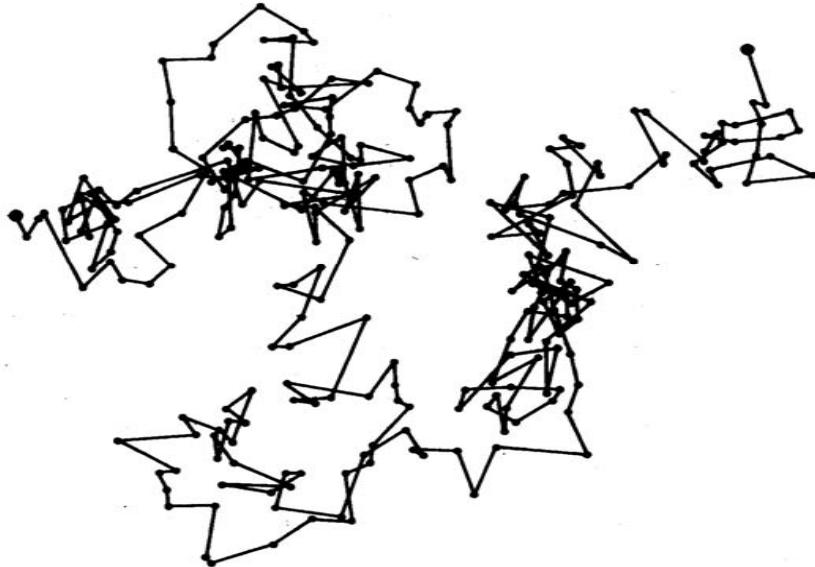


$$T_{\text{return}} = T_r + T_l + 2|T_r T_l|^{1/2} \cos(\varphi_r - \varphi_l)$$

$\varphi_r - \varphi_l = 0$  if no magnetic field and spin scattering  
Factor of two enhancement over classical value

Experimental evidence for backscattering:  
*oscillations in rings and magnetoresistance in films*

# Enhanced backscattering



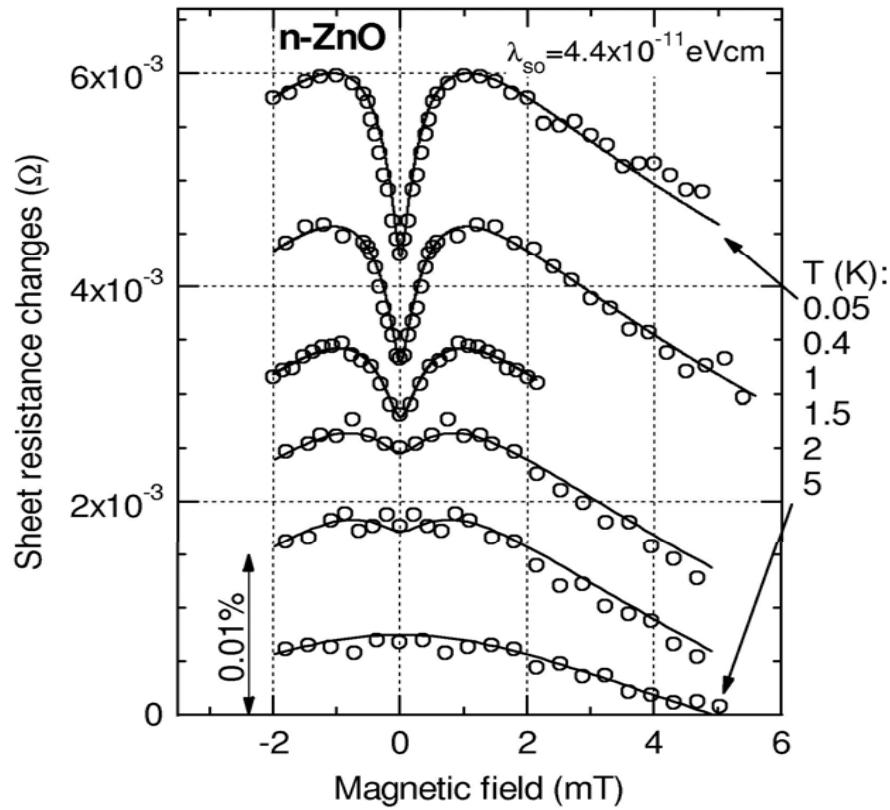
$$T_{\text{return}} = T_r + T_l + 2|T_r T_l|^{1/2} \cos(\varphi_r - \varphi_l)$$

$\varphi_r - \varphi_l = 0$  if no magnetic field and inelastic scattering

Factor of two enhancement over classical value

→ magnetic field and temperature *enhance* diffusion

# Quantum localisation magnetoresistance in *n*-WZ ZnO



*T. Andreczyk, ..., T.D., PRB'05*

$$H_{so} = \lambda_{so} \hat{\mathbf{c}}(\mathbf{s} \times \mathbf{k})$$

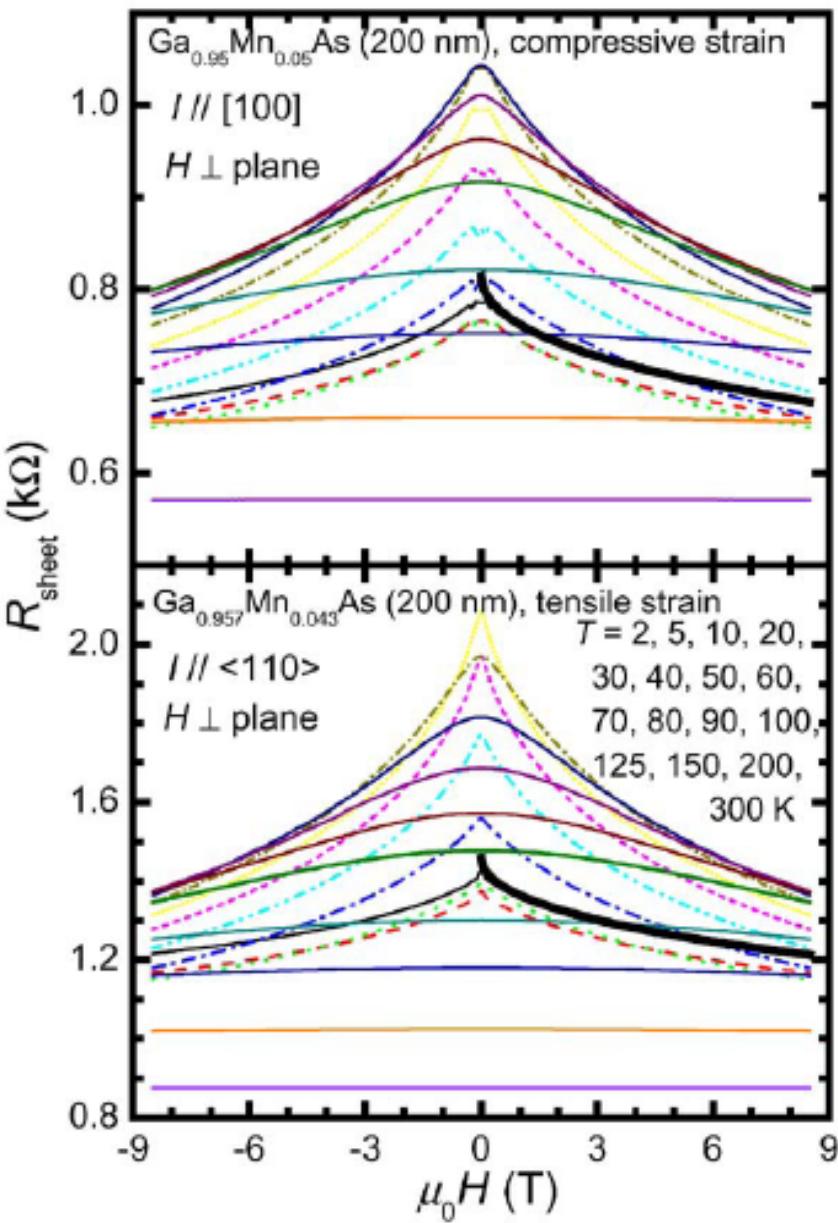
$$\tau_{sox}^{-1} = \lambda_{so}^2 k_F^2 \tau / 12$$

$$B_m \approx 1.6 \alpha_{so}^2 m^{*2}$$

*Dyakonov-Perel; Fukuyama, Hoshino*

$\lambda_{so} [\text{meV}\text{\AA}]$	CdSe	ZnO	$T_2 = 10 \text{ ns}$
WLR	$50 \pm 10$	$4.4 \pm 0.4$	
LMTO-LSD*	30	2.2	*Voon et al. (Stuttgart, Aarhus) PRB'96

