

Introduction to Magnetism (2) : Magnetism today or

How performs the micromagnetic theory now?

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CENTRE NATIONAL
DE LA RECHERCHE
SCIENTIFIQUE



1- Introduction

2 - Micromagnetic theory and applications

statics

domain walls

dynamics

3 - Micromagnetics of nano-elements

macrospin limit

quasi-uniform structures

dynamics

4 - Beyond micromagnetics

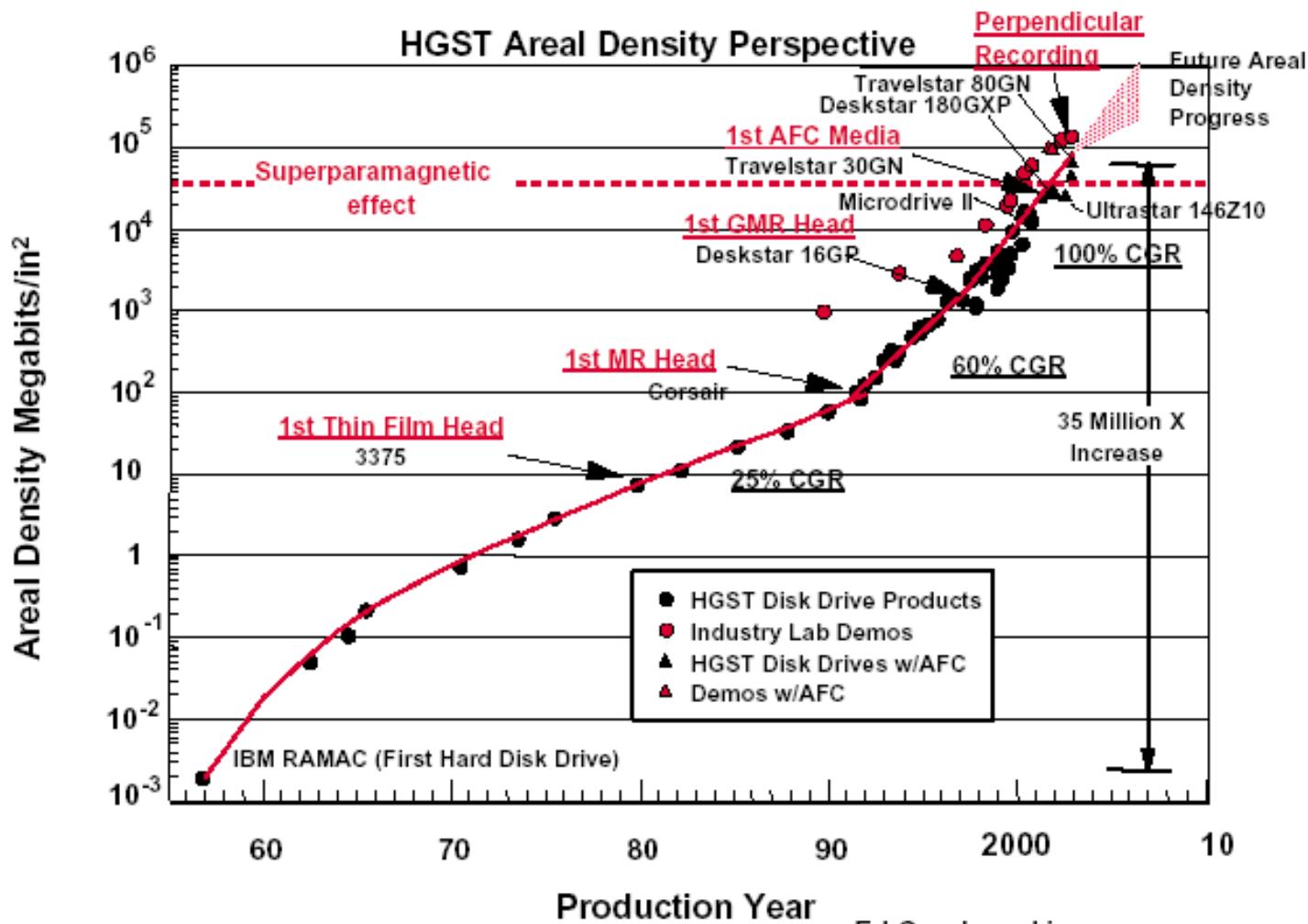
molecular magnetism

clusters of a few atoms

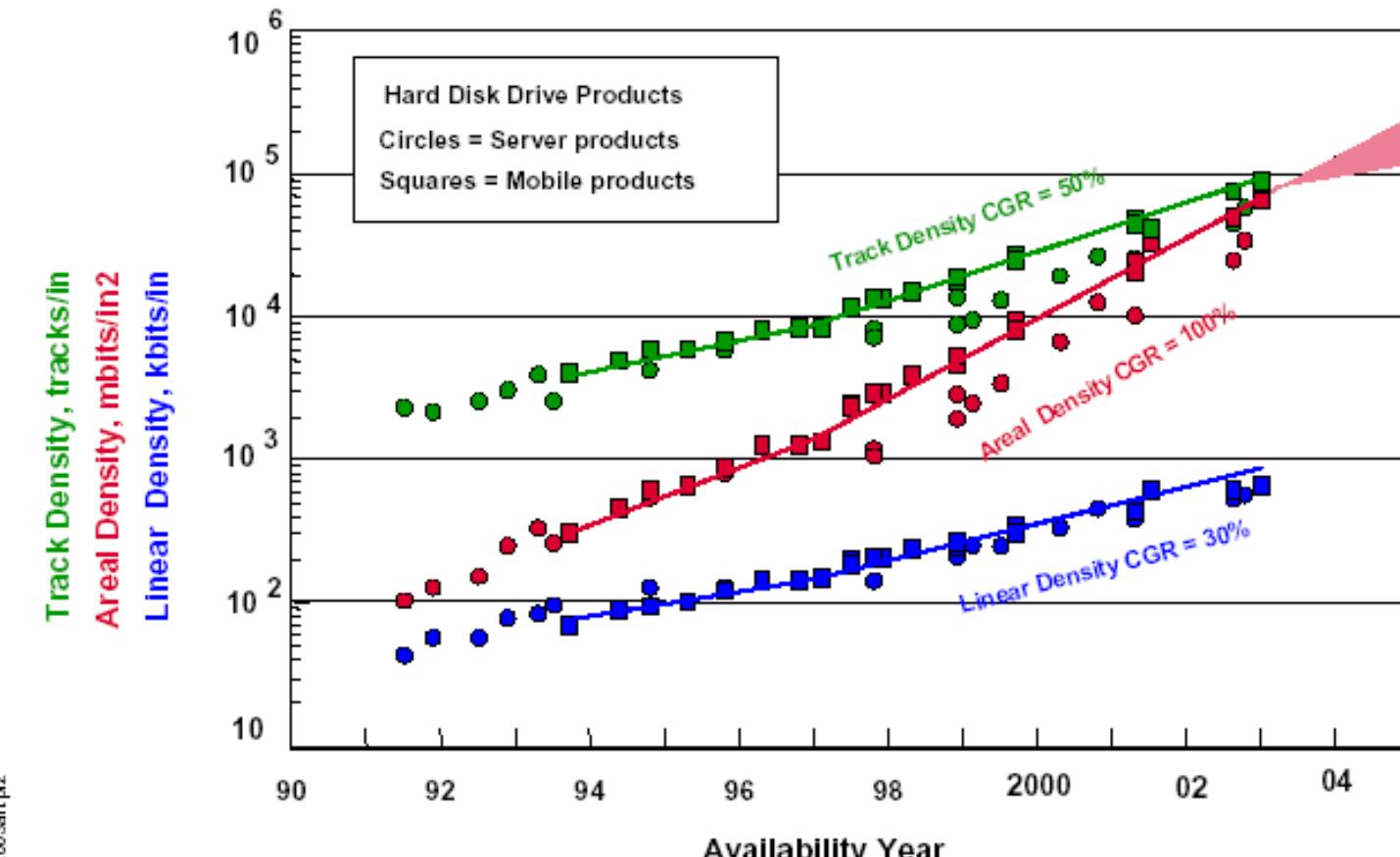
spin-polarized transport

Nanometric size structures are already used

HITACHI
Inspire the Next



Track, Areal, Linear Density Perspective

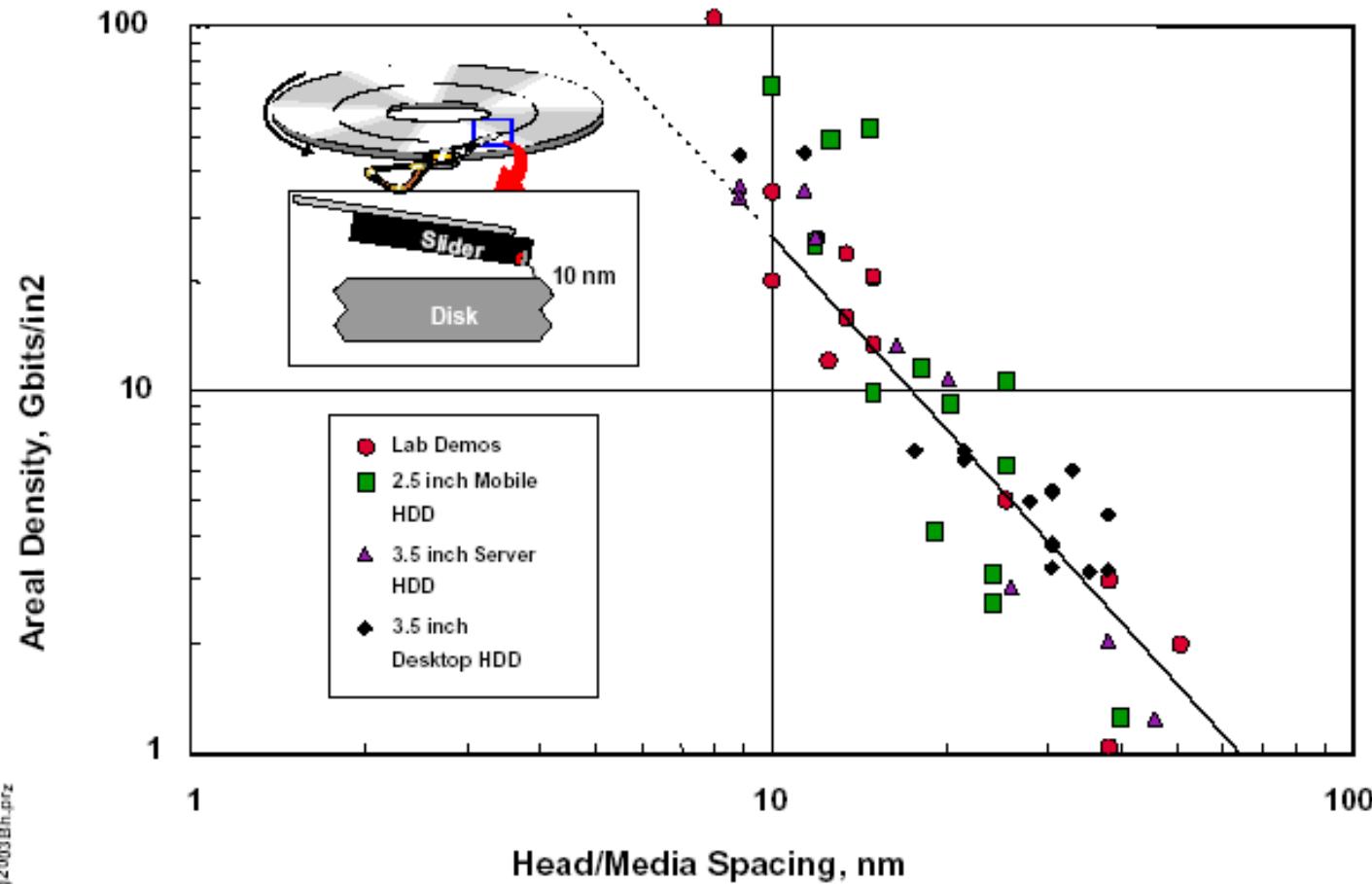


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Spacing-Areal Density Perspective



Spacings2003Bh.ppt2

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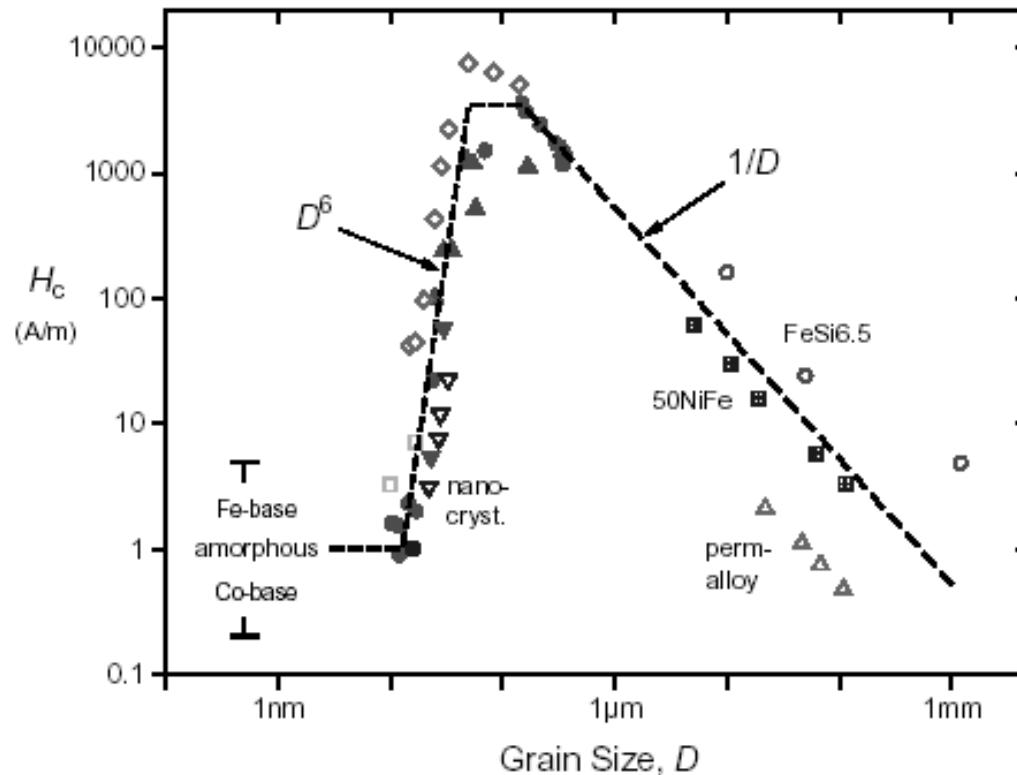


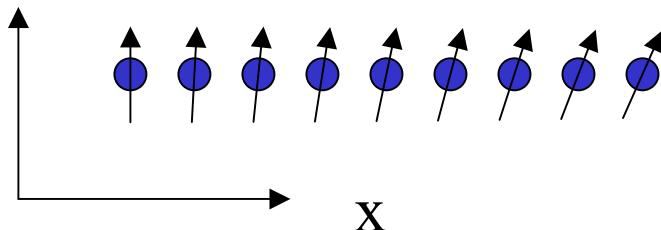
Figure 1. Coercivity, H_c , vs. grain size, D , for various soft magnetic metallic alloys (after [8,9]): Fe-Nb₃Si_{13.5}B₉ (solid up triangles), Fe-Cu₁Nb_{1.3}Si_{13.5}B₉ (solid circles), Fe-Cu₁V_{3.6}Si_{12.5}B₈ (solid down triangles), Fe-Cu₁V_xSi_{19-x}B₈ (open down triangles), Fe-Cu_{0.1}Zr_{0.7}B_{2.6} (open squares), Fe₆₀Co₃₀Zr₁₀ (open diamonds), NiFe-alloys (+ center squares and open up triangles) and FeSi6.5wt% (open circles).

