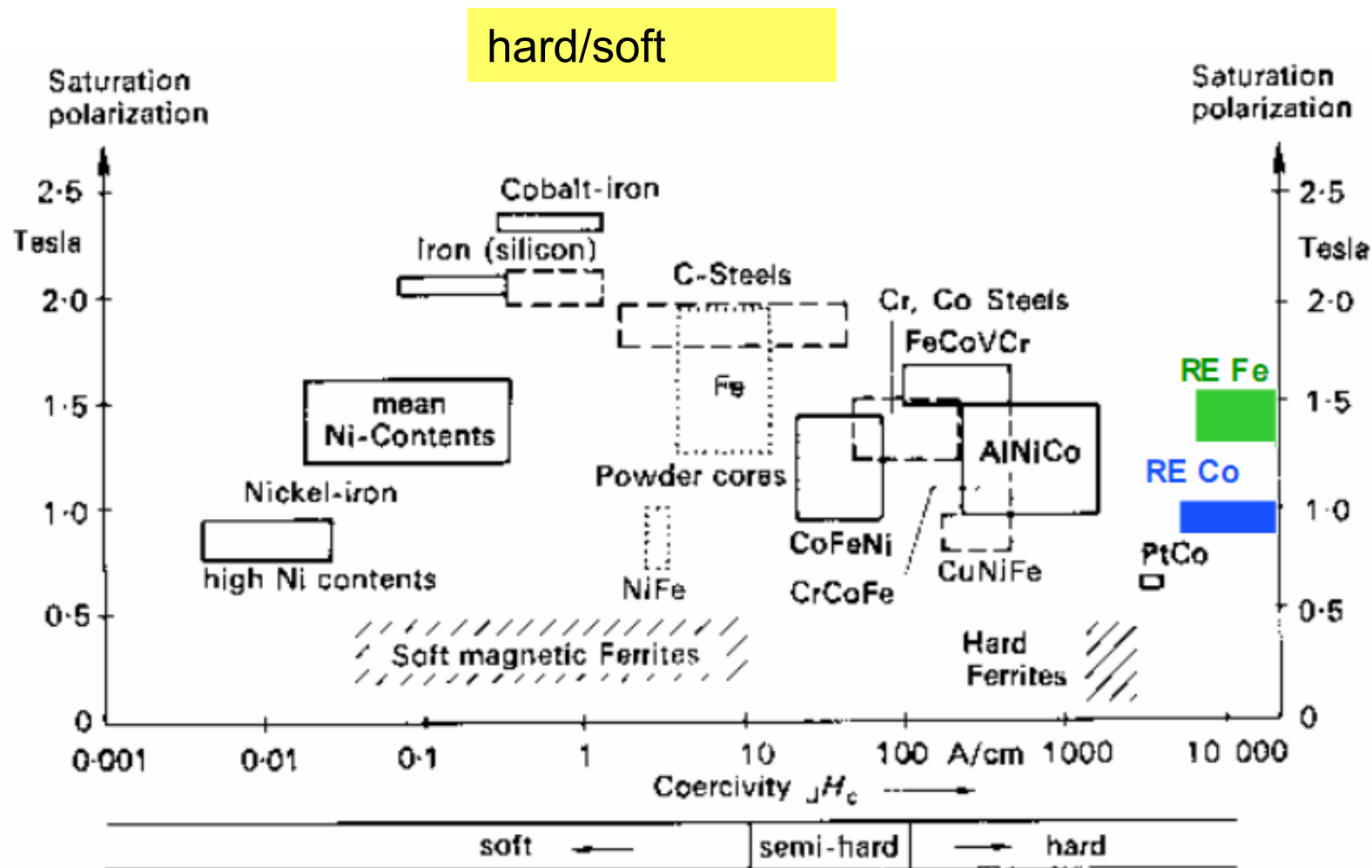


APPLICATIONS OF HIGH ENERGY DENSITY PERMANENT MAGNETS

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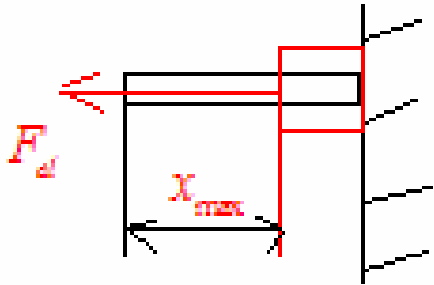
Magnetic Materials



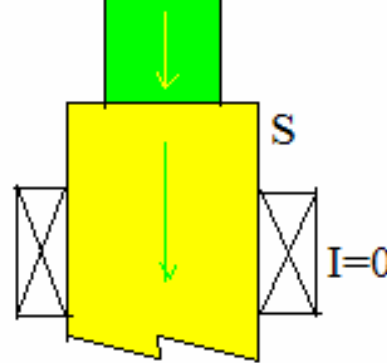
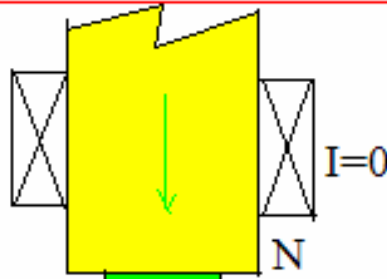
R. Boll, „Soft Magnetic Materials“, Siemens AG, Hyden & Son, 1977

How works a PM?

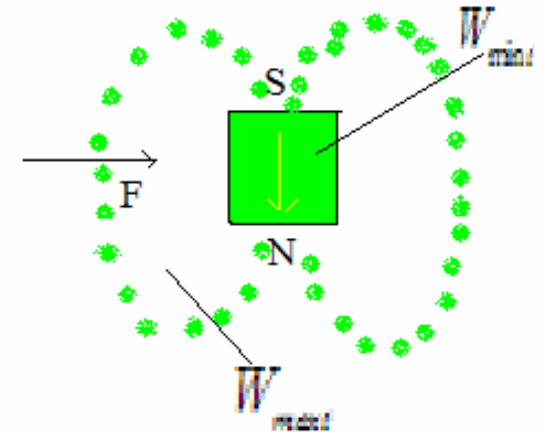
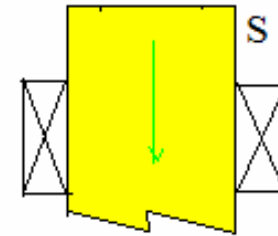
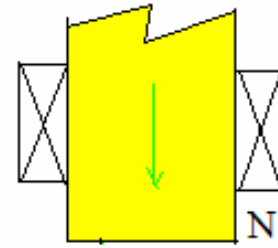
$$W = \int F_{el} dx = -\frac{1}{2} kx_{\max}^2 = -W_{ext F}$$



elastic spring



$$W_m = 0 (H_m = 0)$$



$$W_{\min t} = \frac{1}{2} B_m H_m V_m = -\frac{1}{2} B_m |H_m| V_m = -W_{mext}$$

$$W_{mext} = \int_{\infty=m}^{final} BH dv = \int_{initial} F dl$$

The highest loading energy of a PM

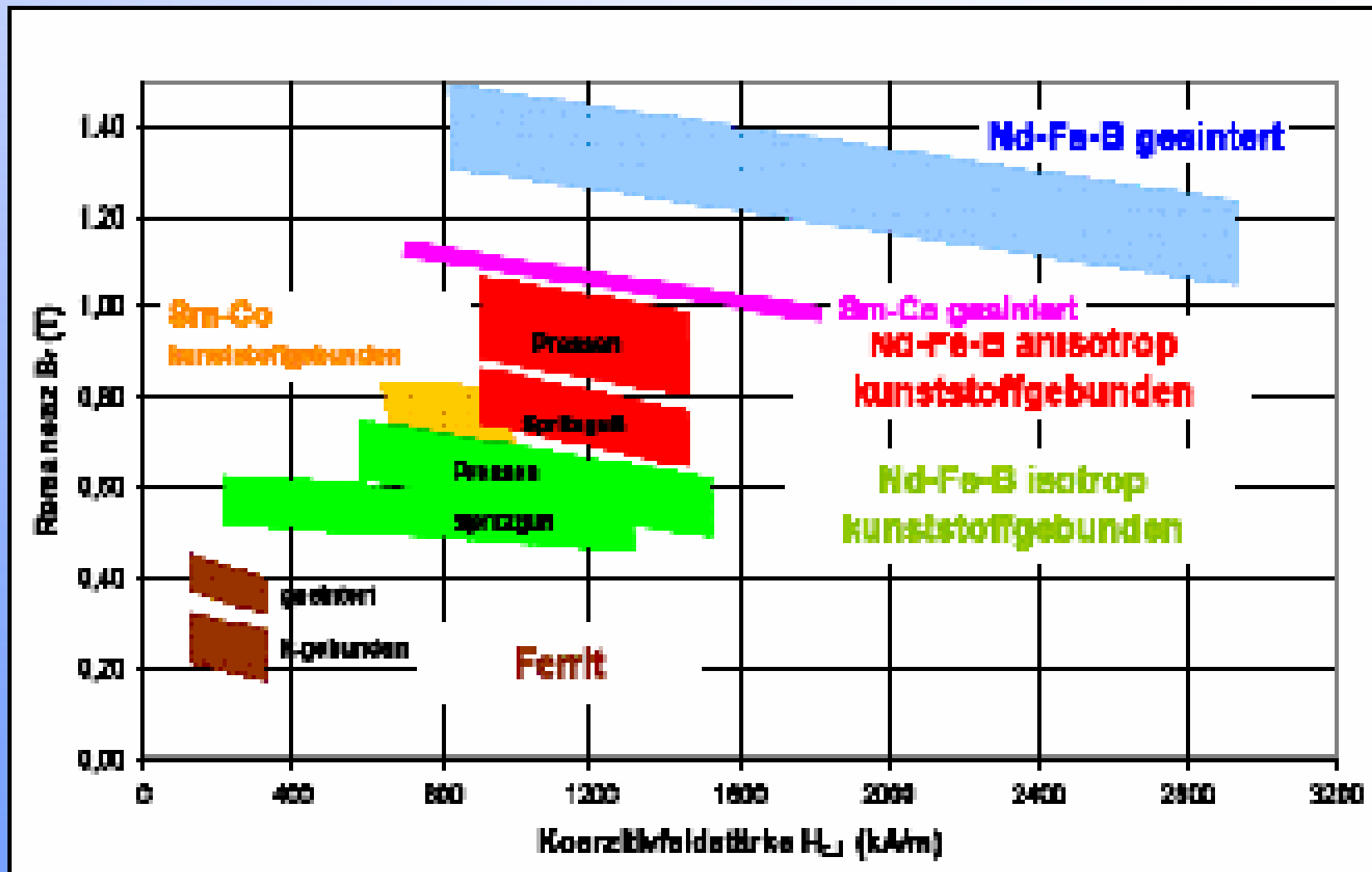
$$\max(W_{\min t}) = \frac{1}{2} (B H)_{\max} V_m$$

Example: for NdFeB-PM with

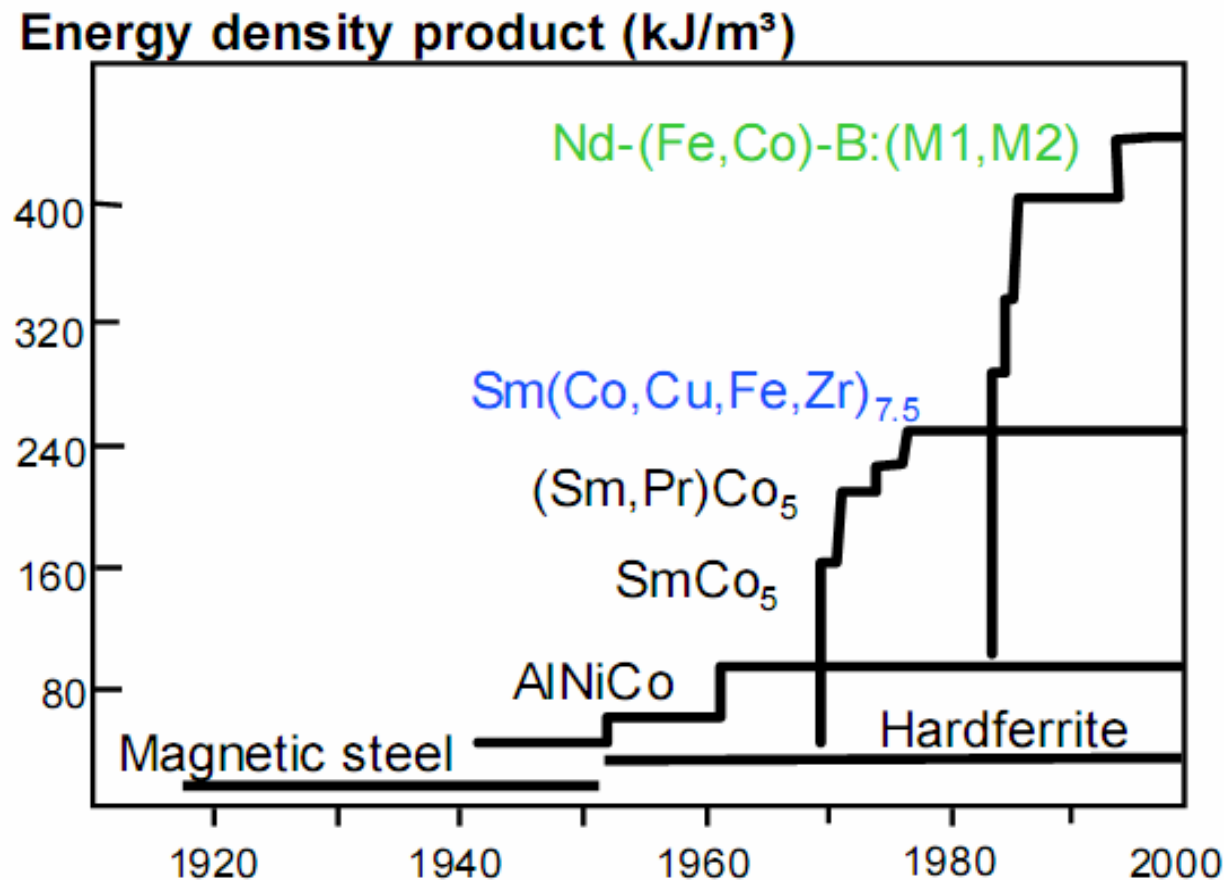
$$\max (W_{\min t}) / mass = 50 J / kg$$

Comparison: car battery 12V / 60Ah $w_{el} = 10^4 J / kg$

Manufactured PM



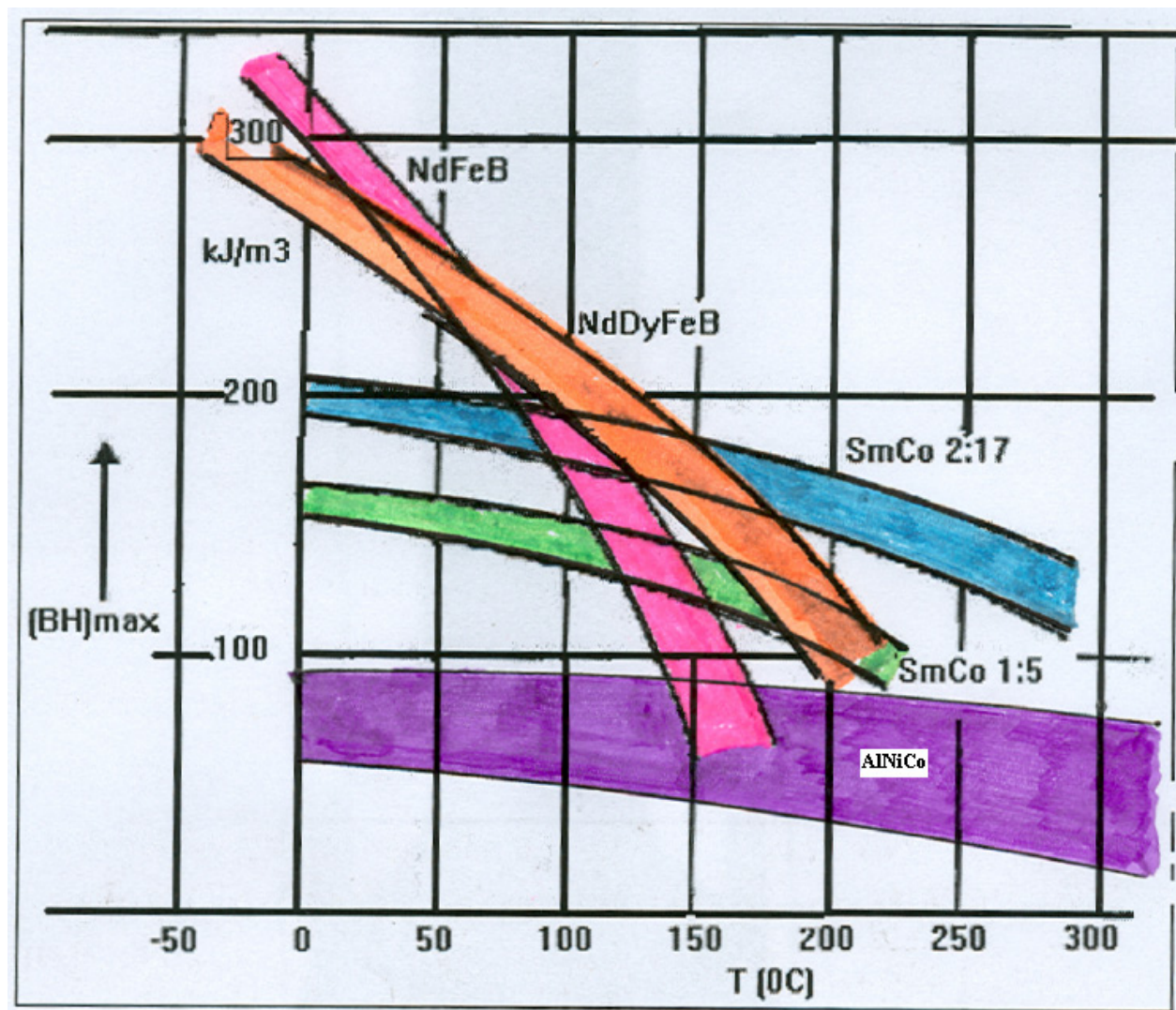
High energy permanent magnets



Magnet	Year	JH_c (kA/m)	T_c (°C)
Magn. steel	1890	1	
AlNiCo	1955	100	850
Hardferrite	1960	200	450
Sm-Co 1:5	1975	3000	720
Sm-Co 2:17	1982	2000	820
Nd-Fe-B	1990	1500	310

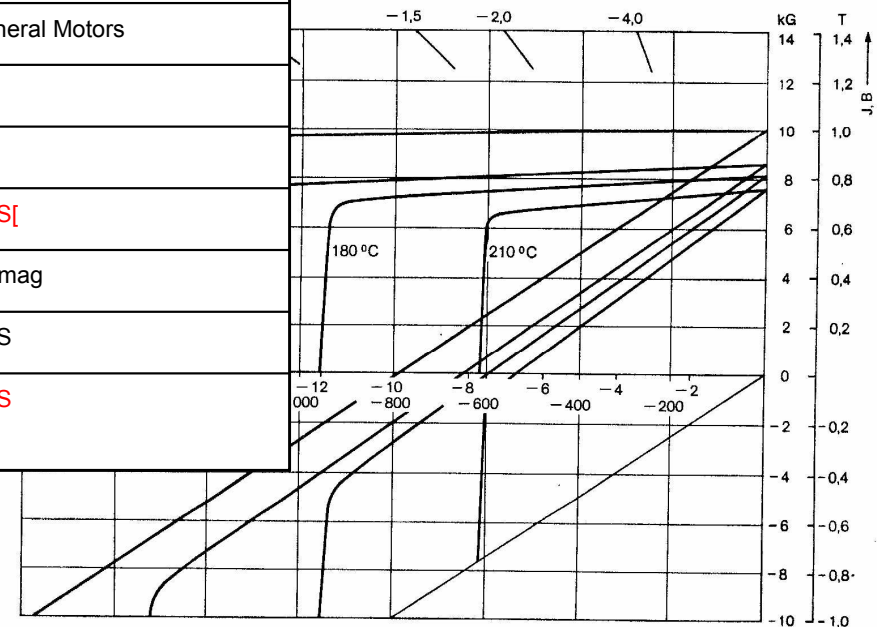
magnet.atp.tuwien.ac.at

Working at high temperature



Working temperature

Properties of some Re-TM permanent magnets						
Permanent magnet	$(BH)_{\max}$ (kJ/m ³)	B_r (T)	jH_c (kA/m)	Manufac-turing method	Highest working Temp. (°C)	Producer
NdFeB	390	1.40	875	sintering	80	Shin Etsu
NdFeB	263	1.17	2387	sintering	180	Shin Etsu
NdFeB	190	1.00	3260	sintering	210	Vacuumschmelze
NdFeB/MQI	64	0.61	1200	bonded	125	General Motors
NdFeB-MQII	112	0,80	1600	densified	200	GM
NdFeB-MQIII	360	1.37	1120	hot worked	150	GM
NdFeB	240	1.11	2800	sintering	220	MFS[
SmGdCo ₅	80	0.64	2400	sintering	250	Ugimag
SmCos	170	0.93	2000	sintering	250	MFS
Sm ₂ Co ₁₇	215	1.06	2000	sintering	350	MFS



Typical demagnetization curves $B(H)$ and $J(H)$ of VACODYM 411 WZ at different temperatures

Working at high temperatures

Linear approximation: $(BH)_{\max} = (BH)_{\max o} [1 + \alpha_{BH} (T - T_o)]$

Where: $\alpha_{BH} = \alpha_I + \alpha_H$ Two PM at T_e : $(BH)_{\max 1} = (BH)_{\max 2}$

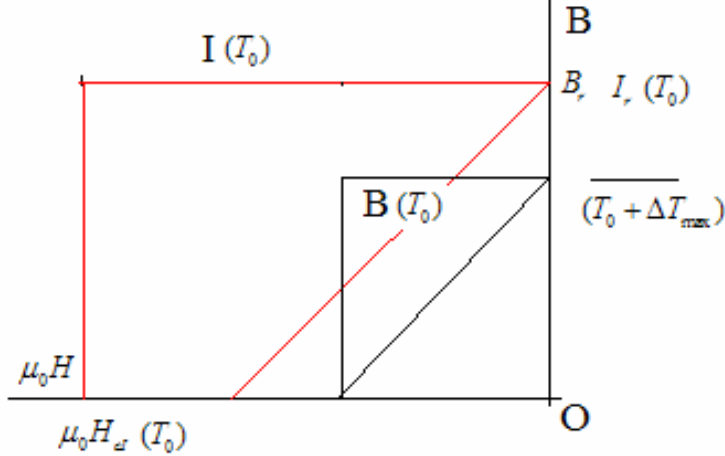
$$\text{at } \Delta T_e = \frac{1 - k_{12}}{k_{12} \alpha_{BH1} - \alpha_{BH2}}, \quad k_{12} = (BH)_{\max 1 o} / (BH)_{\max 2 o}$$

Exemple Alnico IUNDK8AA, $(BH)_{\max 1} = 100 \text{ kJ} / \text{m}^3$, $\alpha_{BH1} = -0.04\% / K$

NdFeB $(BH)_{\max 2} = 300 \text{ kJ} / \text{m}^3$, $\alpha_{BH2} = -0.70\% / K$

$$\Rightarrow \Delta T_e = 100^\circ C$$

Working at high temperatures



$$H_{cl} \mu_o \gg I_r$$

We define $T_{\max}$: $H_{cl} \mu_o = I_r$ from which: $\Delta T_{\max} = \frac{1-k}{k\alpha_I - \alpha_H}$, $k = I_{ro} / \mu_o H_{clo}$

$$k \rightarrow 0 \Rightarrow \Delta T_{\max} \rightarrow -1 / \alpha_H \quad (1 / 0.005 K^{-1} = 200 K)$$

$$k \rightarrow 1 \Rightarrow \Delta T_{\max} \rightarrow 0$$

$$\Rightarrow \Delta T_{\max} = 200 K)$$

If $k_1 > k_2 \Rightarrow \Delta T_{\max 1} / \Delta T_{\max 2} < 1$ That means

For two PM having the same coercivity, the highest working temperature has the PM with the lower remanence (sintered /bonded)

PM worldwide

$$\text{Energy} / \text{mass} = (BH)_{\max} / \rho$$

$$\text{Energy} / \text{cost} = (BH)_{\max} / \rho : \text{cost} / \text{kg}$$

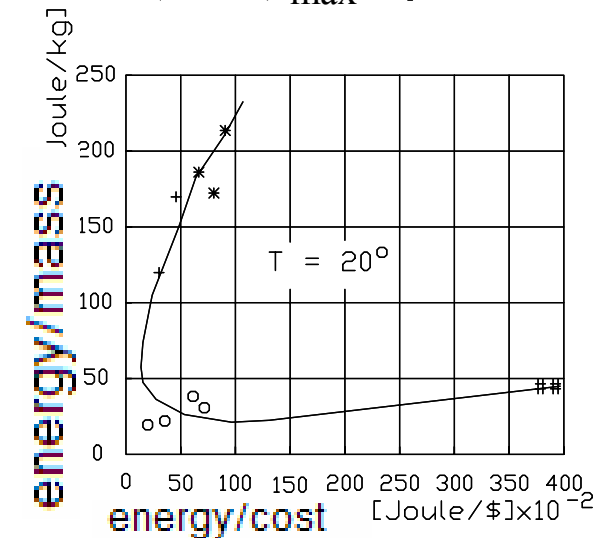
Output of PM in 2004

Country / Area	Alnico (ktons)	Hard ferrite (ktons)	NdFeB (ktons)
China	3.5 (56 %)	S = 360 (51 %) B = 50 (32 %) T = 400 (47 %)	S = 23 (76 %) B = 1.4 (35 %) T = 24 (71 %)
Japan	0.3 (5 %)	S = 196 (28 %) B = 13 (8 %) T = 209 (25 %)	S = 7 (23 %) B = 0.6 (15 %) T = 7.6 (22 %)
USA	0.7 (11 %)	S = 39 (5 %) B = 40 (26 %) T = 79 (9 %)	S = - B = 0.2 (5 %) T = 0.2 (1 %)
Europe	0.8 (12 %)	S = 47 (7 %) B = 42 (27 %) T = 89 (11 %)	S = 0.4 (1 %) B = 0.3 (9 %) T = 0.7 (2 %)
Others	1 (16 %)	S = 60 (9 %) B = 11 (7 %) T = 71 (8 %)	S = - B = 1.4 (36 %) T = 1.4 (4 %)
Total	6.3 (100 %)	S = 692 (100 %) B = 156 (100 %) T = 848 (100 %)	S = 30 (100 %) B = 3.8 (100 %) T = 34 (100 %)