# (Ga,Mn)As: low temperature negative magnetoresistance

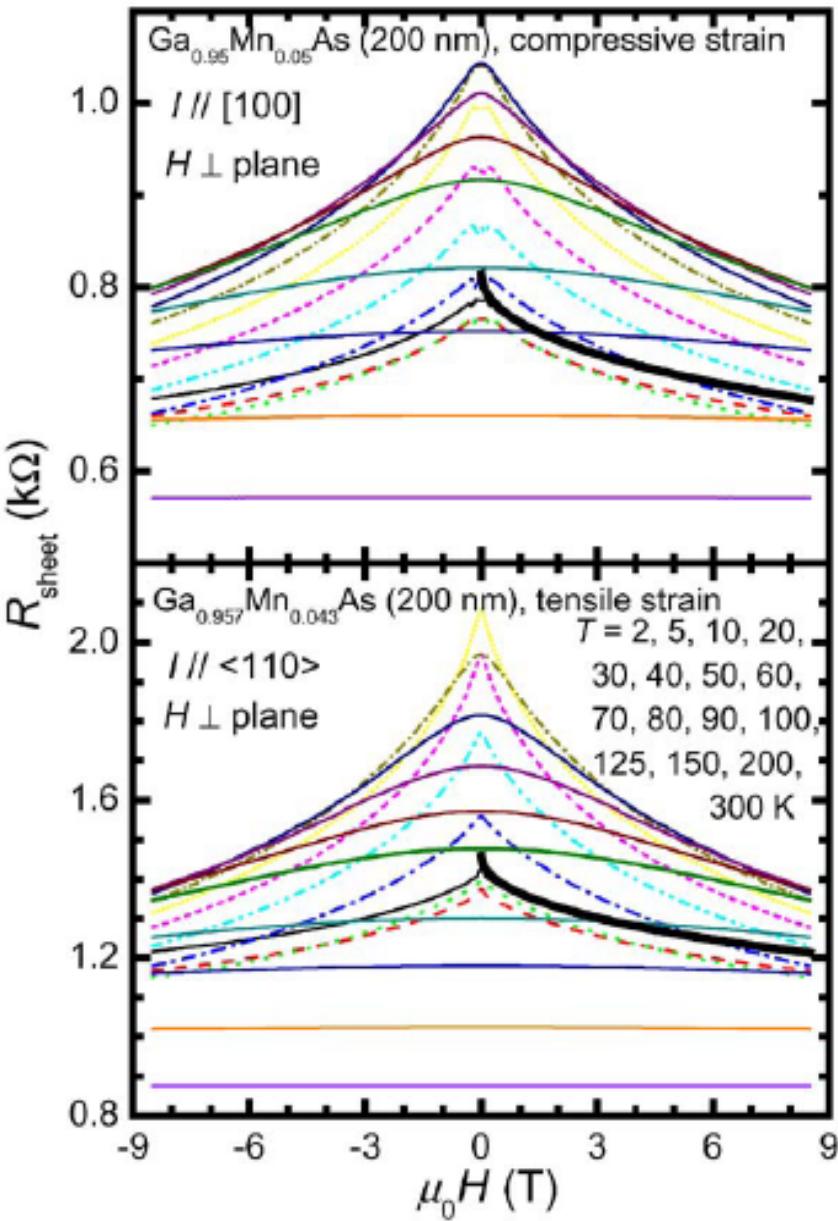


theory —

$$\Delta\rho/\rho = -n_v e^2 C_o \rho (eB/\hbar)^{1/2} / (2\pi^2 \hbar).$$

A. Kawabata'80

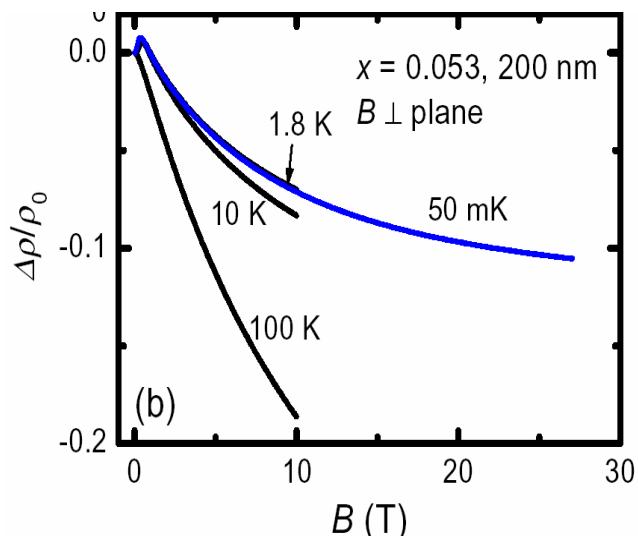
# (Ga,Mn)As: low temperature negative magnetoresistance



theory —

$$\Delta\rho/\rho = -n_v e^2 C_o \rho (eB/\hbar)^{1/2} / (2\pi^2 \hbar).$$

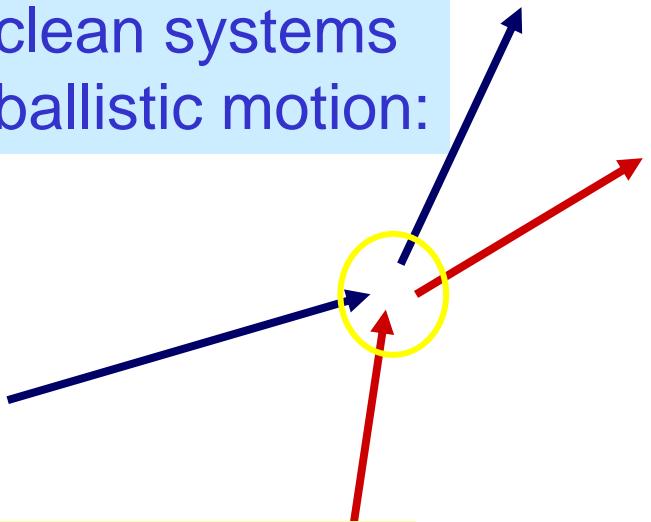
A. Kawabata'80



F. Matsukura ... T.D. (Warsaw, Tohoku)'04

# Electron-electron scattering

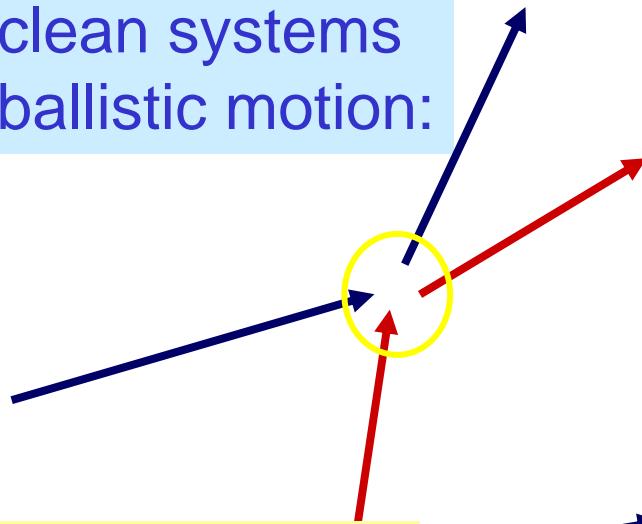
clean systems  
ballistic motion:



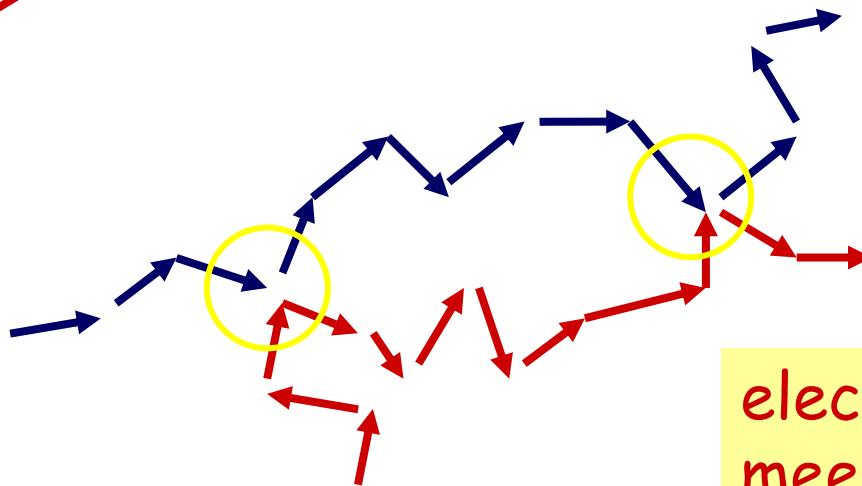
electrons never  
meet again...