G. Herzer, Amorphous and nanocrystalline Soft magnets, in
 Magnetic hysteresis in novel materials, G.C. Hadjipanayis Ed., Nato ASI E338
 (Kluwer, Dordrecht, 1997)

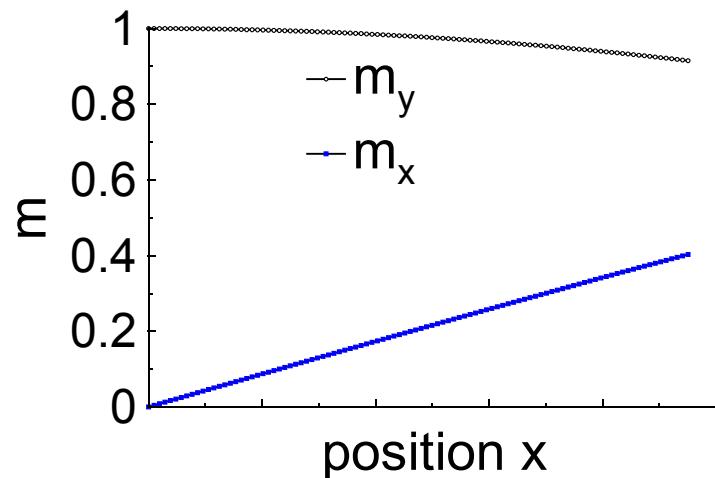
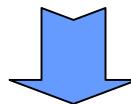
"Standard" Micromagnetics

The “micromagnetic” description of magnetism

y



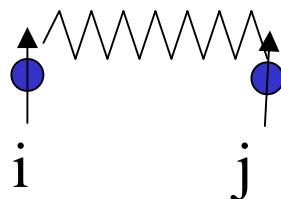
atomic spins



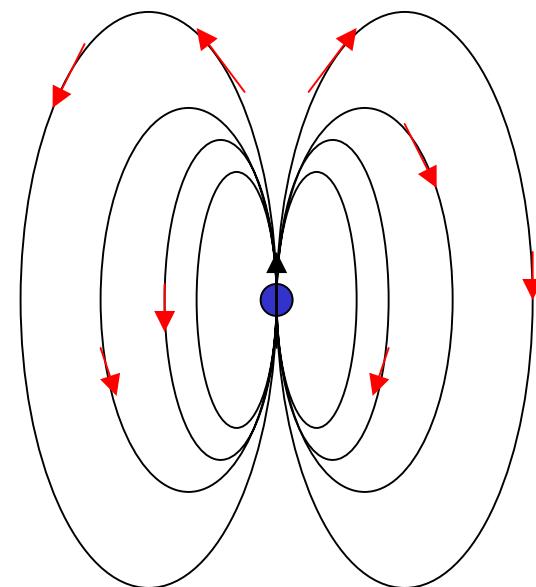
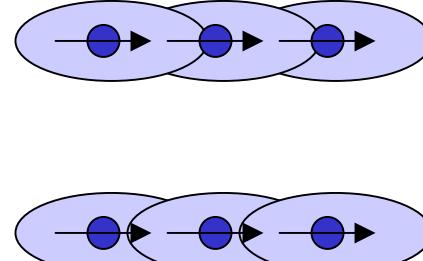
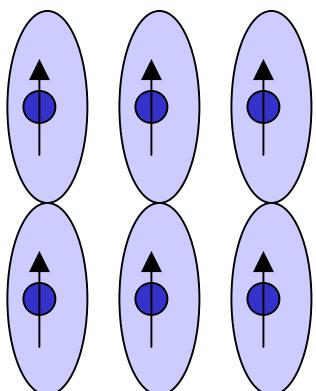
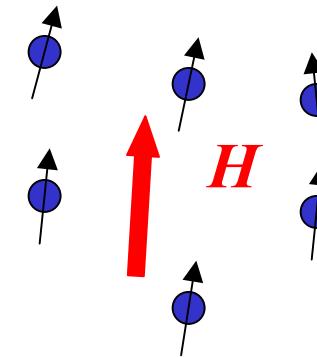
continuous distribution

Assumes that structures to describe are large compared to atomic sizes

Magnetic Interactions



$$E = -J \vec{S}_i \cdot \vec{S}_j$$



Micromagnetic equations

$$\vec{M} = M_s(T) \vec{m} \quad |\vec{m}| = 1 \quad \text{no thermal fluctuations}$$

$$E = A(\vec{\nabla} \vec{m})^2 + K \vec{G}(\vec{m}) - \mu_0 M_s \vec{m} \cdot \vec{H} - \frac{1}{2} \mu_0 M_s \vec{m} \cdot \vec{H}_D$$

/ exchange \ anisotropy \ applied field \ demagnetizing field

Statics : minimise $\int E$ \rightarrow Brown equations

+ boundary conditions

$$\vec{H}_{eff} \times \vec{m} = \vec{0}$$

$$\frac{\partial \vec{m}}{\partial \vec{n}} = \vec{0}$$

effective
field

$$\vec{H}_{eff} = \vec{H}_{applied} + \vec{H}_{demag} + \vec{H}_{aniso} + \vec{H}_{exchange}$$

$$\boxed{\vec{H}_{eff} = -\frac{1}{\mu_0 M_s} \frac{\delta \vec{E}}{\delta \vec{m}}}$$

$$\downarrow$$

$$\frac{2A}{\mu_0 M_s} \Delta \vec{m}$$

Magnetostatics of matter

$$\vec{B} = \mu_0 (\vec{H} + \vec{M}) \quad \text{with} \quad \operatorname{div} \vec{B} = 0 \quad \text{and} \quad \overrightarrow{\operatorname{rot}} \vec{H} = \vec{j}$$

$$\begin{cases} \operatorname{div} \vec{H}_D = -\operatorname{div} \vec{M} \\ \overrightarrow{\operatorname{rot}} \vec{H}_D = \vec{0} \end{cases} \quad \begin{cases} \operatorname{div} \vec{H}_{ext} = 0 \\ \overrightarrow{\operatorname{rot}} \vec{H}_{ext} = \vec{j}_{ext} \end{cases}$$

+ boundary conditions

$$(\vec{H}_D^{ext} - \vec{H}_D^{int}) \cdot \vec{n} = \vec{M} \cdot \vec{n}$$

$$(\vec{H}_D^{ext} - \vec{H}_D^{int}) \cdot \vec{t} = 0$$

demagnetizing field

applied field

Magnetostatic energy

$$E_D = -\frac{1}{2} \mu_0 \int_V \vec{M} \cdot \vec{H}_D = \frac{1}{2} \mu_0 \int_{R^3} (\vec{H}_D)^2 \geq 0$$

proof : introduce the scalar potential $\vec{H}_D = -\vec{\nabla}\phi$

$$\Delta\phi = \operatorname{div}\vec{M} \quad \phi = -\frac{1}{4\pi} \int_V \frac{\operatorname{div}\vec{M}}{|\vec{r} - \vec{r}'|} + \frac{1}{4\pi} \int_{\partial V} \frac{\vec{M} \cdot \vec{n}}{|\vec{r} - \vec{r}'|}$$

and transform by integration by parts both expressions into

$$\frac{1}{2} \mu_0 \int_{\partial V} (\vec{M} \cdot \vec{n})\phi - \frac{1}{2} \mu_0 \int_V \operatorname{div}\vec{M}\phi$$

Characteristic lengths

$$\Delta = \sqrt{\frac{A}{K}}$$

Bloch wall width parameter

$$A = 10^{-11} \text{ J/m}, K = 10^2 - 10^5 \text{ J/m}^3$$

$$\Delta = 1 - 100 \text{ nm}$$

$$\Lambda = \sqrt{\frac{2A}{\mu_0 M_s^2}}$$

exchange length

$$M_s = 10^6 \text{ A/m}$$

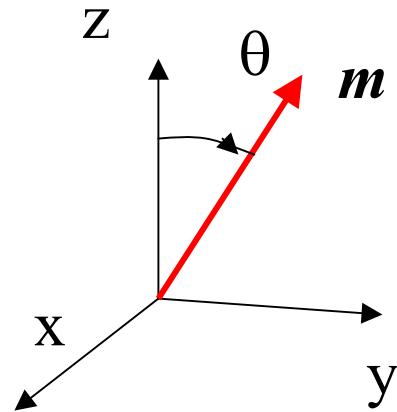
$$\Lambda = \text{some nm}$$

$$Q = \frac{2K}{\mu_0 M_s^2} = \left(\frac{\Lambda}{\Delta} \right)^2$$

Quality factor

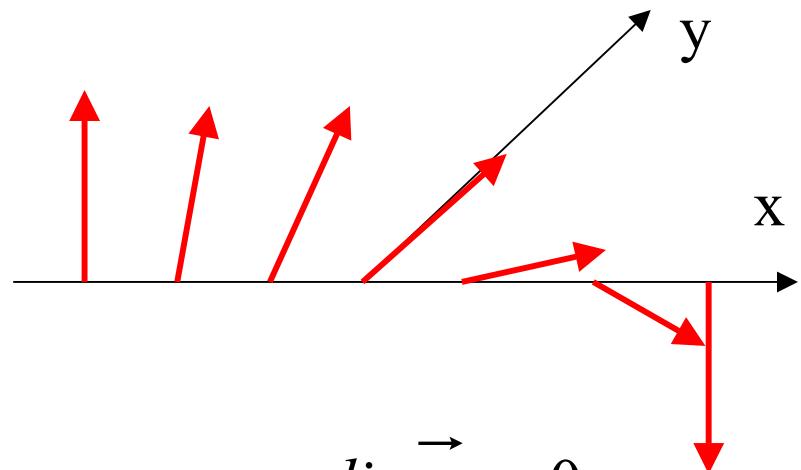
$Q > 1$ hard material
 $Q \ll 1$ soft material

Easy axis



$$\vec{m} = \begin{pmatrix} 0 \\ \sin \theta(x) \\ \cos \theta(x) \end{pmatrix}$$

The Bloch wall (1932)



No demag energy

$$\vec{\operatorname{div}} \vec{m} = 0$$

$$E = A \left(\frac{d\theta}{dx} \right)^2 + K \sin^2 \theta$$

$$\theta(-\infty) = 0, \quad \theta(+\infty) = \pi$$

Energy minimization
equation

$$-2A \frac{d^2\theta}{dx^2} + 2K \sin \theta \cos \theta = 0$$

$$\times \frac{d\theta}{dx} \text{ and } \int dx$$



First integral

$$-A \left(\frac{d\theta}{dx} \right)^2 + K \sin^2 \theta = C^{st} = 0$$

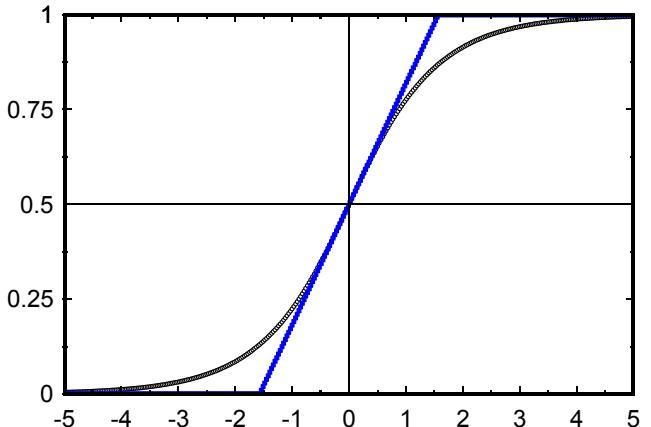
$$\frac{d\theta}{dx} = \pm \frac{\sin \theta}{\Delta}$$

$$\boxed{\Delta = \sqrt{\frac{A}{K}}}$$

$$\theta = 2 \operatorname{Atan} \left[\exp \left(\frac{x - x_0}{\Delta} \right) \right] (+ \pi)$$

Linear width : $\pi \Delta$

Bloch wall width parameter



Properties of the Bloch wall

$$\text{Integrated exchange energy} = \frac{2A}{\Delta} = 2\sqrt{AK}$$

$$\text{Integrated anisotropy energy} = 2K\Delta = 2\sqrt{AK}$$

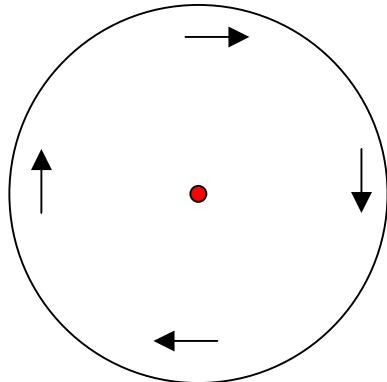
Integrated hard axis component $\int m_y dx = \int \sin \theta dx = \Delta \int d\theta = \pi \Delta$

$$\int m_y^2 dx = \int \sin^2 \theta dx = \Delta \int \sin \theta d\theta = 2 \Delta$$

etc.

The vortex

2D magnetization

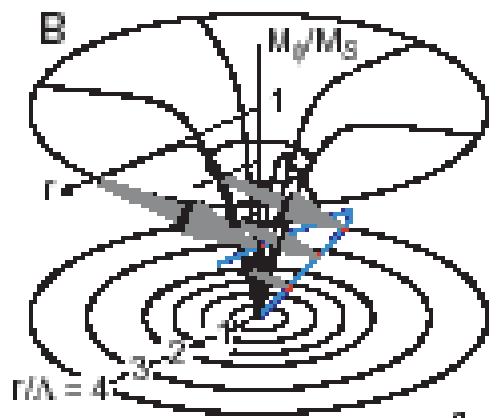


$$\vec{m} = \begin{pmatrix} y/r \\ -x/r \\ 0 \end{pmatrix} \quad \left\{ \begin{array}{l} \operatorname{div} \vec{m} = 0 \\ \vec{m} \cdot \vec{n} = 0 \end{array} \right.$$

Divergence of the exchange energy

$$E_{ech} = A (\vec{\nabla} \vec{m})^2 = A / r^2$$

3D magnetization



approximation

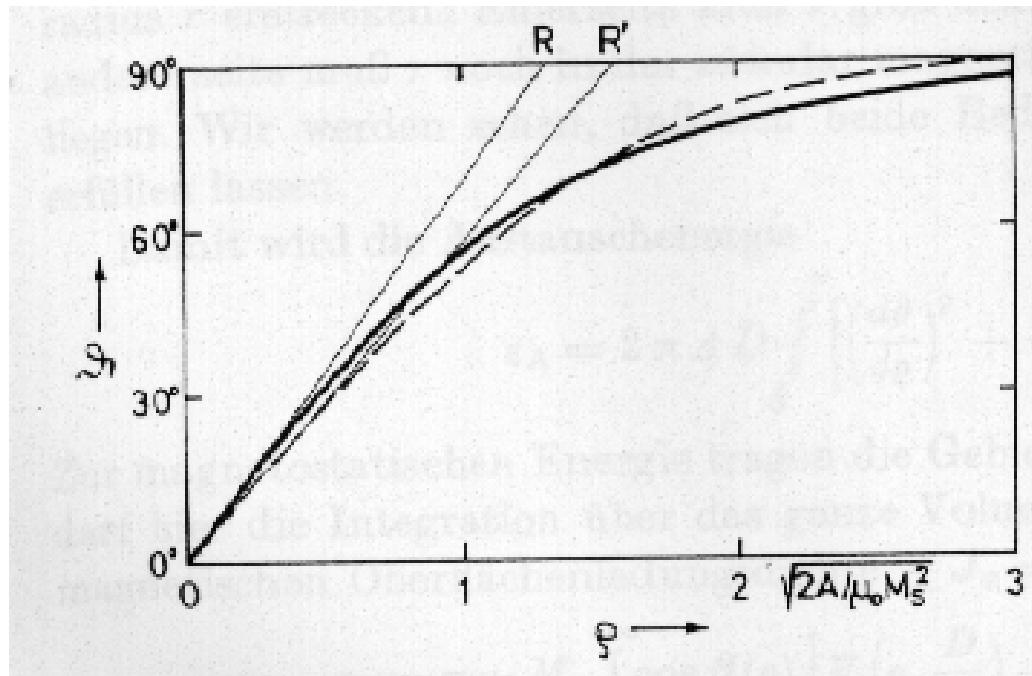
$$\vec{m} = \begin{pmatrix} \sin \theta(r) y / r \\ -\sin \theta(r) x / r \\ \cos \theta(r) \end{pmatrix} \quad \left\{ \begin{array}{l} \operatorname{div} \vec{m} = 0 \\ \vec{m} \cdot \vec{n} \neq 0 \end{array} \right.$$

$$E_{ech} = A \left[\sin^2 \theta / r^2 + \left(\frac{d\theta}{dr} \right)^2 \right]$$

$$\vec{m} = \begin{pmatrix} -\sin \theta(r) y / r \\ \sin \theta(r) x / r \\ \cos \theta(r) \end{pmatrix}$$

$$E_{ech} = A \left[\left(\frac{d\theta}{dr} \right)^2 + \frac{\sin^2 \theta}{r^2} \right]$$

$$E_{dem} = \frac{\mu_0 M_s^2}{2} \cos^2 \theta$$



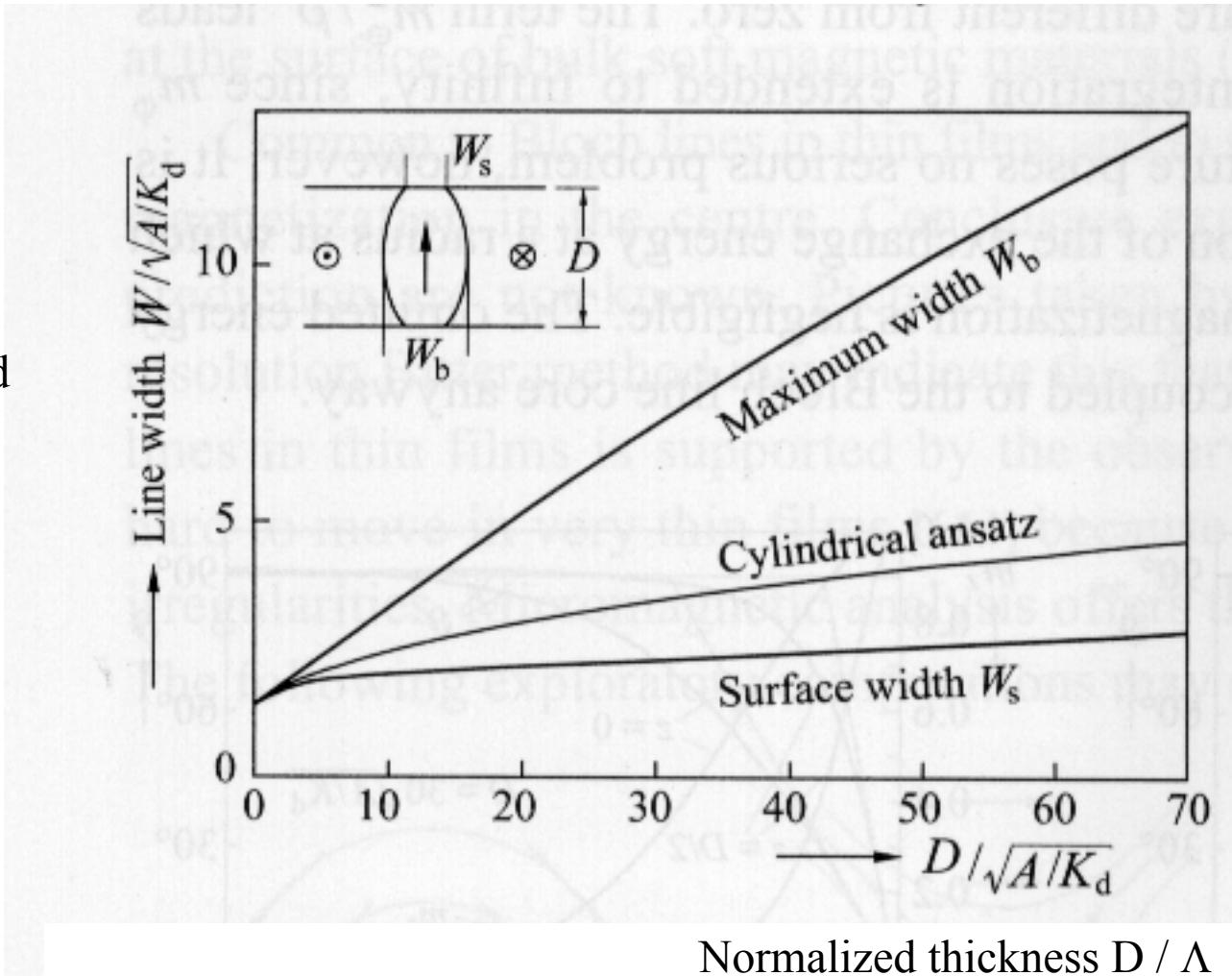
E. Feldtkeller, H. Thomas, Phys. kondens. Materie **4**, 8 (1965)

$$\frac{d^2(2\theta)}{dr^2} + \frac{1}{r} \frac{d(2\theta)}{dr} + \left(\frac{1}{\Lambda^2} - \frac{1}{r^2} \right) \sin 2\theta = 0$$

$$\Lambda = \sqrt{\frac{2A}{\mu_0 M_s^2}}$$

Variational calculation

Normalized
widths
 W / Λ



A. Hubert et R. Schäfer *Magnetic Domains* (Springer, 1998)

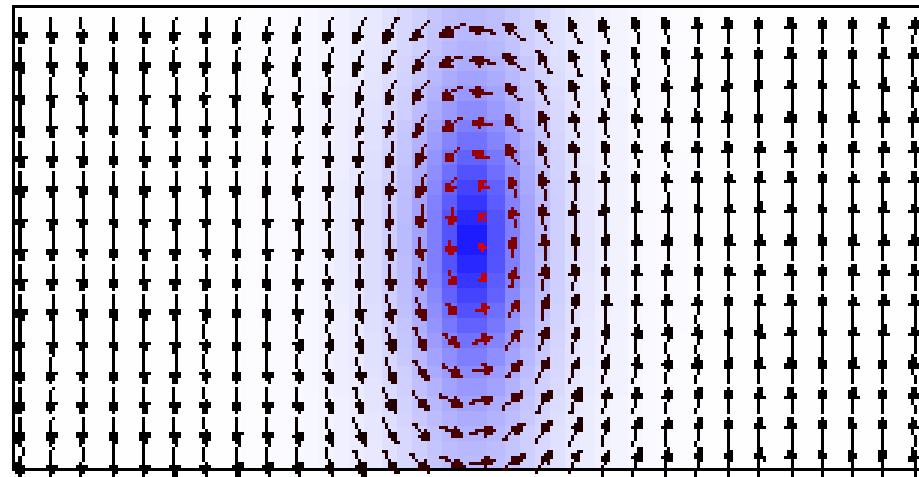
Walls in films with perpendicular anisotropy