S – sintered

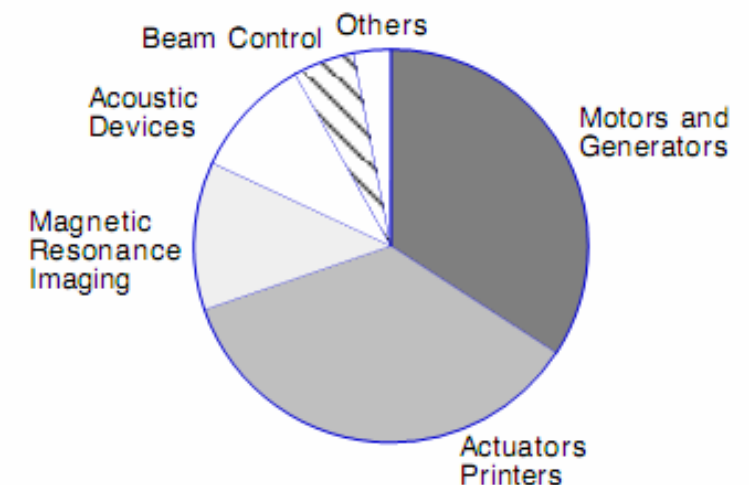
B – bonded

T - total



+ - PRCo; * - NdFeB; # - Ferrite; o - Alnico

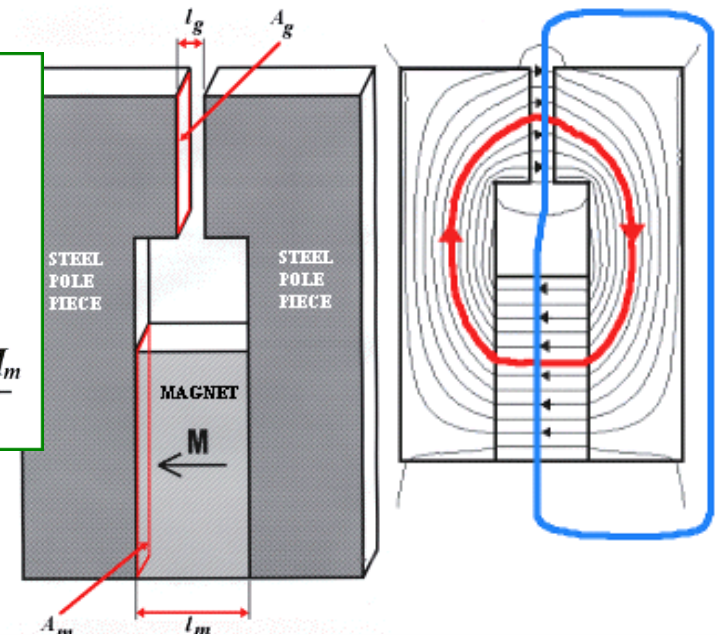
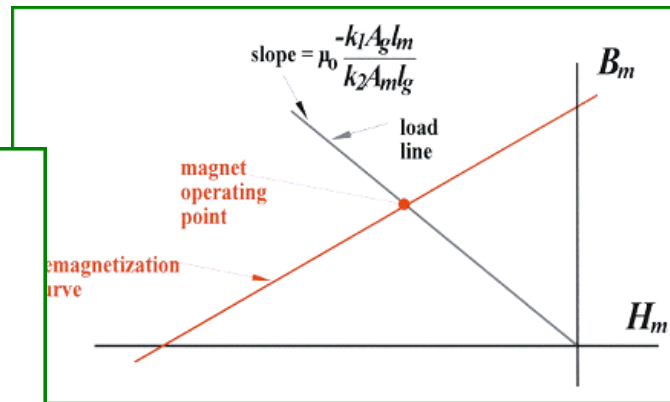
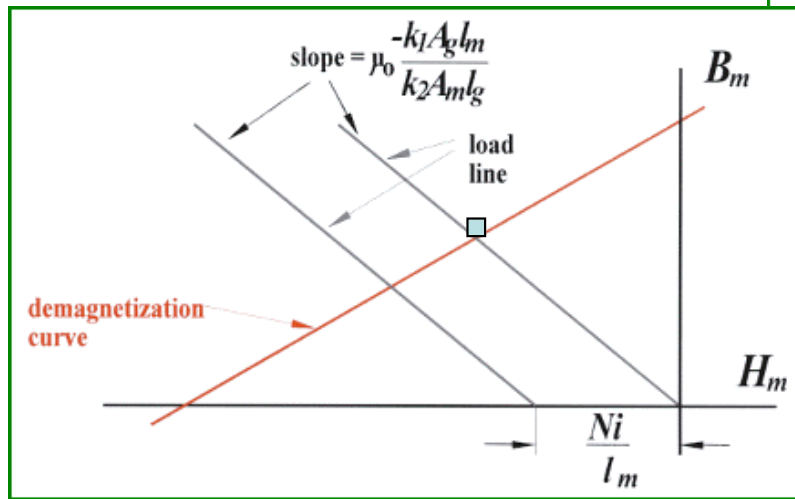
US \$ 11.5 Billion
in 2000



PM worldwide

	B_r	H_c	T_c	BH_{max}	Rel. cost	Row material basis
W-steel	10	0.07	1000	0.31	10	critically(W)
Co-Steel	9	0.2	1200	1.0	20	critically(Co)
Alnico 5	12	0.5	850	5.0	15	critically(Co)
Ticonal	11.8	1.3	850	11	30	
Ba-Ferrite	3.9	1.8	450	3.5	5	very good
Sr-Ferrite	3.6	3.6	450	4.2	8	
SmCo ₅	11.6	26	700	27	100	critically(Co)
Sm ₂ Co ₁₇	11	14	800	32	90	limited(Sm)
Nd ₂ Fe ₁₄ B	14.1	13.5	300	48	65	good
Sm ₂ Fe ₁₇ N	6.8	12	550	12	75	limited(Sm)
FePt	12.3	5	750	9	200	critically(Pt)
CoPt	10.3	6	720	10.4	250	critically(Pt, Co)

Load line



For a PM

$$\frac{B_m}{\mu_0 H_m} = \frac{H_0 + M(1-N)}{H_0 - NM} \xrightarrow{H_0 \rightarrow 0} -\frac{1-N}{N} = -S$$

For the circuit

$$H_m l_m + \int_{\text{circuit}-m} H dl = H_m l_m + \Phi \int \frac{dl}{\mu A} = 0,$$

$$\int_{\text{circuit}-m} \frac{dl}{\mu A} = \frac{1}{\Lambda_c} \quad \Lambda_c \equiv \text{permeance}$$

$$S = \frac{k_1 A_g}{l_g} / \frac{k_2 A_m}{l_m} = \Lambda_c / \Lambda_m = \lambda \quad (\text{unit permeance})$$

$$\oint \mathbf{B} \cdot d\mathbf{A} = 0$$

$$\oint \mathbf{H} \cdot d\mathbf{l} = I$$

circuit

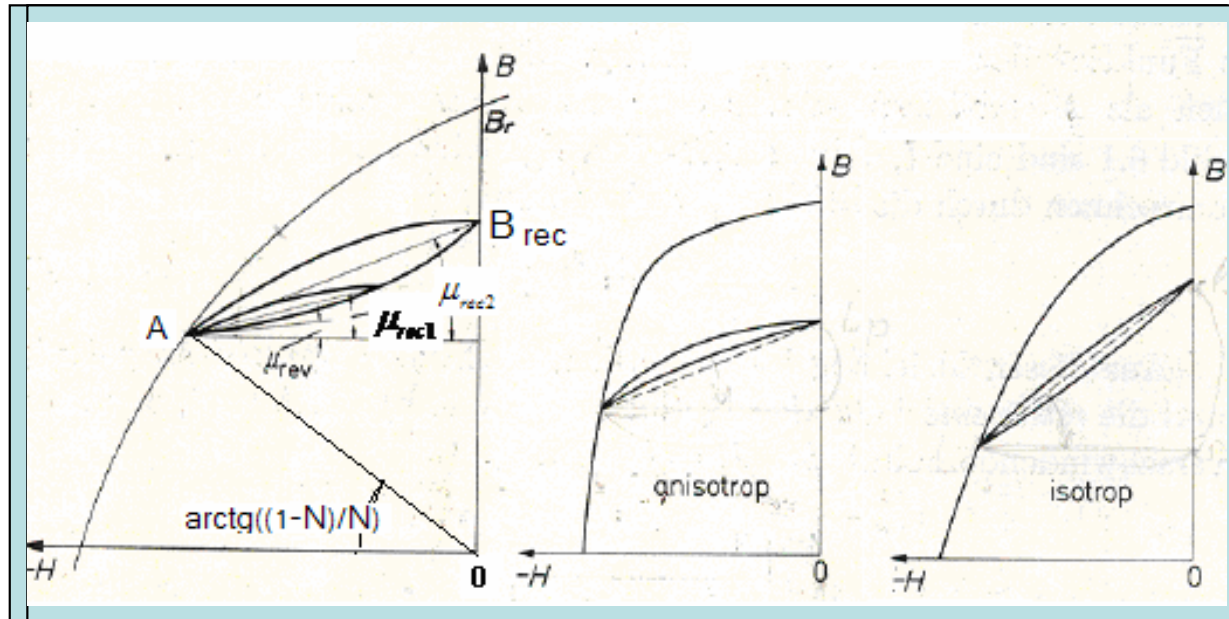
$$B_m A_m - k_1 B_g A_g = 0$$

$$H_m l_m + k_2 H_g l_g = 0$$

$$B_m = \frac{k_1 B_g A_g}{A_m} ; \quad H_m = \frac{-k_2 H_g l_g}{l_m}$$

$$\frac{B_m}{H_m} = -\mu_0 \frac{k_1 A_g l_m}{k_2 A_m l_g} = -\mu_0 S$$

Recoil line/minor hysteresis loop



Equation of the recoil line: $B_m = \mu_o (\mu_{rec} H_m + M_r)$

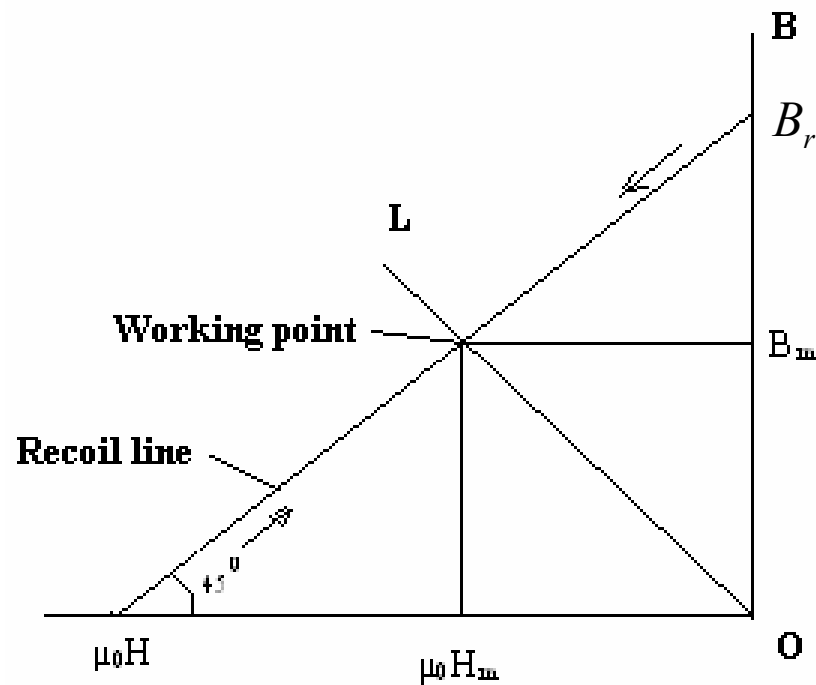
N – demagnetization factor of the PM

Ideal Permanent magnet

$$B_m = \mu_0 (\mu_{rec} H_m + M_r)$$

$$\mu_{rec} = 1 \rightarrow B_m = \mu_0 (H_m + M_r)$$

(main demagnetisation curve)

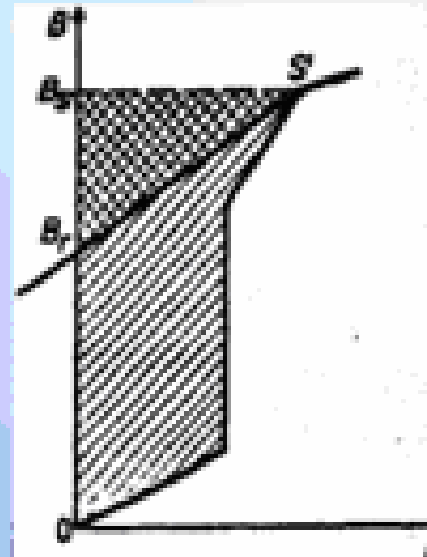
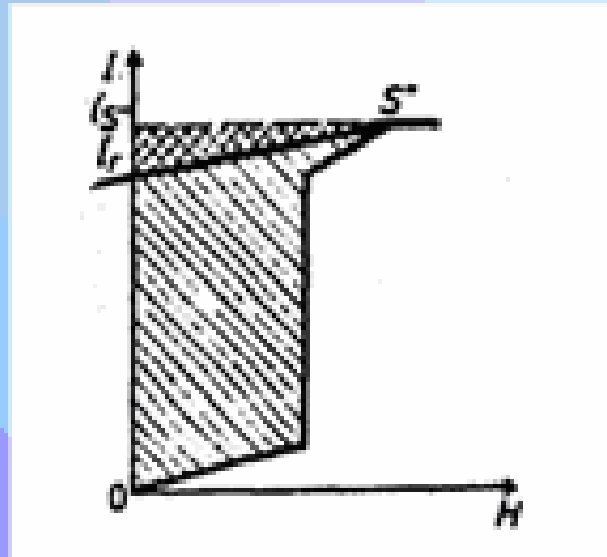


An ideal permanent magnet :

no irreversibil losses until Hd= intrinsic coercivity!

$$(BH)_{\max} = (B_r)^2 / (4\mu_0)$$

Energy Relations in PM



$$AM = AH + AI$$

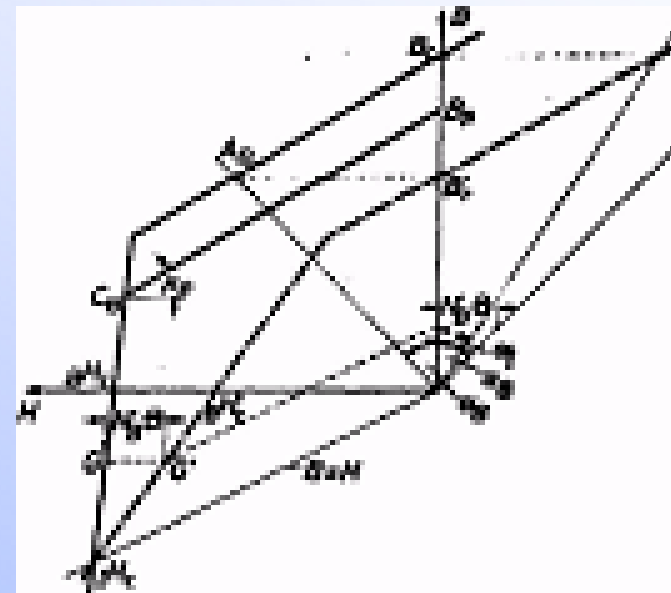
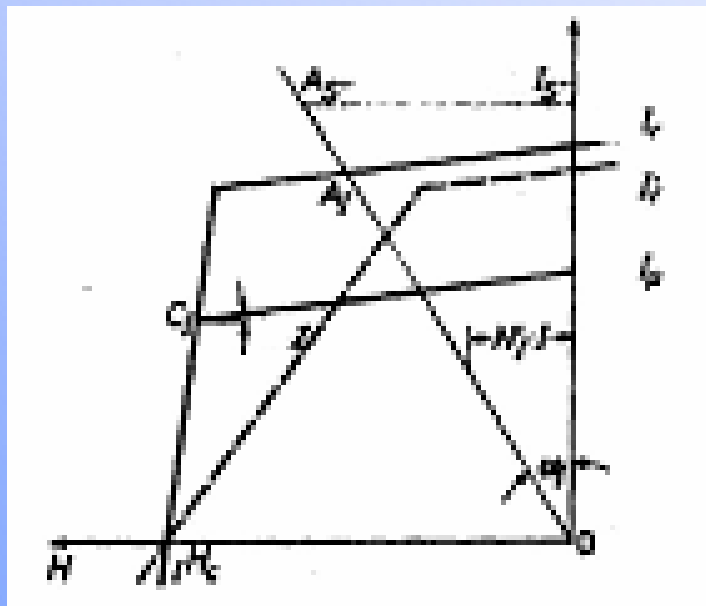
AH = the work done by the field

AI = Surface $(OS'S')$ = the real work necessary to magnetize at saturation the PM

AM = Surface $(OS'SS')$ = the total work to magnetize the PM

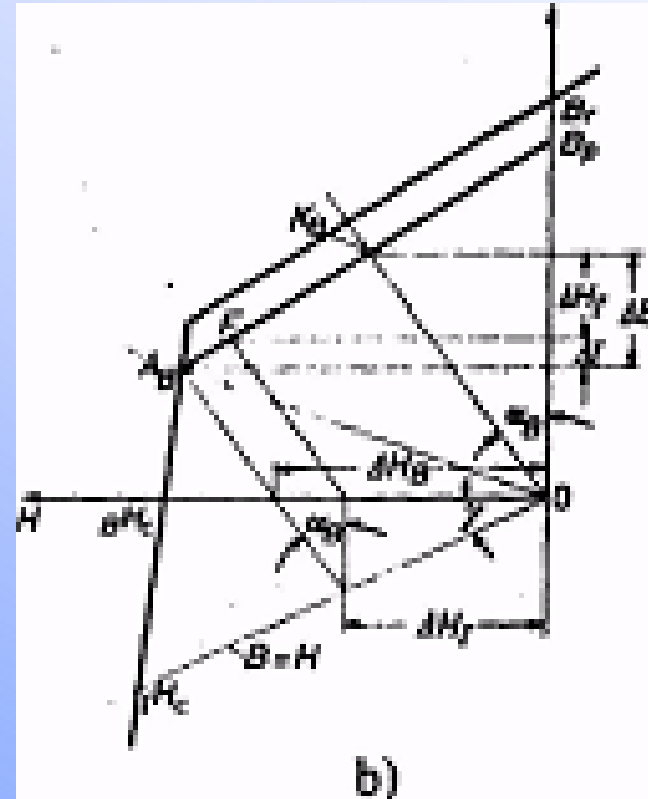
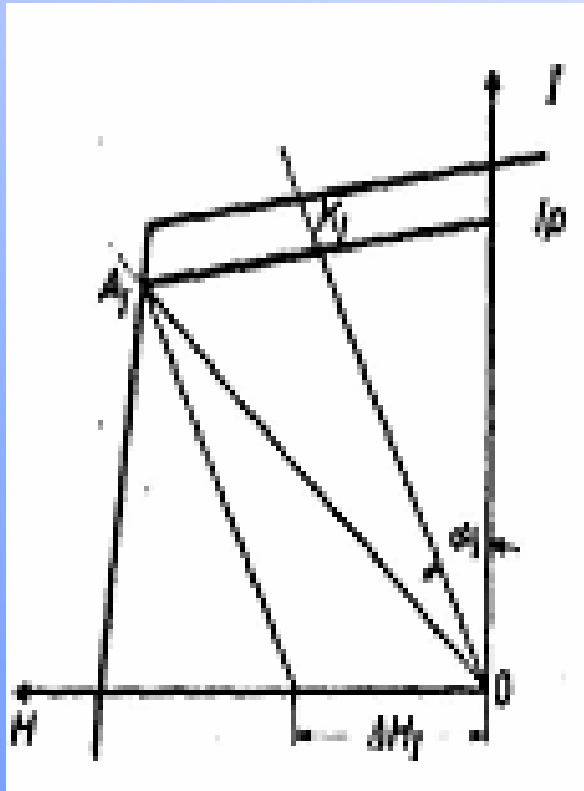
After removing of the magnetizing field, the working point of the permanent magnet moves to I_r resp. B_r .
The energy density $S'I'I'S''$ and $S'B'S'B_r$ send back to the current supply by the permanent magnet alone resp. permanent magnet together with the magnetic field.

The circuit is Open



When we open the magnetising circuit, the working point of the permanent magnet moves, done by the shearing introduced by the demagnetizing field of the whole circuit to the points A_1 resp A_2 in the second quadrant of the hysteresis loop

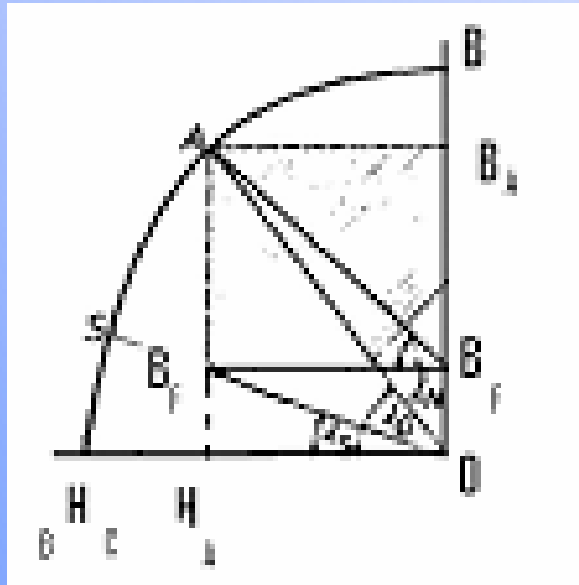
Action of demagnetising fields



-if the permanent magnet has the working point K / resp K_B , than a demagnetizing field of H brings the working point at A and if the field is cancelled, then the working point will go back to K .

if the demagnetization field $H_d > H_c$ then after removing of the demagnetization field, the working point will be, on the load line OK_1 , but below K_1 (irreversible losses).

PM magnetised in the circuit



$$\mathcal{B}AHAV_m = (\mathcal{B}_A - \mathcal{B}_F)HA + \mathcal{B}_FHA$$

. In the outer space of the PM,
the energy $\mathcal{B}AHAV_m$ (V_m The
volume of the PM) is stored

(always equal and with an opposite
sign with the energy inside the magnet, because $\int \mathcal{B}d\mathcal{H} = 0$),

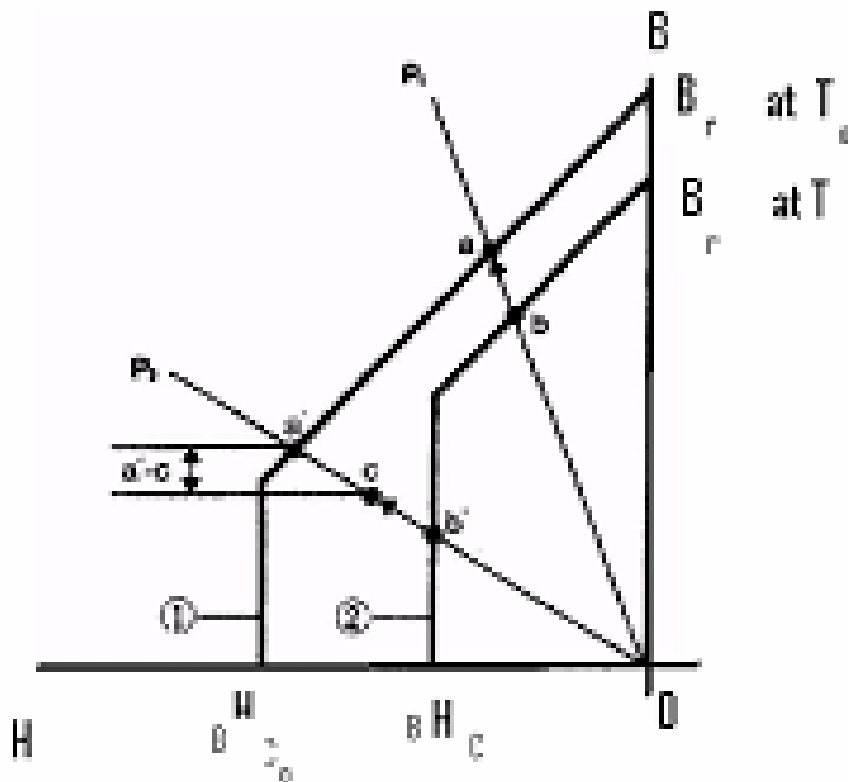
composed from the useful energy in the air gap,

proportional (up to a factor 2) to $(\mathcal{B}_A - \mathcal{B}_F)HA$

$$\lambda_G = \lambda_N + \lambda_S$$

and the leakage energy $\mathcal{B}_FHA$

Magnetic temperature losses

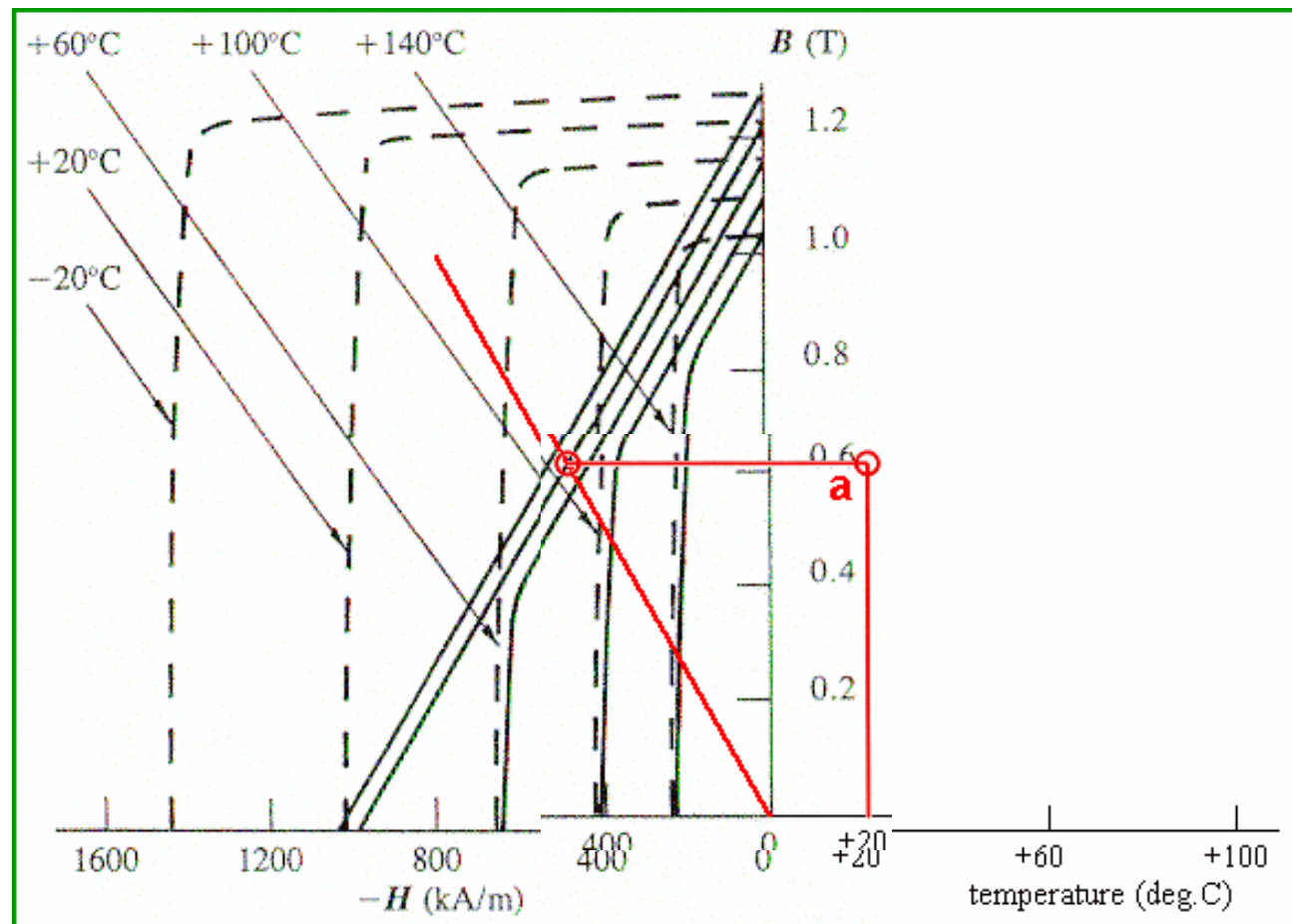


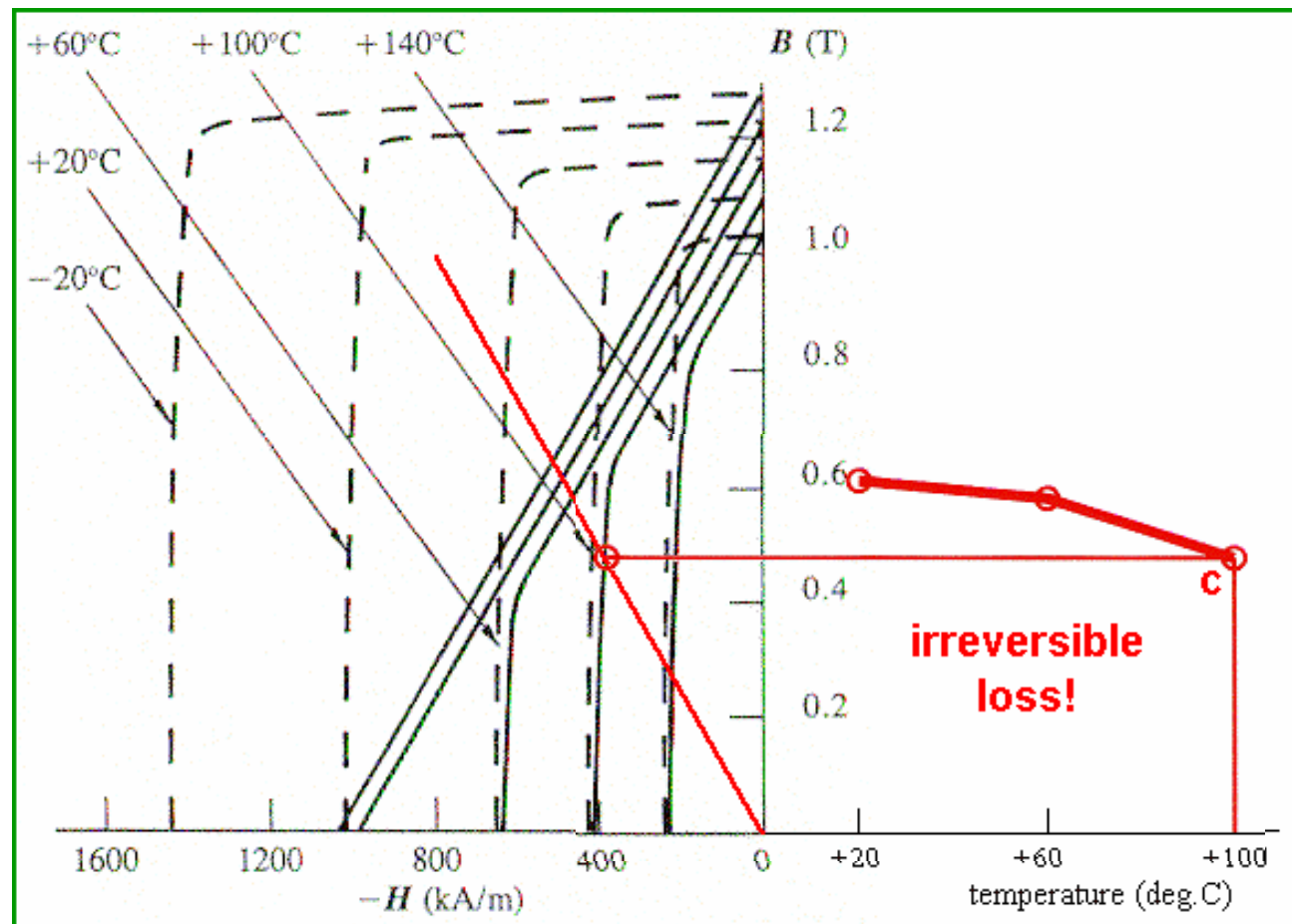
$$H_c = H_{c0} (1 + \alpha_H (T - T_0)), \alpha_H < 0$$