# Electron-electron scattering

clean systems  
ballistic motion:



disordered systems  
diffusive motion:

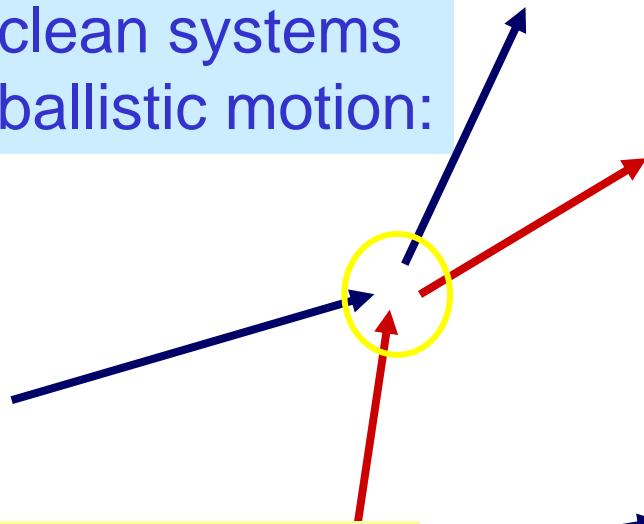


electrons never  
meet again...

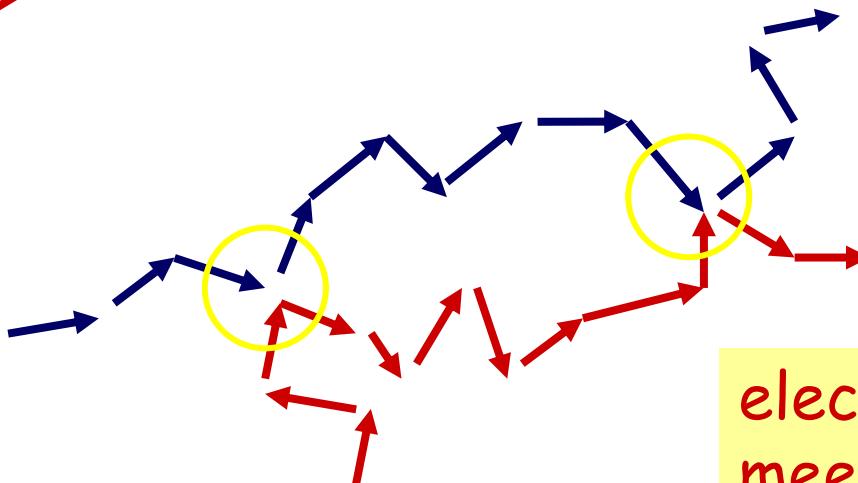
electrons can  
meet again...

# Electron-electron scattering

clean systems  
ballistic motion:



disordered systems  
diffusive motion:



electrons never  
meet again...

electrons can  
meet again...

interference of scattering amplitudes

$$T_{\sigma\sigma'} = T_\sigma + T_{\sigma'} + 2|T_\sigma T_{\sigma'}|^{1/2} \cos(\varphi_\sigma - \varphi_{\sigma'})$$

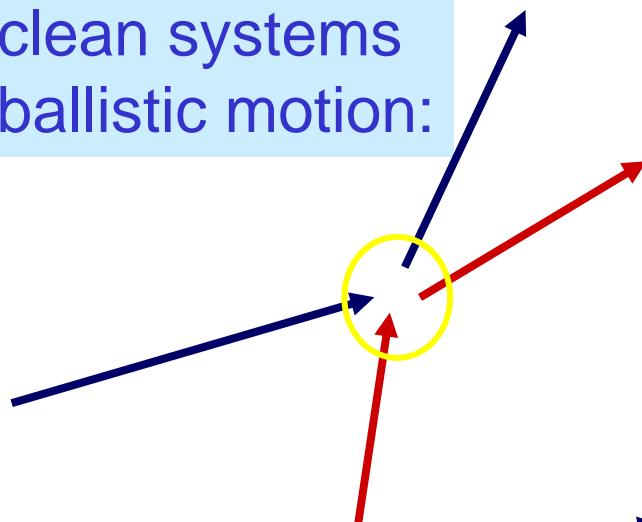
depending of spins (triplet vs. singlet):

diffusion reduced/enhanced

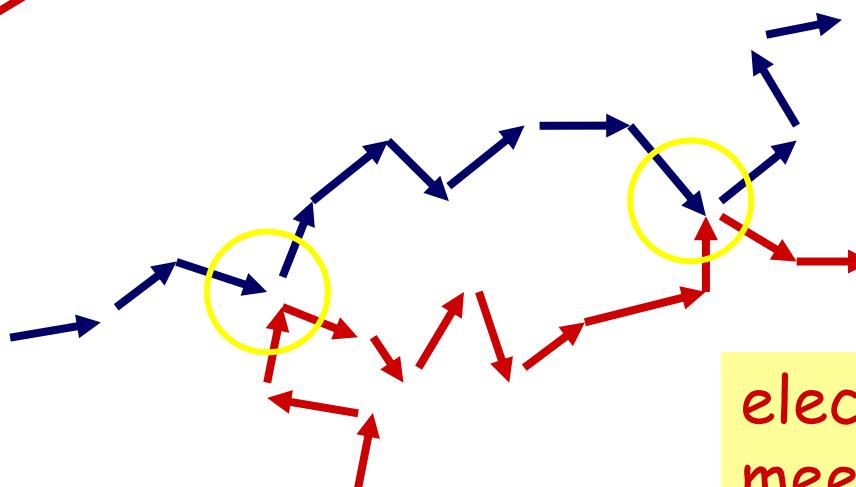
Coulomb anomaly at  $E_F$

# Electron-electron scattering

clean systems  
ballistic motion:



disordered systems  
diffusive motion:



electrons never  
meet again...

electrons can  
meet again...