Epaisseur 30 nm, facteur de qualité Q= 1.77

boîte 60 nm de large

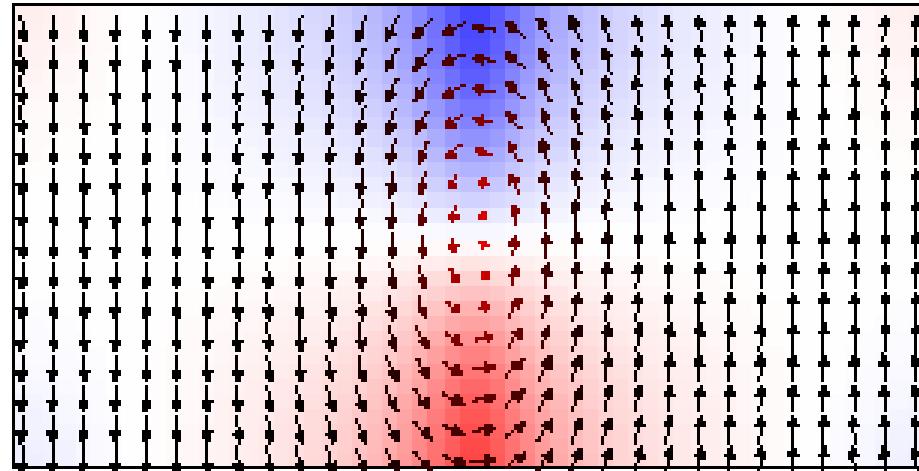
$$\Lambda = 4 \text{ nm}$$

composante



Bloch

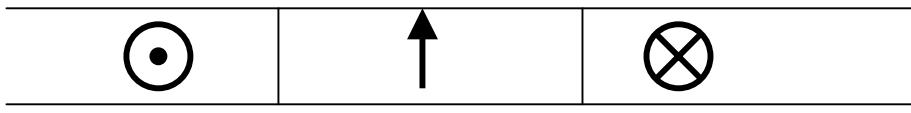
composante



Néel

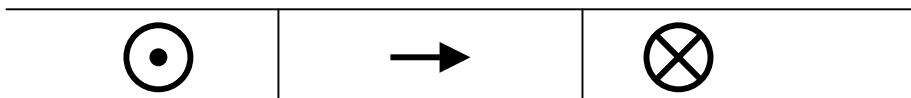
Néel

The Néel wall (1955)



Bloch wall

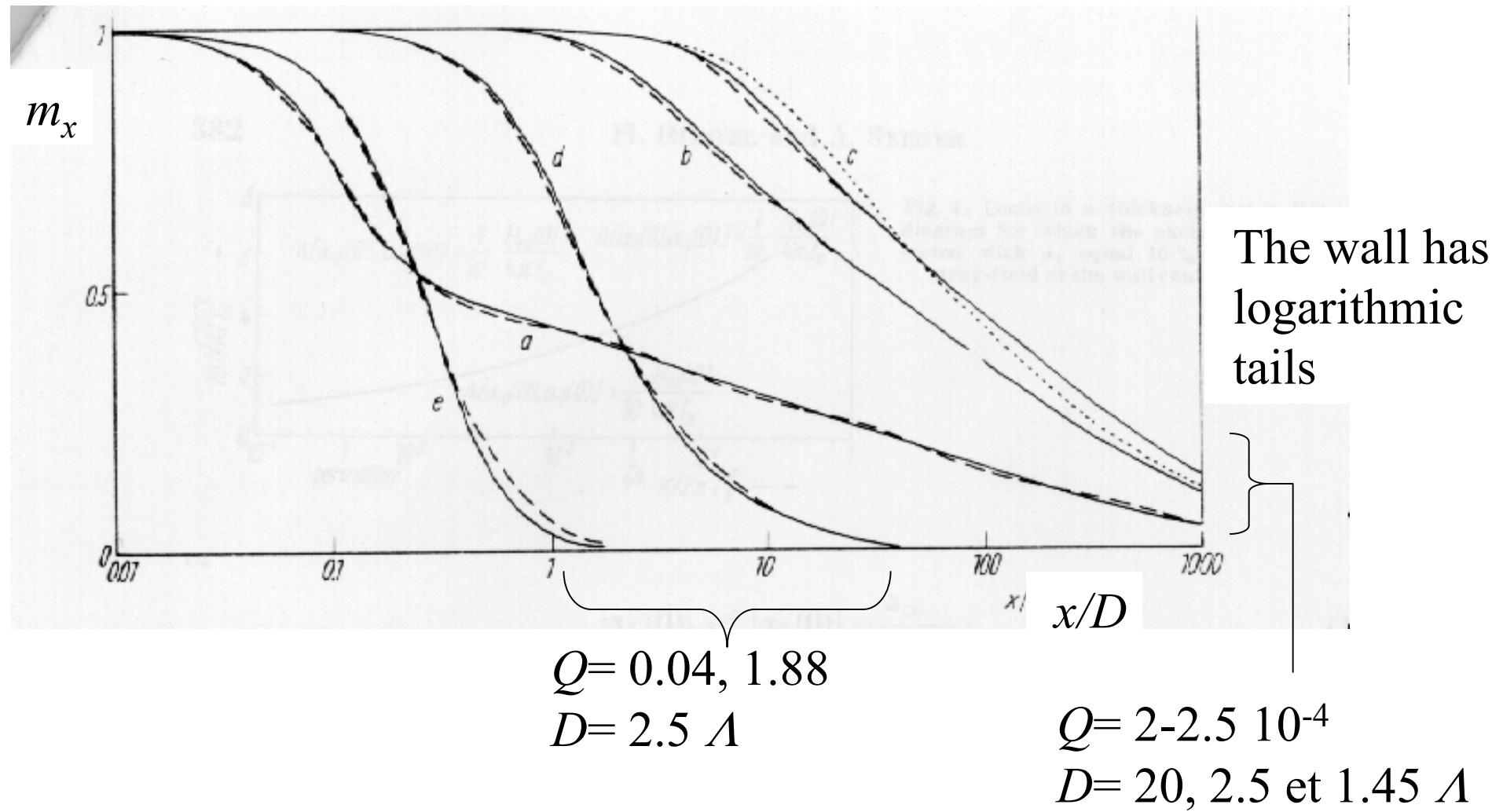
Thin film without
anisotropy, or small
in-plane anisotropy



Néel wall



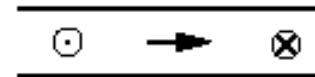
Approximate analytical model



H. Riedel, A. Seeger, phys. stat. sol. **46** 377 (1971)

Walls in soft thin films

paroi de Néel symétrique



composante →

NiFe 30 nm

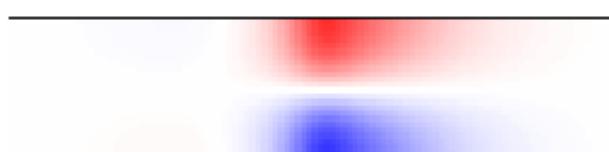
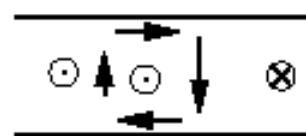
composante ⊖

paroi de Néel asymétrique



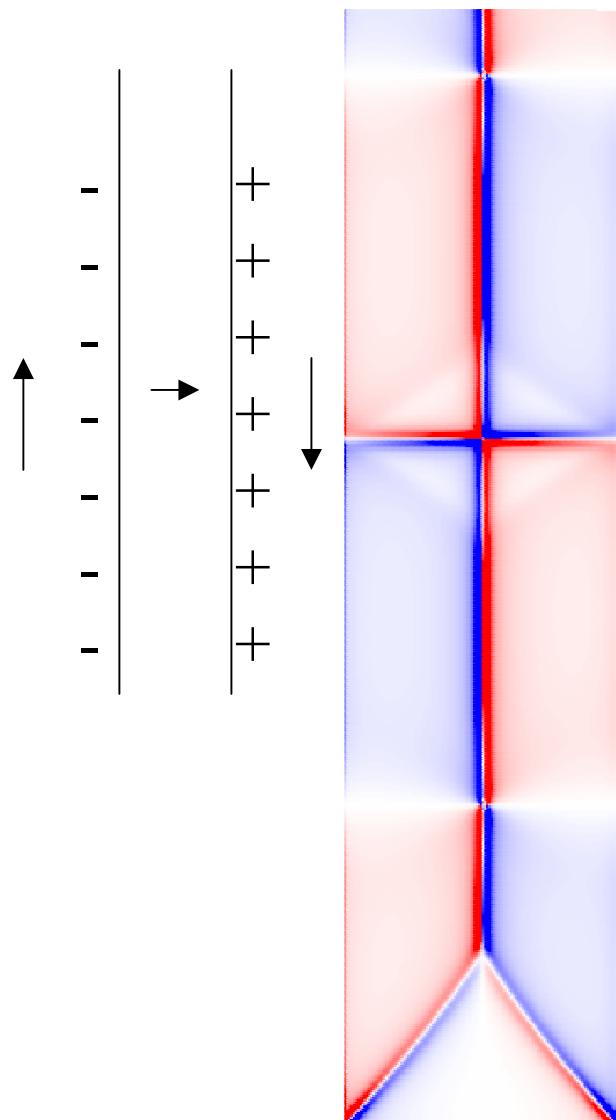
NiFe 40 nm

paroi de Bloch asymétrique



NiFe 50 nm

2D instability of the Néel wall : cross-tie



map of the magnetic charges



electron holography image

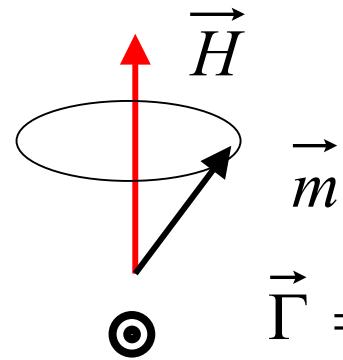
A. Tonomura et al., Phys. Rev. **B25** 6799 (1982)

Magnetization dynamics

$$\vec{L} = -\vec{M} / \gamma \quad \gamma \text{ gyromagnetic ratio } (>0) \quad \gamma = \frac{g\mu_B}{\hbar} = g \frac{e}{2m}$$

Angular momentum
dynamics

$$\frac{d\vec{L}}{dt} = \vec{\Gamma}$$



$$\frac{d\vec{m}}{dt} = \gamma_0 \vec{H} \times \vec{m}$$

$$\gamma_0 = \mu_0 \gamma \approx 2.2 \cdot 10^5 \text{ S.I.}$$

Can be found directly from
quantum mechanics

0.28 GHz/ mT

Dynamics of a magnetization continuum

Effective
field

$$\vec{H}_{eff} = \vec{H}_{applied} + \vec{H}_{demag} + \vec{H}_{anisotropy} + \vec{H}_{exchange}$$



$$\vec{H}_{eff} = -\frac{1}{\mu_0 M_s} \frac{\delta E}{\delta \vec{m}}$$

$$\frac{2A}{\mu_0 M_s} \Delta \vec{m}$$

$$\frac{d\vec{m}}{dt} = \gamma_0 \vec{H}_{eff} \times \vec{m} + \alpha \vec{m} \times \frac{d\vec{m}}{dt}$$

Landau-Lifshitz-Gilbert

$$= \frac{\gamma_0}{1 + \alpha^2} \left[\vec{H}_{eff} \times \vec{m} + \alpha \vec{m} \times \left(\vec{H}_{eff} \times \vec{m} \right) \right]$$

α : Gilbert
damping
parameter

another magnetization dynamics equation

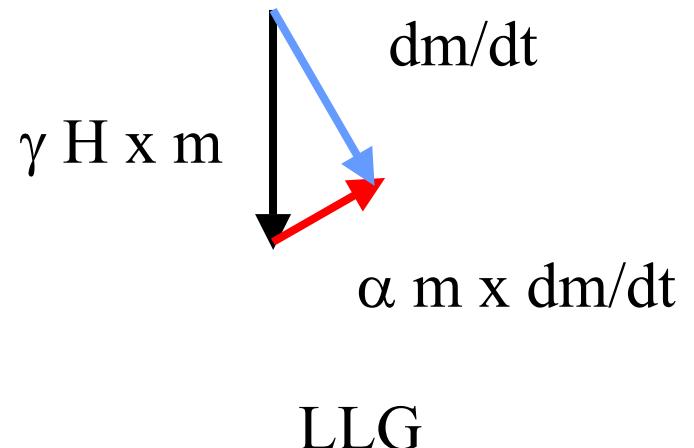
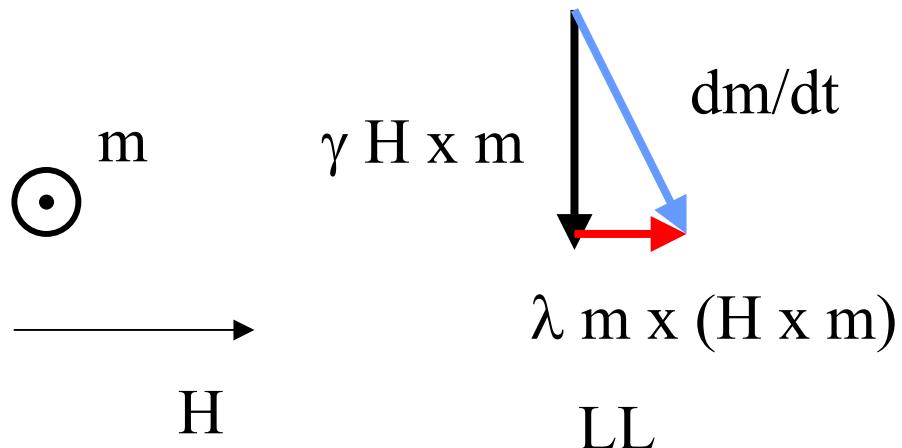
$$\frac{d\vec{m}}{dt} = \gamma_0 \vec{H}_{eff} \times \vec{m} + \alpha \vec{m} \times \frac{d\vec{m}}{dt}$$

Landau-Lifshitz-Gilbert (1955)

$$\frac{d\vec{m}}{dt} = \gamma_L \vec{H}_{eff} \times \vec{m} + \lambda \vec{m} \times (\vec{H}_{eff} \times \vec{m})$$

Landau-Lifshitz (1935)

are mathematically equivalent



Properties of the magnetization dynamics

1) $\frac{d(\vec{m}^2)}{dt} = 2\vec{m} \cdot \frac{d\vec{m}}{dt} = 0$ Conservation of the magnetization modulus

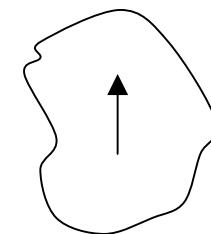
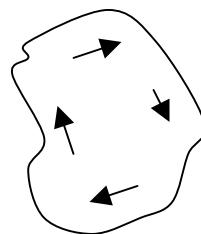
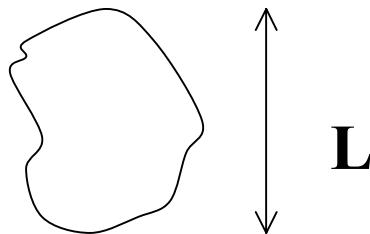
2) $\frac{dE}{dt} = -\mu_0 M_s \vec{H}_{eff} \cdot \frac{d\vec{m}}{dt} = -\alpha \mu_0 M_s \vec{H}_{eff} \cdot \left(\vec{m} \times \frac{d\vec{m}}{dt} \right)$

$$= -\alpha \mu_0 M_s \frac{d\vec{m}}{dt} \cdot \left(\vec{H}_{eff} \times \vec{m} \right) = -(\alpha \mu_0 M_s / \gamma) \left(\frac{d\vec{m}}{dt} \right)^2$$