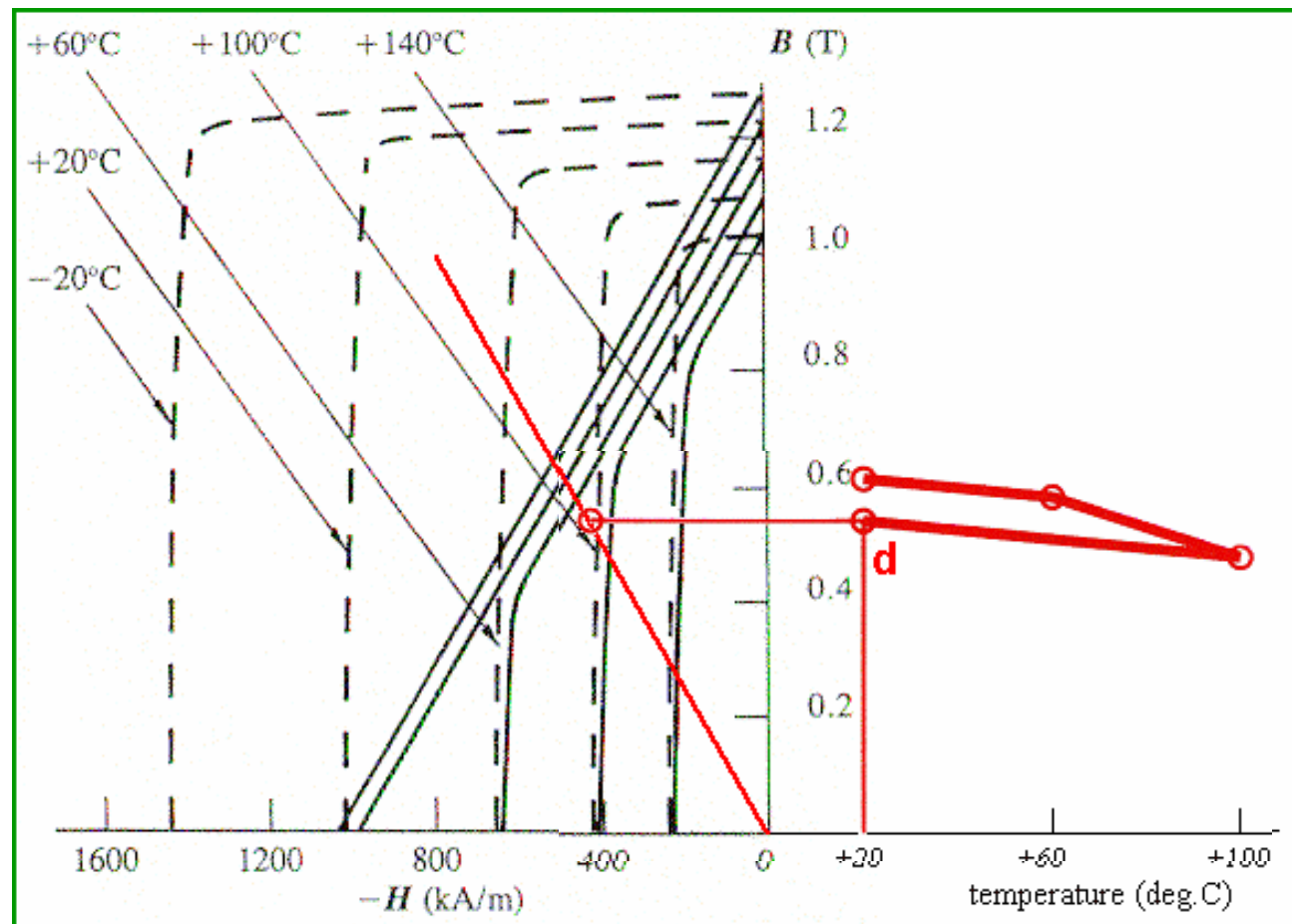
$$I = I_0 (1 + \alpha_I (T - T_0)), \alpha_I < 0$$

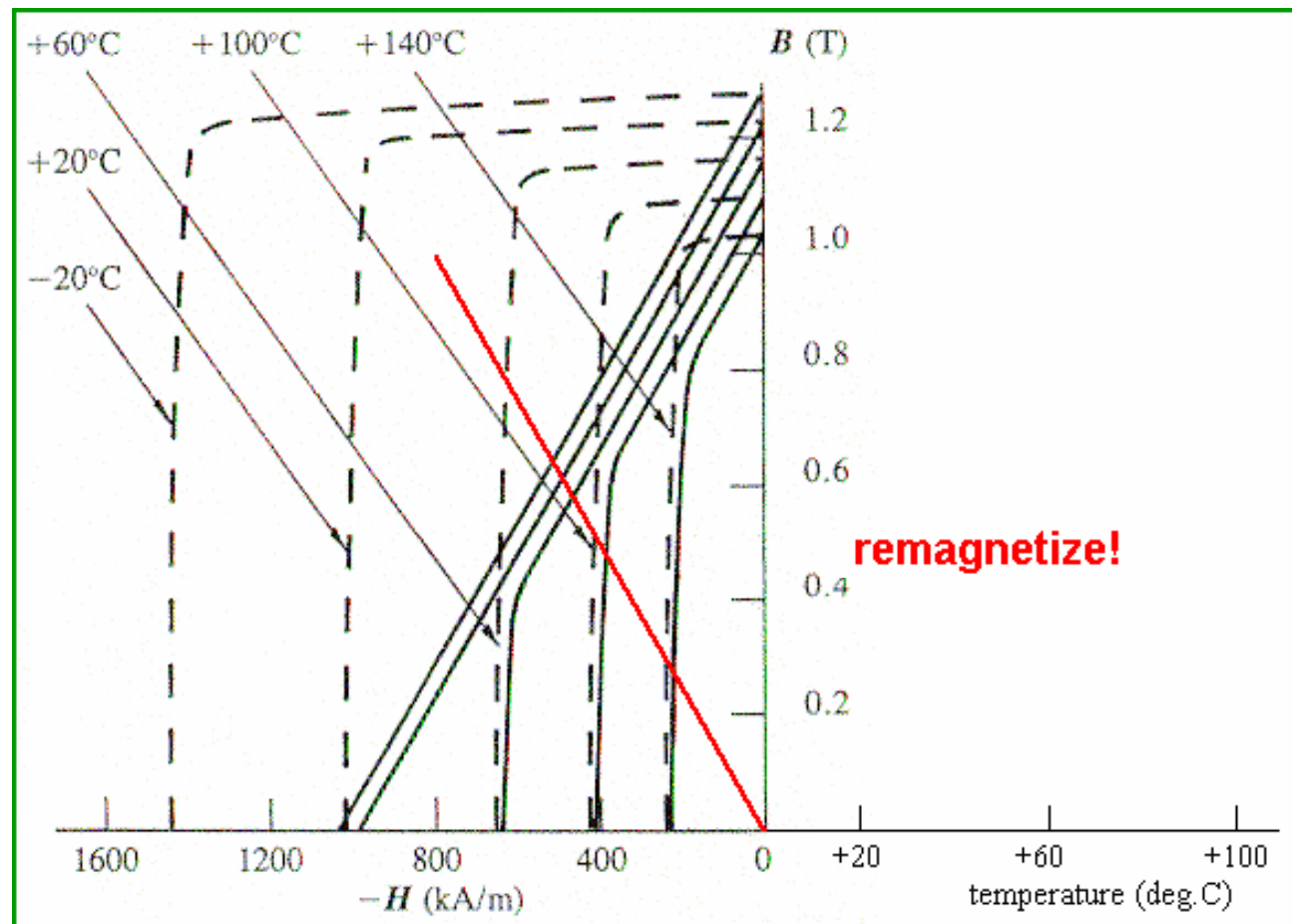
. If the load line of the PM is **P1** —
reversible losses:
 if the temperature becomes again T_0 ,
 the working point goes
 back to „a”, because the variation of
 the induction was
 identically with that of the
 magnetization.

If load line is P2 (at T the working point is in “b”, it is under the ‘knee’, so that returning to T_0 , B can be restored only to point ‘c’) — **irreversible losses a'-c**

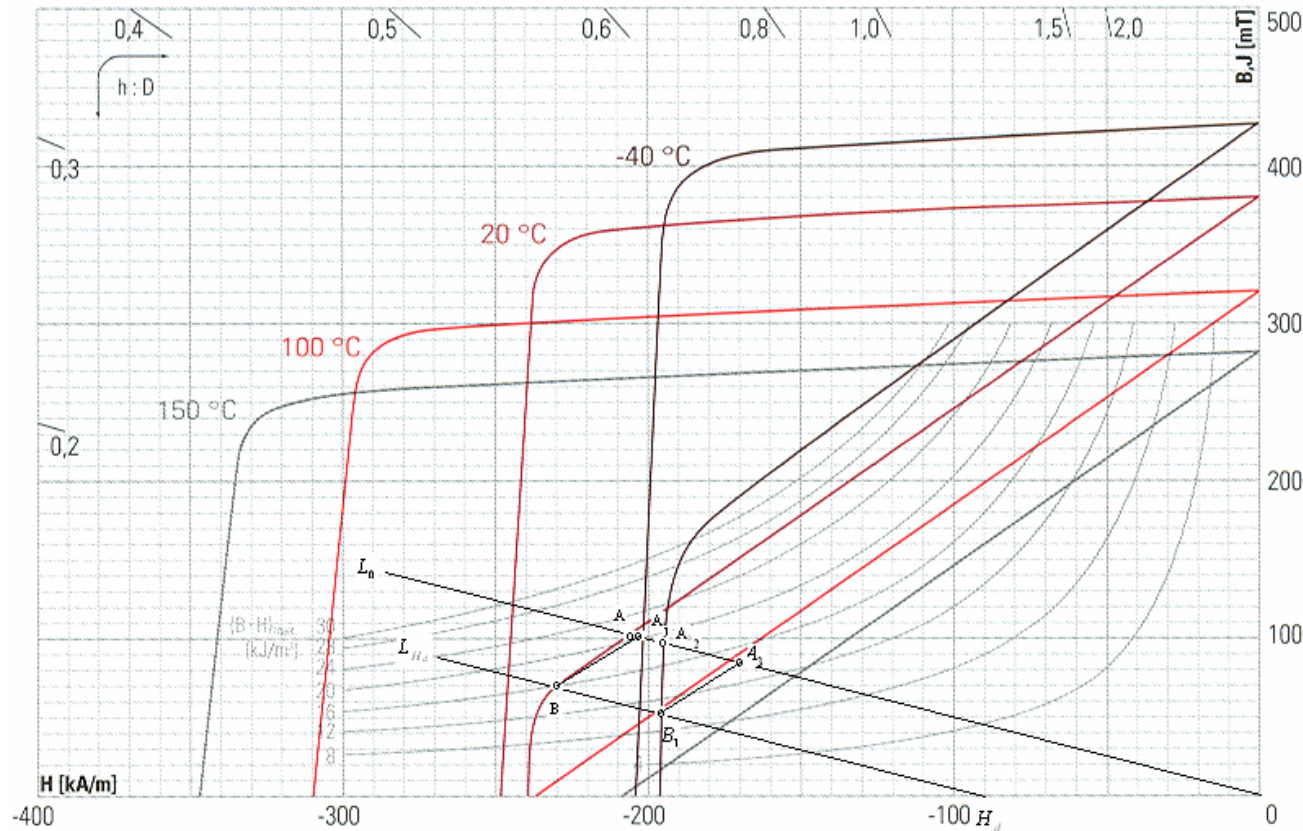








Ferrites at low temperatures



$$\alpha_H > 0$$

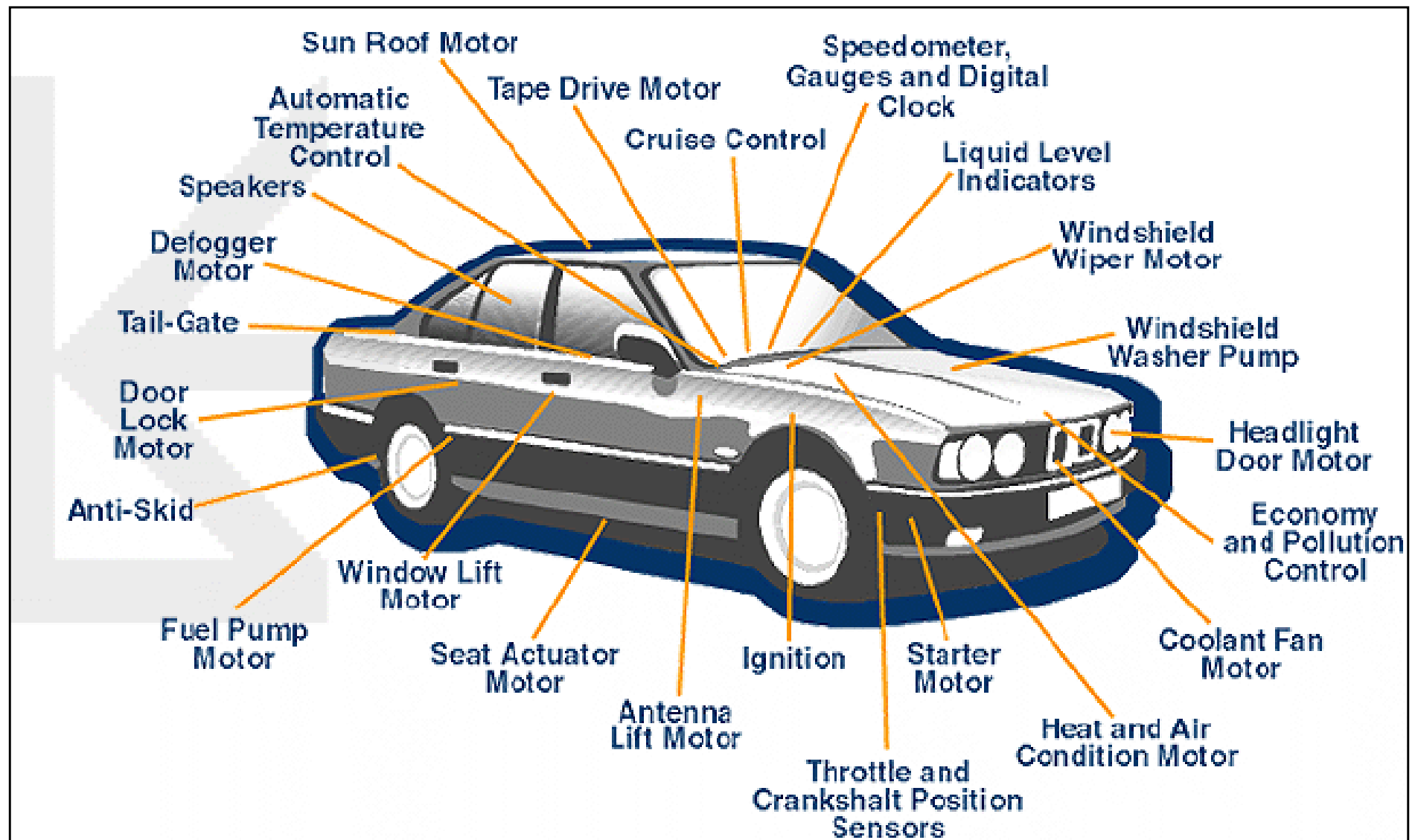
If $T \rightarrow -40^\circ\text{C}$, $A \rightarrow A_2$
on the load line

If H_d is applied,
 $A \rightarrow B$ at 20°C
resp. B_1 at -40°C

If $H_d = 0$, then $B \rightarrow A_1$ resp $B_1 \rightarrow A_3$ along the corresponding recoil lines.

If $T_{-40} \rightarrow T_{20}$, A_1 is not restored because the induction (magnetisation) even become smaller at higher temperature

PM Applications



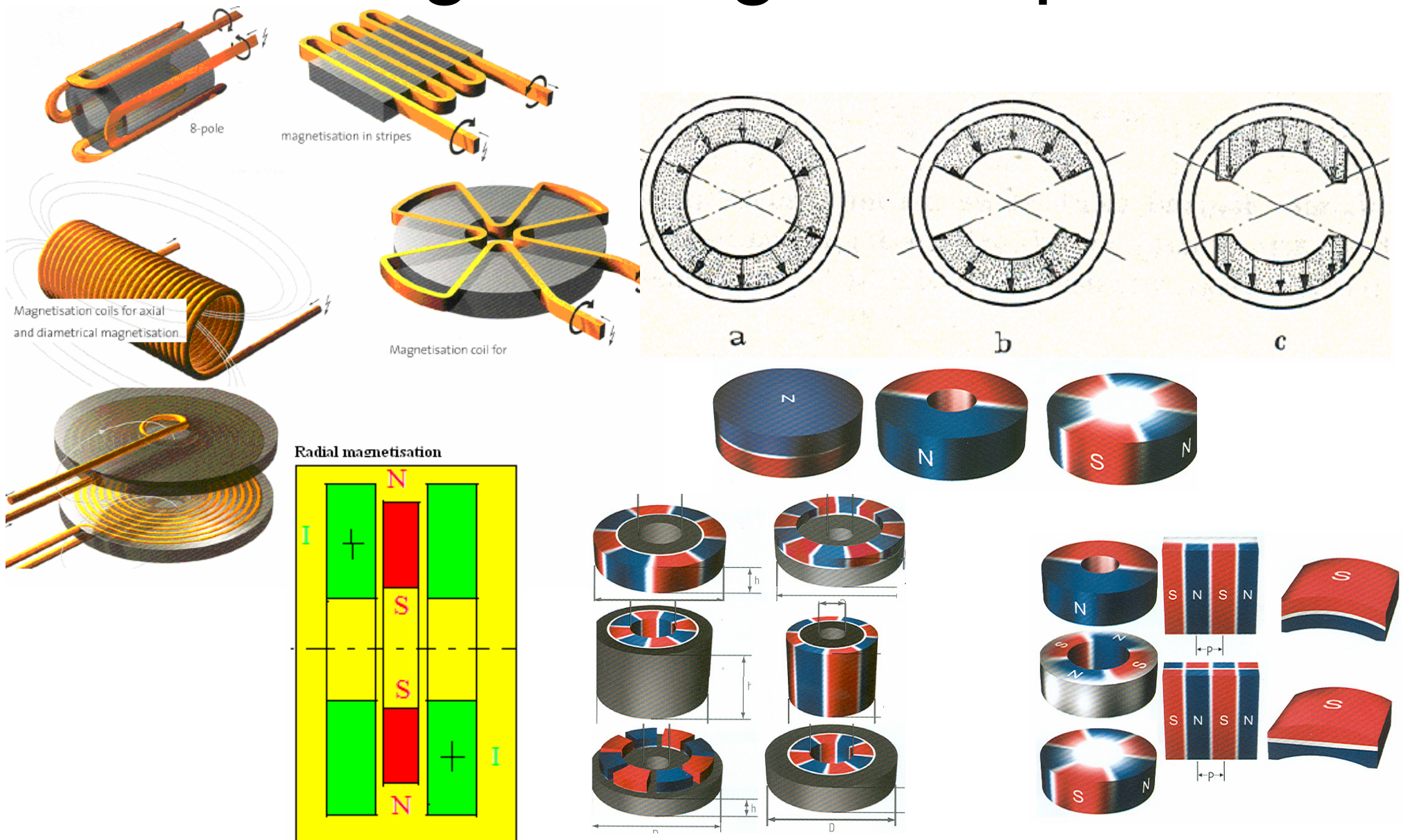
Applications

Different types of magnetic materials

Type of magn. material	SOFT MAGNETIC MATERIALS				HARD MM		Magn. memory	Magnetostriiction material		Transport properties
Field of appl.	E-tron.	Sensors	EMC	E-techn.	E-techn.	E-tron.	IT	Actua-tors	Sensors	Sensors
TM-alloys	FeSi, Nano & am FeNi	Nano FeNi	<i>Compo sites M+pol ymers</i>	FeSi, FeNi, FeCo, Fe	<i>AlNi-Co</i>				FeCoZr	Permalloy
RE-TM					<i>NdFeB SmCo</i>	<i>NdFeB SmCo</i>	TbFeCo	RE-Fe ₂		
Ferrit. Mangani tes	<i>Soft ferrites</i>	<i>Soft ferrites</i>	<i>Soft ferrites</i>	<i>Magn. liquids</i>	<i>Hexa-ferrites</i>	<i>Hexa-ferrites</i>	<i>Fe₂O₃, CrO₂</i>			LaREMnO ₃
Thin films		Alloys, oxids			Metall & oxid systems		CoCrTM-RE/CoCr	RE-TM	Ni	
Multi-layers		M-mu. layers	Mu.-lay.+in sulater		Metall & oxid systems		PtCo	RE-TM,TM-TM [?]		TM/nonmag/TM,TM/insul./TM
Nano		Am.(Co)	<i>Fe₂O₃</i>		<i>Comp.with exch. interaction</i>		Magn. wires			

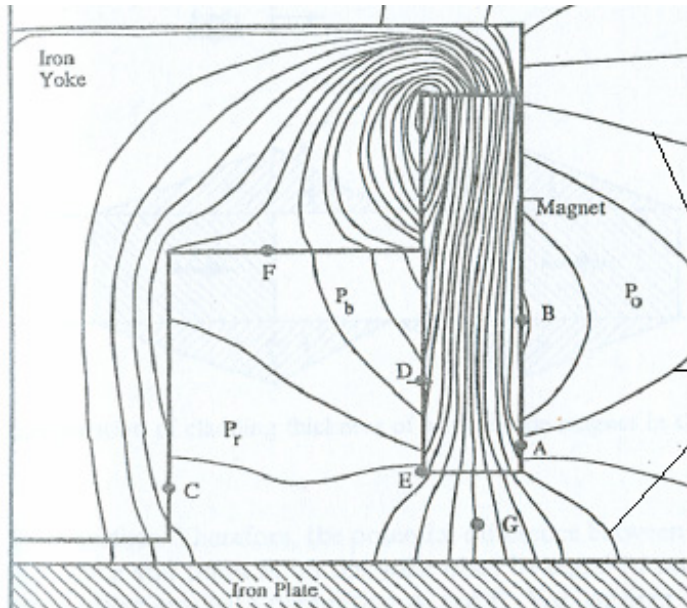
TM=3d-transition metal, RE=rare earth, M=metal