interference of scattering amplitudes

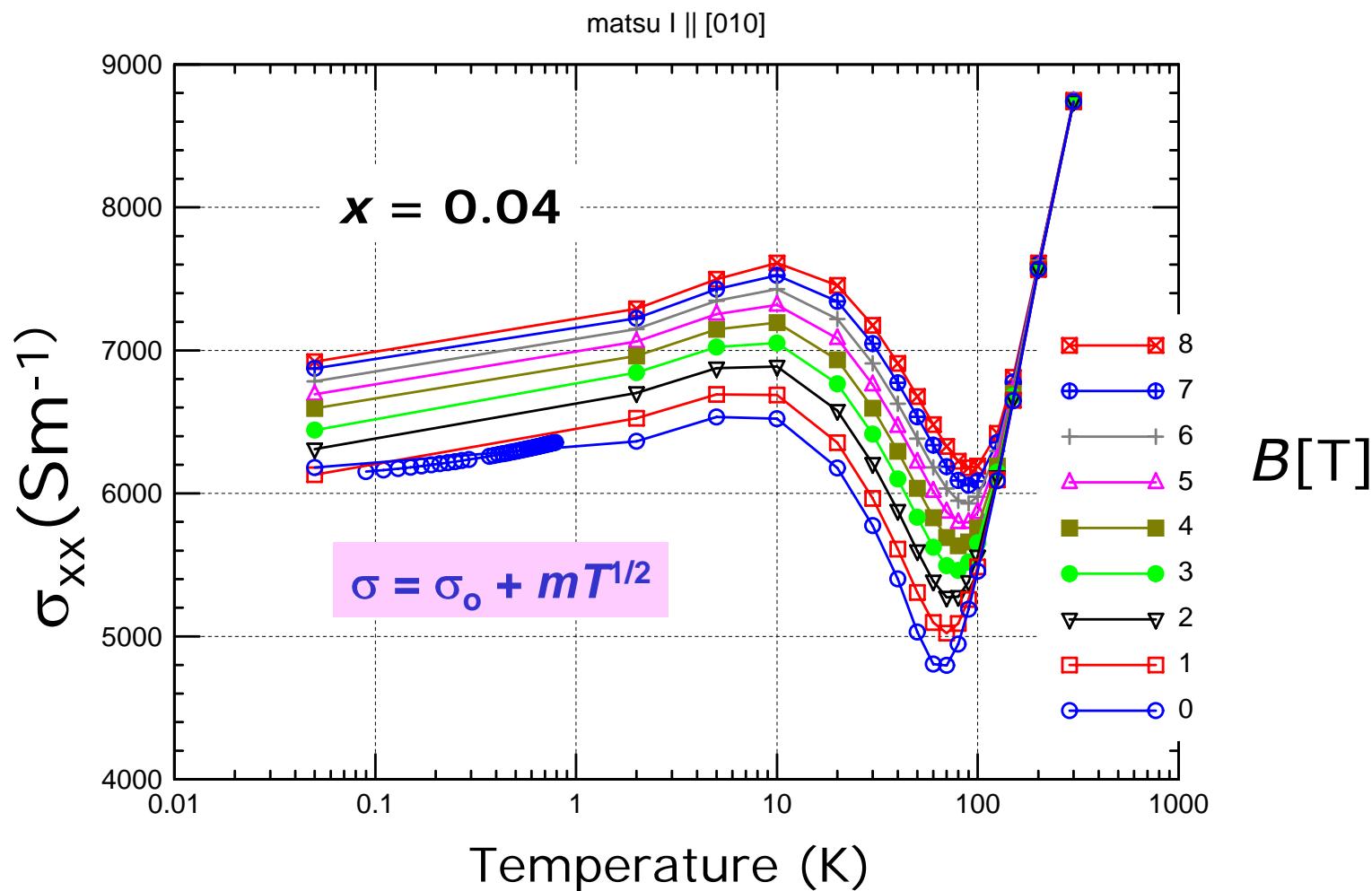
$$T_{\sigma\sigma} = T_\sigma + T_{\sigma'} + 2|T_\sigma T_{\sigma'}|^{1/2}\cos(\varphi_\sigma - \varphi_{\sigma'})$$

same spins: diffusion reduced

opposite spins: diffusion enhances

→ spin splitting and spin scattering reduce diffusion

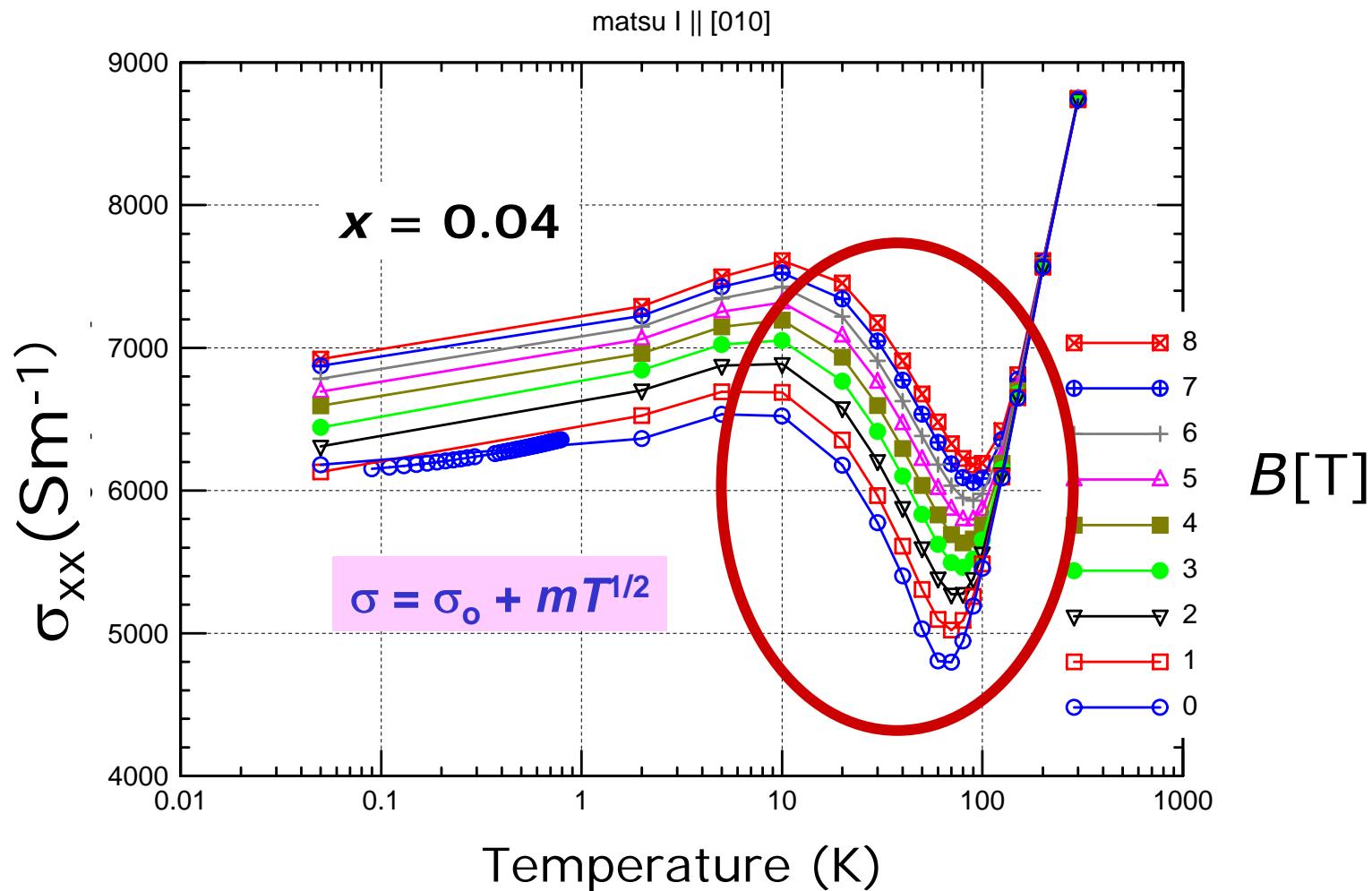
# Temperature dependence of conductance in various magnetic fields in (Ga,Mn)As