Decrease of the energy with time : the magnetic system is not isolated

Micromagnetics & Nano-objects

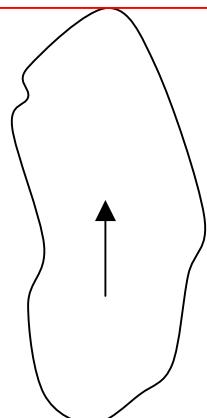
Nanoparticles and small elements



$$E_{ech} \approx A \left(\frac{\pi}{L} \right)^2, E_{dem} \approx 0 \quad E_{ech} \approx 0, E_{dem} \approx \frac{1}{3} \frac{\mu_0 M_s^2}{2}$$

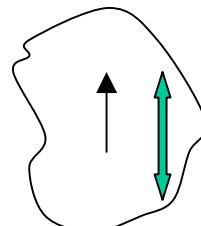
stable monodomain state for

$$\frac{1}{3} \frac{\mu_0 M_s^2}{2} < A \left(\frac{\pi}{L} \right)^2 \Leftrightarrow L < \pi \sqrt{3} \Lambda$$



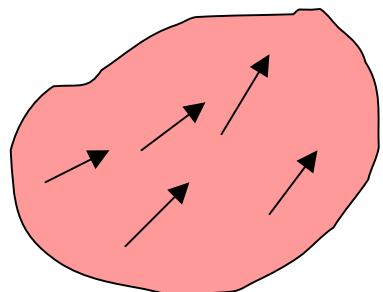
Demagnetising
factor N

$$L < \pi \frac{\Lambda}{\sqrt{N}}$$



With anisotropy,
the transition
size increases
too

Nanoparticles in the monodomain state



≡



« macrospin »

↔

several Λ

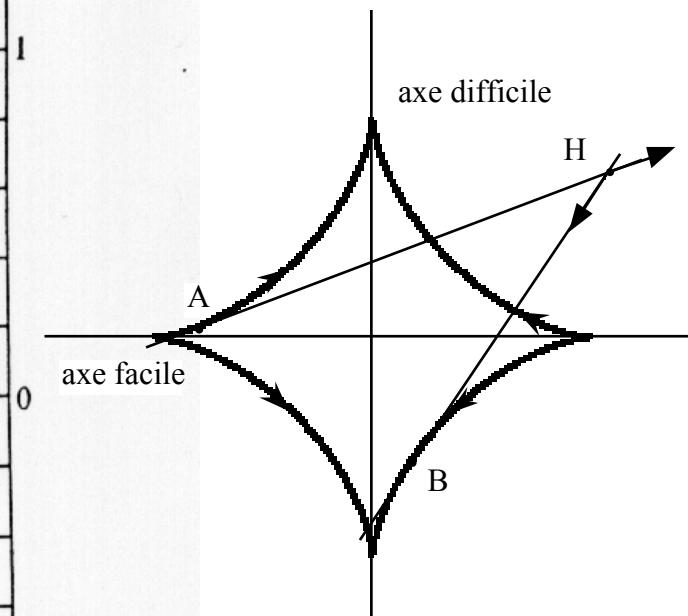
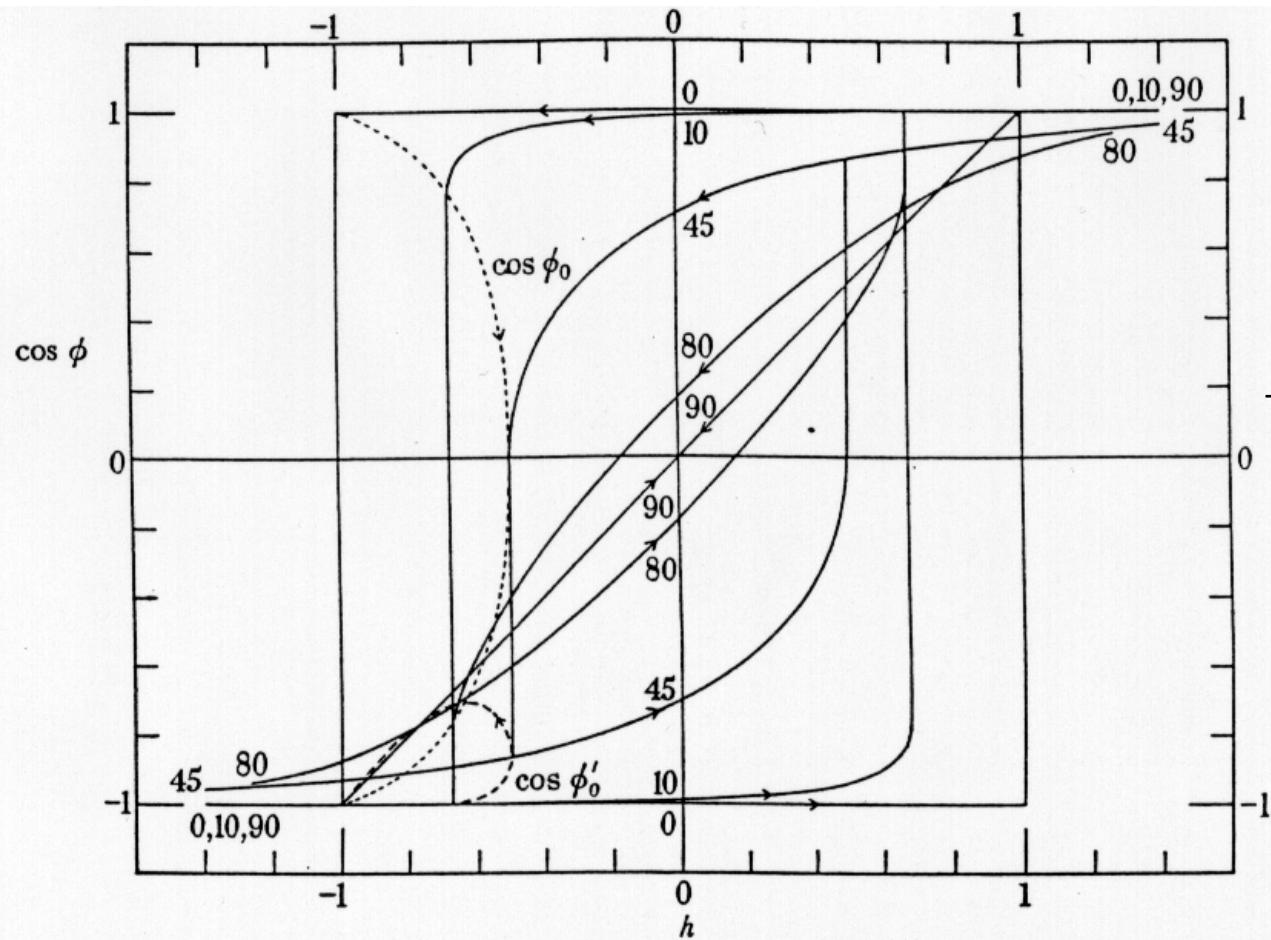
$$E = V \left(K G(\vec{m}) - \mu_0 M_s \vec{H} \cdot \vec{m} \right) \quad \left| \vec{m} \right| = 1$$

$$H_K = \frac{2K}{\mu_0 M_s}$$

$$U = V_{\vec{H}}(\vec{m}) = G(\vec{m}) - 2\vec{h} \cdot \vec{m}$$

Uniaxial case of degree 2

(Stoner-Wohlfarth 1948, Slonczewski 1956)



JC Slonczewski, IBM Research
Memorandum RM 003.111.224,
october 1956 (unpublished)

EC Stoner, EP Wohlfarth Phil. Trans. Roy. Soc. London
A240 599 (1948), reprinted IEEE Trans. Magn. **27** 3475 (1991)

European School of Magnetism,
Constanta, 2005: André THIAVILLE

Geometric solution

(inspired from J.C. Slonczewski, IBM report, 1956)

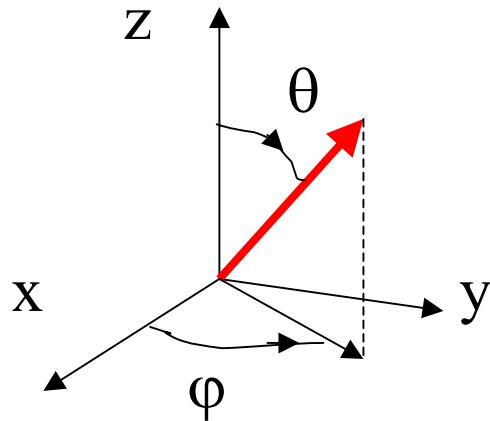
$$U = V_{\vec{H}}(\vec{m}) = G(\vec{m}) - 2\vec{h} \cdot \vec{m}$$

Initial problem (statics) : given H , find m

Dual problem : given m , find H

$$\begin{aligned} \text{equilibrium : } & \vec{u} \cdot \frac{d\vec{U}}{d\vec{m}} = 0 & \forall \vec{u} \perp \vec{m} \\ \text{stability : } & \vec{u} \cdot \frac{d^2\vec{U}}{d\vec{m}^2} \vec{u} > 0 \end{aligned}$$

3D Solution in spherical angles



$$G_\theta - 2 \vec{h} \cdot \vec{e}_\theta = 0 \quad G_\varphi - 2 \sin \theta \vec{h} \cdot \vec{e}_\varphi = 0$$

equilibrium

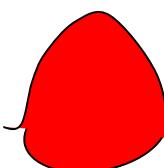
$$\vec{h} = \frac{1}{2} G_\theta \cdot \vec{e}_\theta + \frac{1}{2 \sin \theta} G_\varphi \cdot \vec{e}_\varphi + \lambda \vec{m} = 0$$

$$U_{\theta\theta} = G_{\theta\theta} + 2\lambda \quad U_{\theta\varphi} = \sin \theta \frac{\partial}{\partial \theta} \left(\frac{G_\varphi}{\sin \theta} \right) \quad U_{\varphi\varphi} = G_{\varphi\varphi} + \sin \theta \cos \theta G_\theta + 2\lambda \sin^2 \theta$$

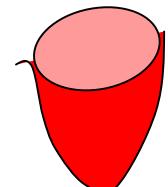
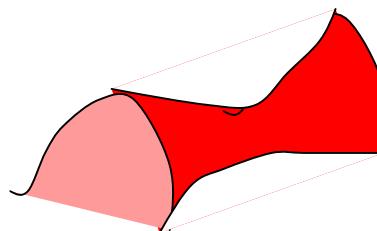
stability



$$U_{\theta\theta} + U_{\varphi\varphi} > 0$$



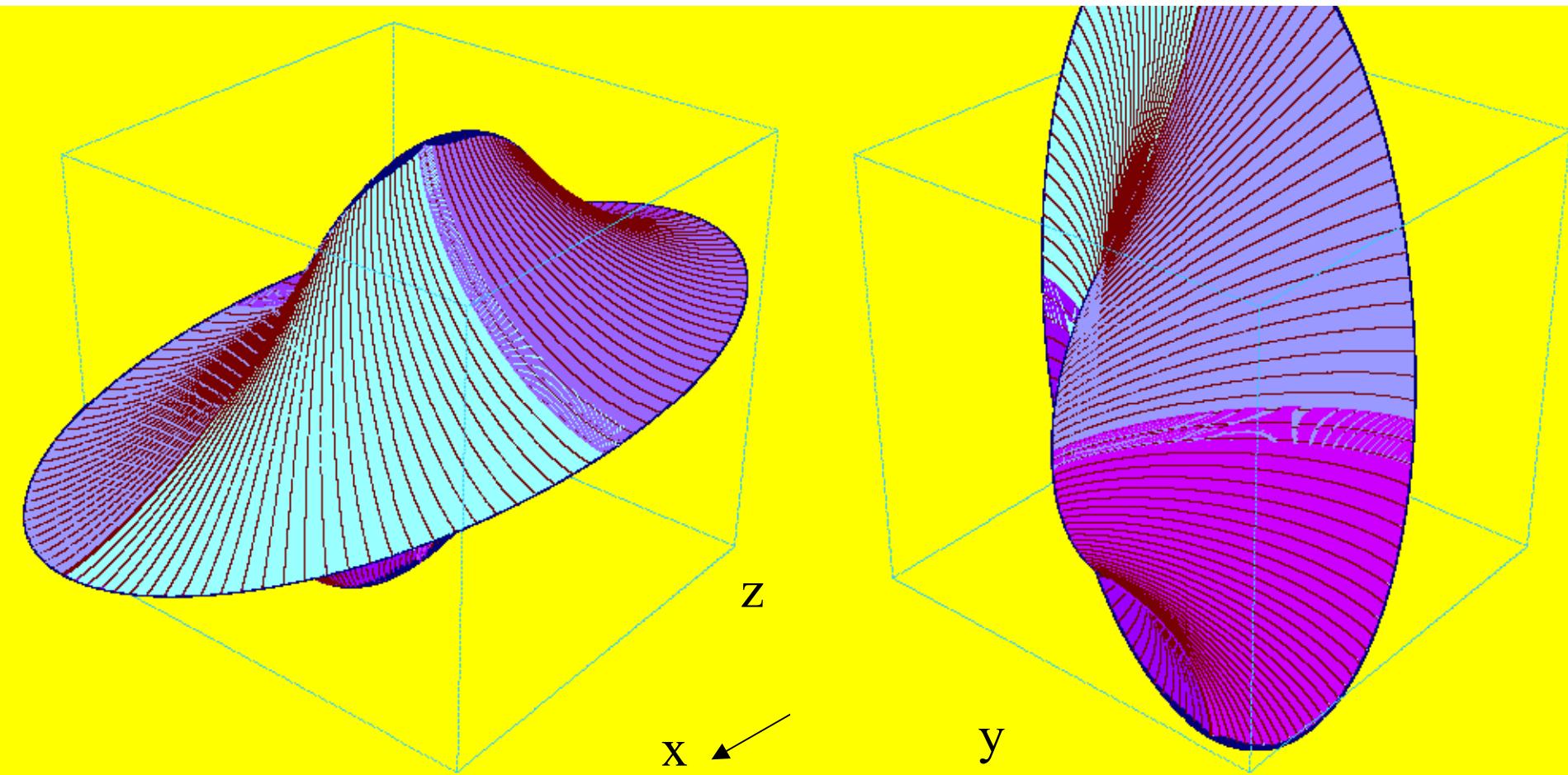
$$U_{\theta\theta} U_{\varphi\varphi} - (U_{\theta\varphi})^2 > 0$$