Magnetizing & shapes

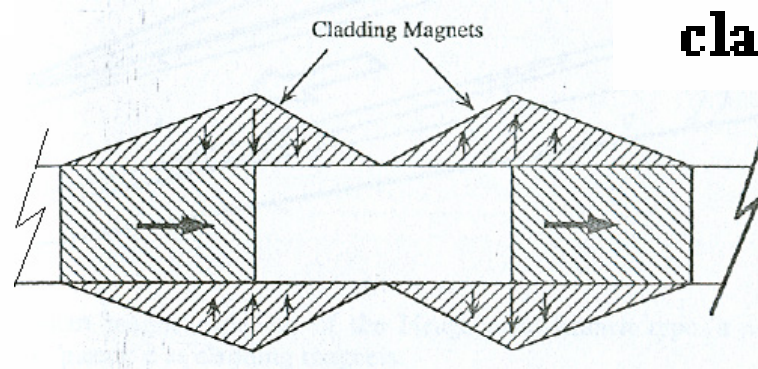


Applications of high energy PM

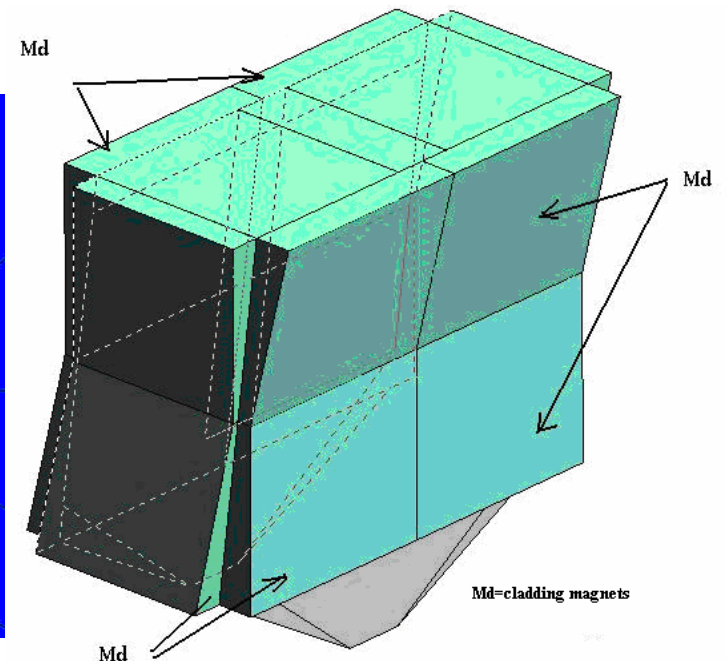
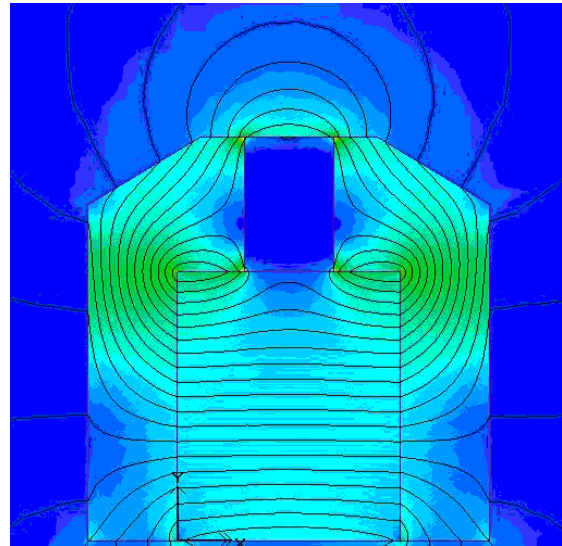
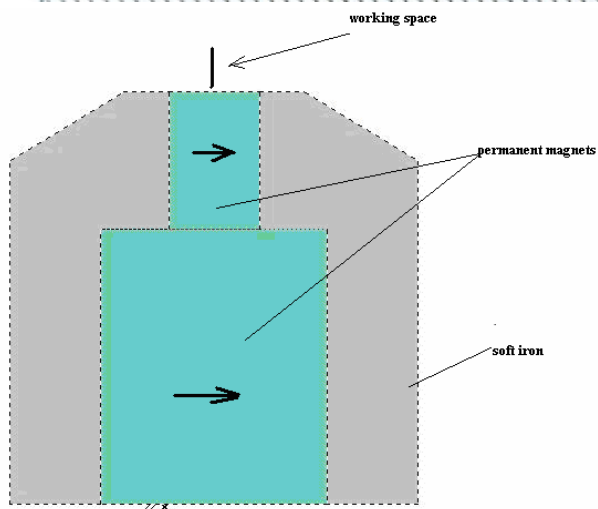
Generating mag. fields



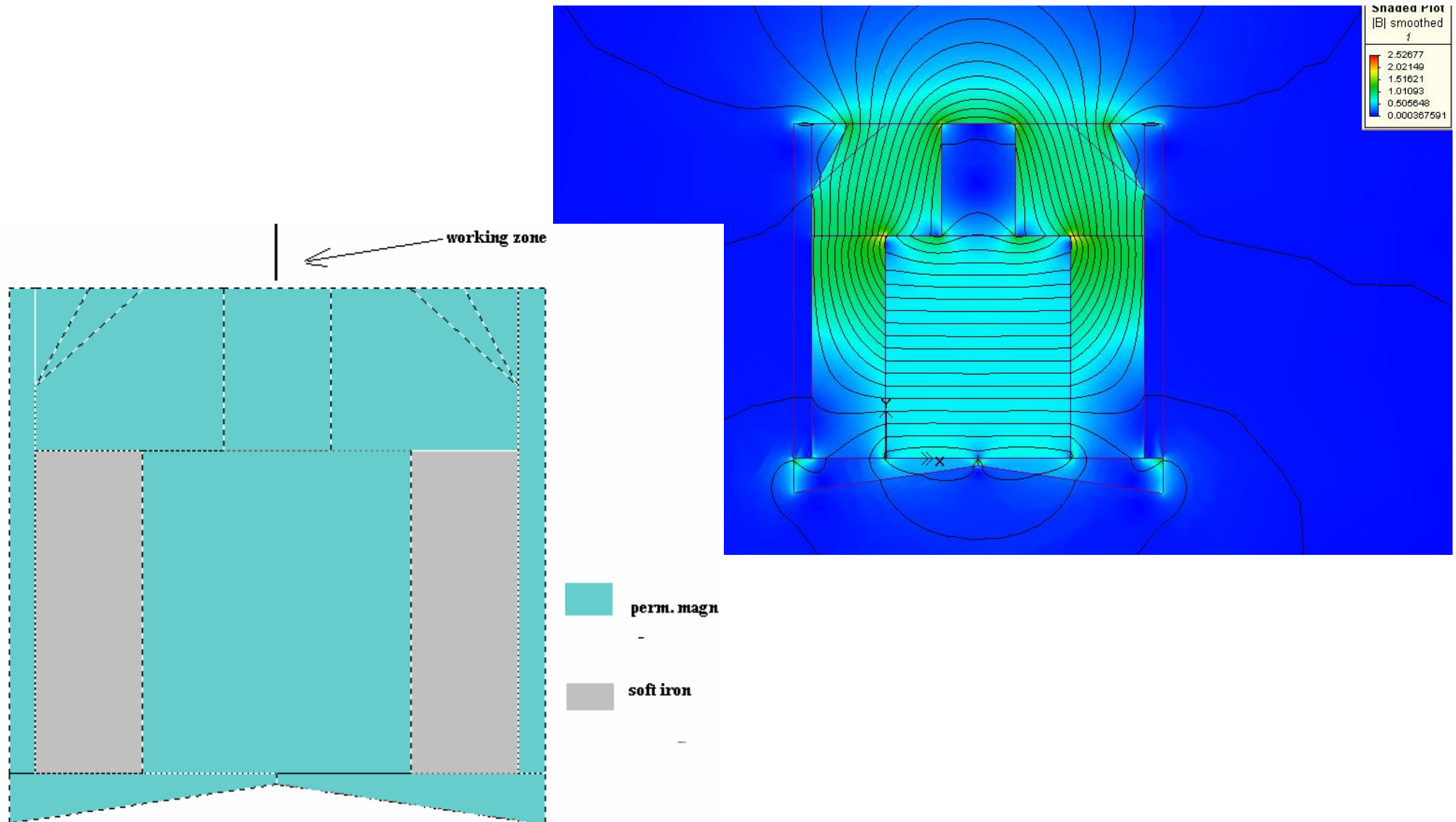
Stray field



cladding magnets



Cladding magnets/effects

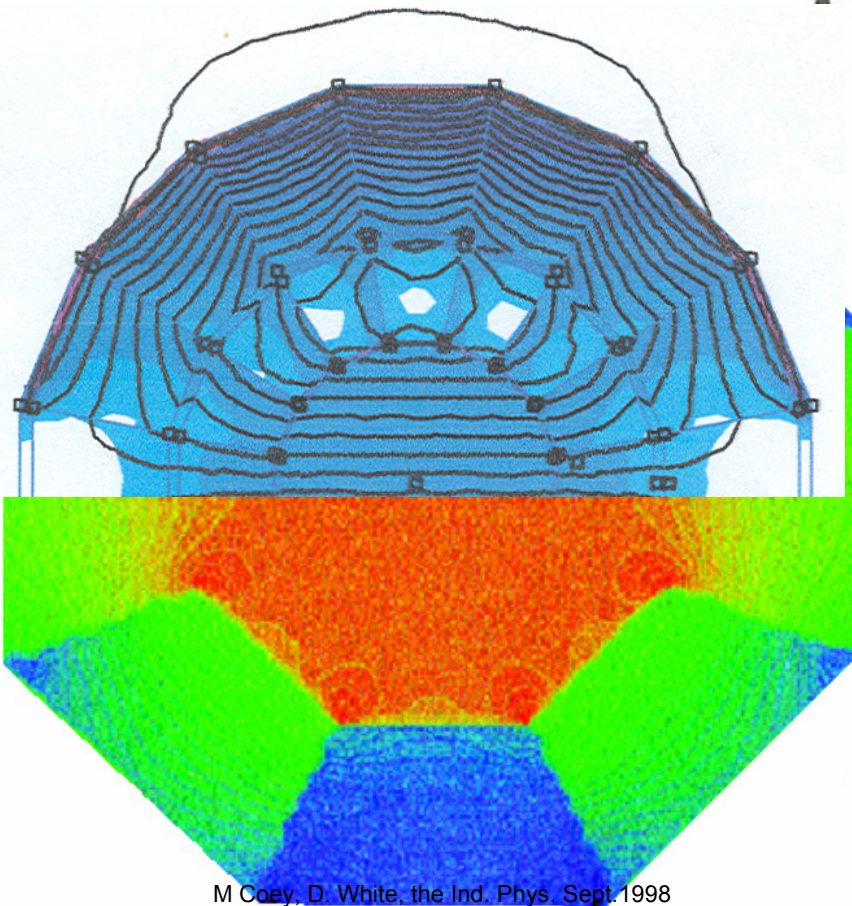


PM Applications

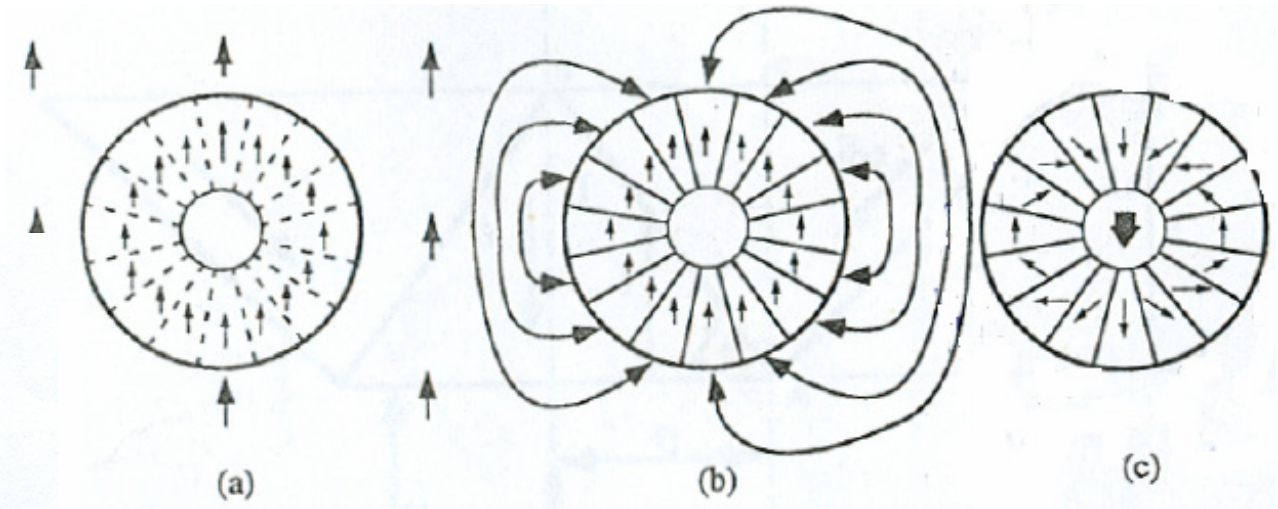
Generating mag. fields

$$B = B_r \frac{\sin(2\pi / N)}{2\pi / N} \ln(R_2 / R_1)$$

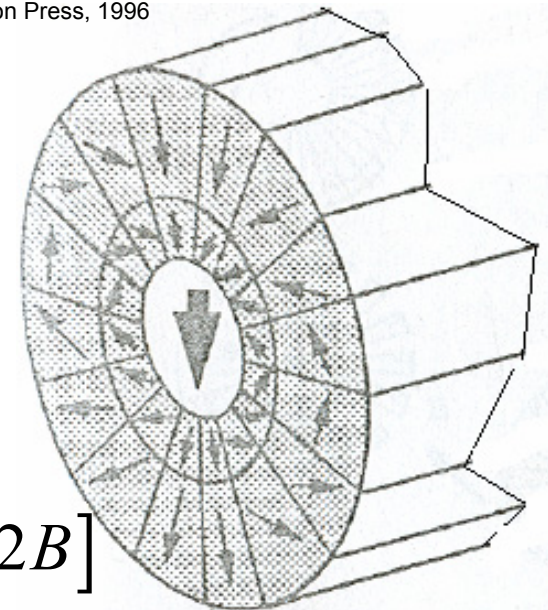
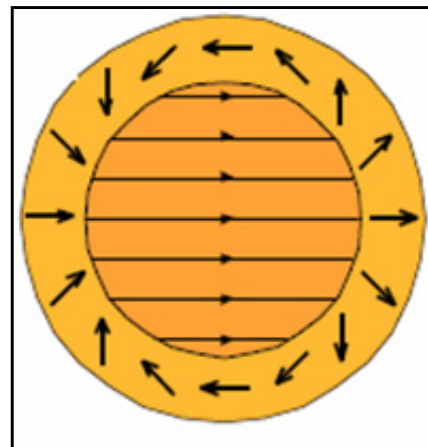
Hallbach (magic) cylinder



M Coey, D. White, the Ind. Phys. Sept. 1998

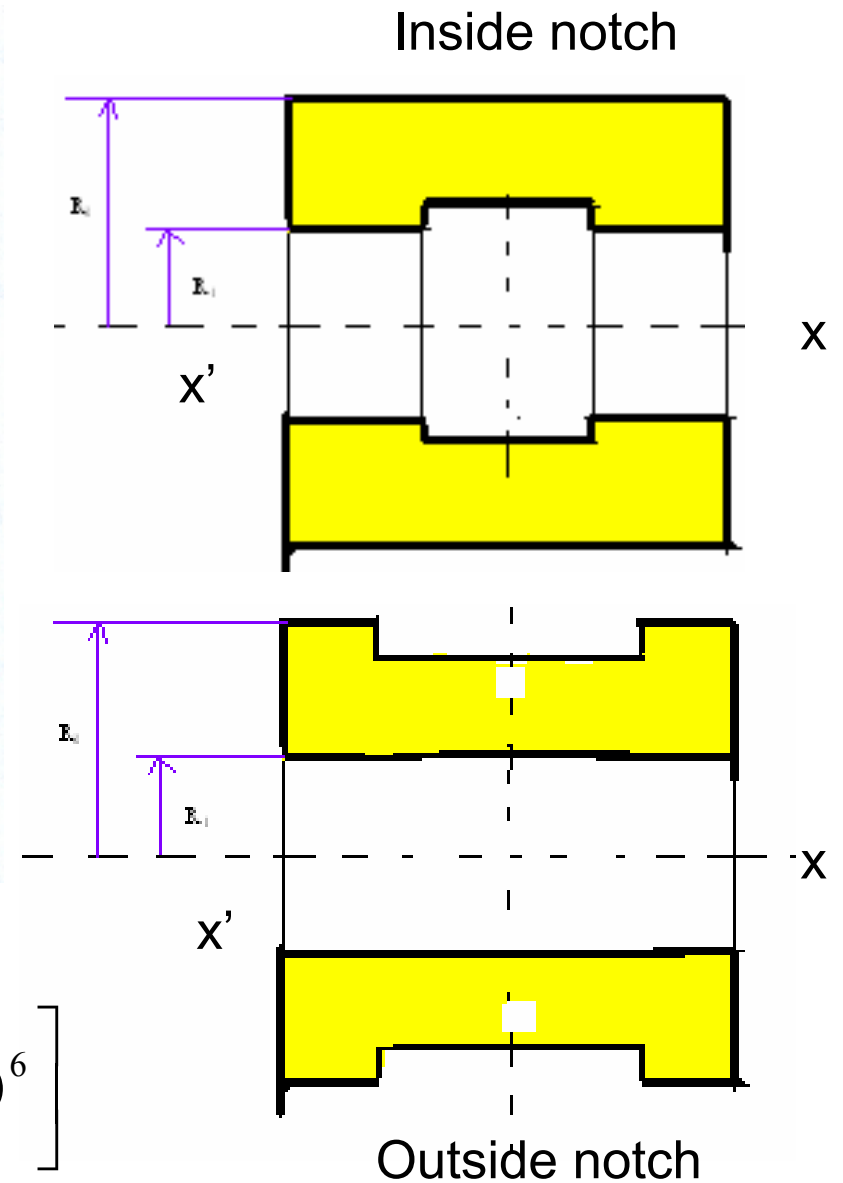
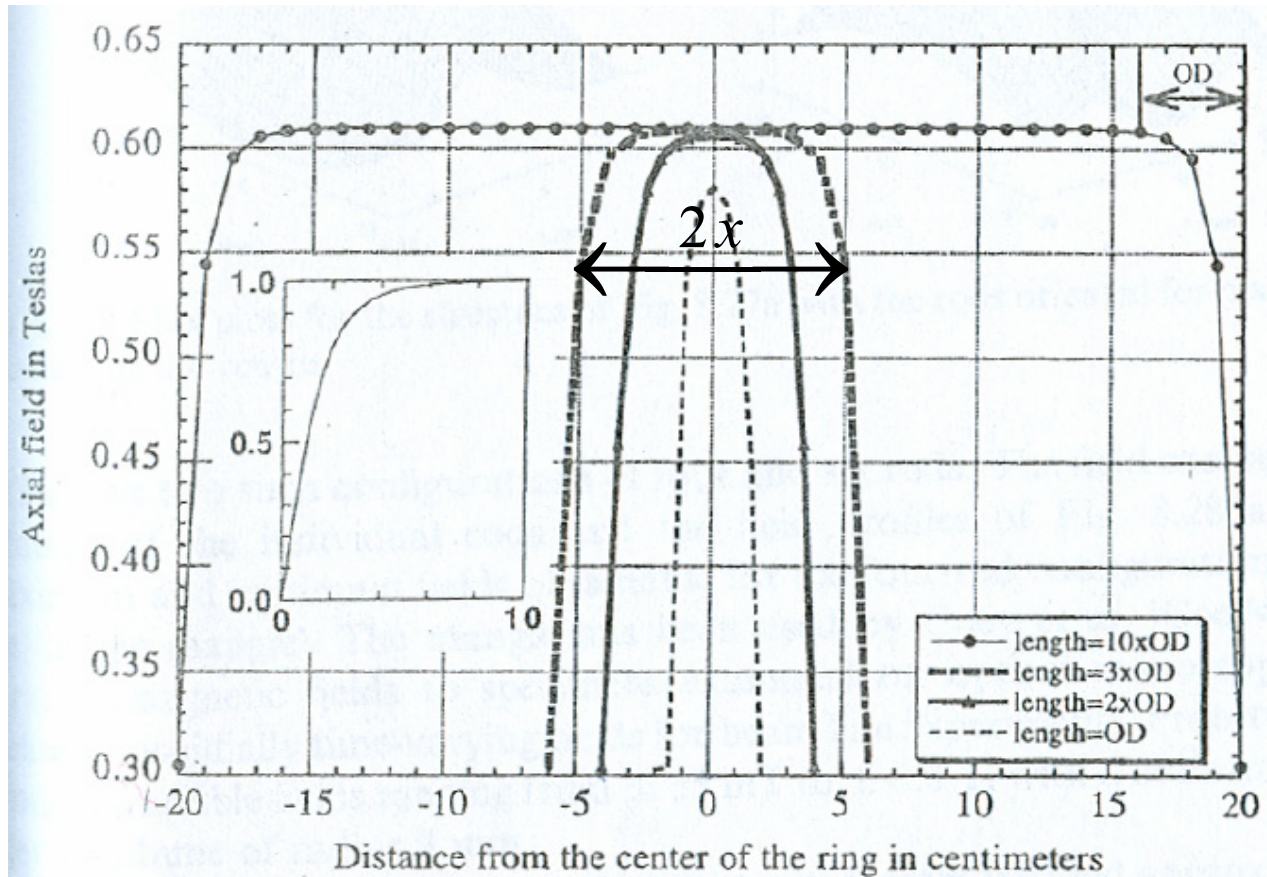


H. A. Leupold, Static Applications, Re-Fe PM, J.M. Coey, Clarendon Press, 1996



$$B_{\text{int}} \in [-2B, 2B]$$

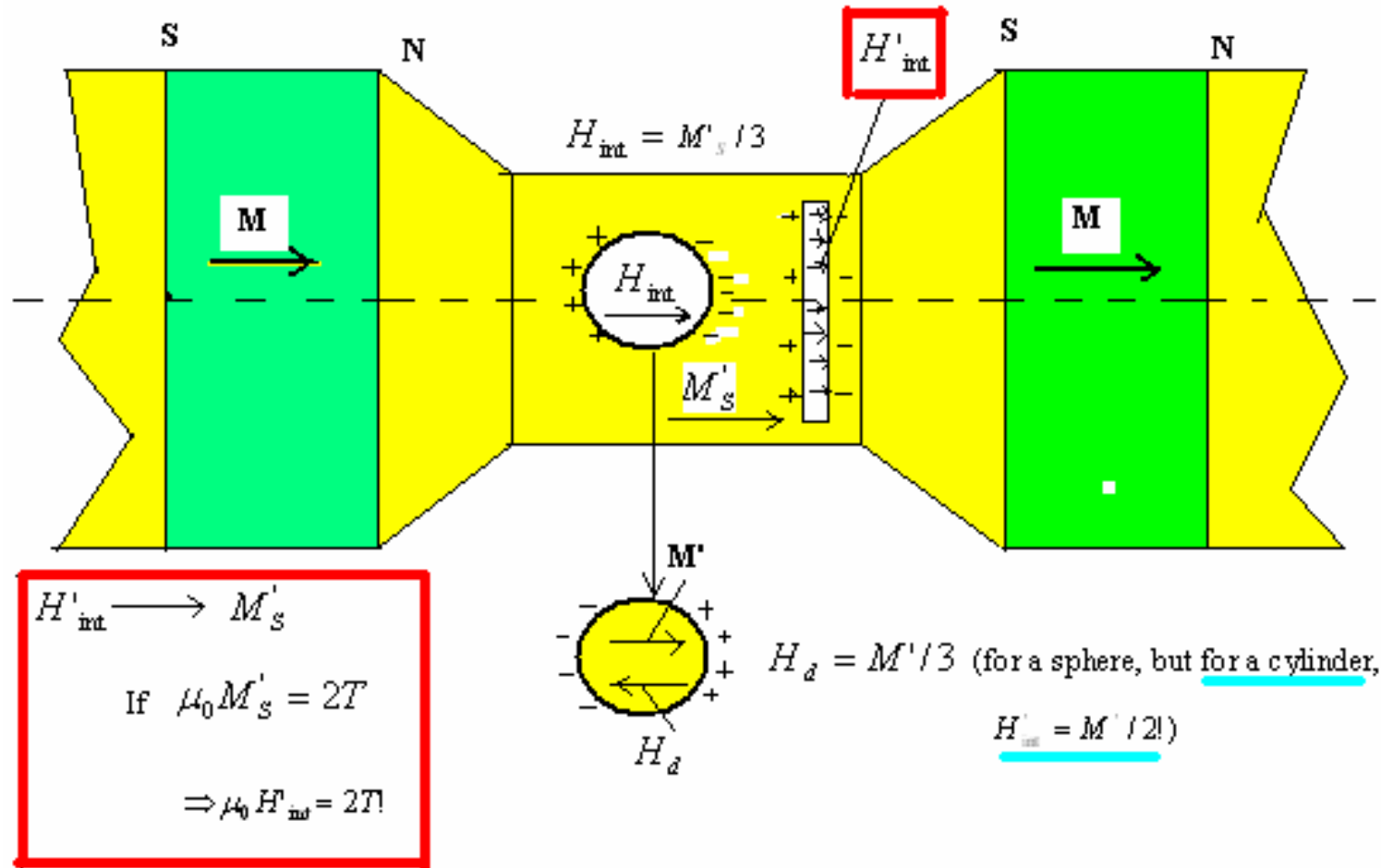
Hallbach Cylinder



$$B(x) = B_{inside}(0) \left[1 - P_{inside}(geometry) \left(\frac{x}{R_1} \right)^6 \right]$$

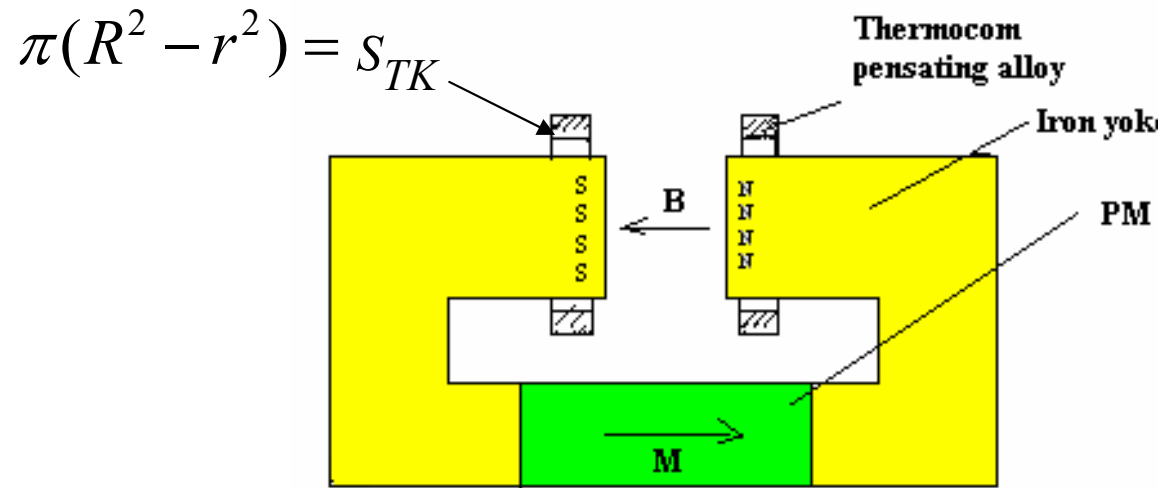
PM Applications

Magnetic Field



Applications: *PM powder pressing tools for anisotropic PM, built from ferromagnetic steels*