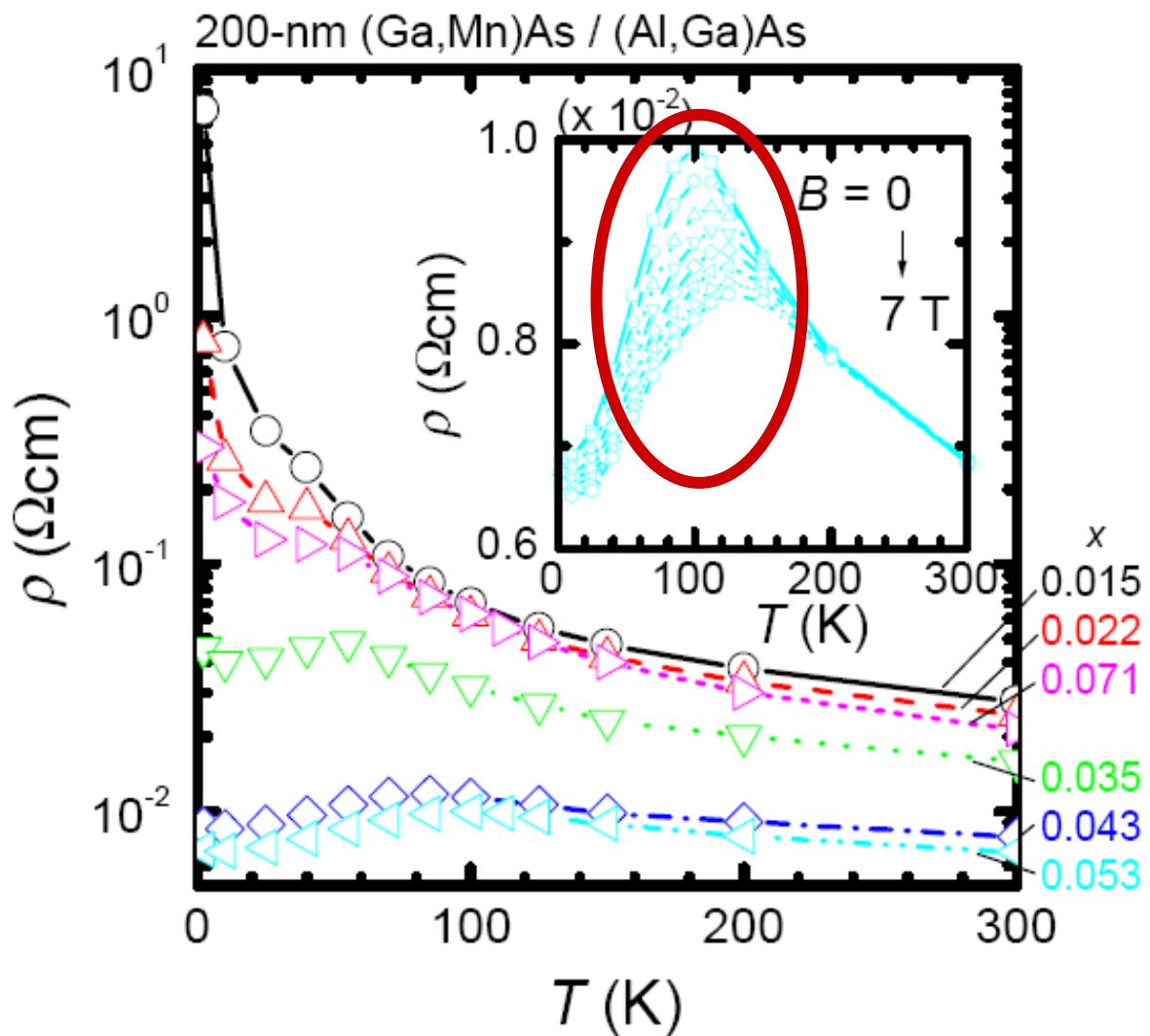
# we do not understand

- critical scattering at  $T_C$   
( at  $T \rightarrow 0$  in paramagnets)
- CMR

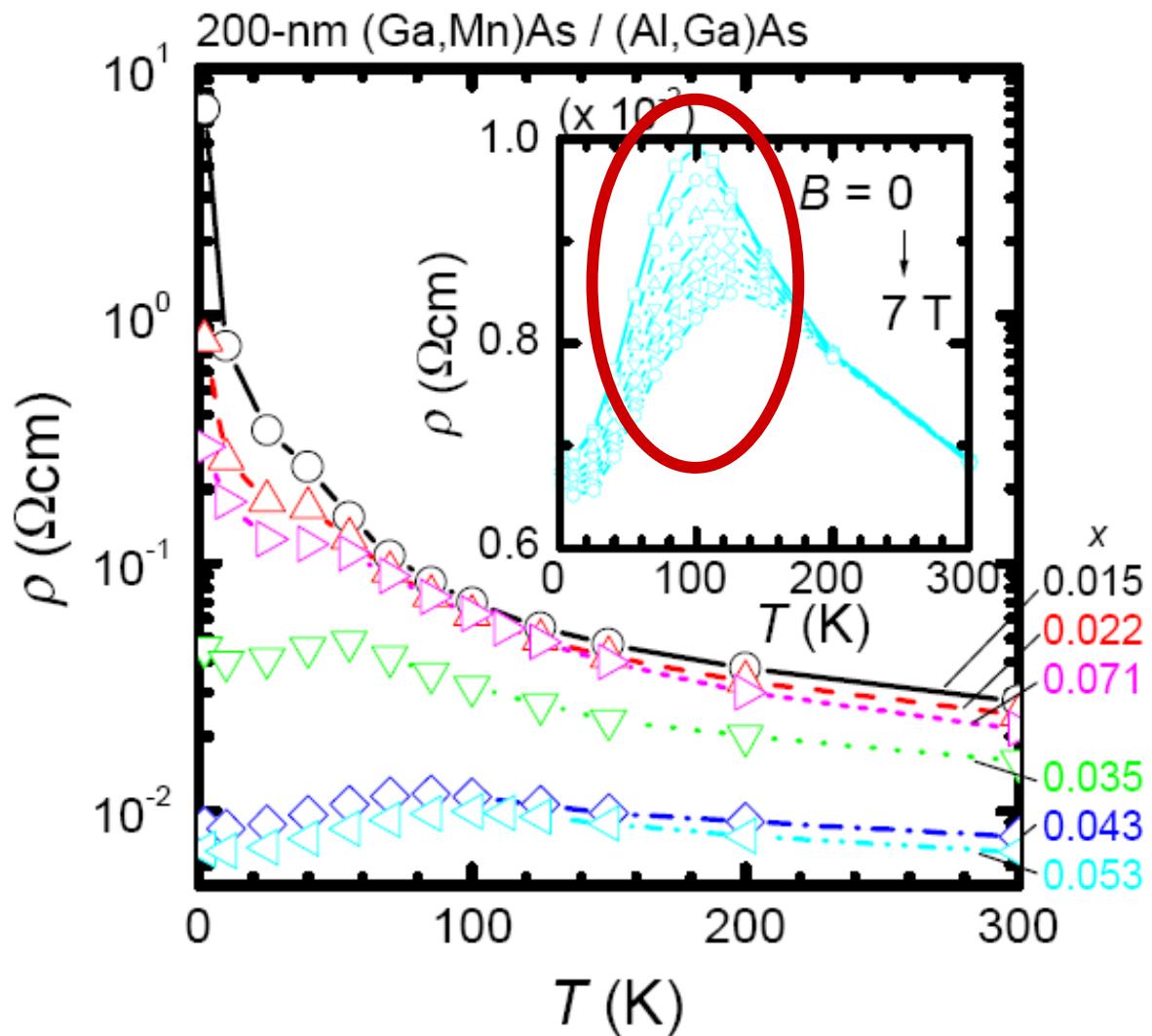
# Temperature dependence of conductivity in various magnetic fields in (Ga,Mn)As