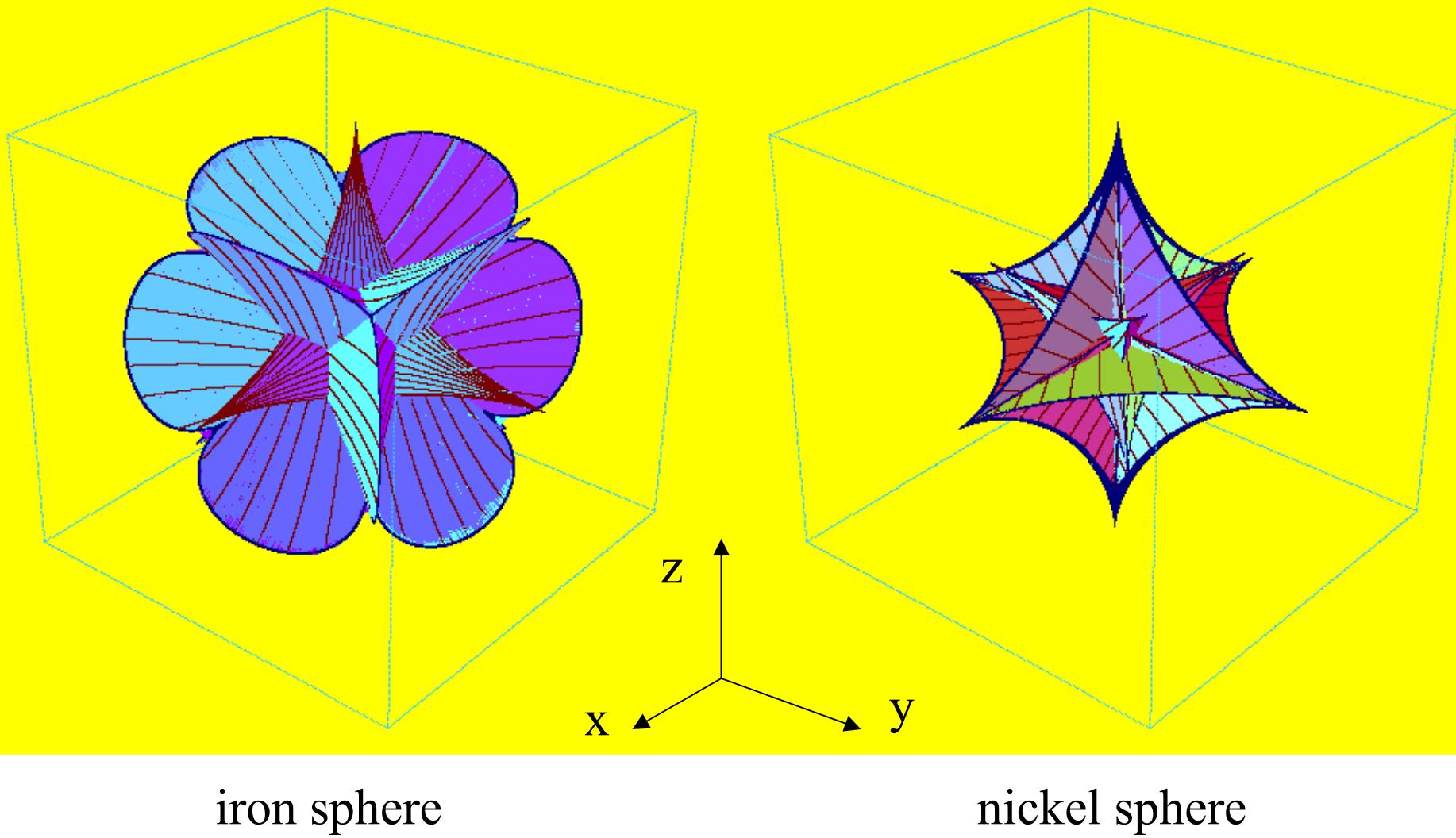
$$G = m_x^2 + 0.5m_y^2$$

surface S_+

surface S_-



x : hard axis ; z : easy axis ; y : intermediate



iron sphere

nickel sphere

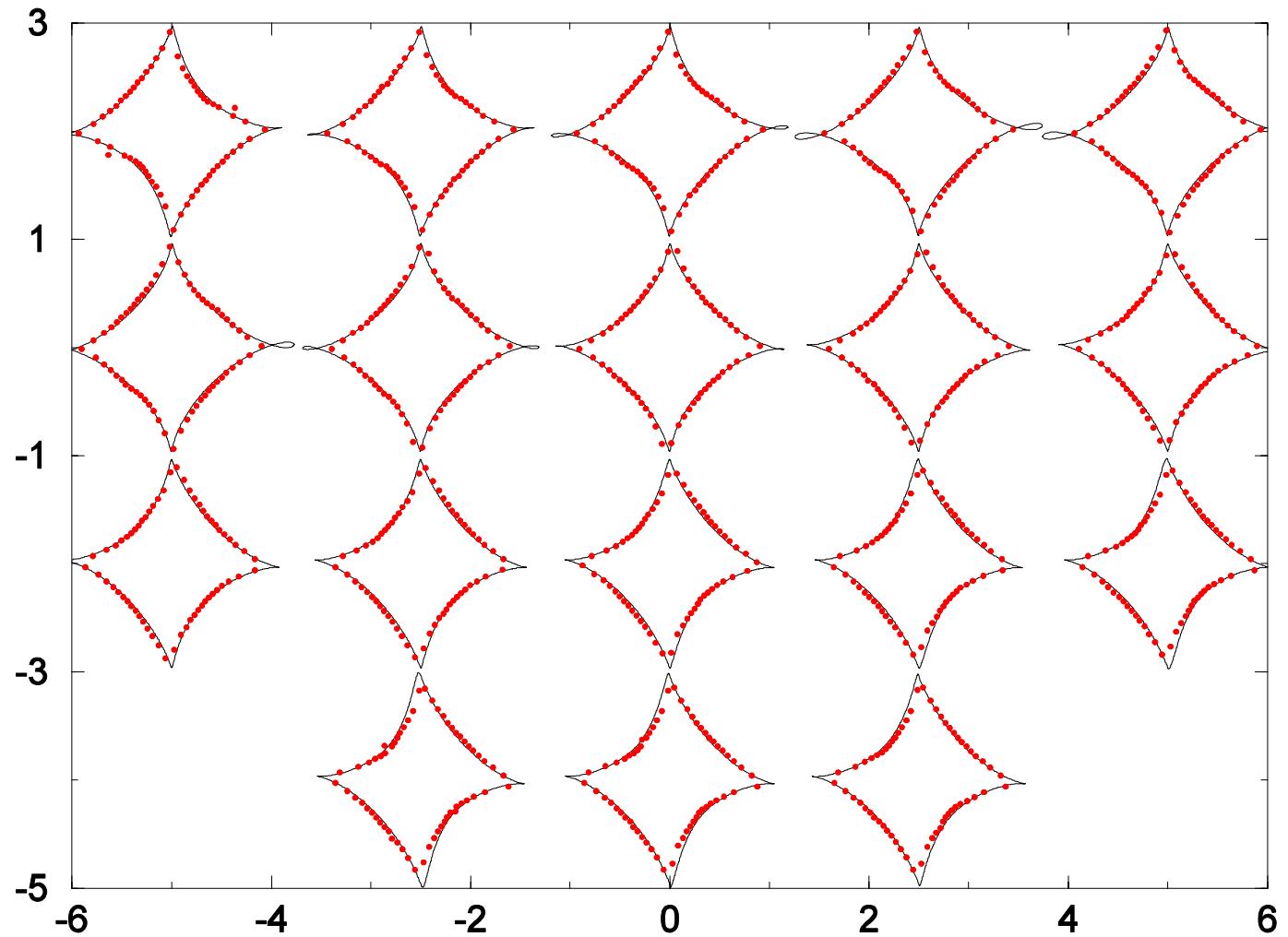
A. Thiaville, Phys. Rev. B**61** 12221 (2000)

European School of Magnetism,
Constanta, 2005: André THIAVILLE

Measurements on an isolated nanoparticle

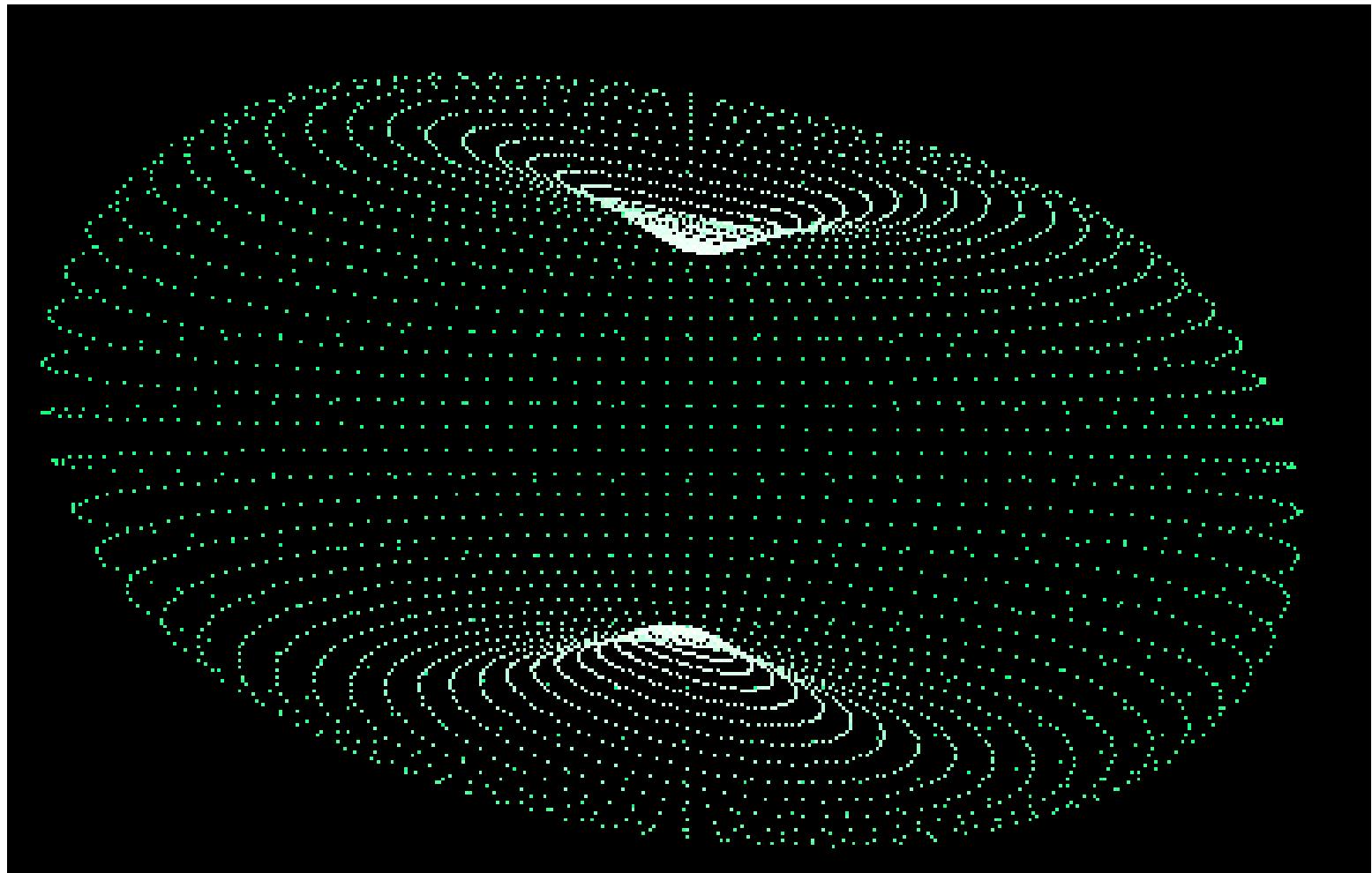
(E. Bonet et coll., Phys. Rev. Lett. 83, 4188 (1999))

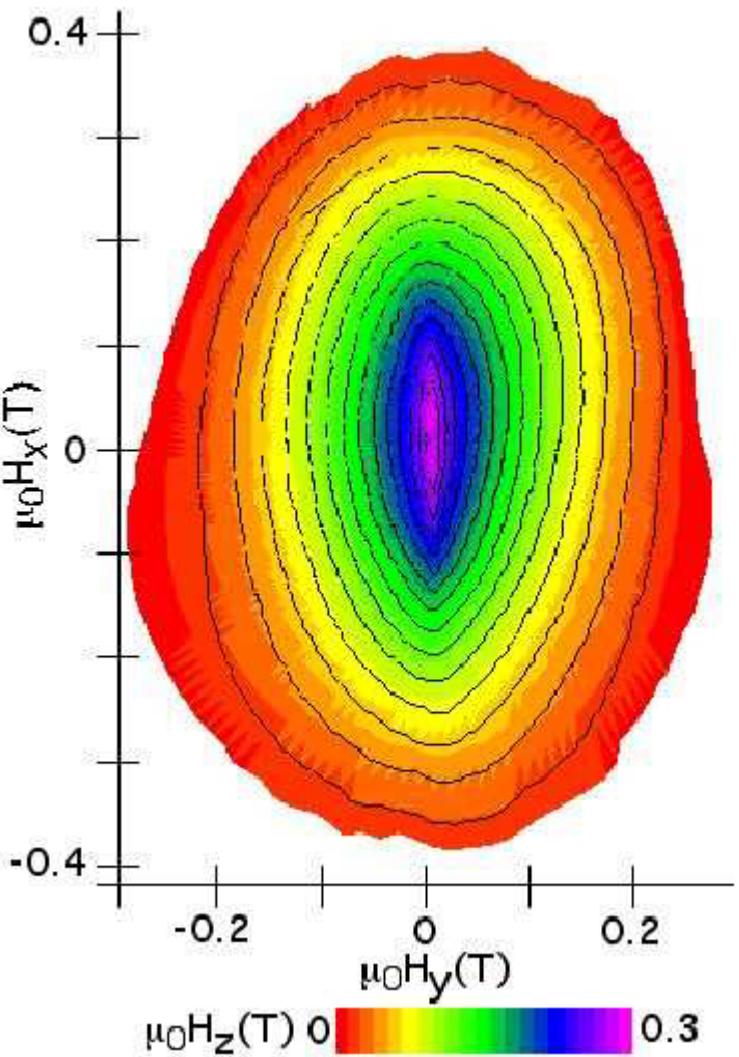
Zone axis
for 18
cuts



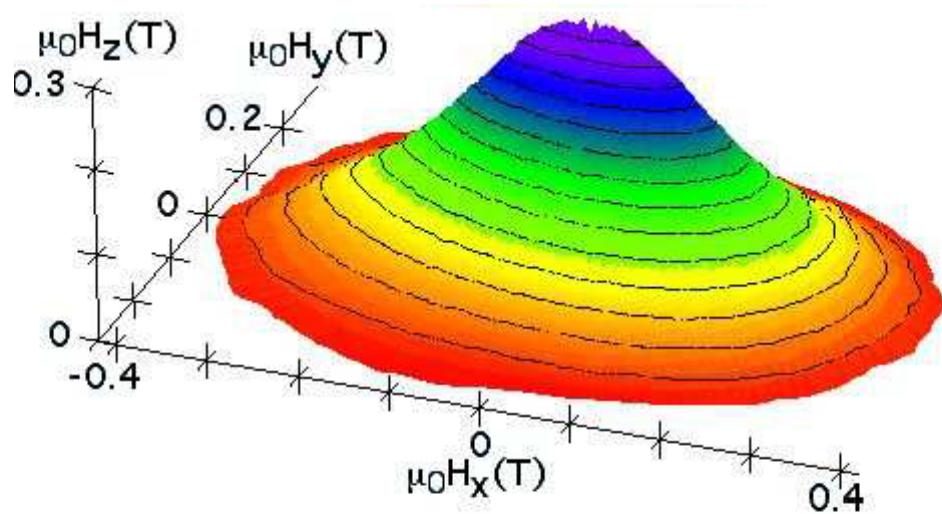
$G = \text{degree 2} + (\text{degree 4 et 6, disoriented})$

The anisotropy energy of that nanoparticle





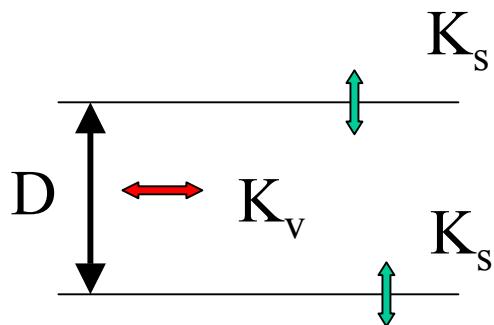
3 nm cobalt cluster



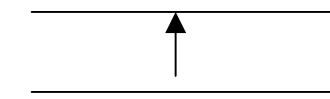
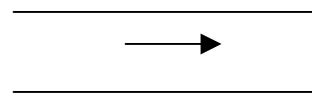
Thèse M. Jamet, Lyon 2001
 W. Wernsdorfer
 Adv. Chem. Phys.
 118 (2001)

Fig. 2.6 Top view and side view of the experimental three dimensional angular dependence of the switching field of a 3 nm Co cluster at 35 mK. This surface is symmetrical with respect to the H_x-H_y -plane and only the upper part ($\mu_0 H_z > 0$ T) is shown. Continuous lines on the surface are contour lines on which $\mu_0 H_z$ is constant.

Surface anisotropy in ultrathin films



$$K_{\text{eff}} = K_v + 2 K_s / D$$



$$K_{\text{eff}} < \mu_0 M_s^2 / 2$$

$$K_{\text{eff}} > \mu_0 M_s^2 / 2$$

$$K_s : 10^{-3} \text{ J/m}^2$$

$$D_c : 1 \text{ nm}$$

Transition thickness

$$D_c = \frac{2K_s}{\mu_0 M_s^2 / 2 - K_v}$$

Another 3 nm cobalt cluster

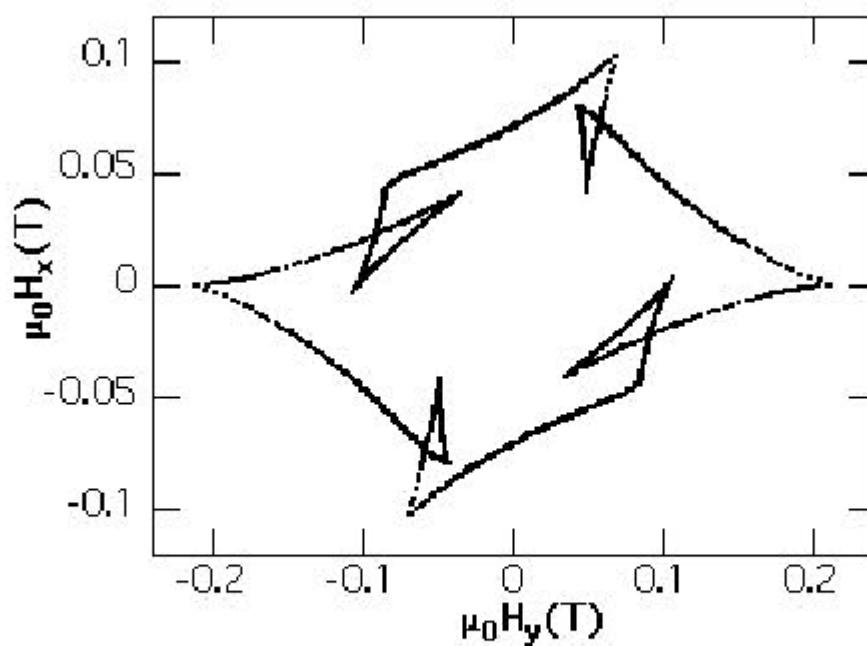
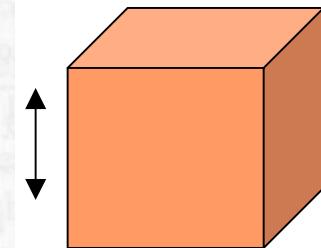
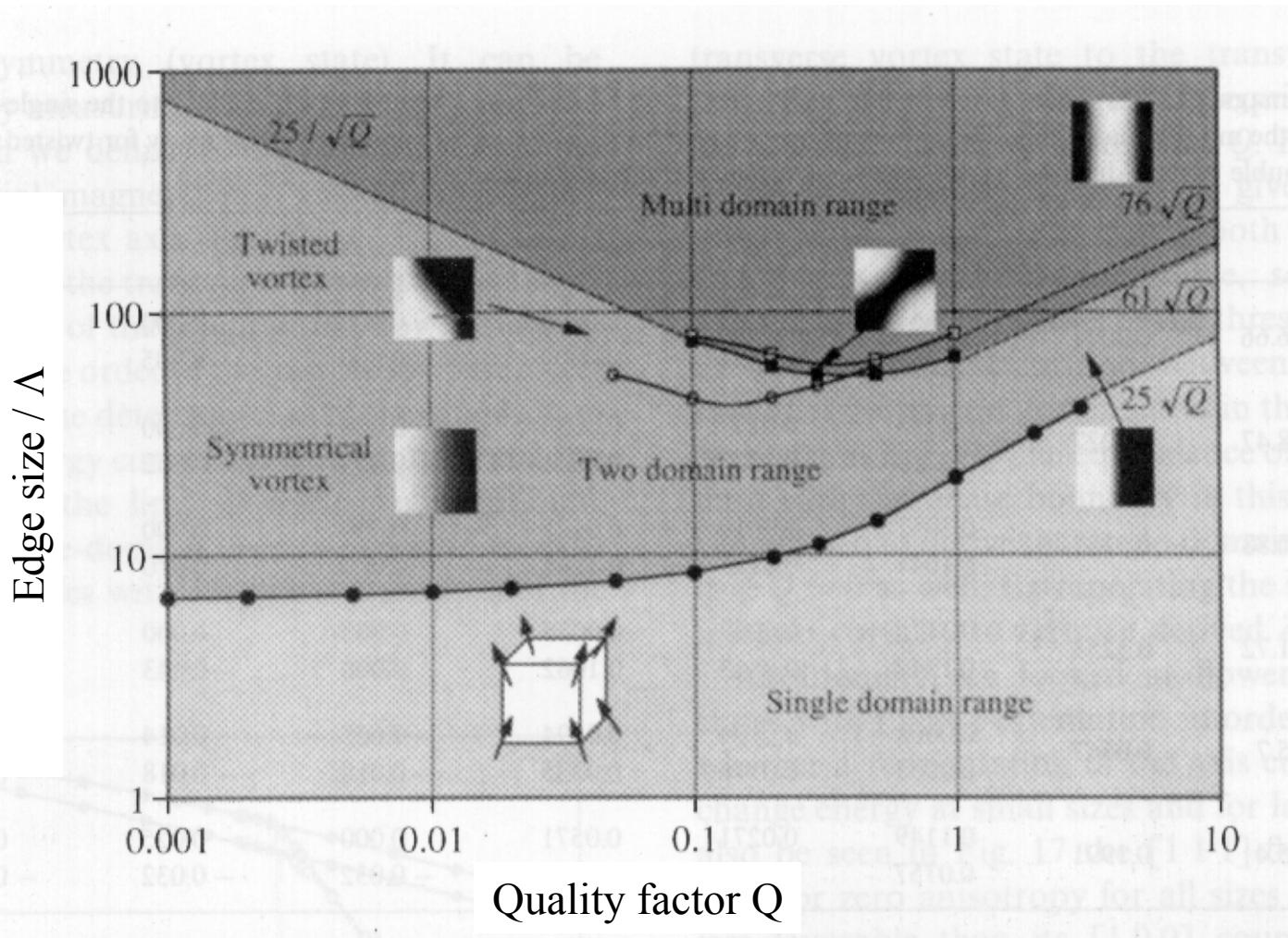


Fig. 2.11 Angular dependence of the switching field of a 3 nm Co cluster showing a strong influence of crystalline anisotropy.