$dB/dT=0$ with thermocompensating alloys



$$B_m(T) = B_{mo}(1 + \alpha_m(T - T_o))$$

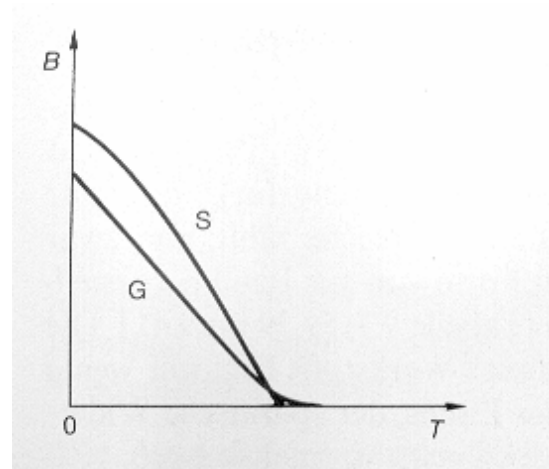
$$B_m S_m = BS + B_{TK} S_{TK}$$

$$S_m \frac{dB_m}{dT} = \frac{dB}{dT} \cdot S + S_{TK} \frac{dB_{TK}}{dT}$$

$$dB/dT = 0$$

$$S_{TK} \frac{dB_{TK}}{dT} = S_m B_m(T_o) \alpha_m$$

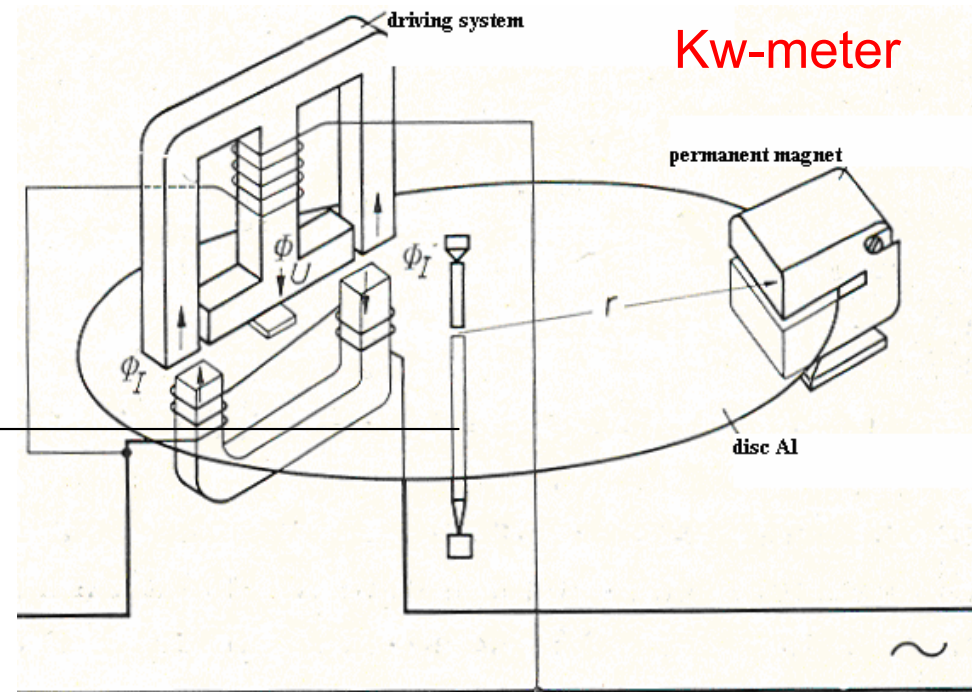
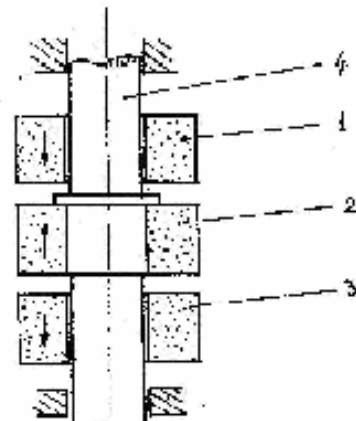
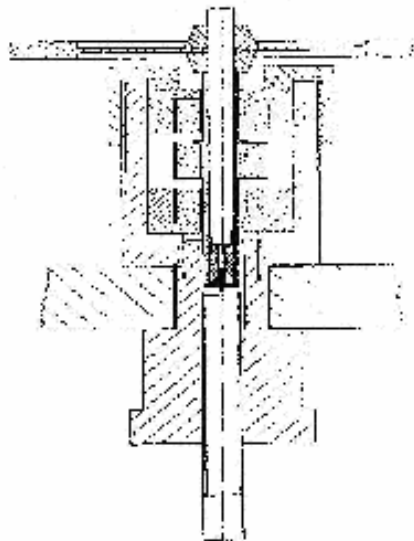
Thermoflux



$$S_{TK} = \frac{S_m B_{mo} \alpha_m}{dB_{TK}/dT}$$

$$dB/dT=0$$

$$F_x = \frac{1}{2} B_{m1} \frac{dH_2}{dx} V_1$$

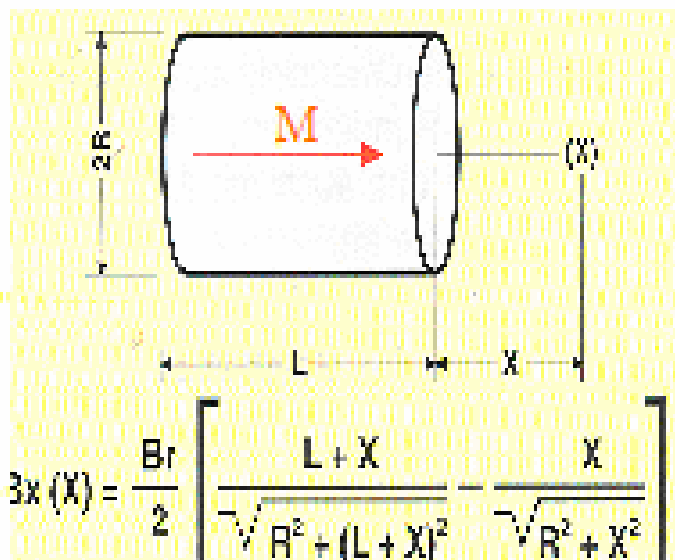
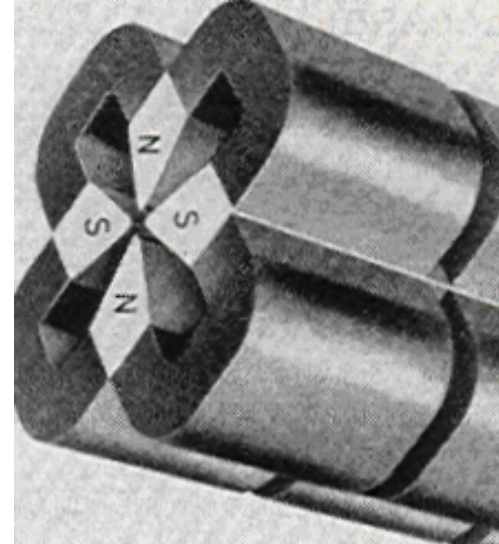


$$M_{break} \propto B^2 / \rho_{Al}$$

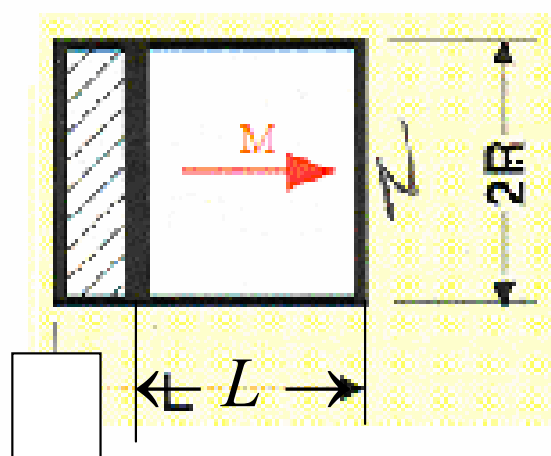
$$\rho_{Al}(T) = \rho_{Al}(T_0)(1 + \alpha_{Al,T}(T - T_0))$$

$$\alpha_{Al,T} = -0,4\% / ^\circ C$$

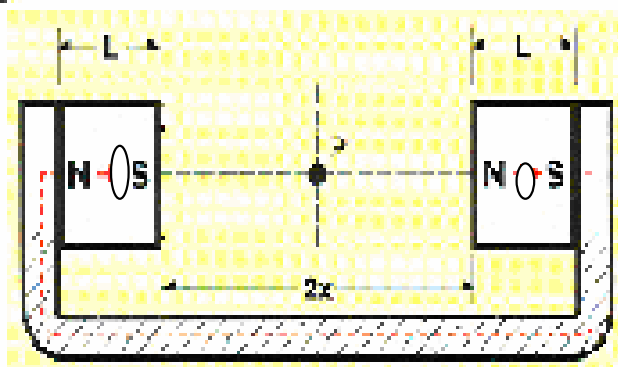
Field Generator



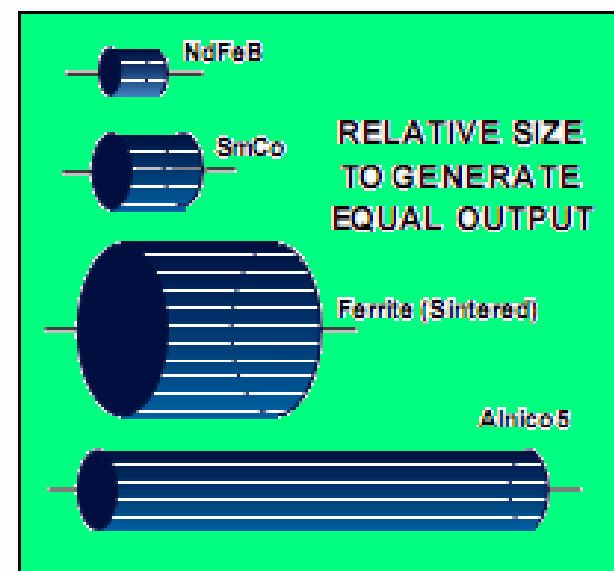
$$L \rightarrow \infty \& x=0 \Rightarrow B_x = \mu_0 M / 2!$$



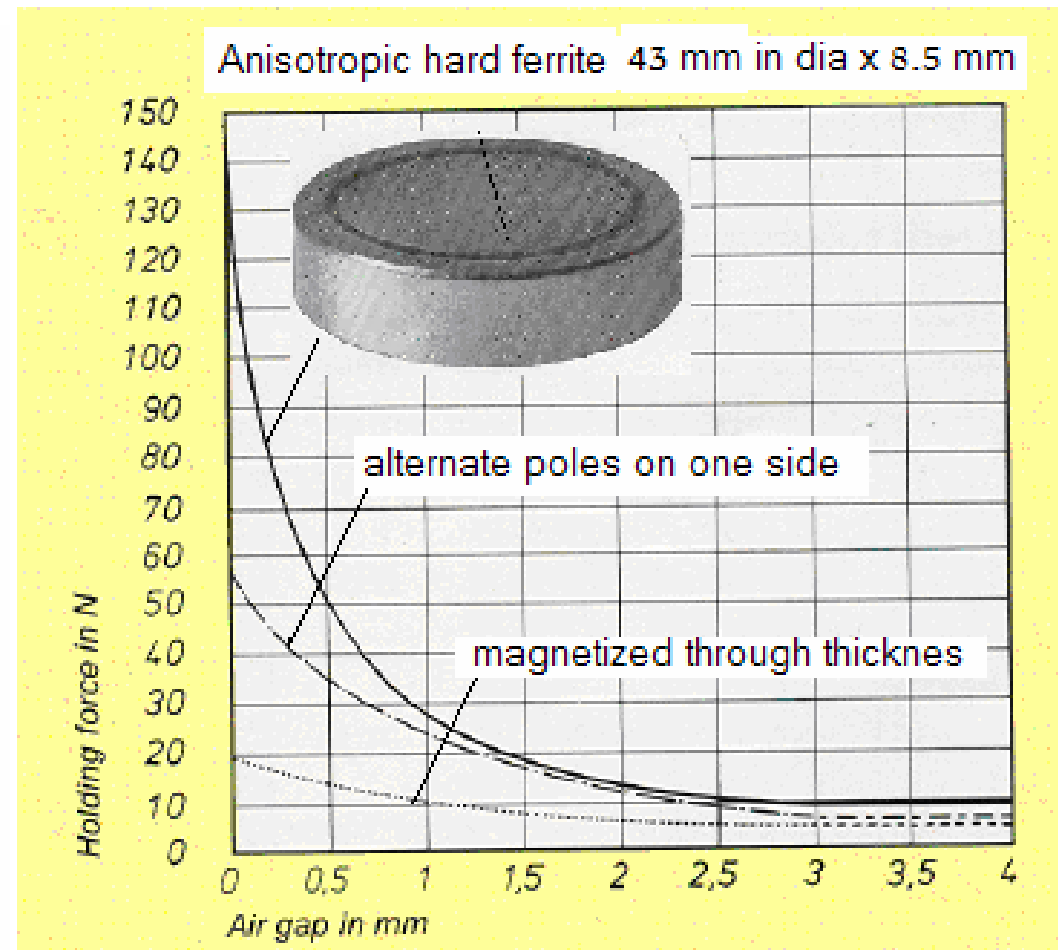
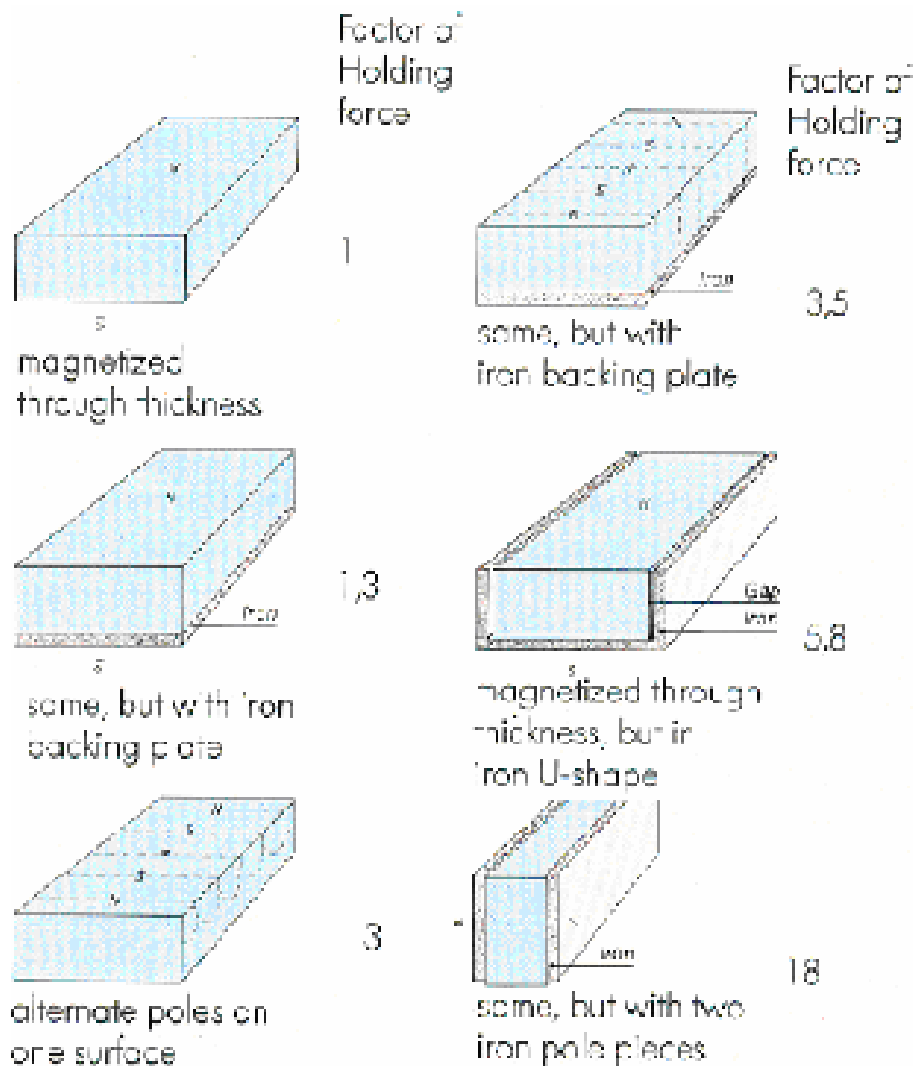
$$L \rightarrow 2L$$



$$B_x \rightarrow 2B_x$$

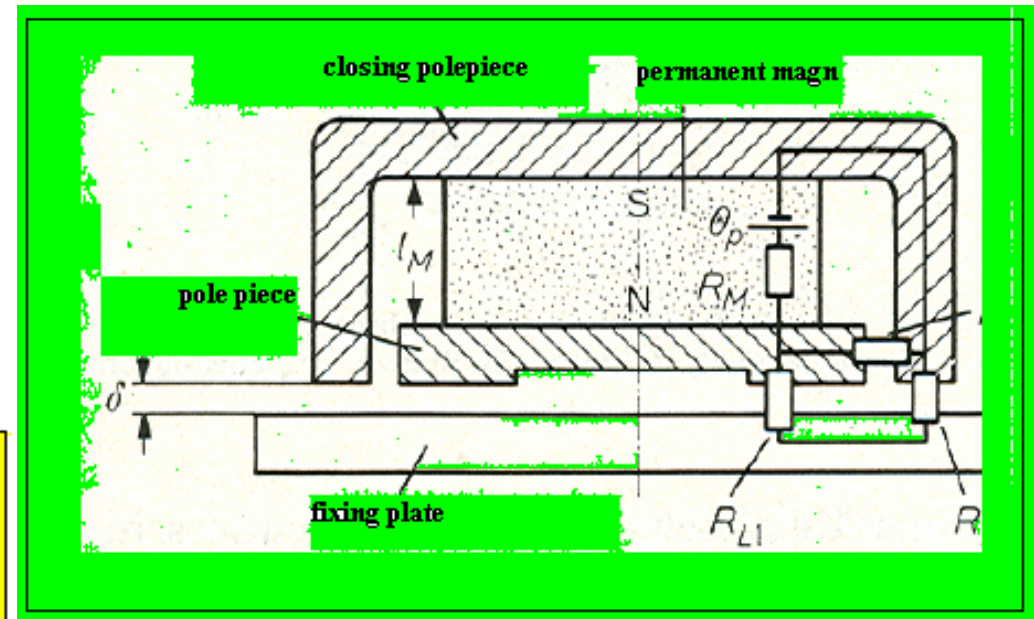
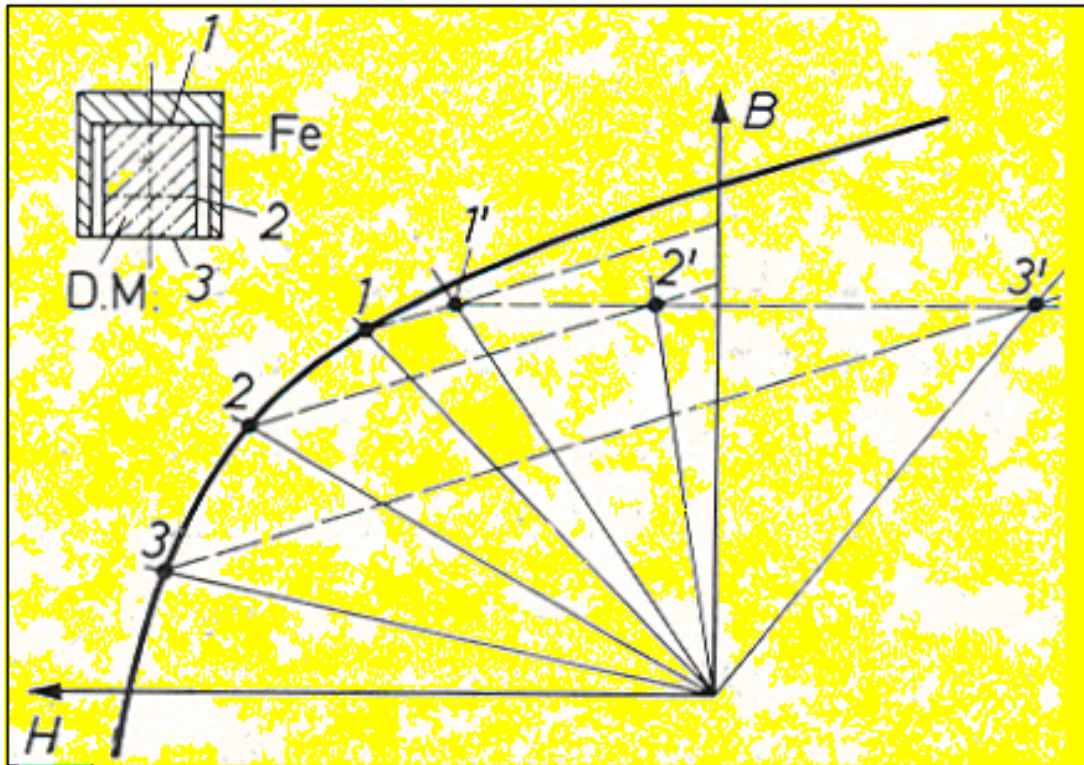


Holding magnets



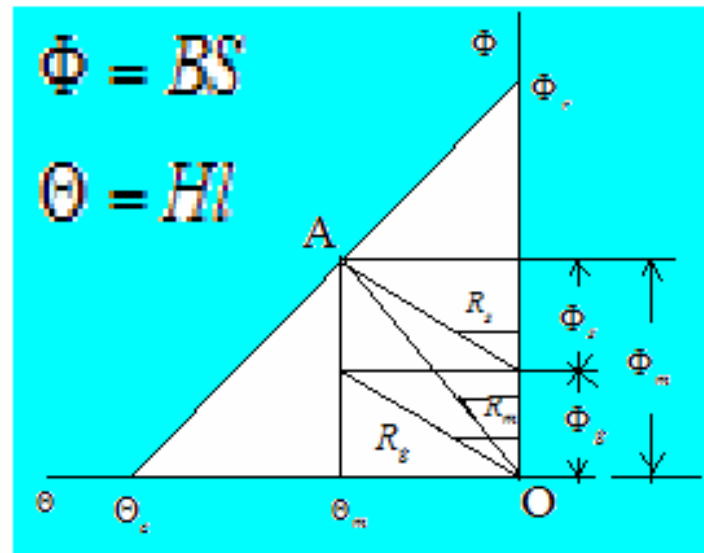
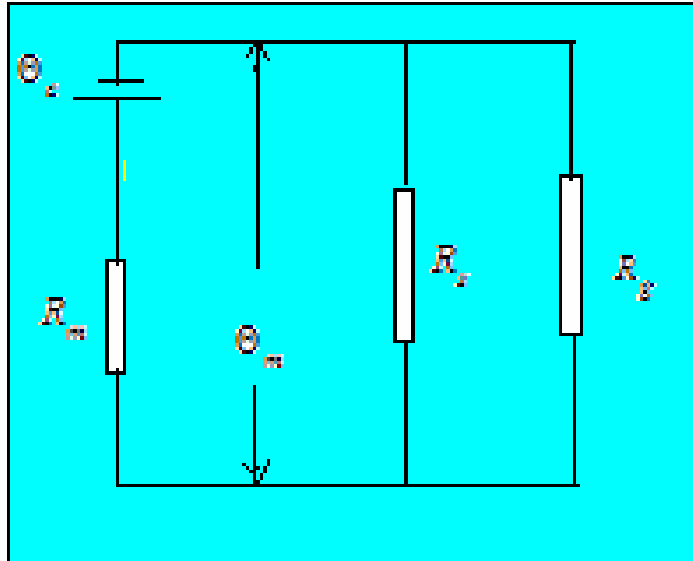
Holding magnets

$$R = 1 / \Lambda$$



$$F = A \frac{B_L^2}{2\mu_0}$$

$\Phi - \Theta$ -Demagnetisation curve



optimal

$$\Phi_m = B_m S_m = B_g S_g + B_s S_s = \Phi_g + \Phi_s$$

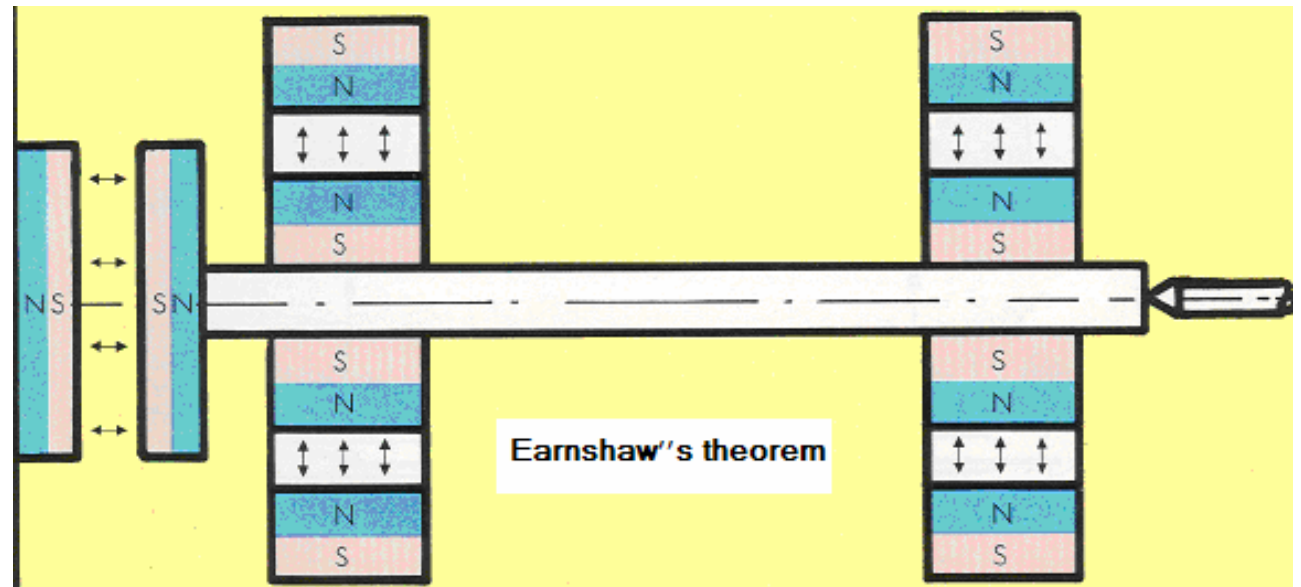
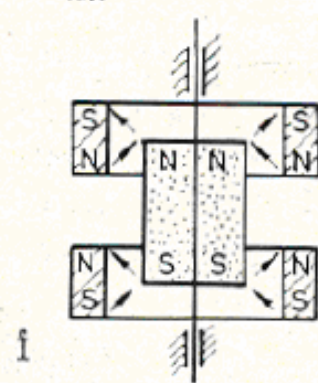
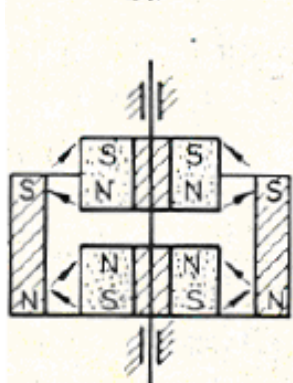
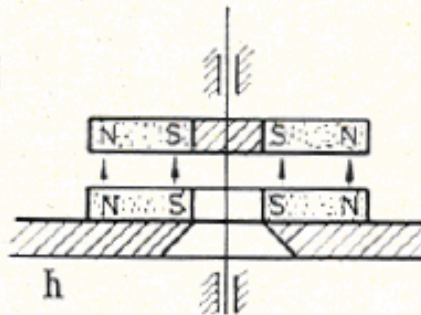
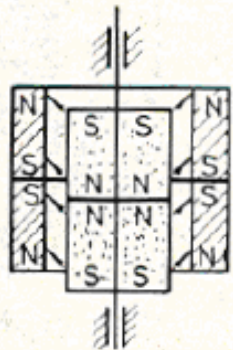
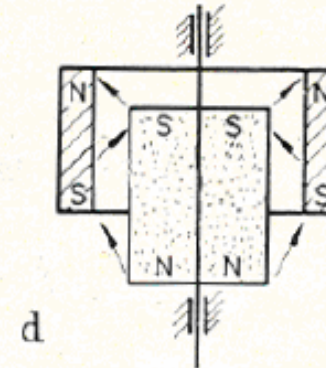
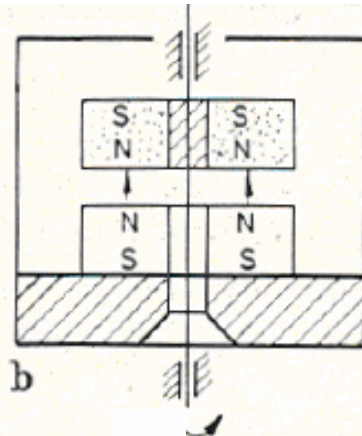
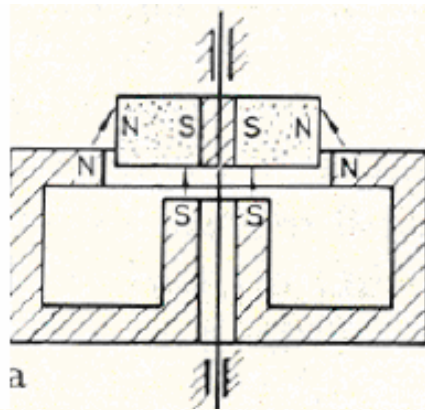
$$\Theta_m = H_m l_m = H_g l_g = \Theta_g = \Theta_s = R_m \Phi_m$$

$$tg \alpha = \frac{\Theta_m}{\Phi_m} = R_m = \frac{l_m}{S_m \lambda_m} = \frac{l_m}{S_m B_m / H_m} = \frac{1}{\Lambda_m}$$