# Temperature dependence of resistivity in various magnetic fields in (Ga,Mn)As



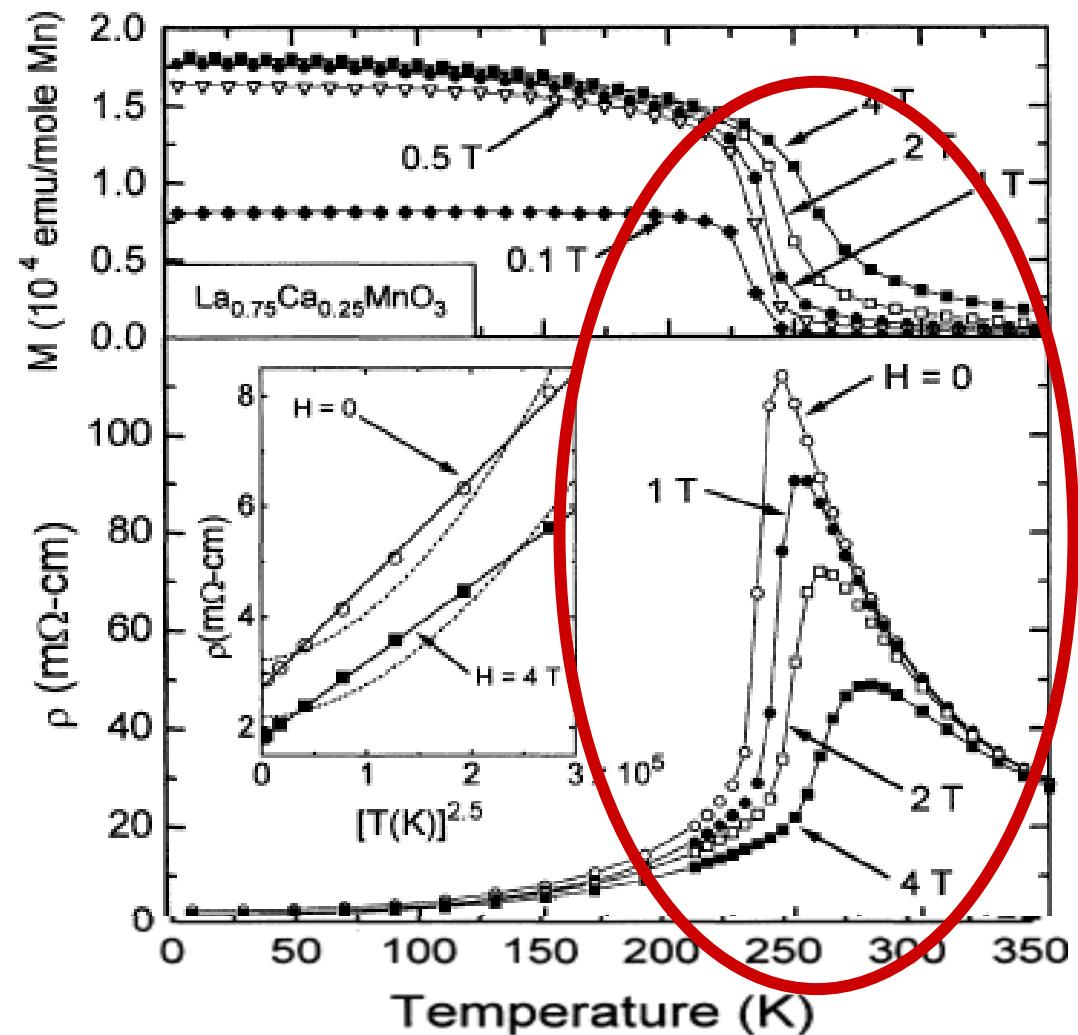
# Temperature dependence of resistivity in various magnetic fields in (Ga,Mn)As



Reminiscent to CMR oxides

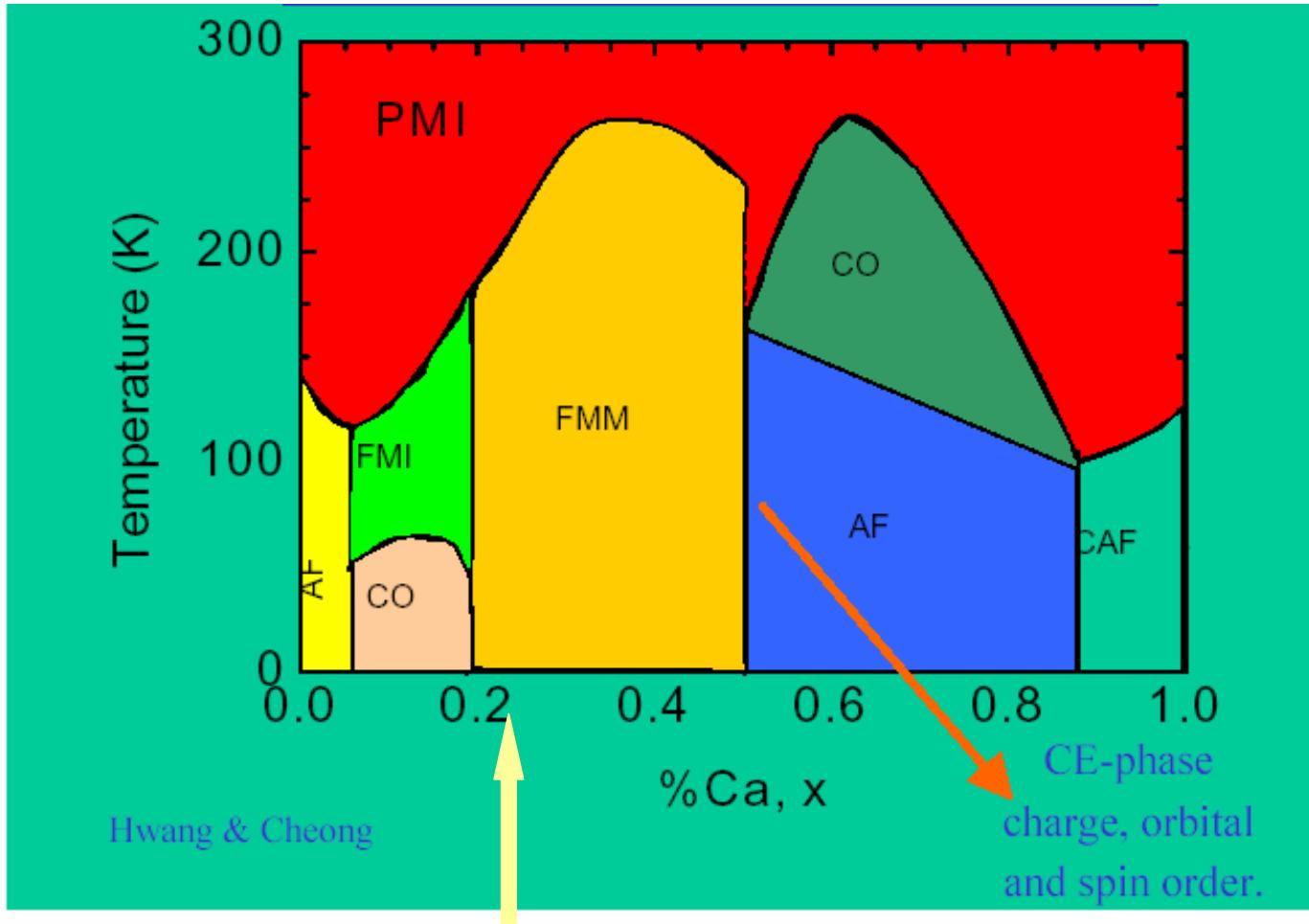
F. Matsukura et al., PRB'98

# Magnetization and resistivity in (La,Ca)MnO<sub>3</sub>



P. Schiffer et al. (PSU), PRL'95

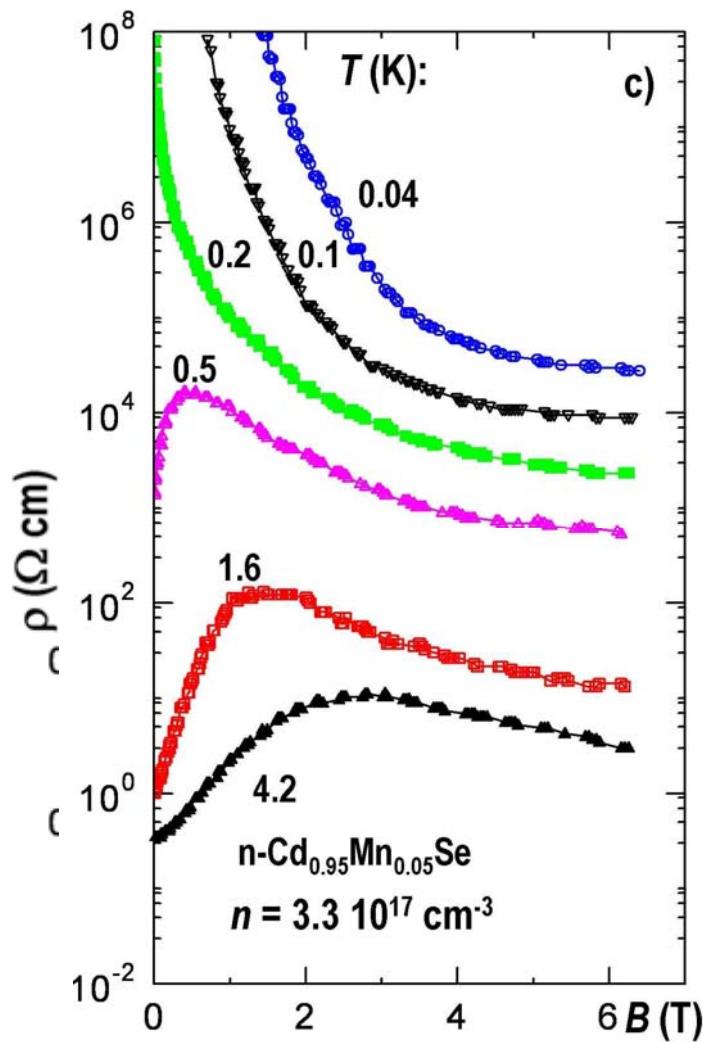
# Phase diagram of $\text{La}_{1-x}\text{Ca}_x\text{MnO}_3$