W. Wernsdorfer Adv. Chem. Phys. 118 (2001)

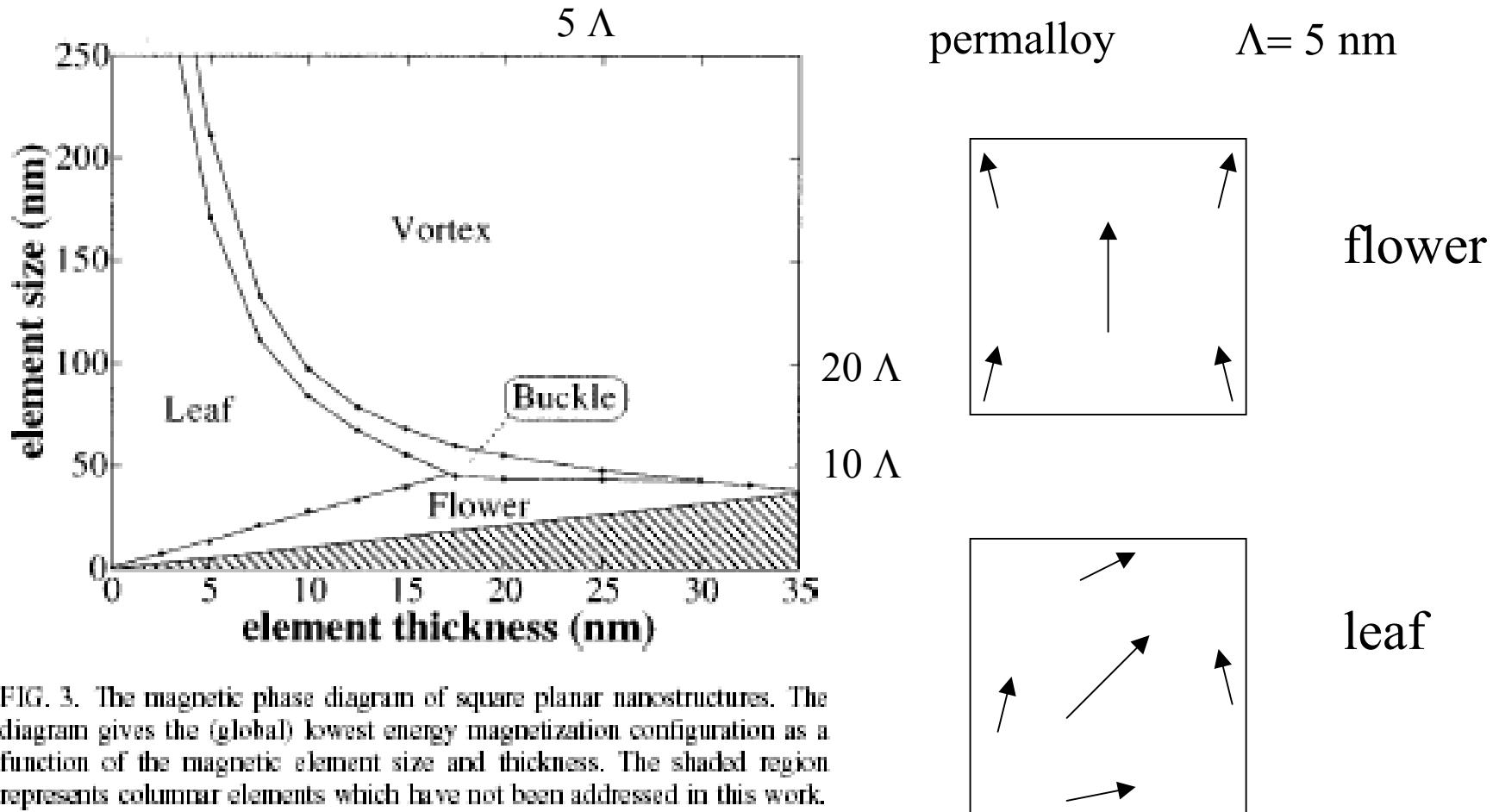
A cube with uniaxial anisotropy



$$Q = \frac{2K}{\mu_0 M_s^2}$$

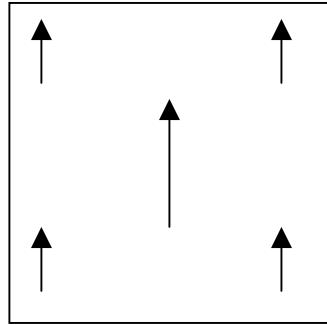
W. Rave et al. JMMM 190 332 (1998)

A square platelet

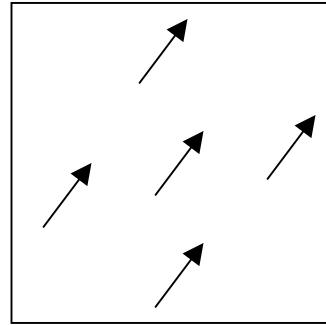


R.P. Cowburn et al. APL 72 2041 (1998)

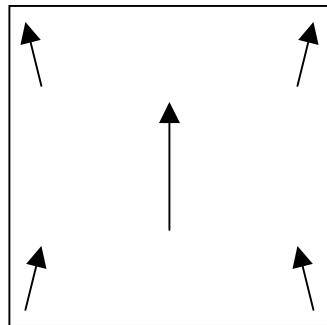
Configuration anisotropy



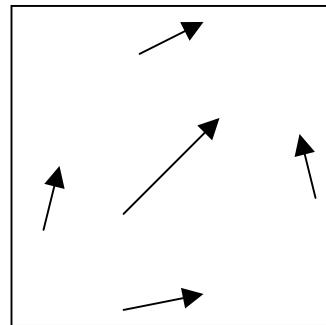
=



permalloy :
no anisotropy



≠

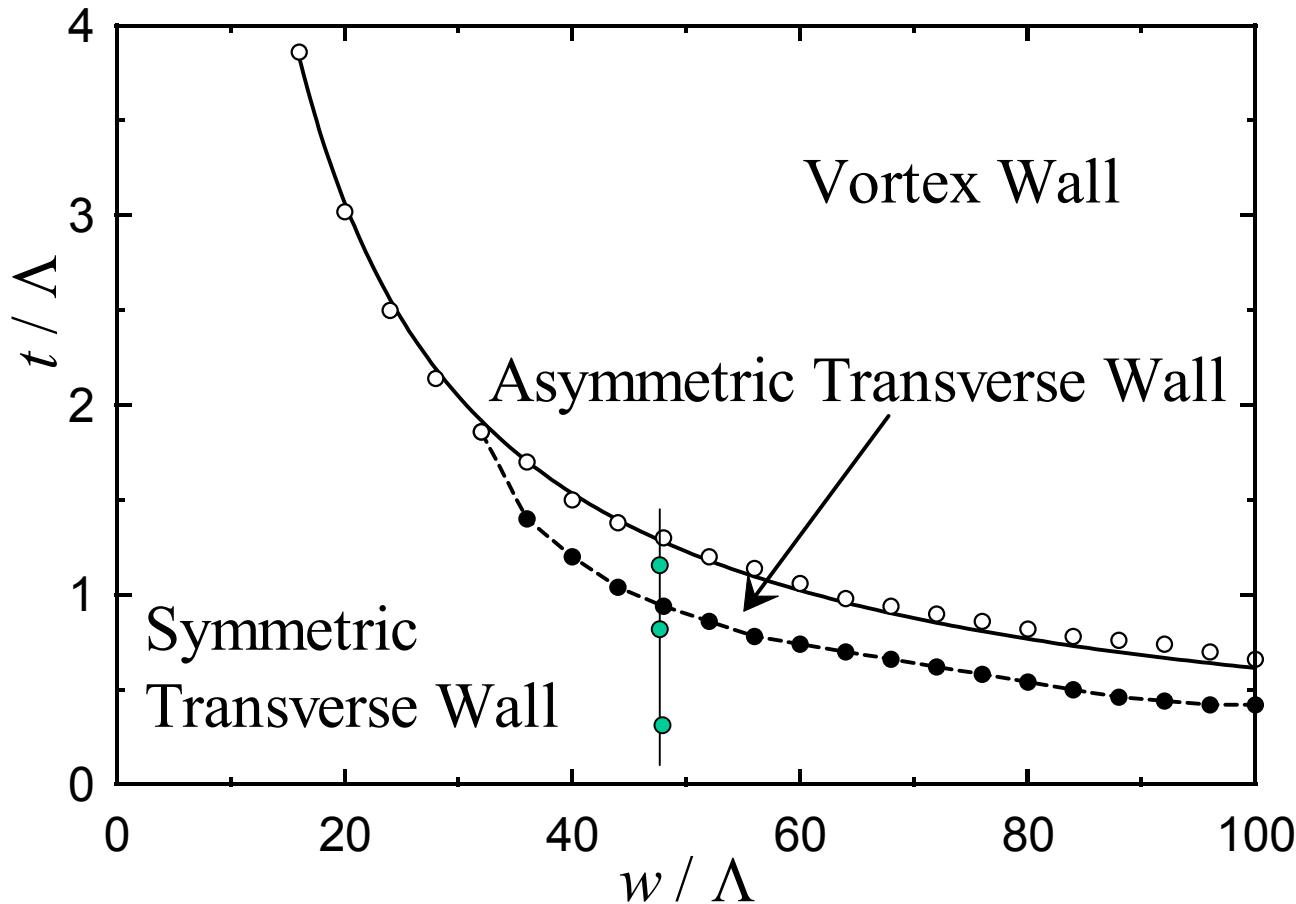
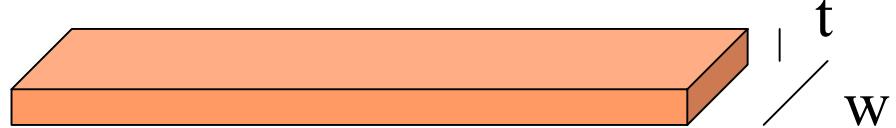


R.P. Cowburn et al. APL **72** 2041 (1998); Phys. Rev. B (1998)

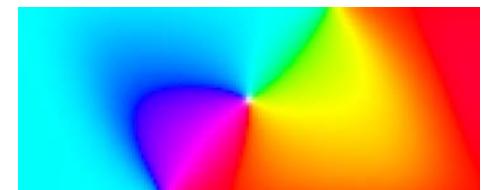
Phase diagram of domain walls in a soft nanostrip