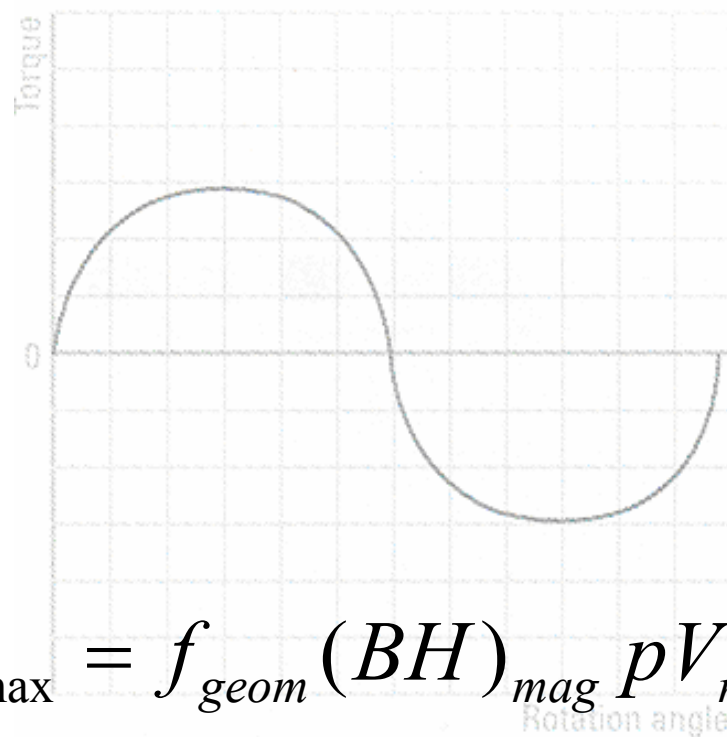
$$R_{int} \equiv R_{ext} = \frac{R_g R_s}{R_g + R_s}$$

Bearings

$$F_x = \frac{1}{2} B_{m1} \frac{dH_2}{dx} V_1$$

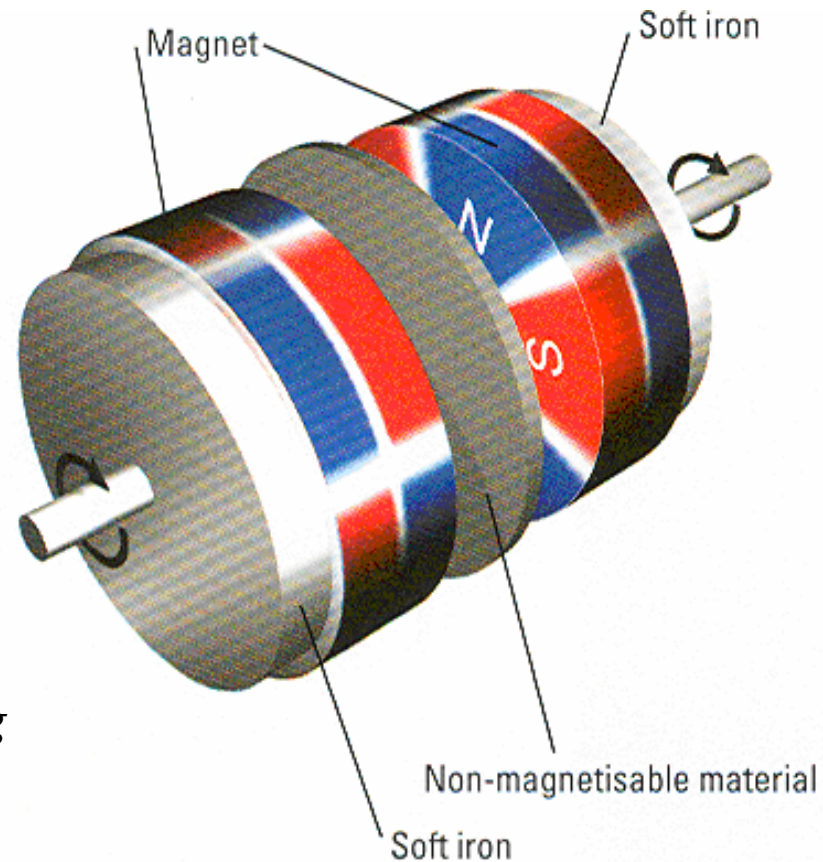


Axial coupling

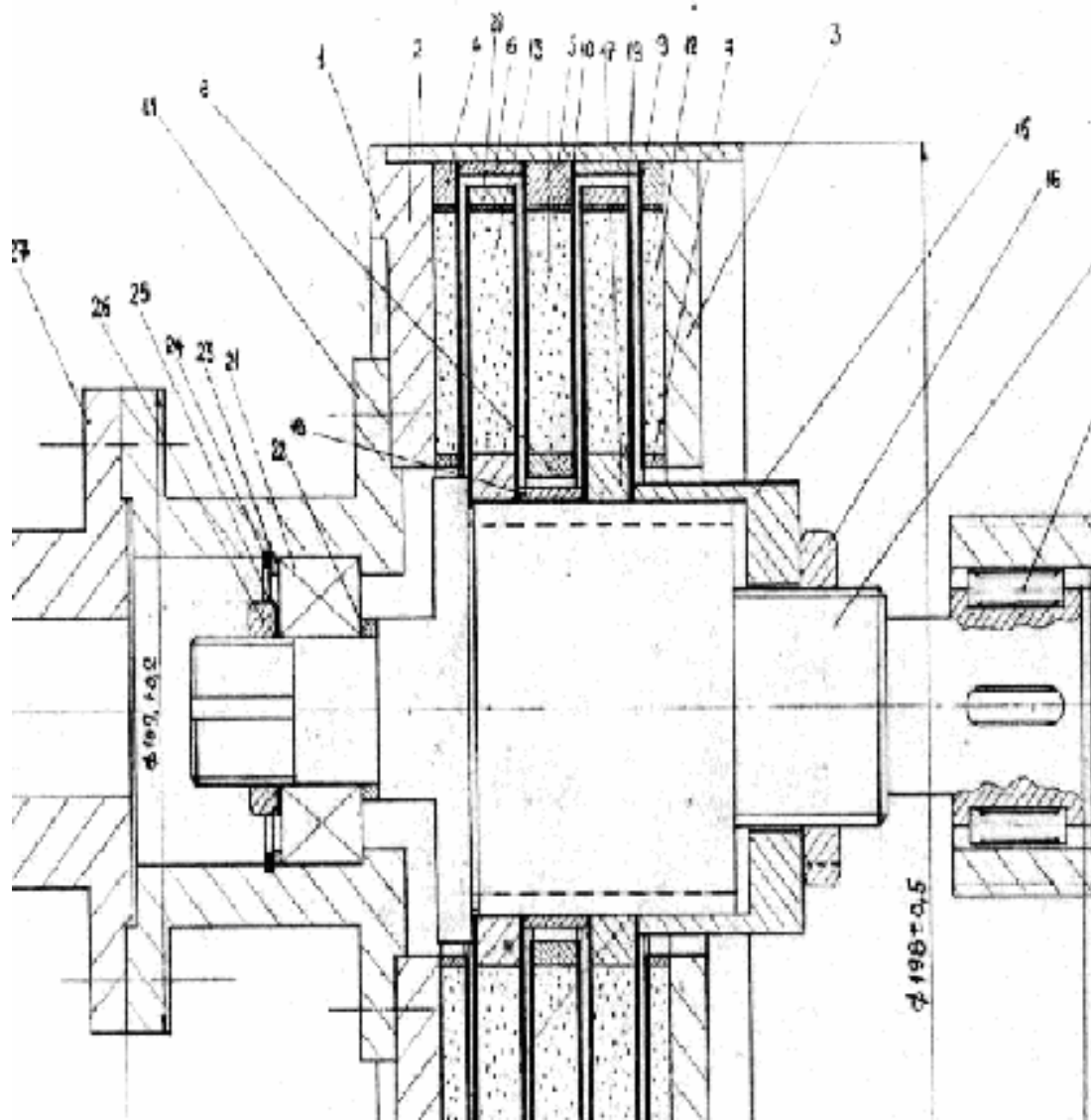


$$M_{\max} = f_{\text{geom}} (BH)_{\text{mag}} p V_{\text{mag}}$$

Disc coupling

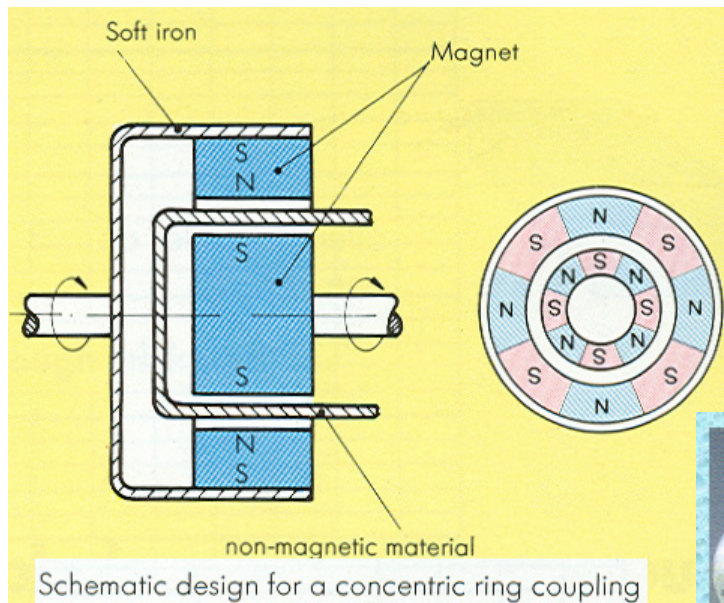
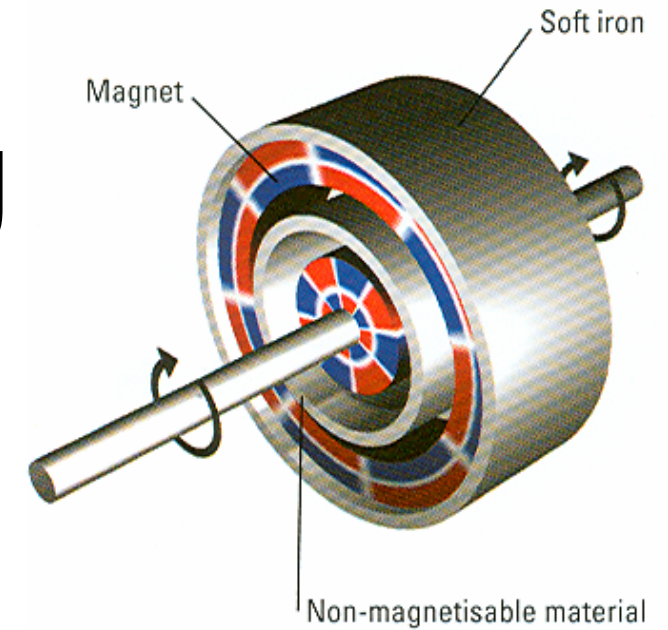
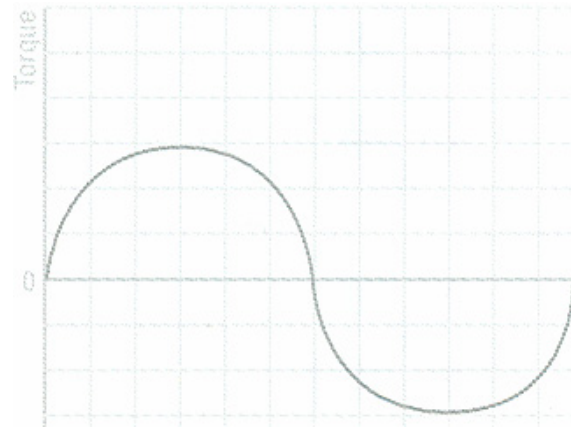
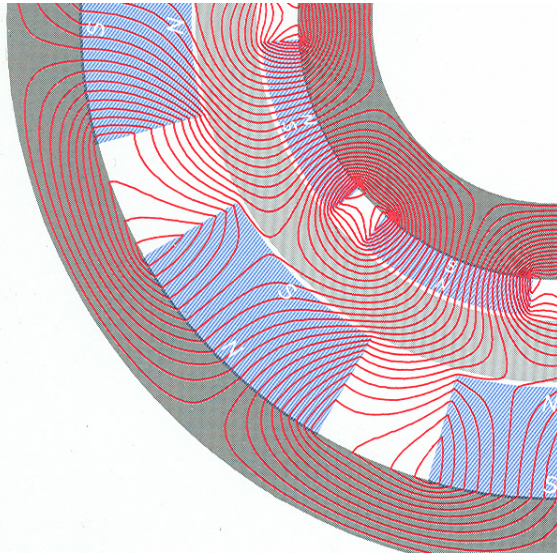


Multiple Radial Coupling

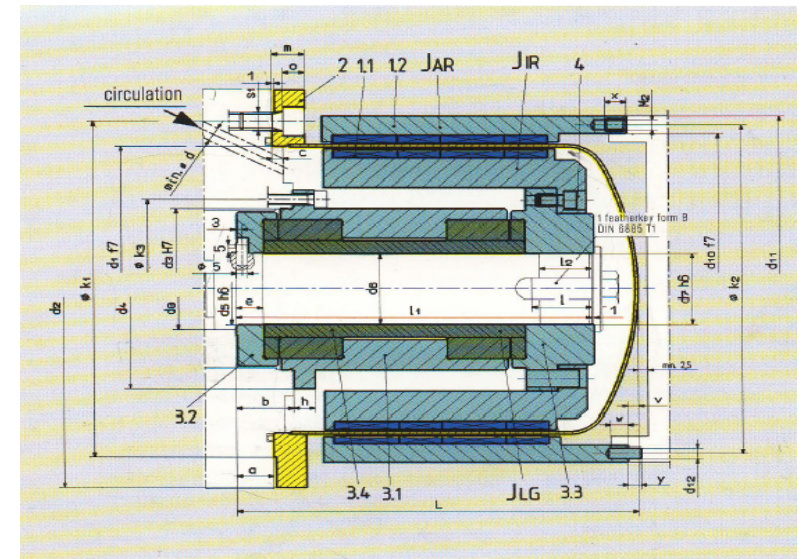
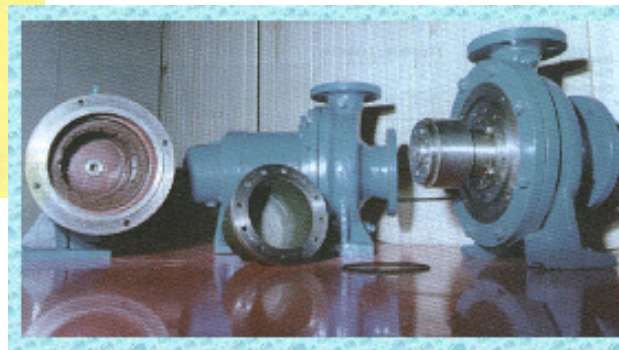


$$T \sim 10^2 - n10^3 \text{ Nm}$$

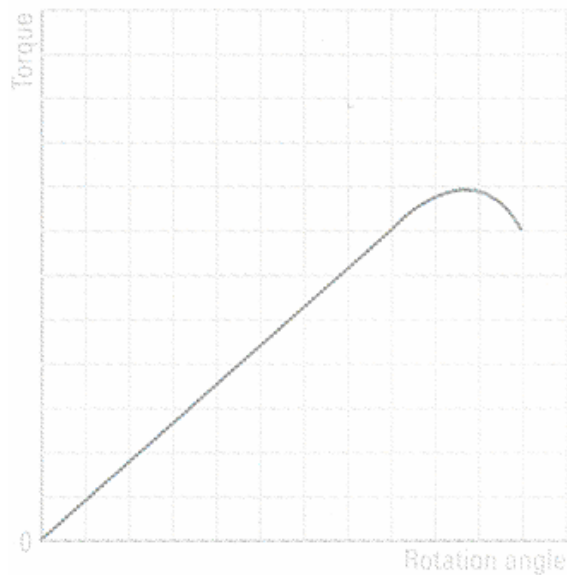
Radial coupling



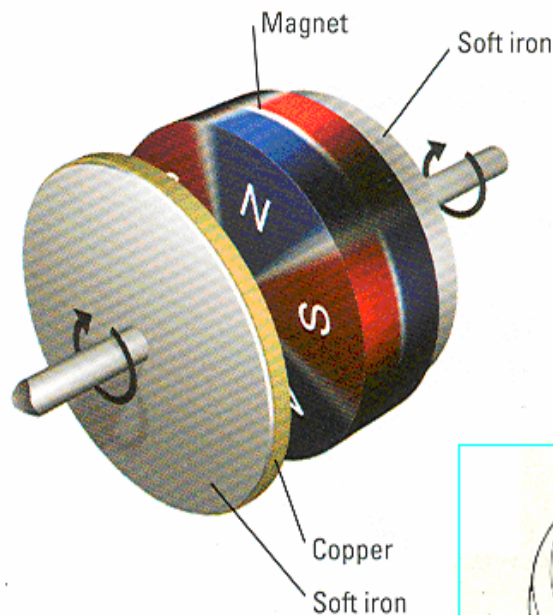
$$M_{\max} \propto B_L^2 R^2 L$$



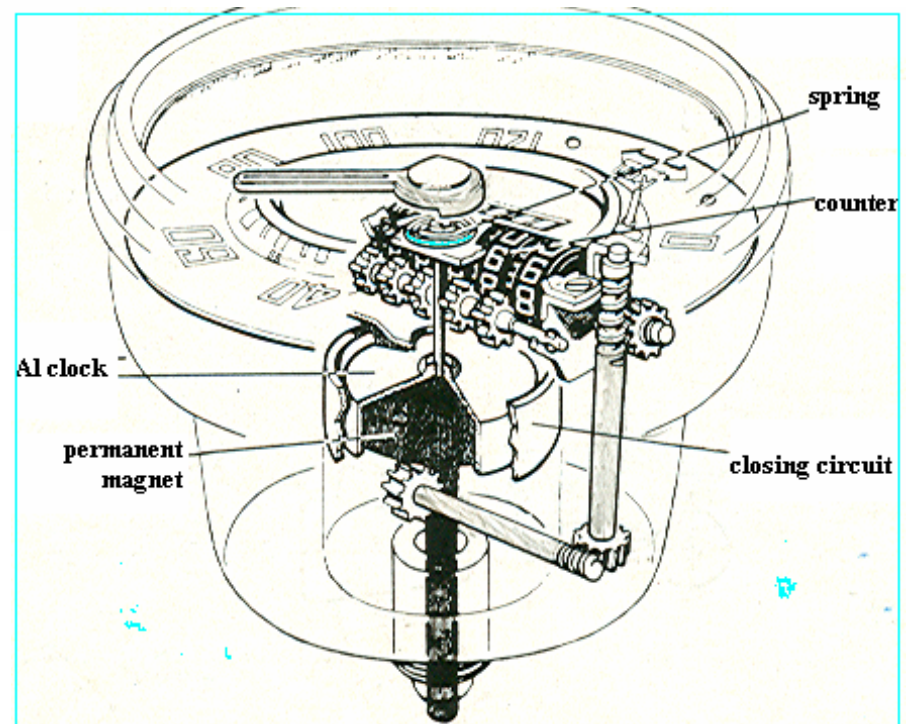
Eddy current coupling



Eddy current coupling and brake

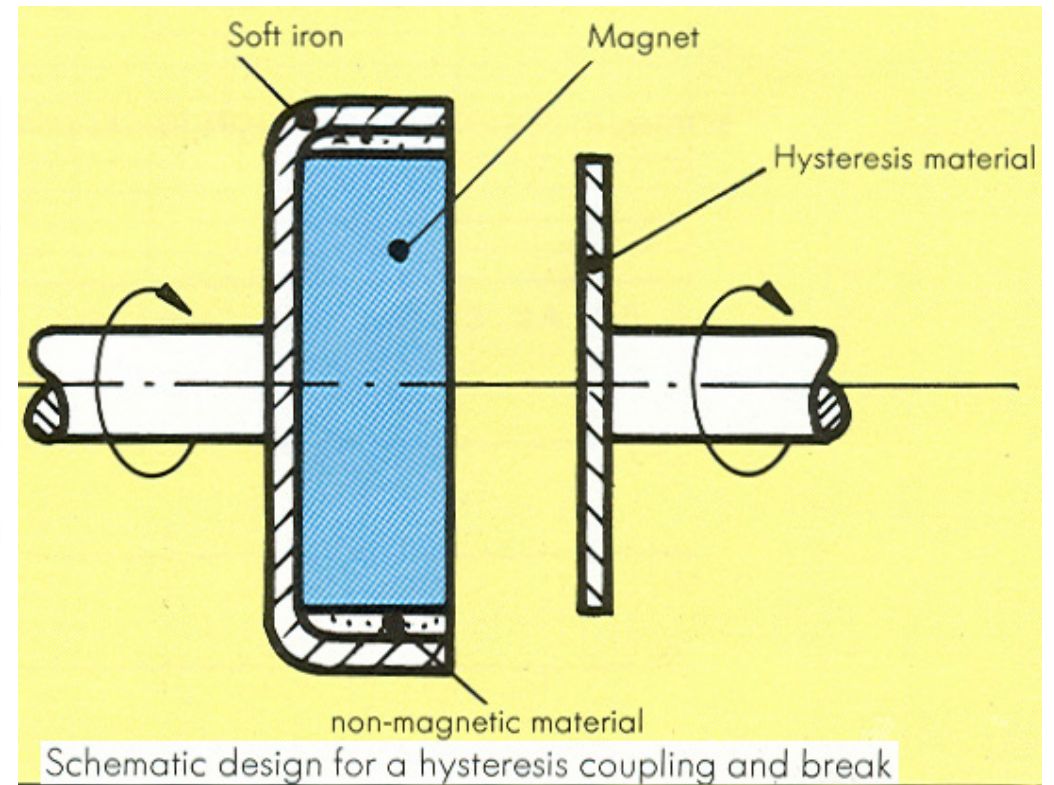
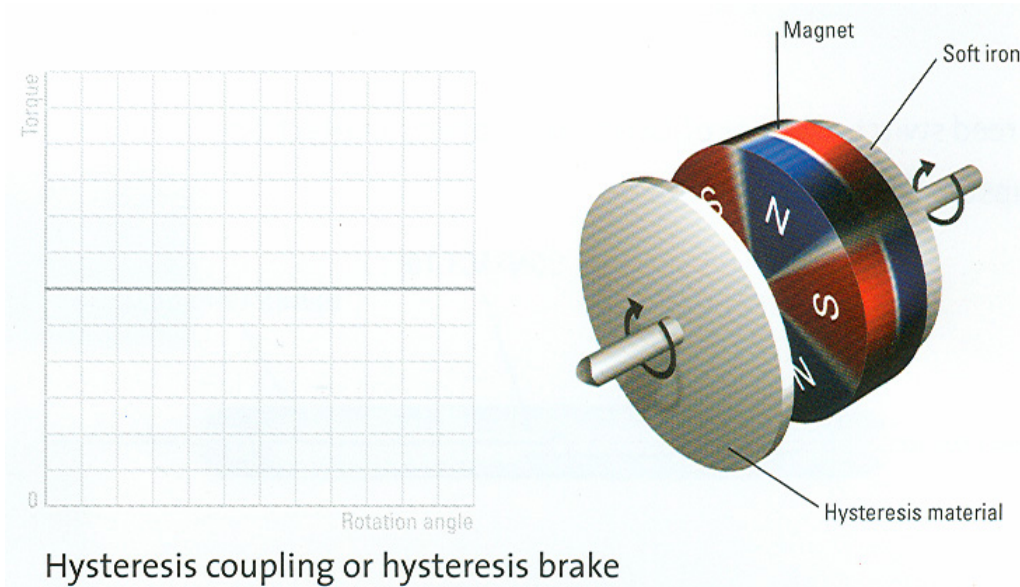


Tahometer



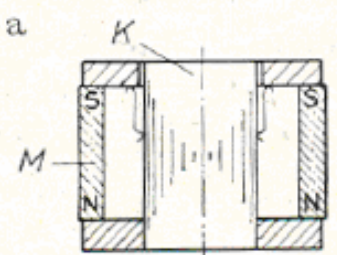
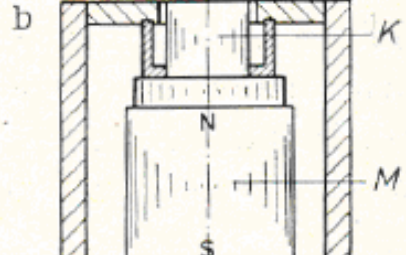
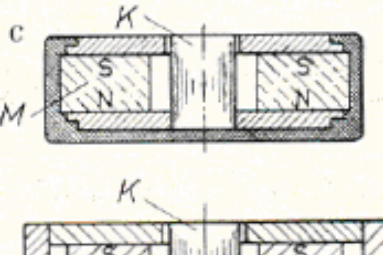
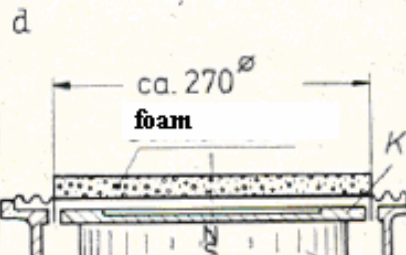
$$M_{\max} \propto R^2 B_L^2 / \rho$$