Hwang & Cheong

**CMR near MIT**

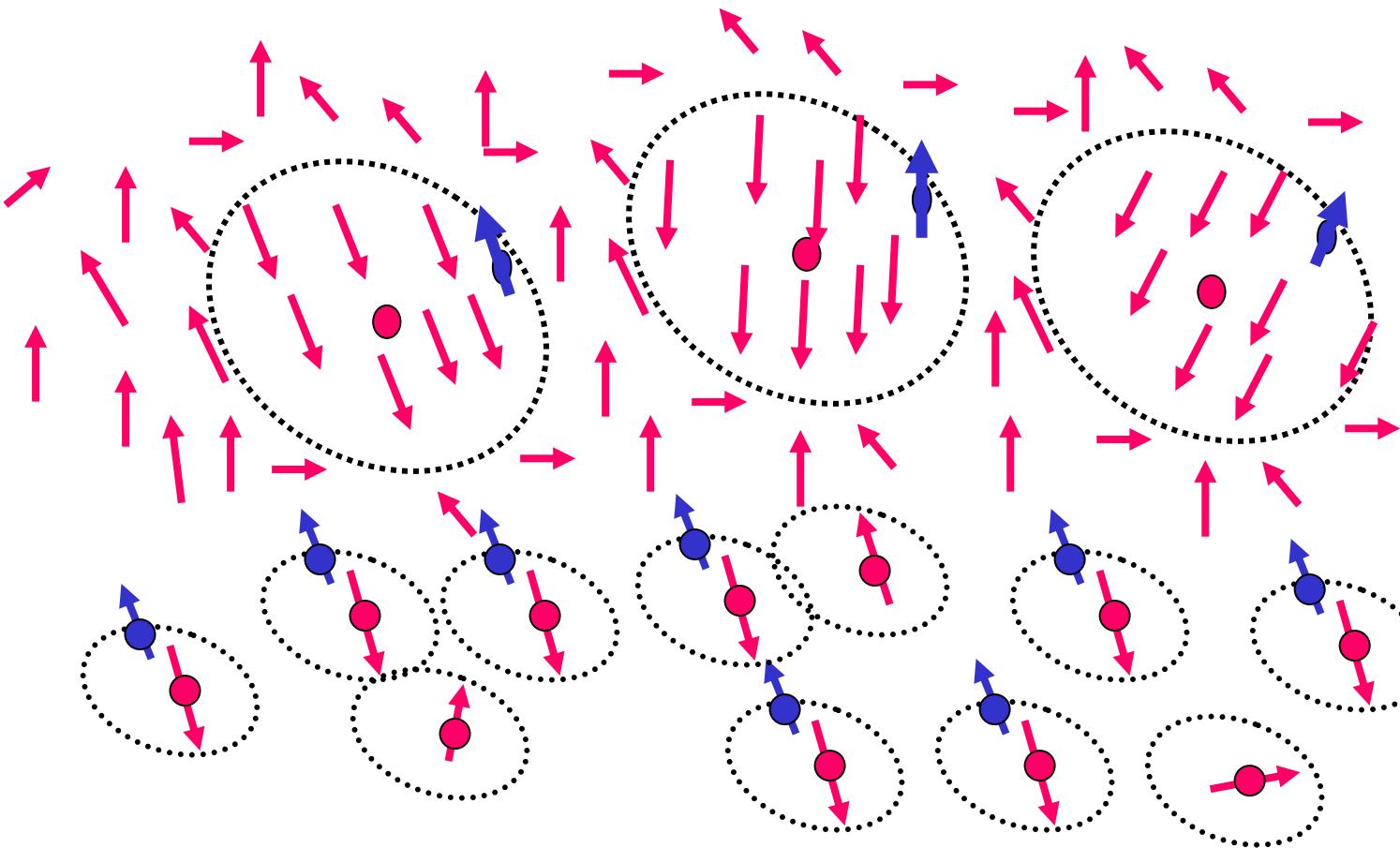
# CMR in n-(Cd,Mn)Se



# Possible model: enhancement of localization by bound magnetic polaron formation

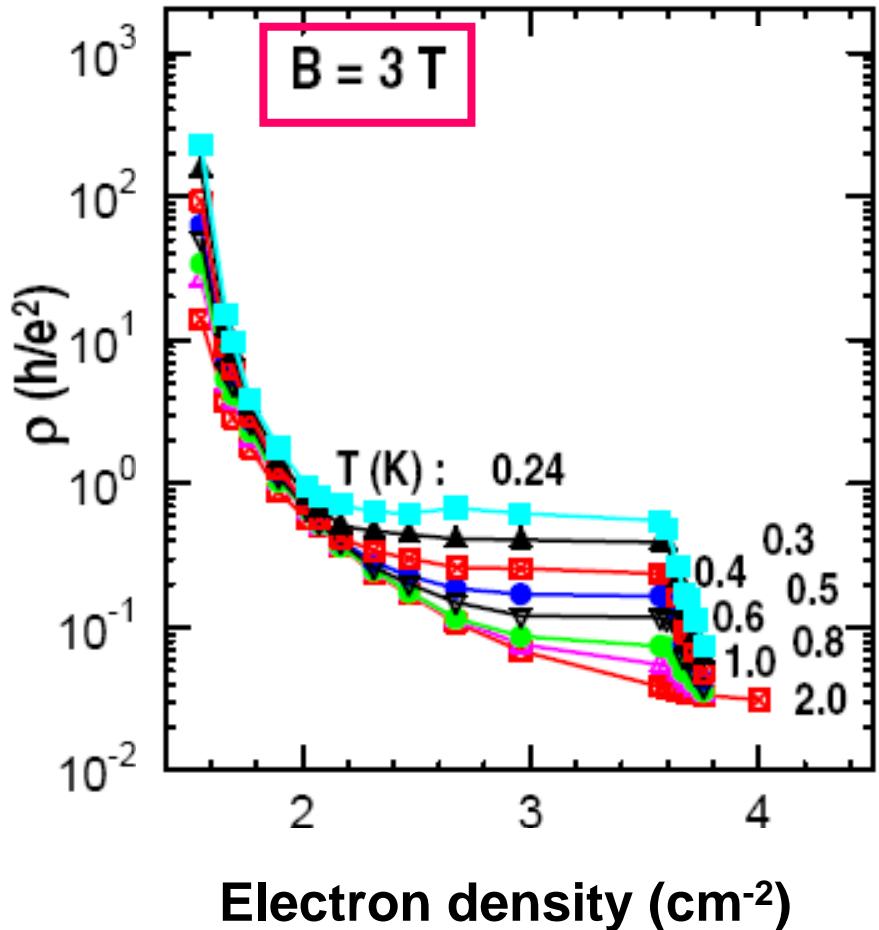
**p-type  
(II,Mn)VI**

**(III,Mn)V**



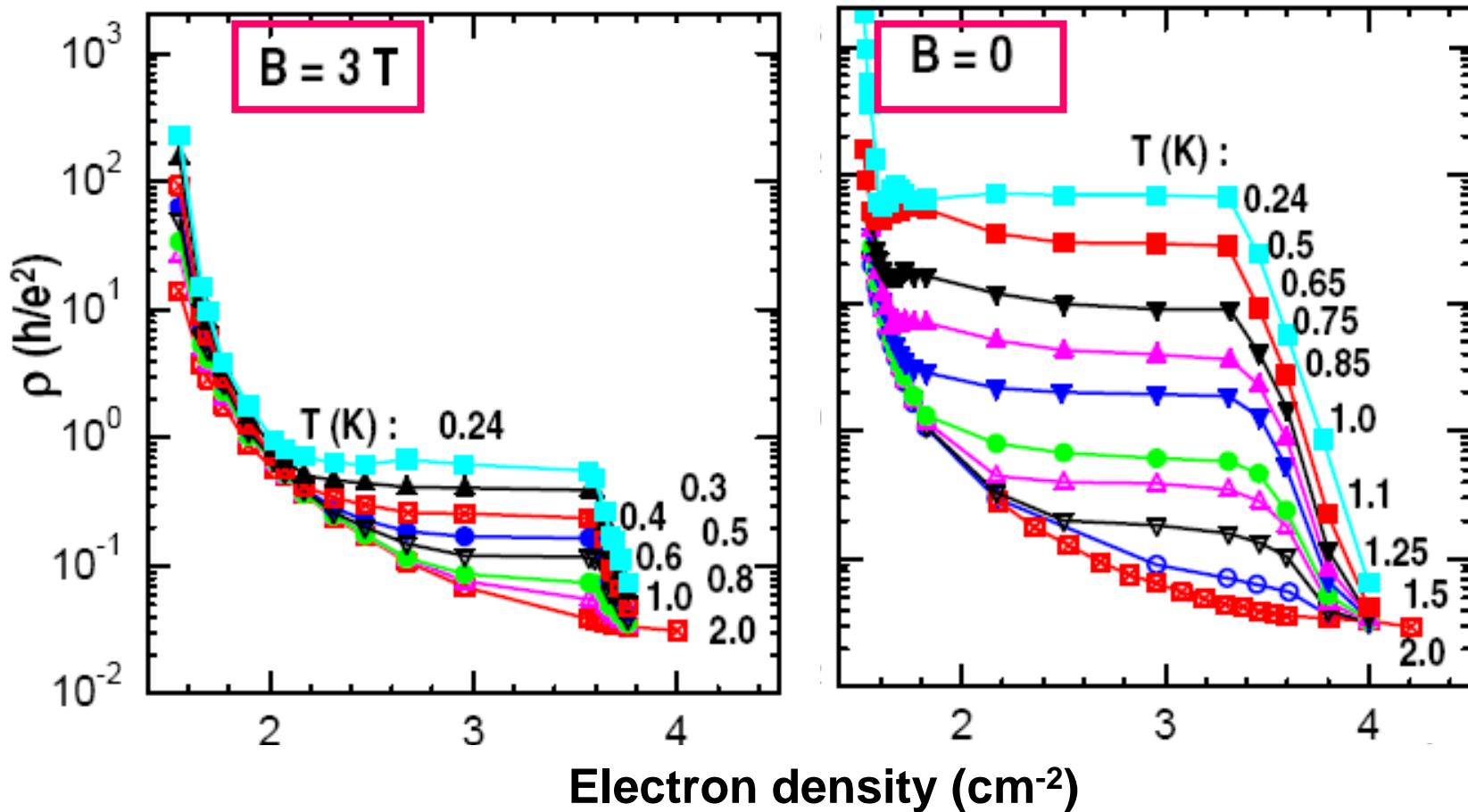
BMP binding energy  $\sim \chi(T)$

# Resistivity vs. carrier density at various $T$ in (Cd,Mn)Te/(Cd,Mg)Te:I quantum well



*J. Jaroszynski , TD et al.  
(Warsaw, NHMFL) PRB'07*

# Resistivity vs. carrier density at various $T$ in (Cd,Mn)Te/(Cd,Mg)Te:I quantum well

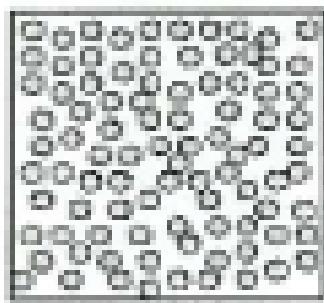


no BMP but critical  
scattering and CMR!

*J. Jaroszynski , TD et al.  
(Warsaw, NHMFL) PRB'07*

# Pictorial representation of states near MIT

strong disorder