permalloy

$\Lambda = 5 \text{ nm}$



$t = 7.5 \text{ nm} : \text{VW}$



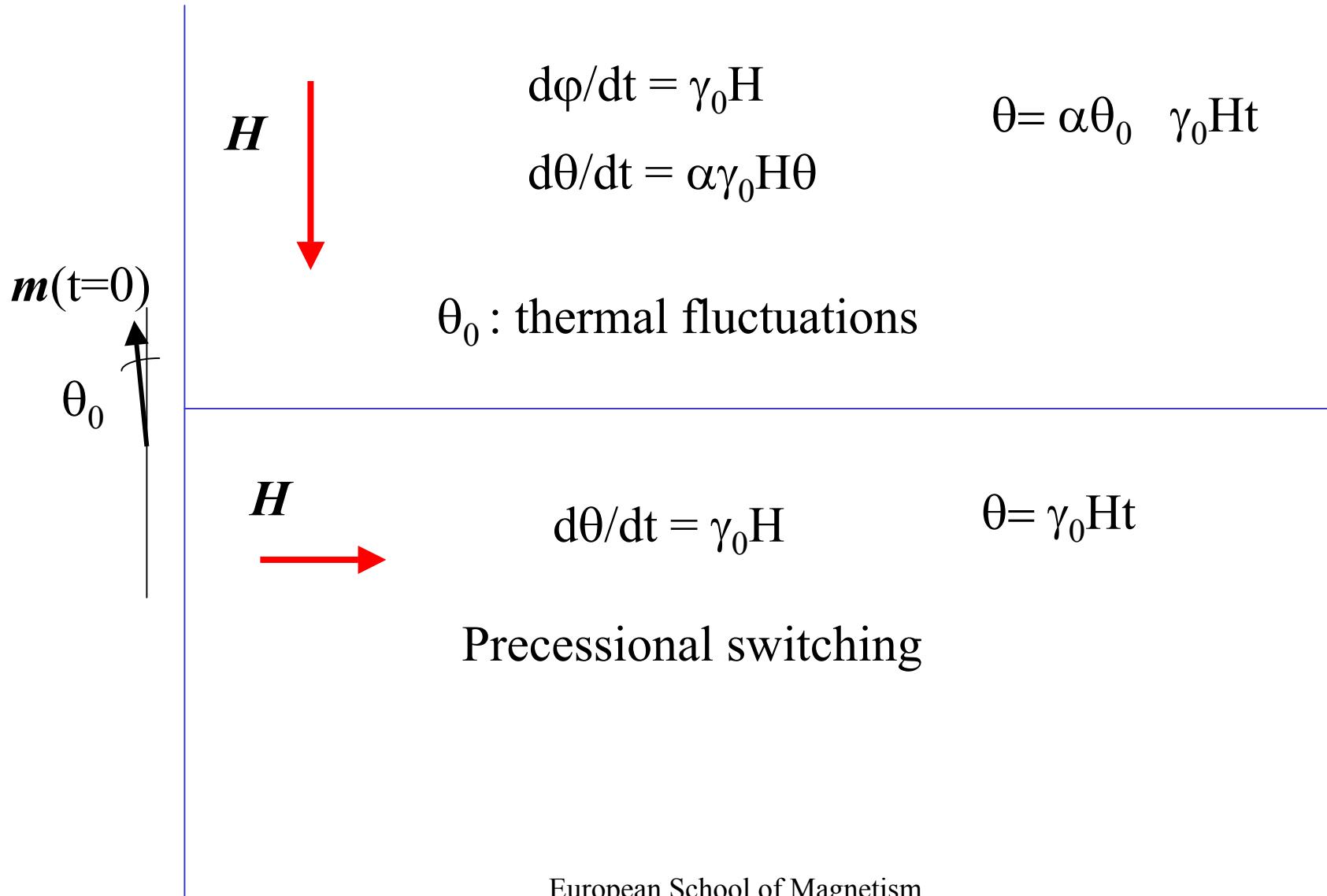
$t = 6.0 \text{ nm} : \text{ATW}$



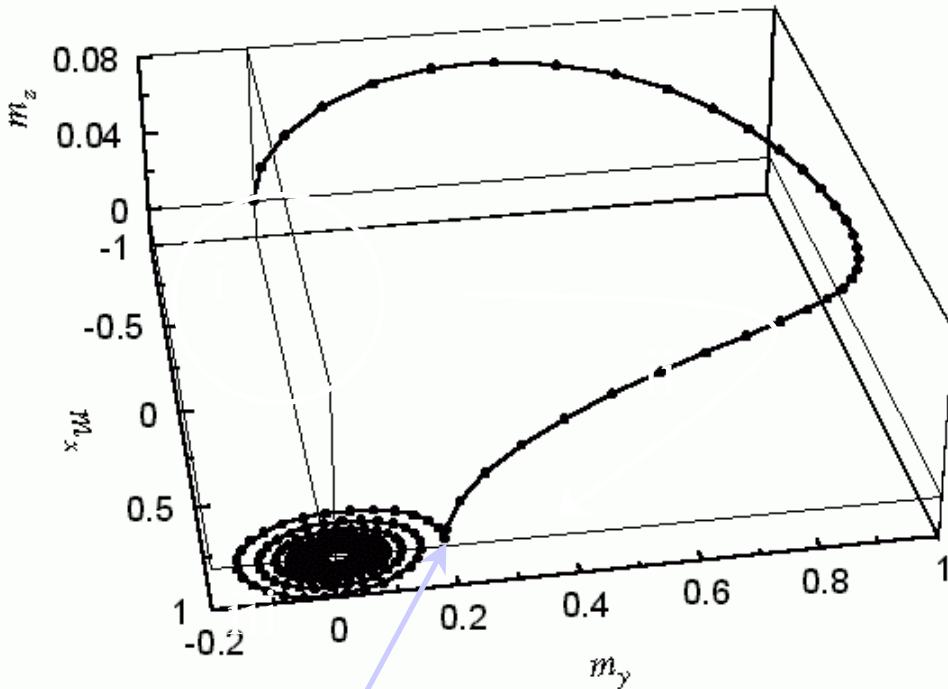
$t = 3.5 \text{ nm} : \text{TW}$



Macrospin : magnetization reversal strategies

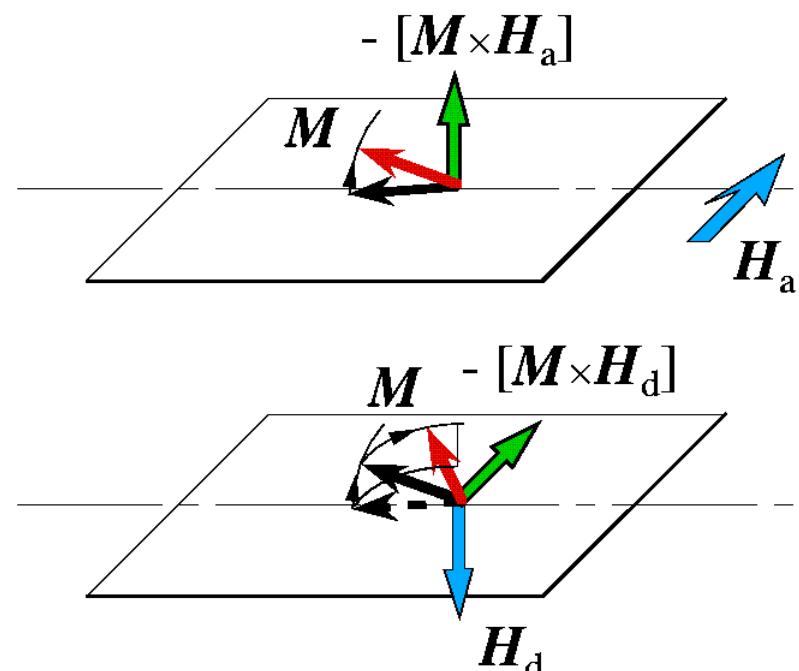


Precessional switching in a platelet

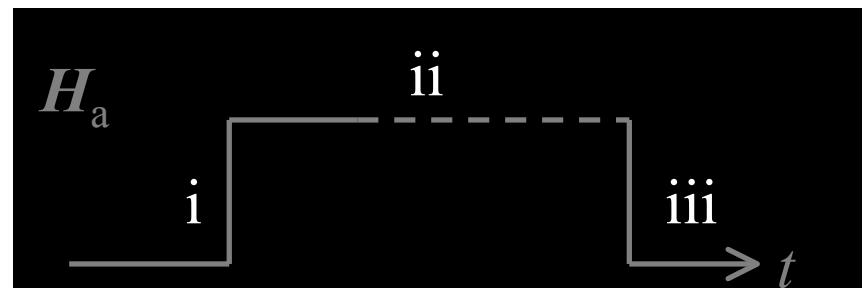


Field cutoff strategy:
Magnetisation vector
back to the film plane

A basically 2 step process

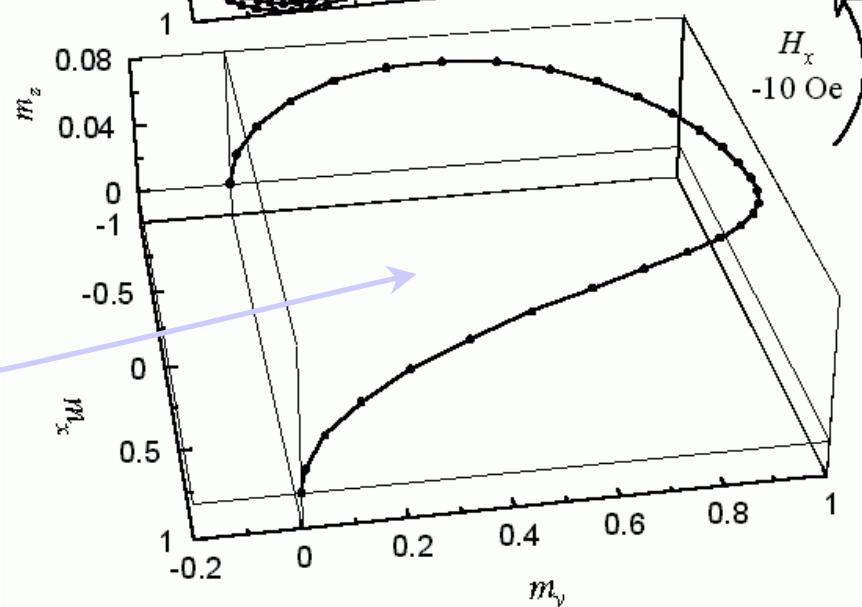
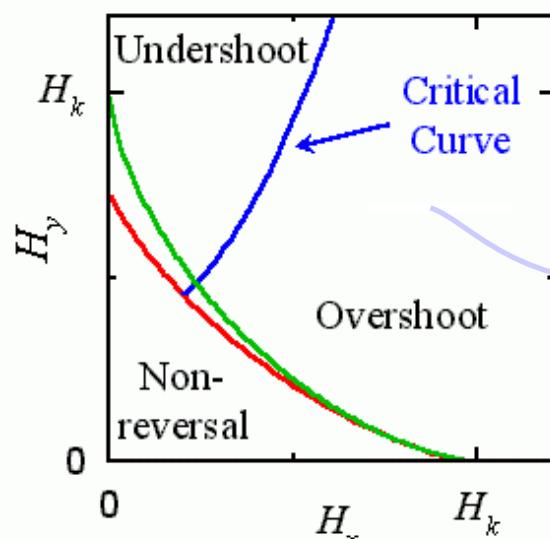
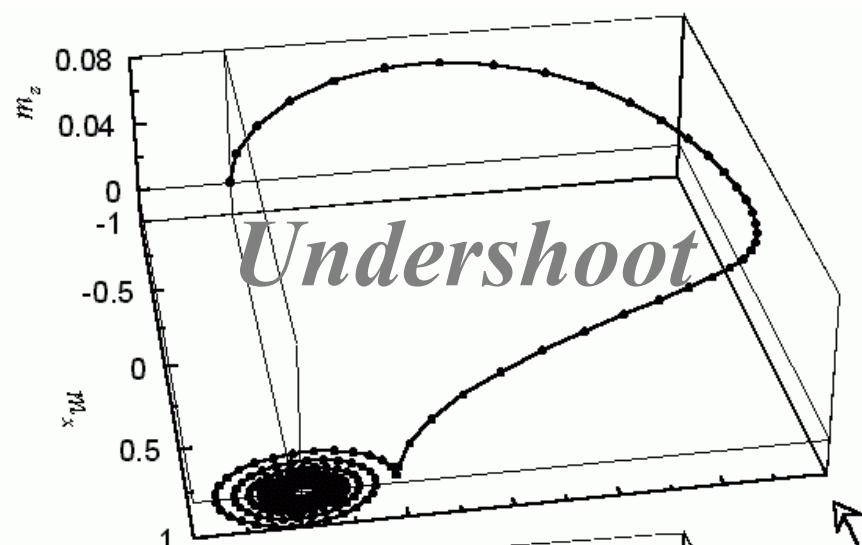
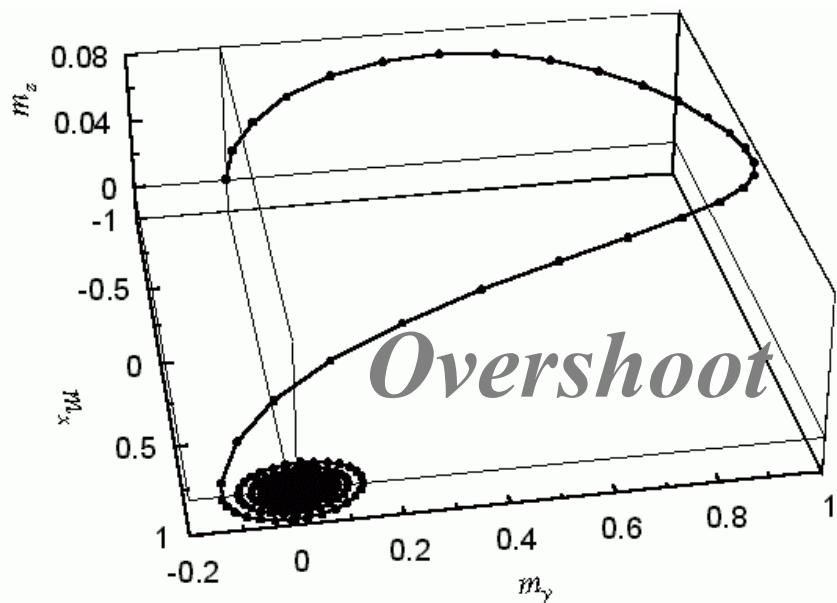


Field pulse profile

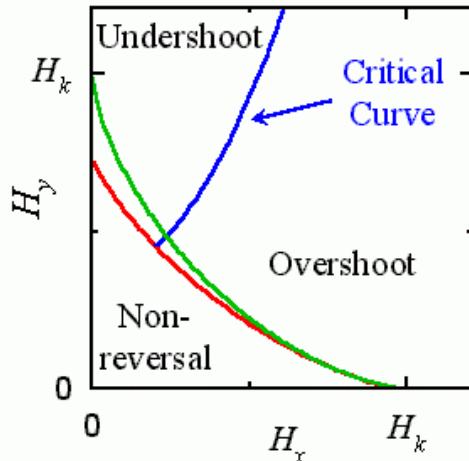


Thèse G. Albuquerque, Orsay, 2002

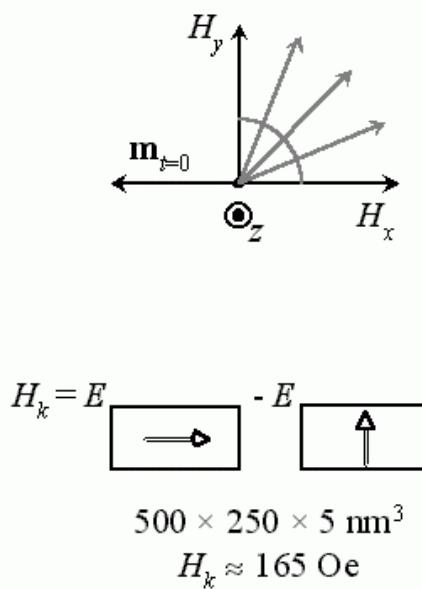
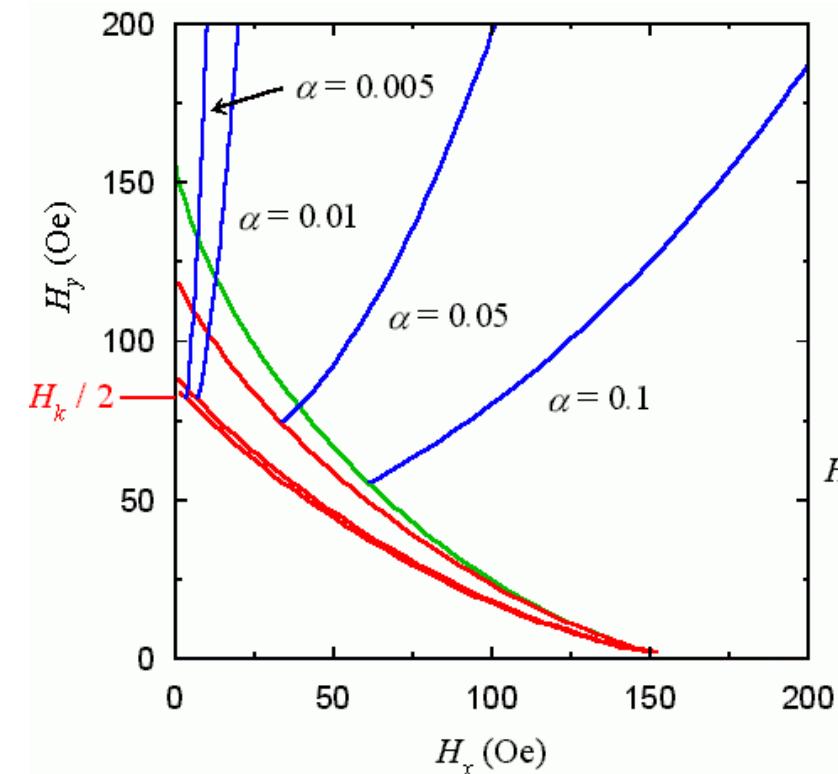
Macrospin magnetisation trajectories



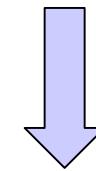
Macrospin precessional dynamics : switching phase diagram



Green: Static switching threshold
Red: Dynamic switching threshold
Blue: Ballistic trajectories



Main Conclusion:
 Switching possible
 below
 the static threshold



Most favorable case:
 Transverse field
 $H_y = H_k/2$

Precessional switching of a MRAM memory cell

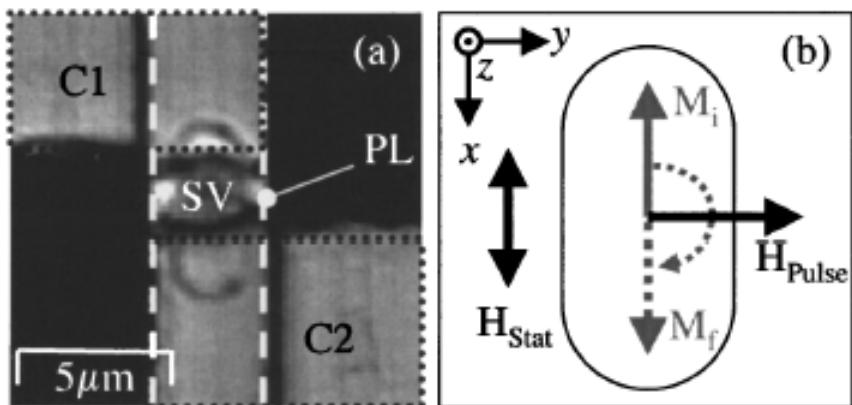
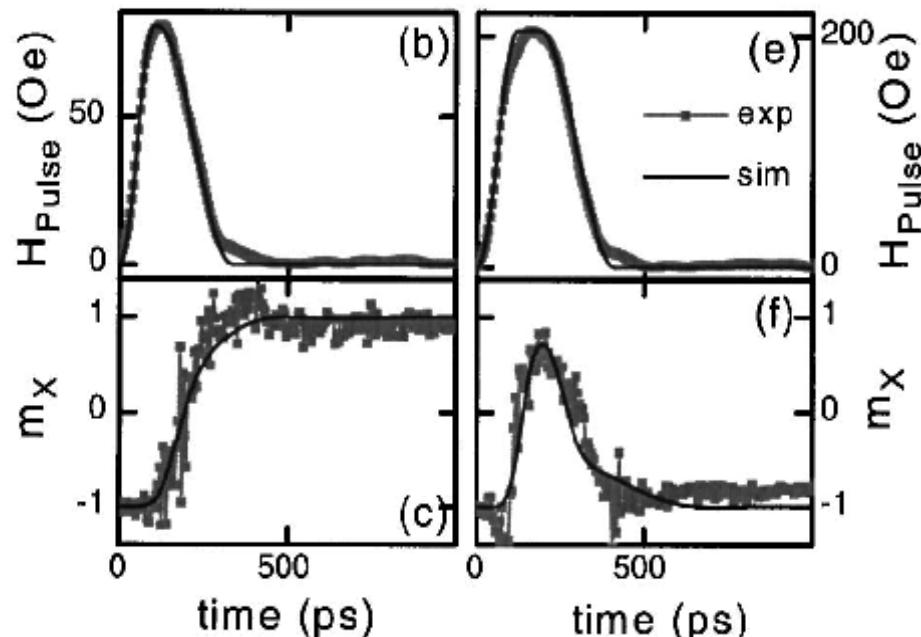


FIG. 1. Magnetic memory cell used in the experiments. (a) Optical micrograph. Spin valve cell (SV) with electrical contacts (C_1 , C_2 , surrounded by the dotted lines) and buried pulse line (PL, marked by the white dashed line). (b) Sketch of the magnetic field configuration H_{pulse} (along y) is applied perpendicular to the initial and final magnetization M_i , M_f .