Hysteresis couplings

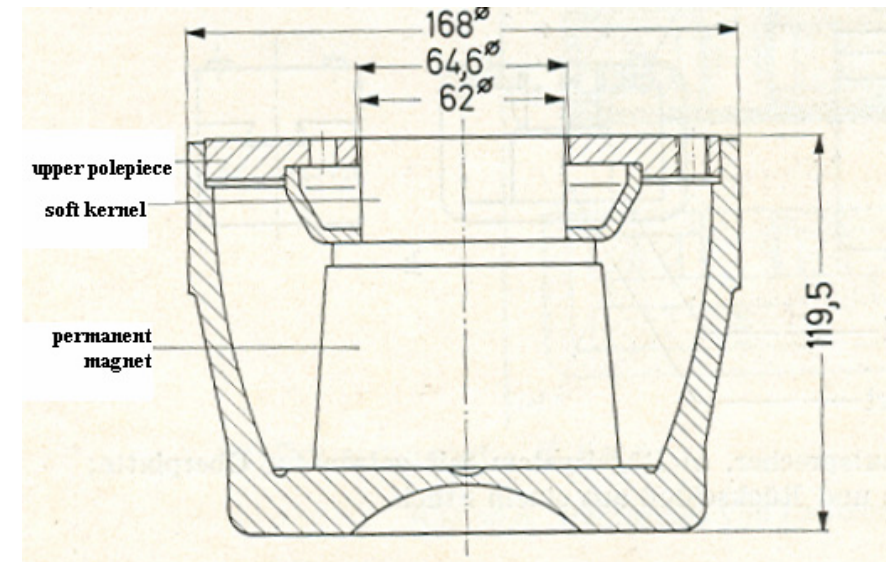


$$M \sim pV_{hyst} \int H dB$$

Loudspeaker

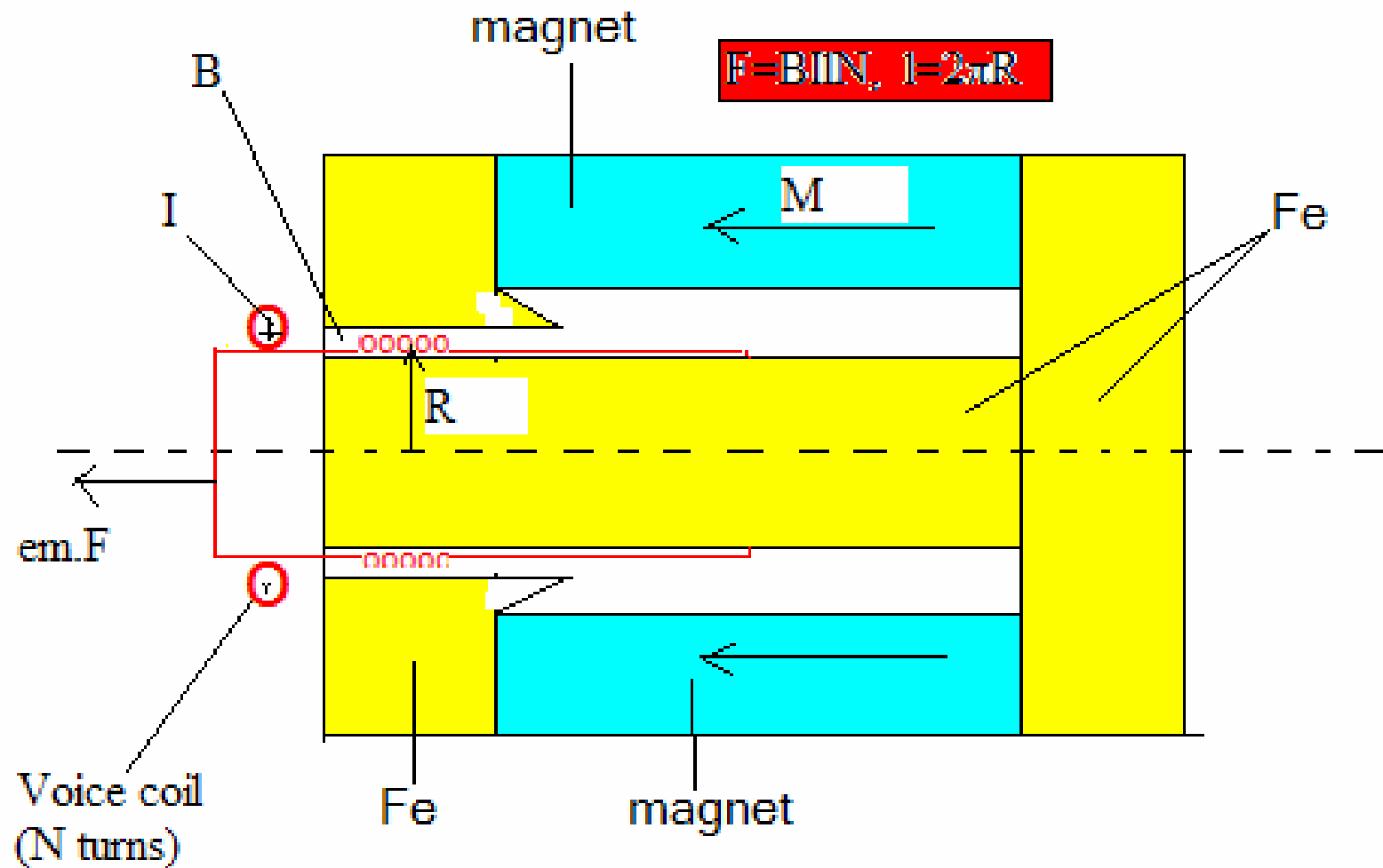
Magnetic material	system	
	external magnet	central magnet
Al Ni Co	a 	b 
hard ferrite	c  d 	

M: permanent magnet
K: soft kernel

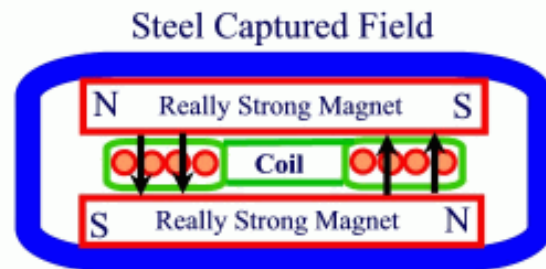


$$W_g = \frac{1}{2} (B_m H_m) V_m \frac{1}{\gamma \sigma}$$

Voice coil motors

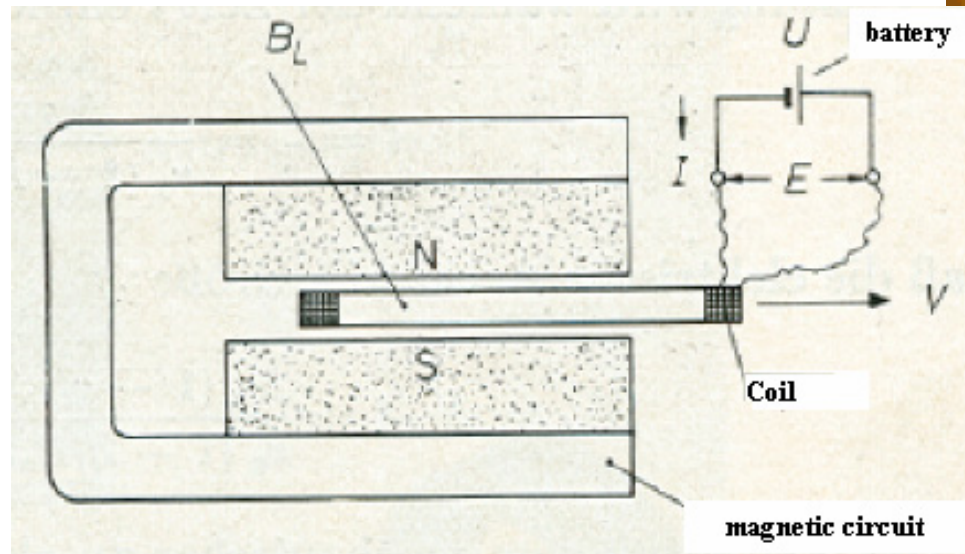
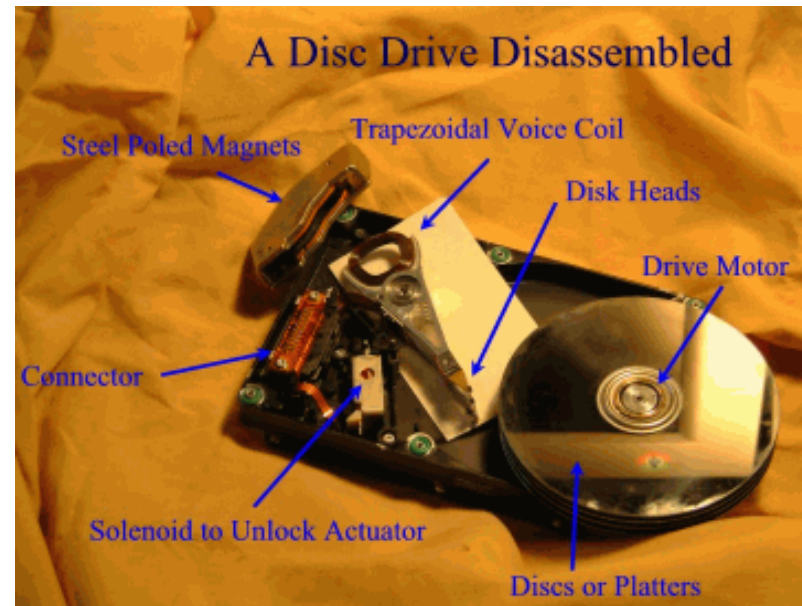


Voice coil motors



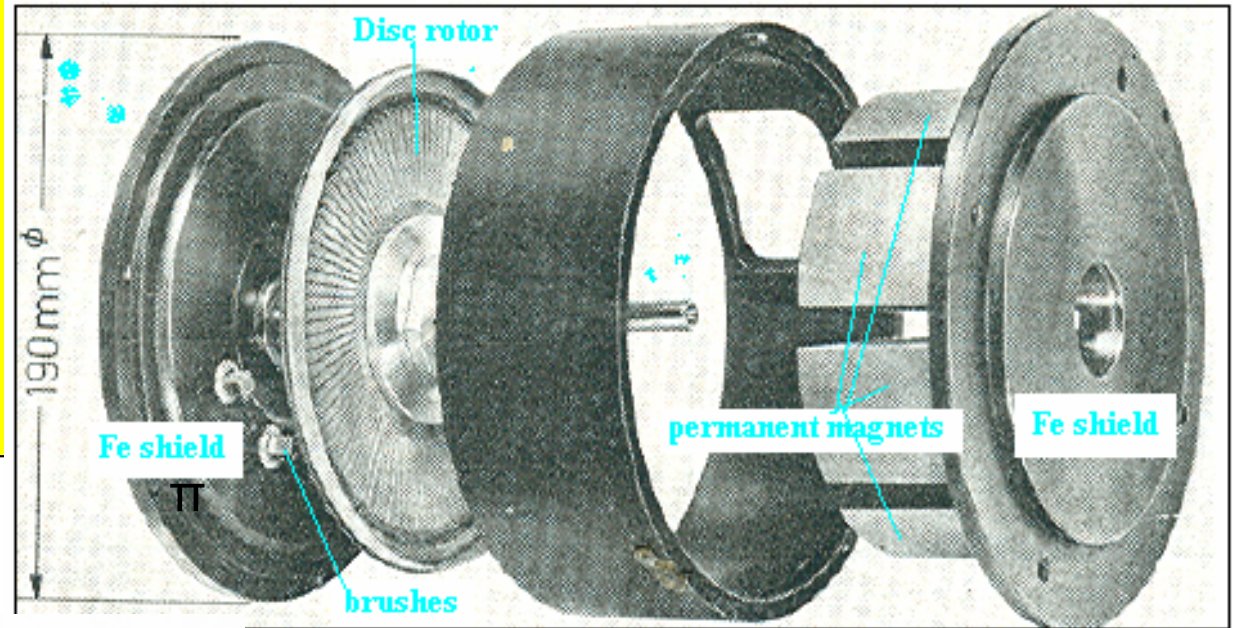
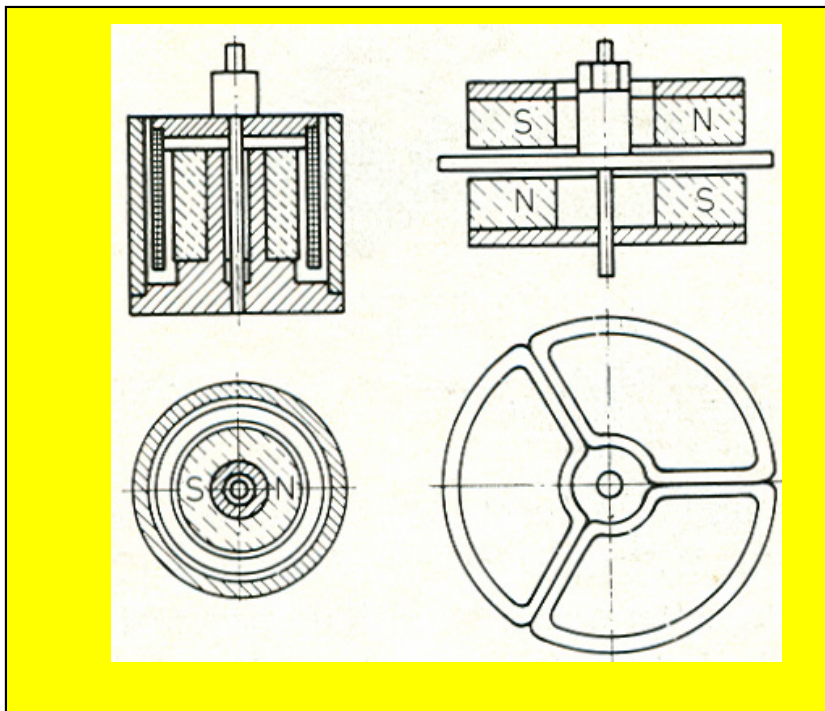
Current Comes Out on Left and In on Right Side of Flat Coil
Force Goes Right in Both Cases, Causing Coil to Move Right

Reverse the Current and Coil Moves Left



The world's smallest hard disk drive

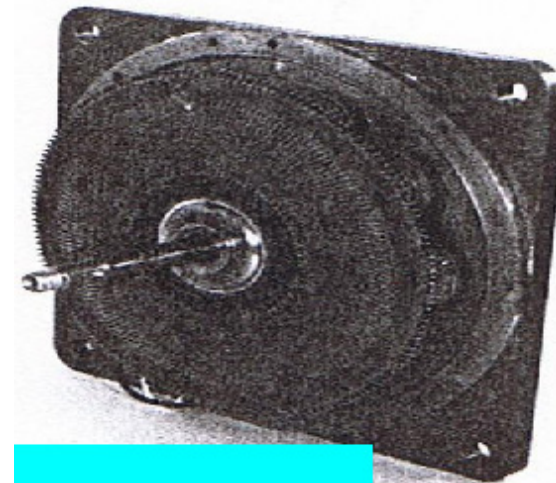
Motors with Nonferrous rotors



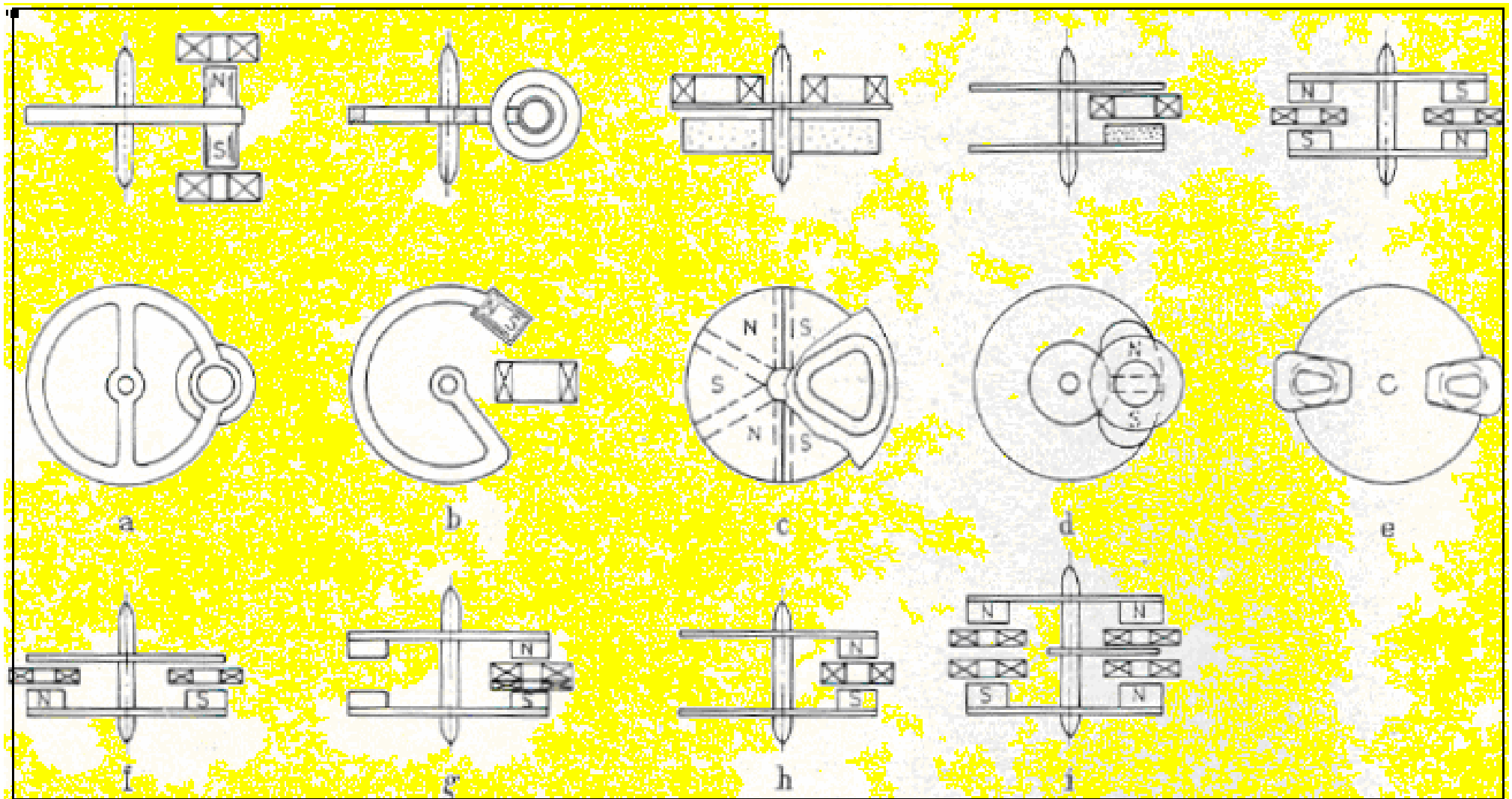
SEA/France



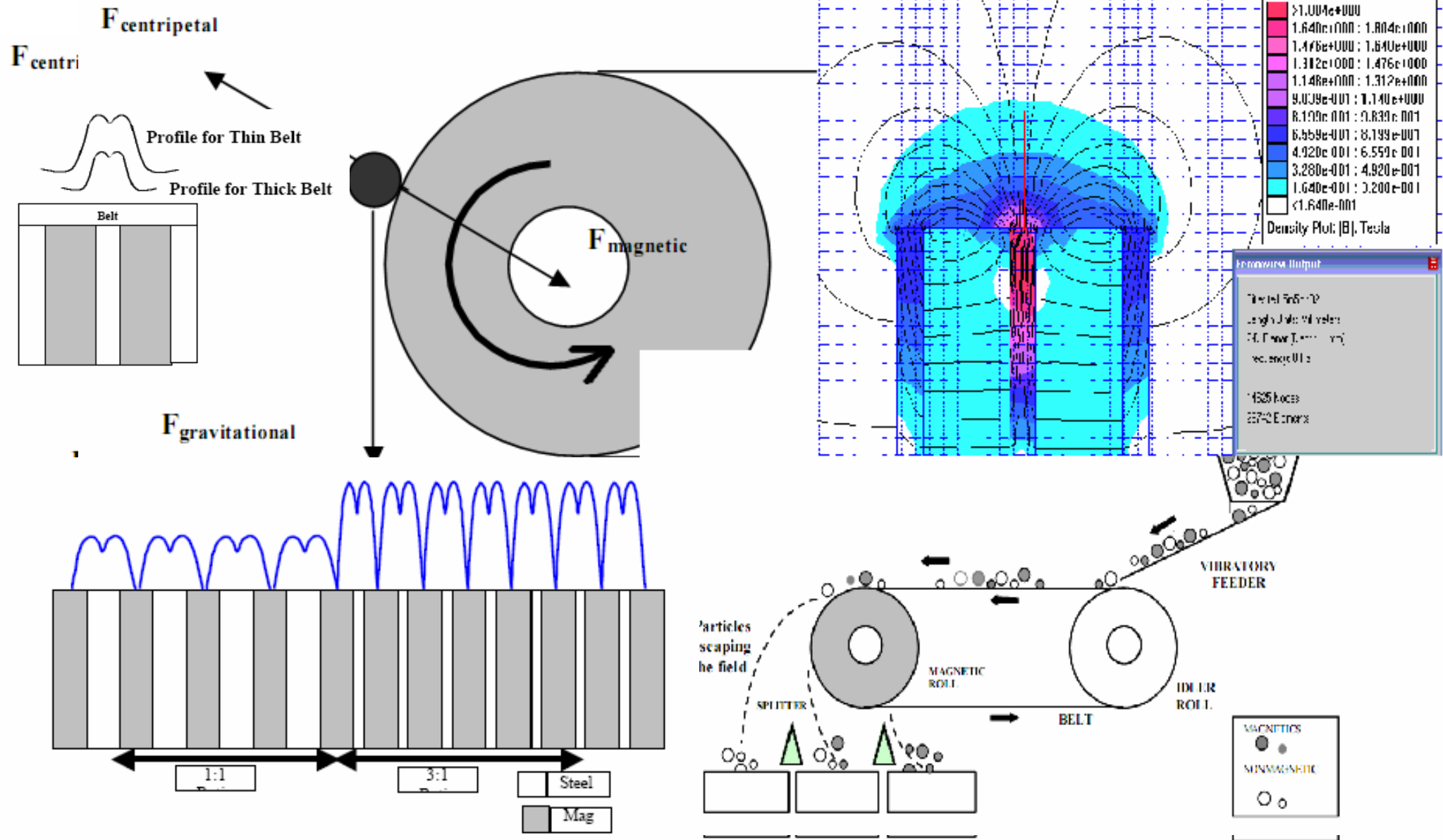
ICPE-1980



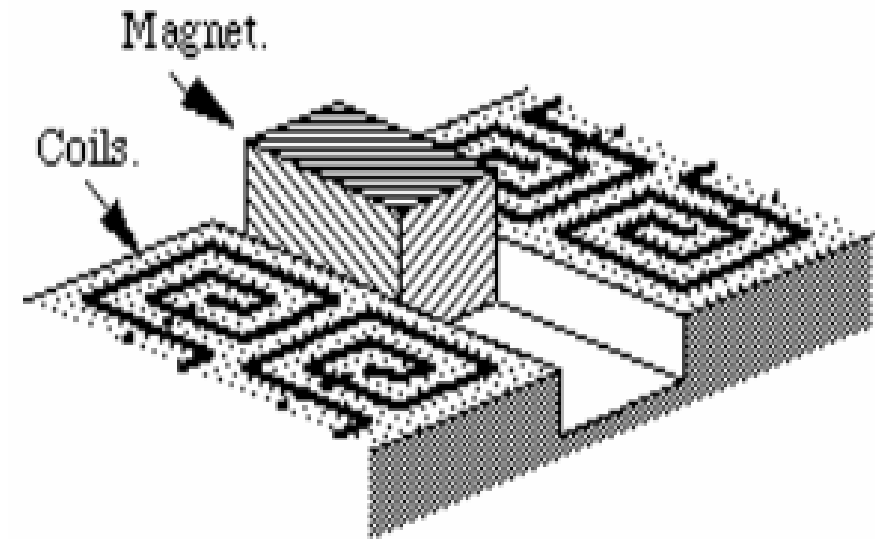
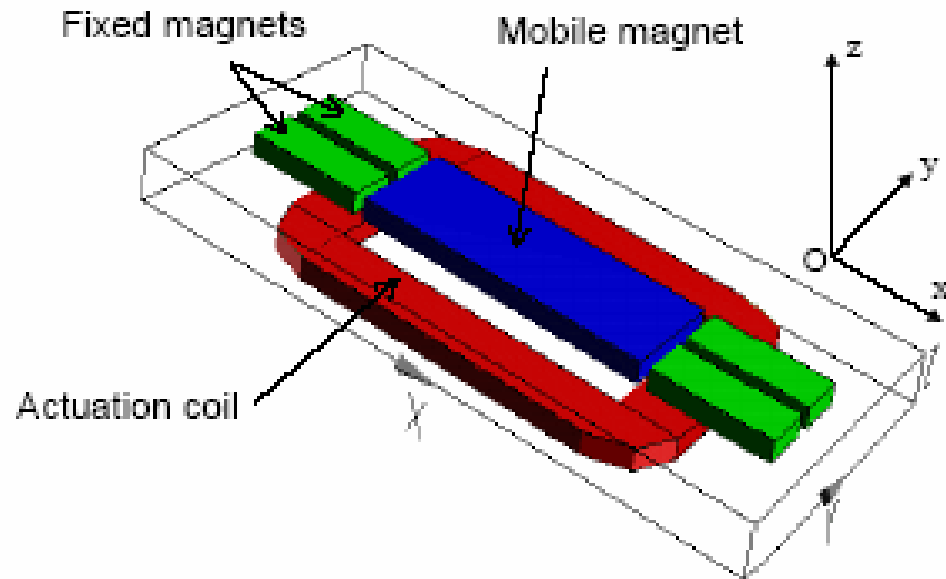
Watches



Magnetic separators



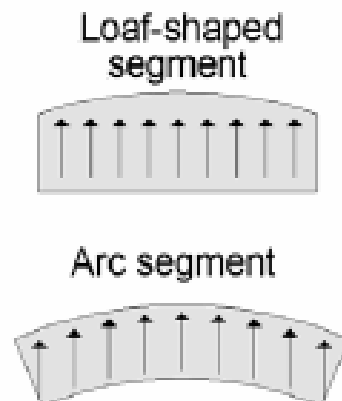
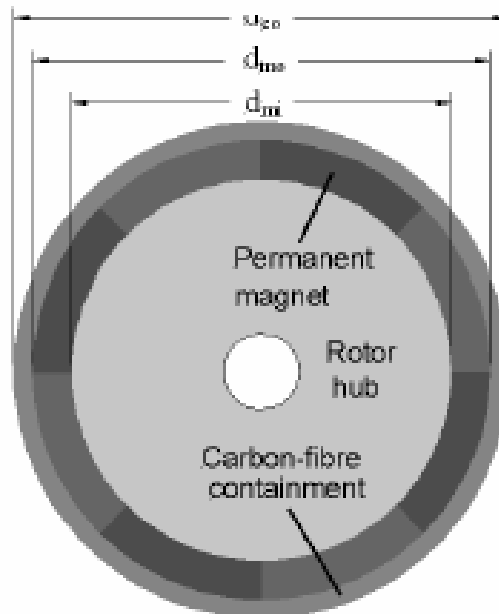
Actuators with PM



High speed motors

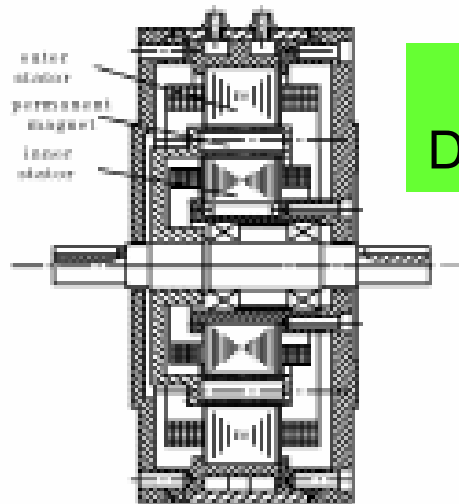
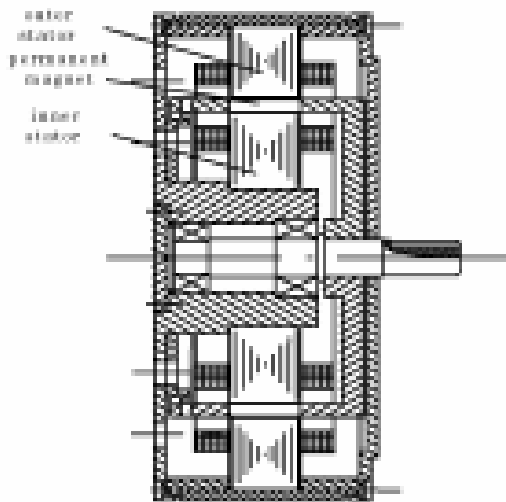
Rotor poles	8
Rotor outer diameter	145mm
Magnet thickness at centre	10mm
Containment thickness	7.8mm
Permanent magnet material (NdFeB)	NdFeB (Neomag 31VC)
Magnet segment axial length	2×45mm