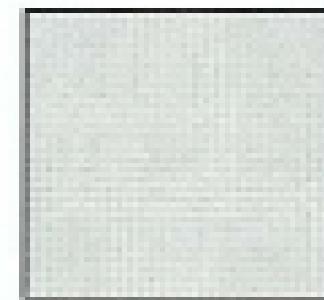


no disorder

Insulator

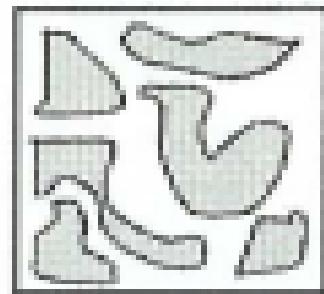


metal



or

compromise



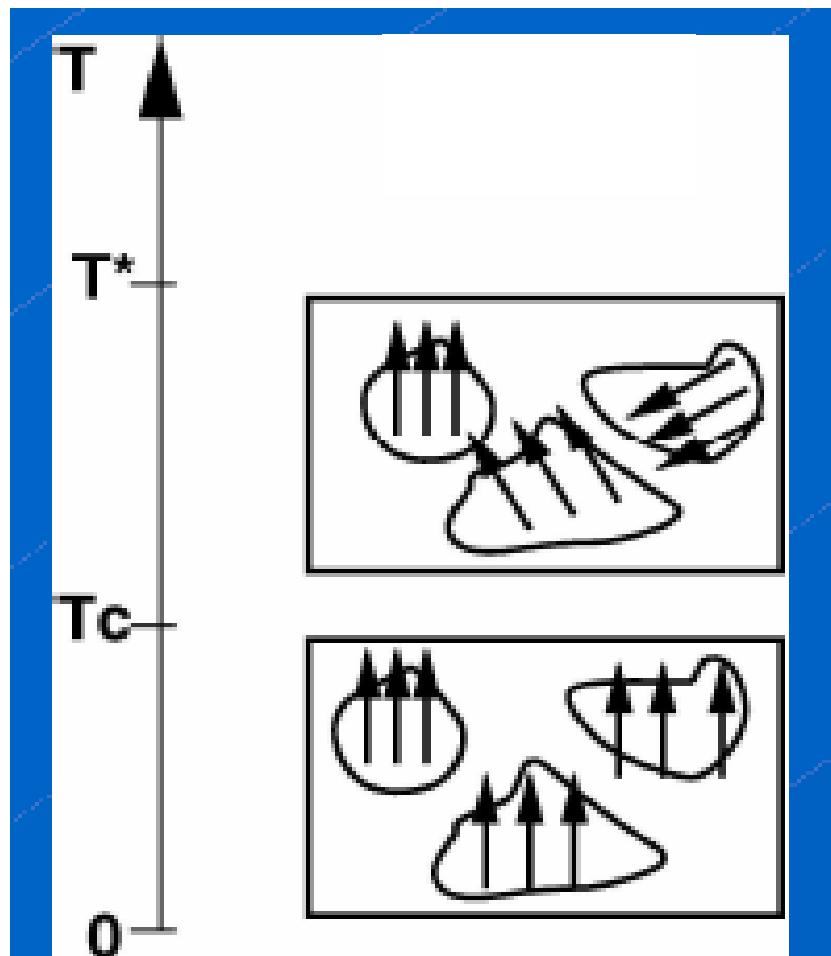
large clusters.  
equal density.  
disorder-induced  
phase separation

*cf. A. Moreo et al.  
Science'99  
Nagaev'85*

white = para    grey = ferro (mesoscopic scale)

# Nanoscale electronic phase separation

$T_C > 0$  in  
p-type DMS  
 $T_C \approx 0$  in  
n-type DMS



strong-spin  
dependent  
scattering  
and CMR

# SUMMARY

Quantum effects essential at the Anderson-Mott transition

Leads to:

- Coulomb anomaly of DOS at  $E_F$
- specific dependence  $\sigma(T,H)$
- nanoscale phase separation into para and ferro regions
  - colossal negative magnetoresistance
  - much enhanced critical scattering

END