Stator teeth	12
Stator bore diameter	149mm
Slot opening to tooth pitch ratio	0.5
Stator core outer diameter	225mm
Stator slot depth	25mm
Stator core axial length	90mm
Stator core material grade (Silicon Iron)	NO20 (0.2mm)



G. W. Jewell, 2002, UK

PM motors

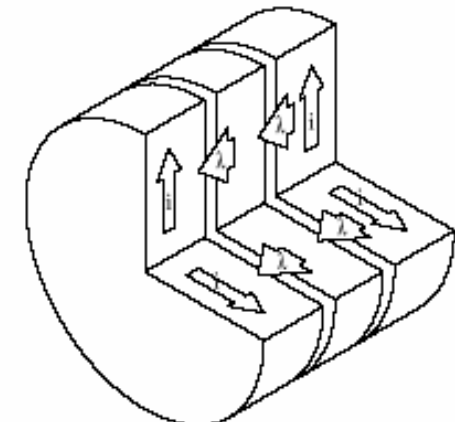
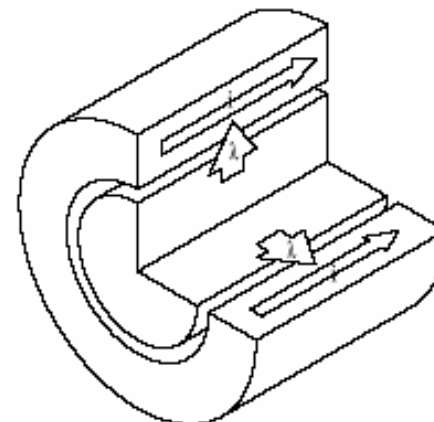


Double Stator Motor

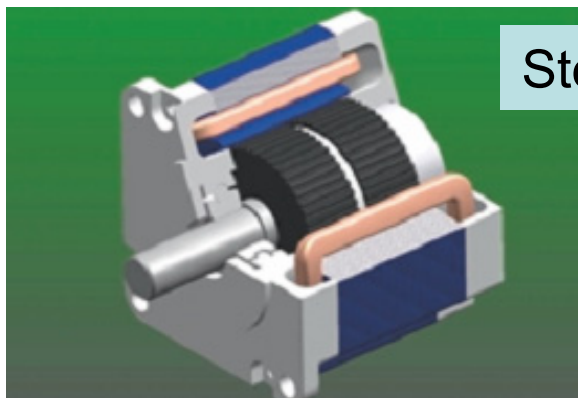
Flux Directions

Radial

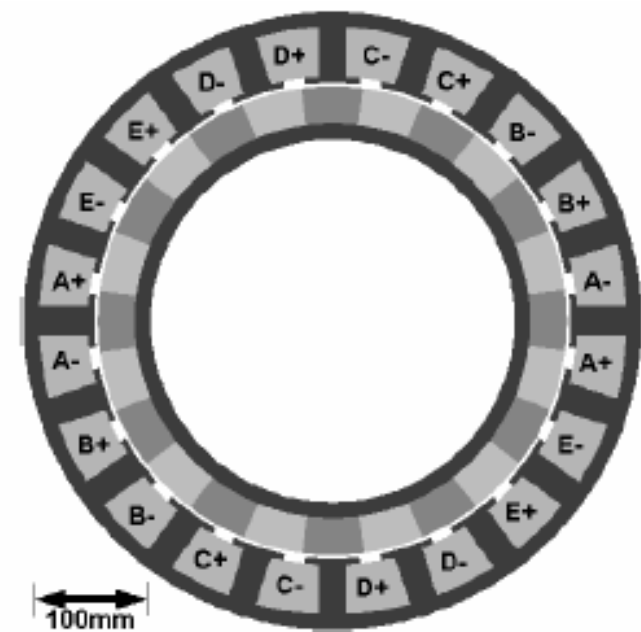
Axial



Stepper Motor



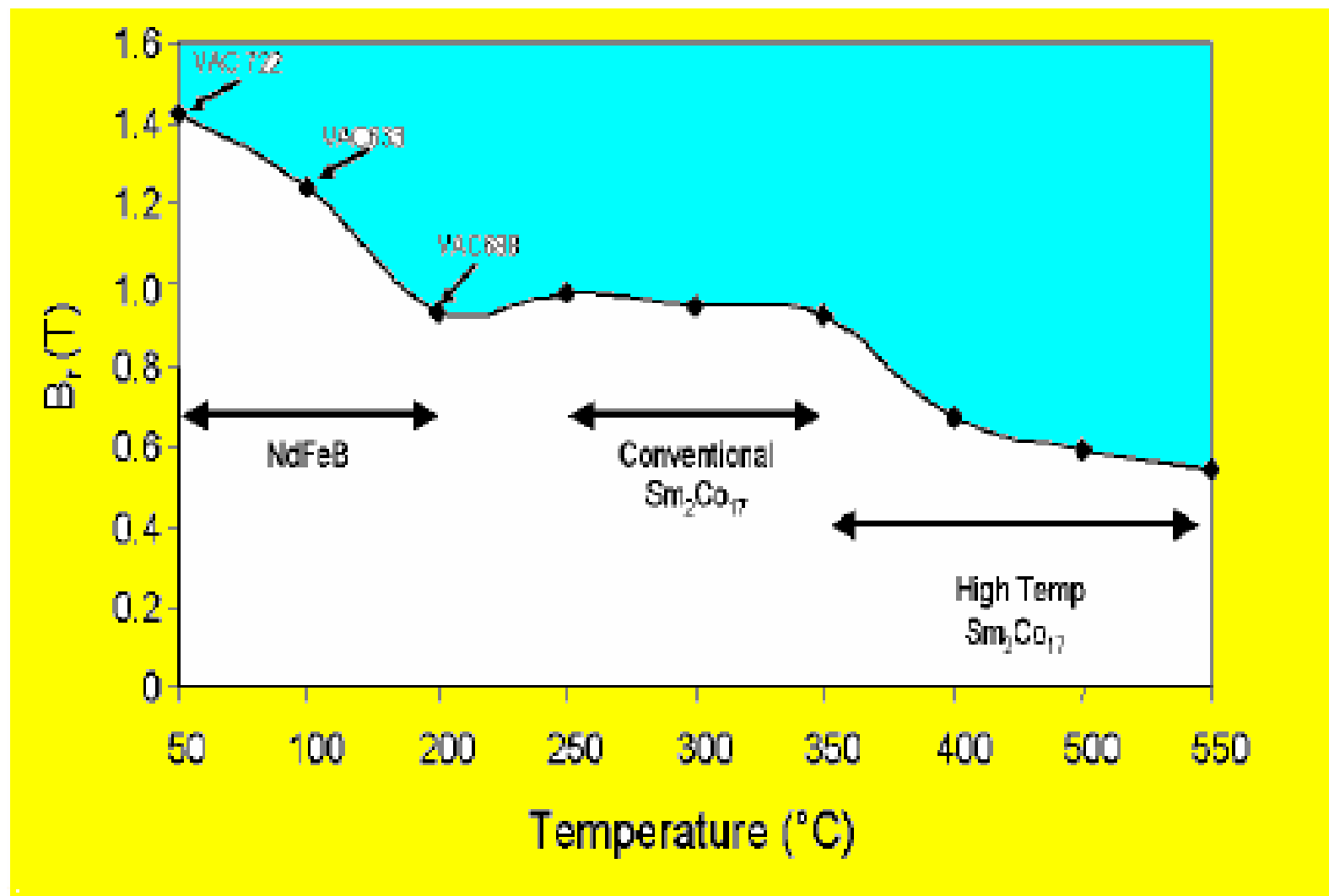
250 kW Generator



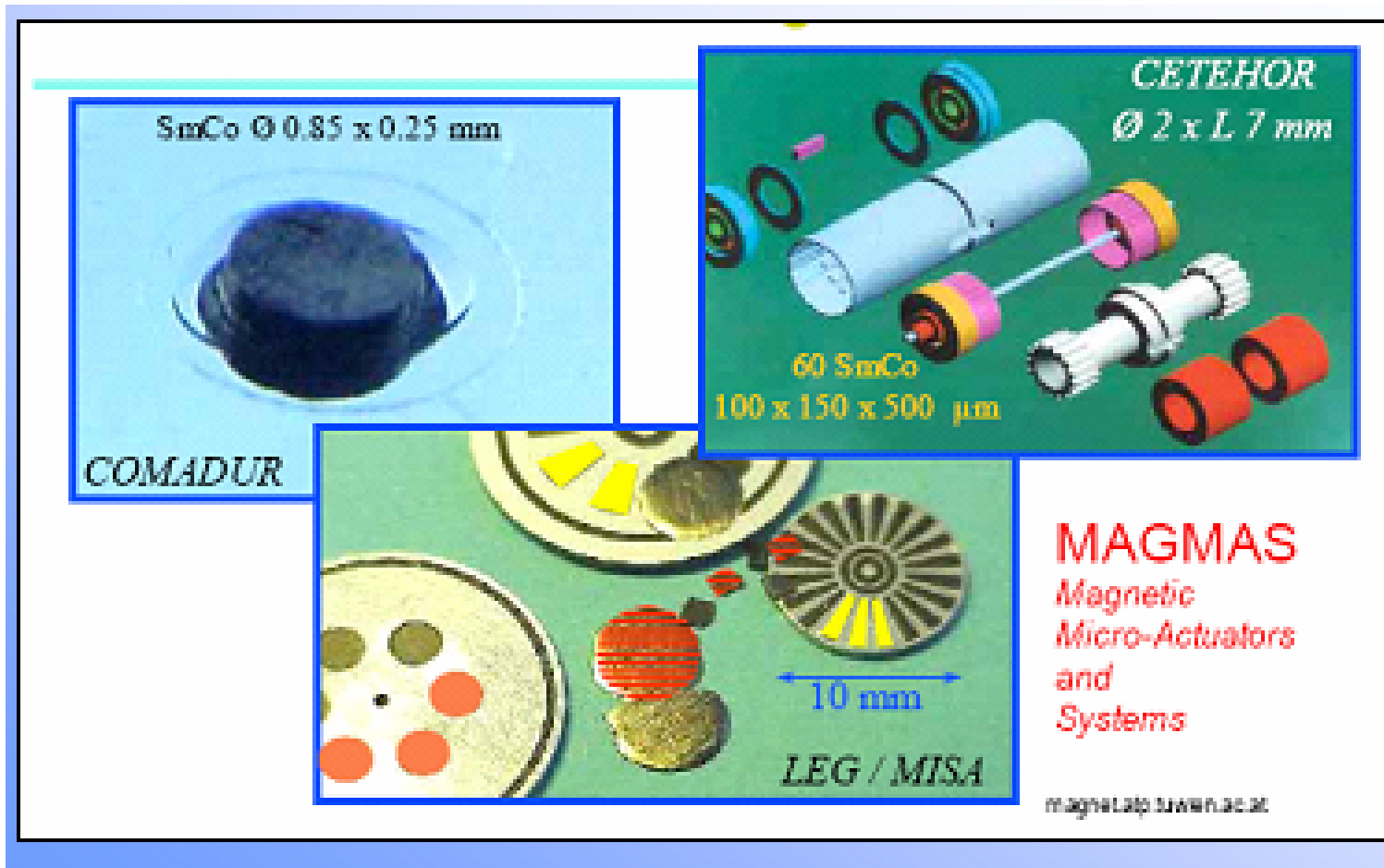
Phases	5
Slots	20
Pole-pairs	12
Stator outer diameter	540 mm
Stator bore diameter	416 mm
Mechanical airgap	3 mm
Magnet radial thickness	32 mm
Rotor inner diameter	317 mm
Active length	190 mm
Stator and rotor core material	49% Cobalt Iron laminations
Magnet	$\text{Sm}_2\text{Co}_{17}$ (Arnold S3-225)
Magnet mass	60.6 kg
Lamination mass	76.8 kg
Copper mass	43 kg
Overall mass of active components	202.9 kg

G. W. Jewell, 2002, UK

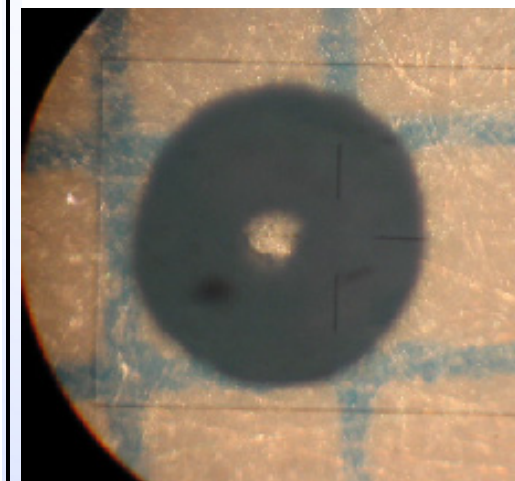
Very high temperature motors



Micromagnets

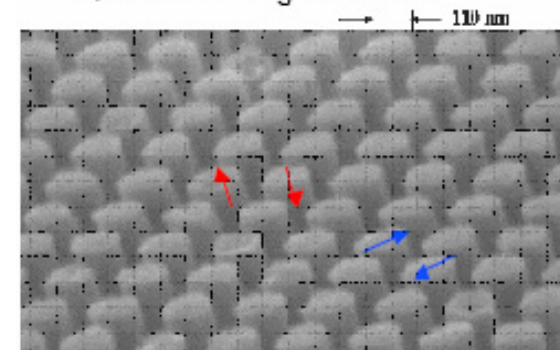


PM for e.m. watch



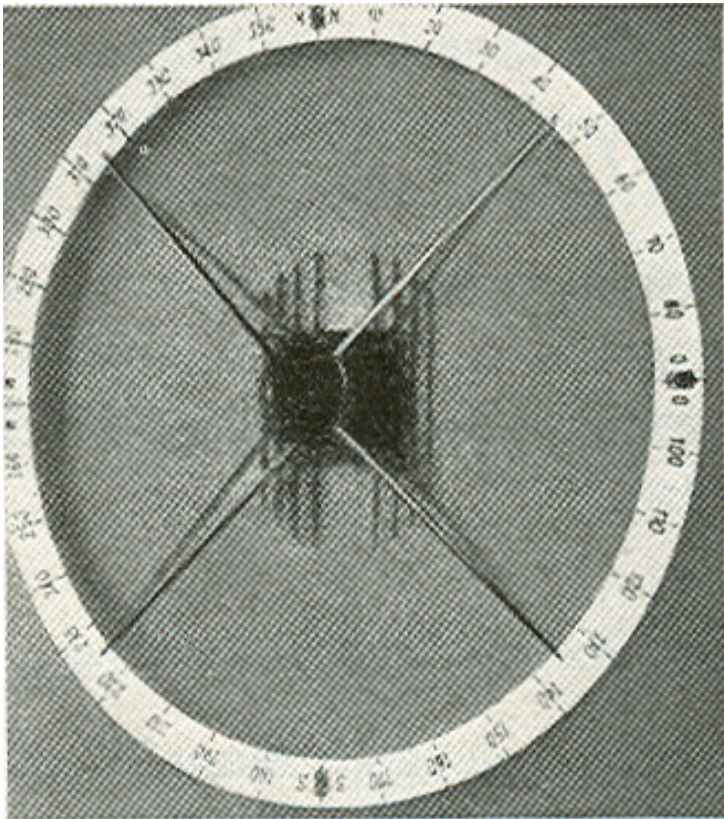
ICPE-1982

Quantized magnetic disk

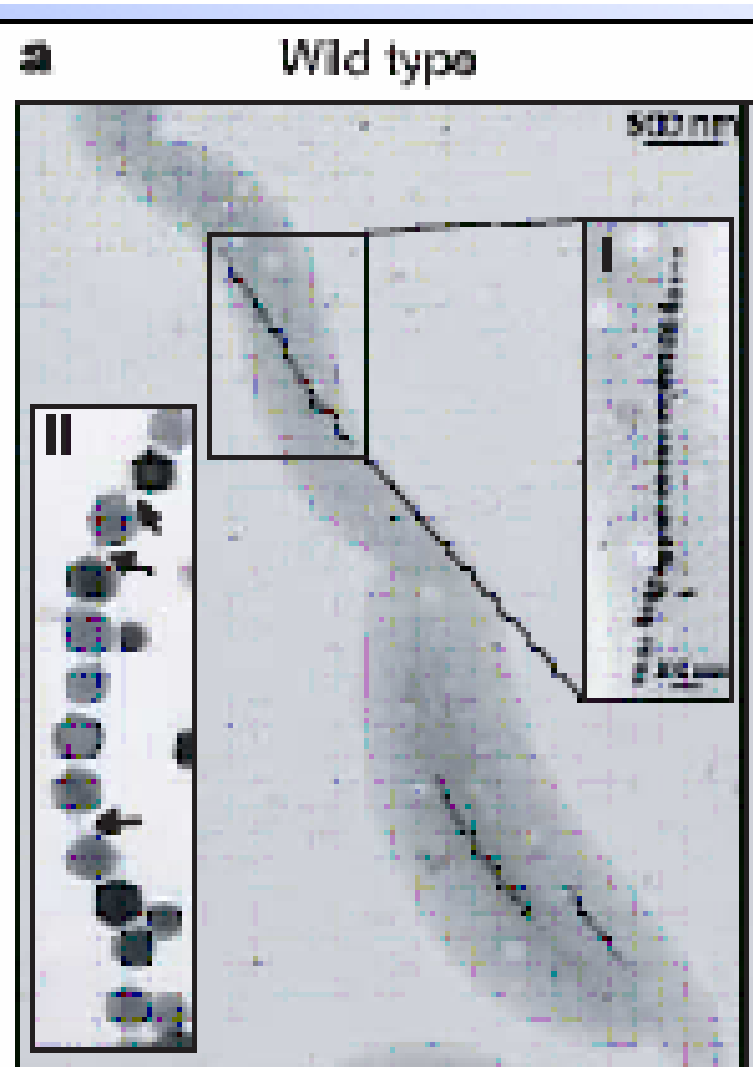


S Chou, J. Vac. Sci. Techn. B16 (1998) 3825.

Magnetic orientation

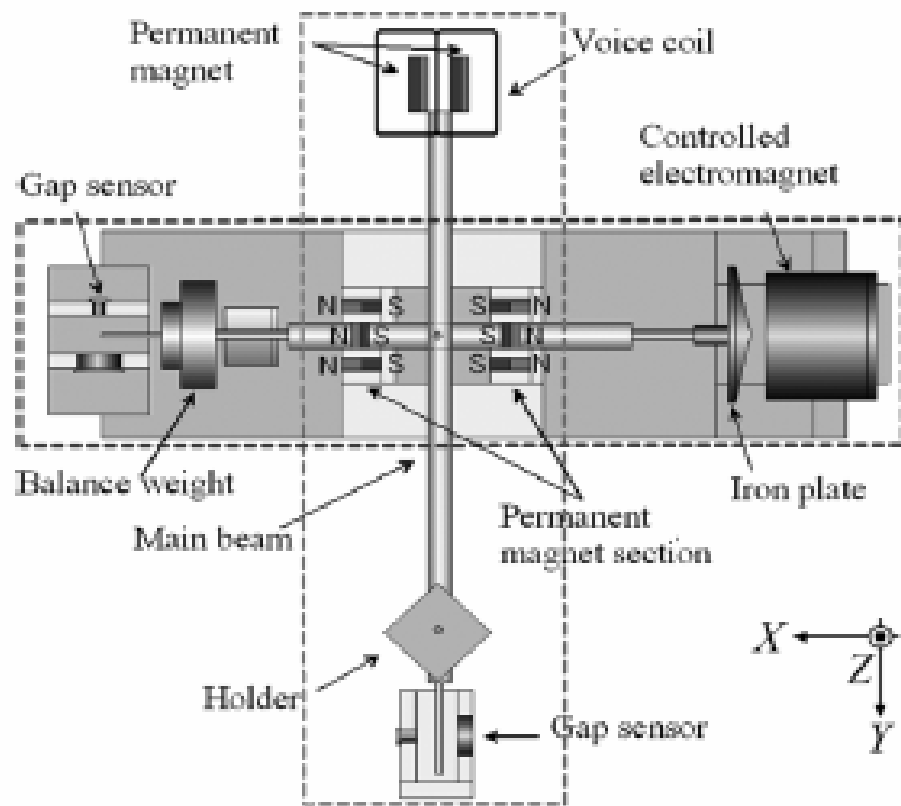


Magnetic navy compass



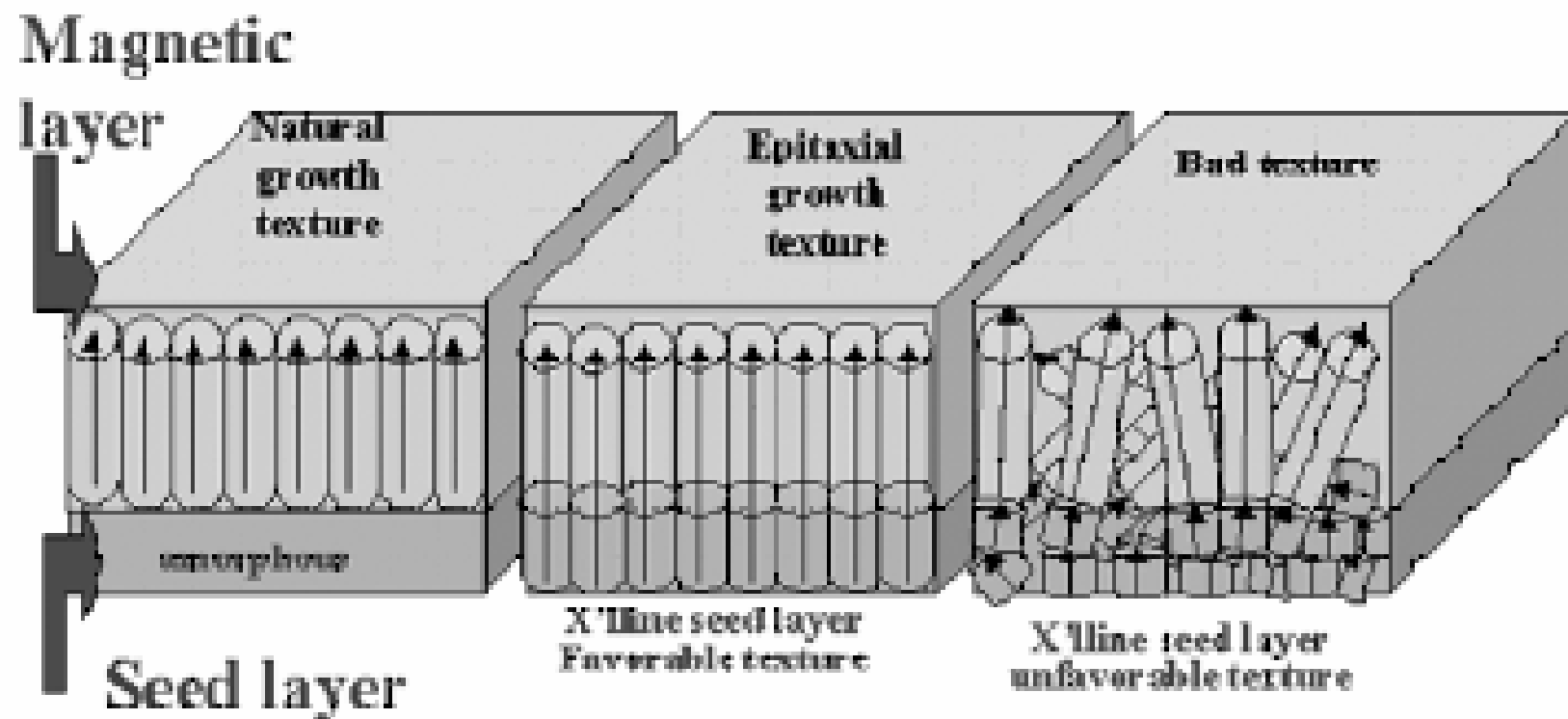
Magnetotactic
bacteria

Measuring Equipment

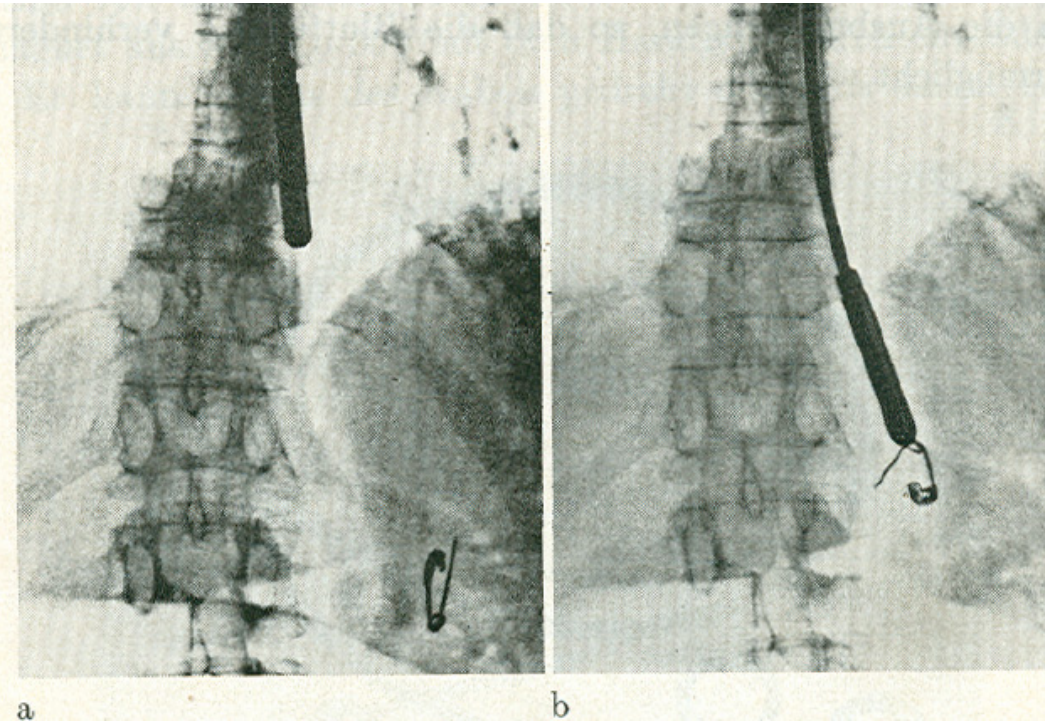


Dipole magnet with a diameter of 1.5 m in the „Alpha Magnetic Spectrometer“ particle detector (about 5000 rectangular magnets).

Magnetic recording



Medical Applications



Magnetic Resonance Imaging



Many thanks to



Eros Patroi



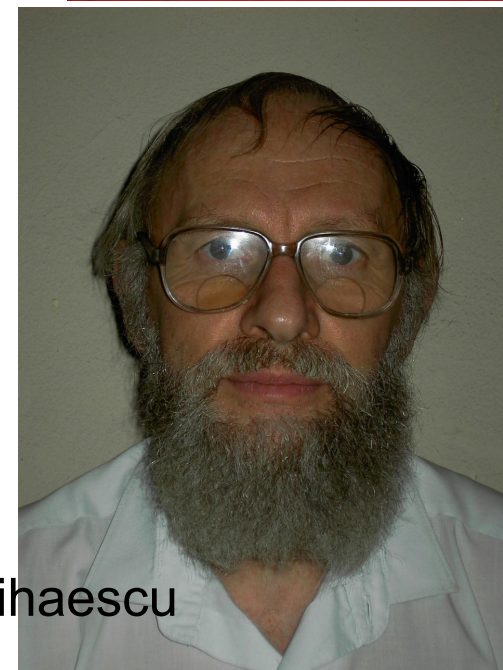
Mircea Ignat



Mirela Codescu



Iulian Iordache



Mihai Mihaescu