$$H = 81 \text{ Oe}$$

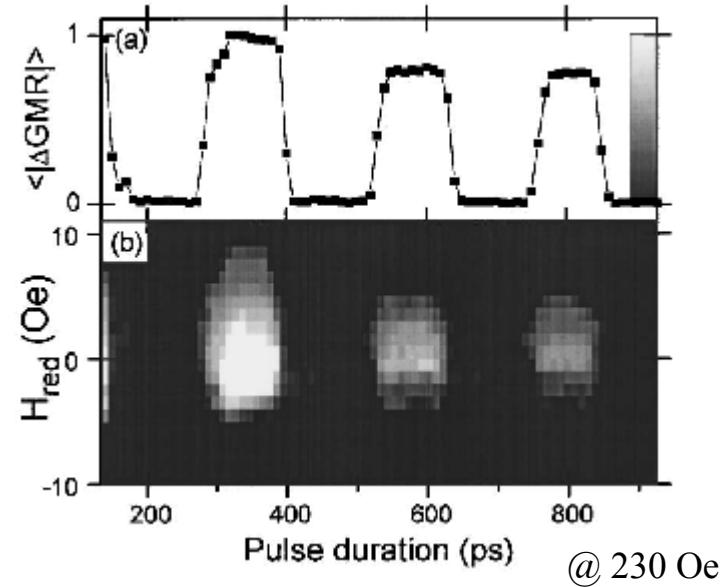
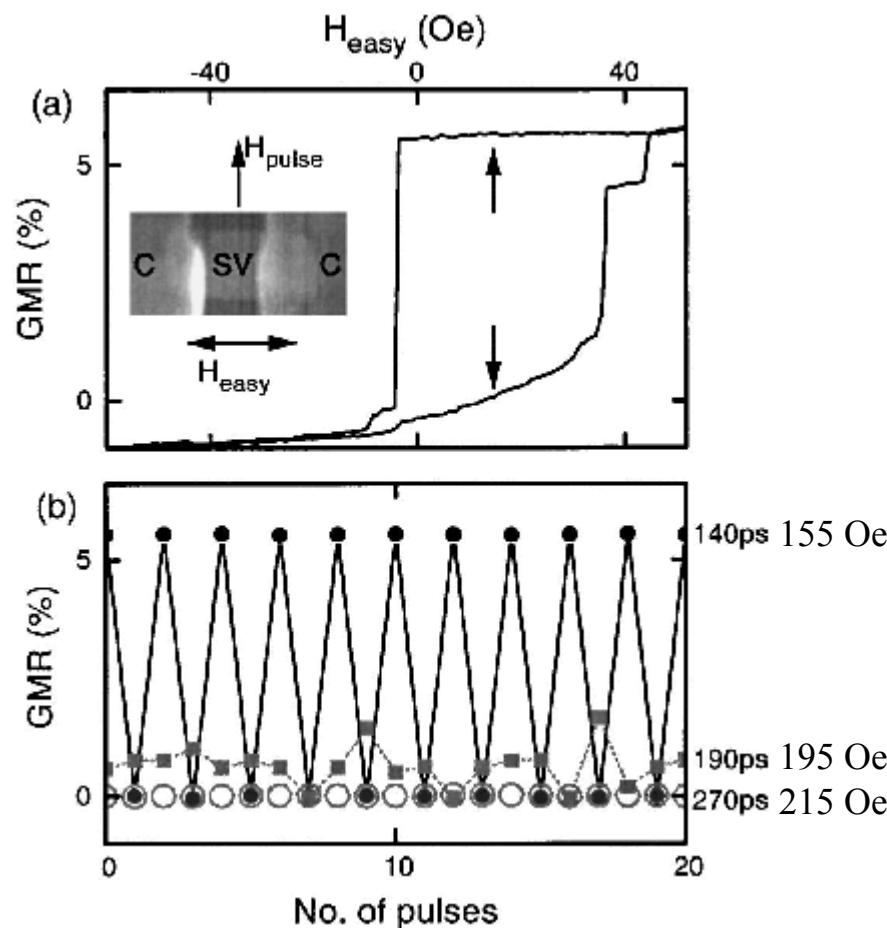
$$T = 175 \text{ ps}$$

$$H = 205 \text{ Oe}$$

$$T = 240 \text{ ps}$$

© 2003 The American Physical Society 017204-1

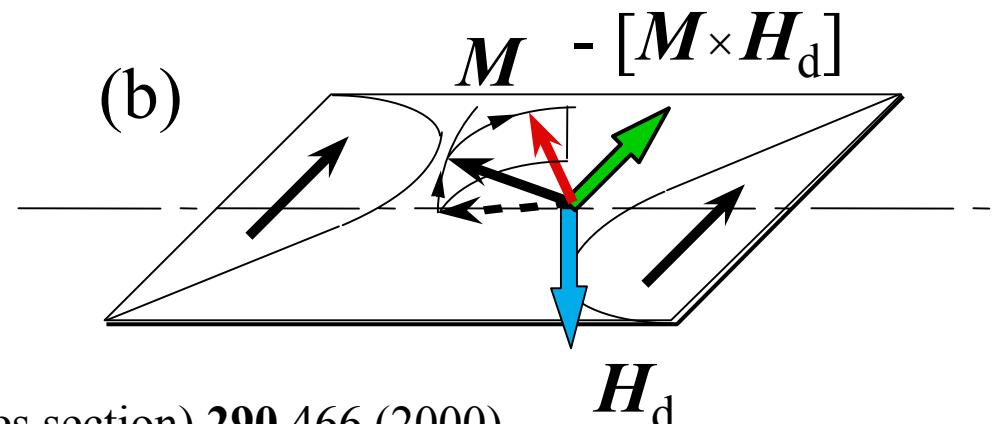
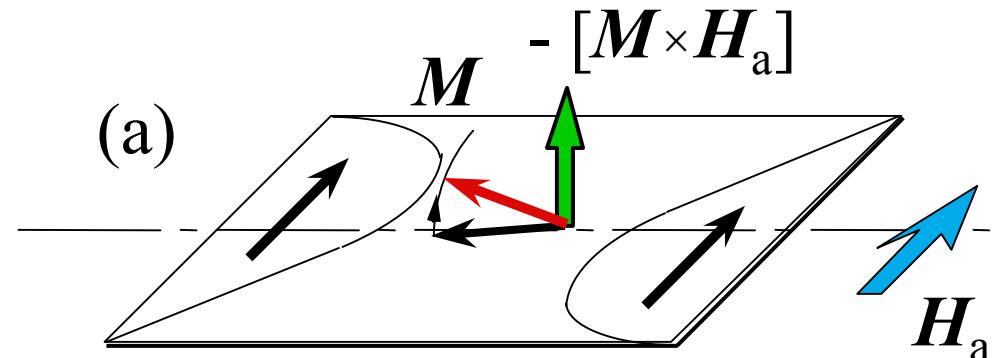
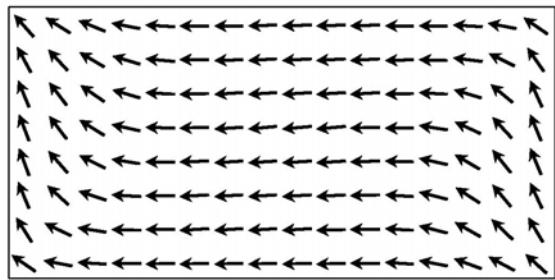
H.W. Schumacher et al.
Phys. Rev. Lett. **90** 017204 (2003)



H.W. Schumacher et al.
Phys. Rev. Lett. **90** 017201 (2003)

Precessional reversal of small elements

NiFe 500x 250x 5 nm, « S » state

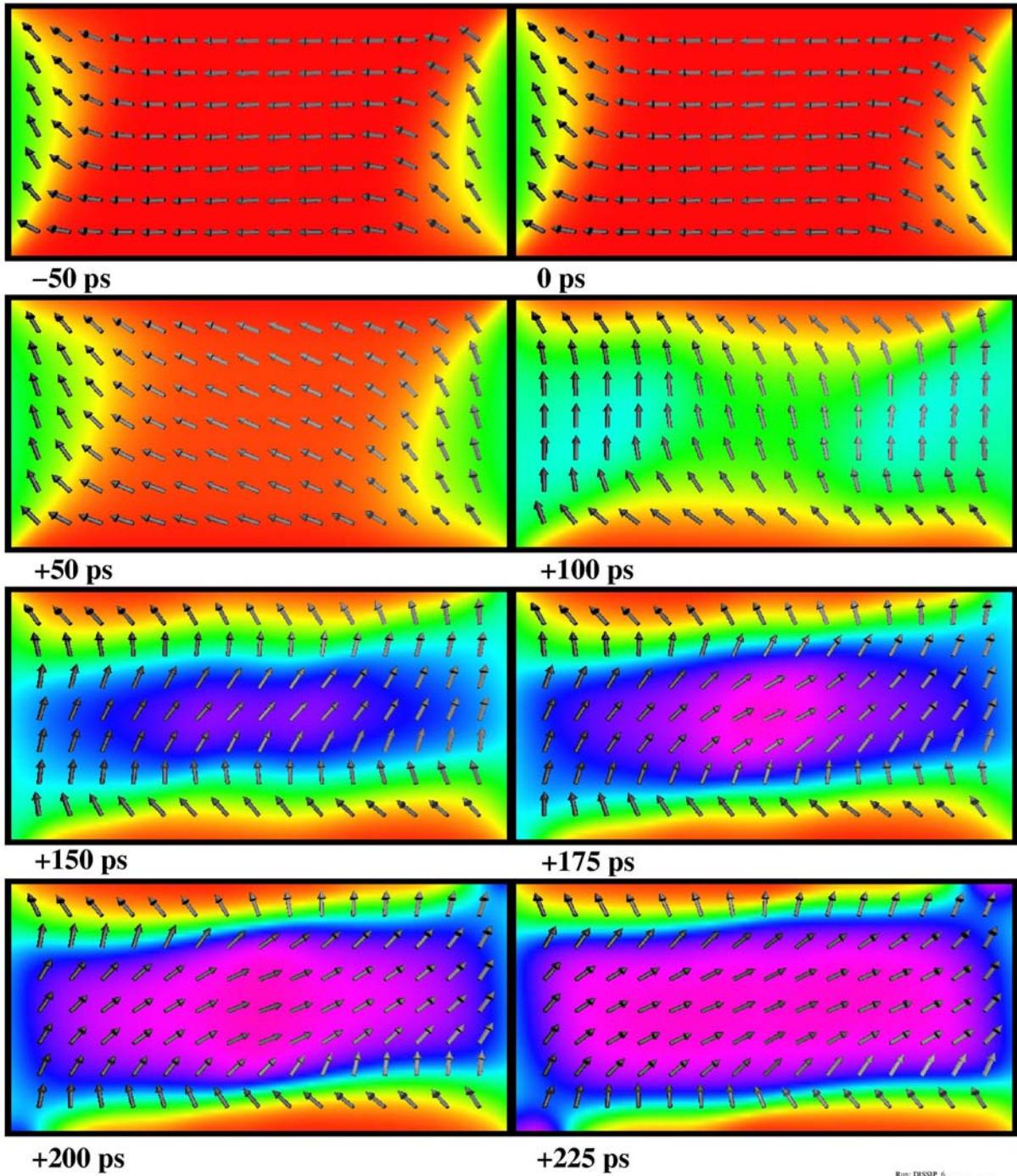


J. Miltat, A. Thiaville Science (perspectives section) 290 466 (2000)

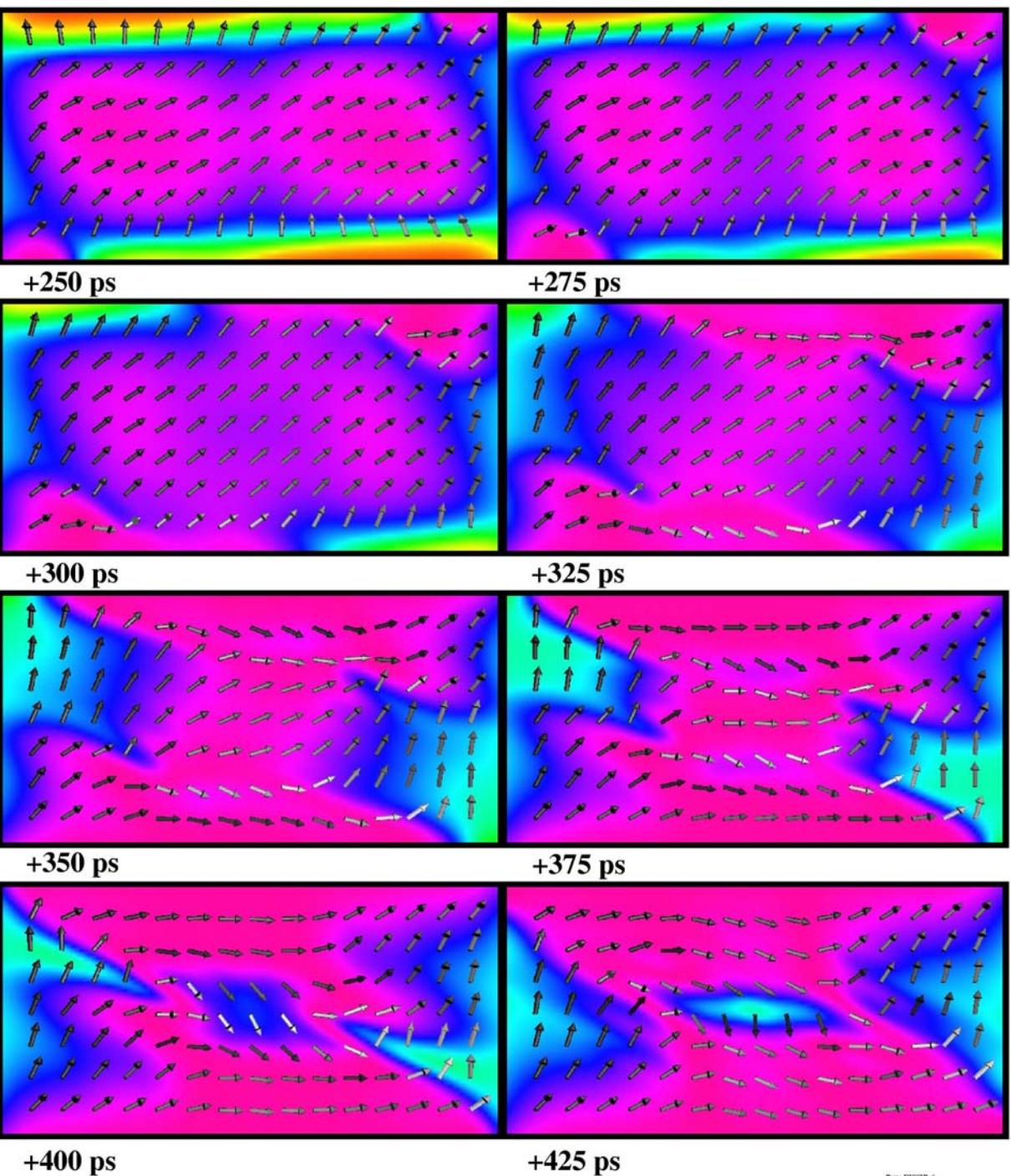
(1) Initial phase :
quasi-coherent
reversal

250 ps

J. Miltat et al., in
*Spin Dynamics in
confined structures I*,
B. Hillebrands and
K. Ounadjela Eds.
(Springer, 2002)

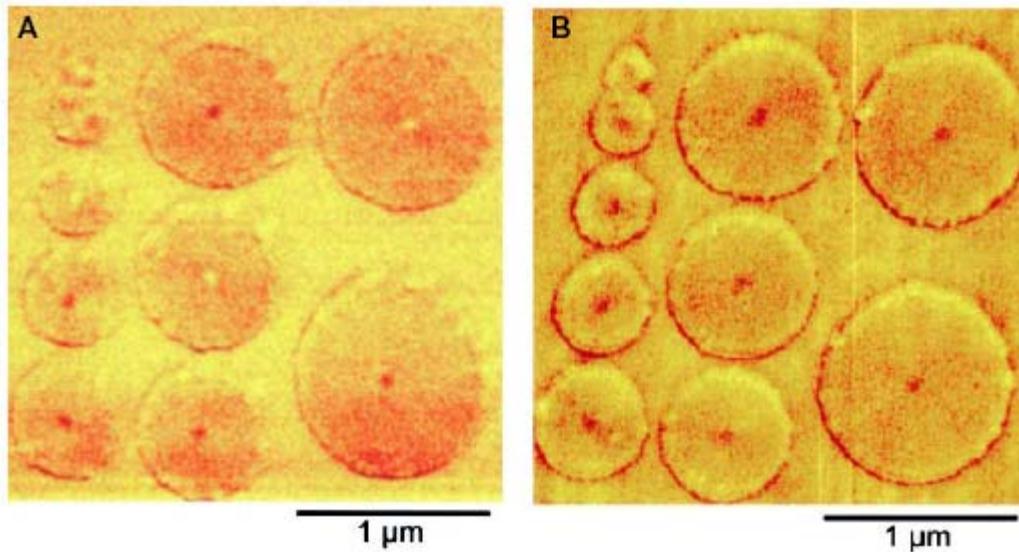


(2) Breaking into
magnetization waves
with large out of plane
components



MFM of magnetic dots in a vortex state

First observation: T. Shinjo et al., Science **289** (2000) 930



Natural state

After saturation under 1 T

Sample : permalloy, 50 nm thick

Vortex core switching : Experimental measurements

T. Okuno *et al.*, J. Magn. Magn. Mater. 240, 1 (2002)

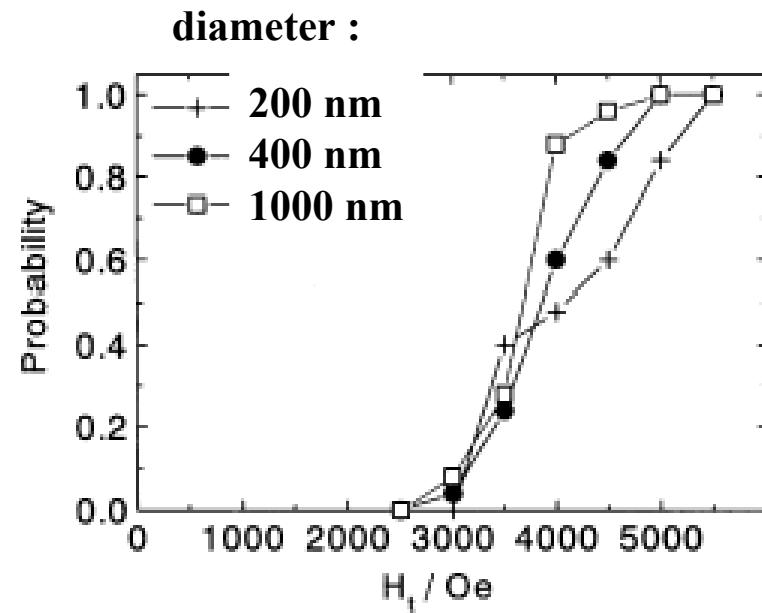
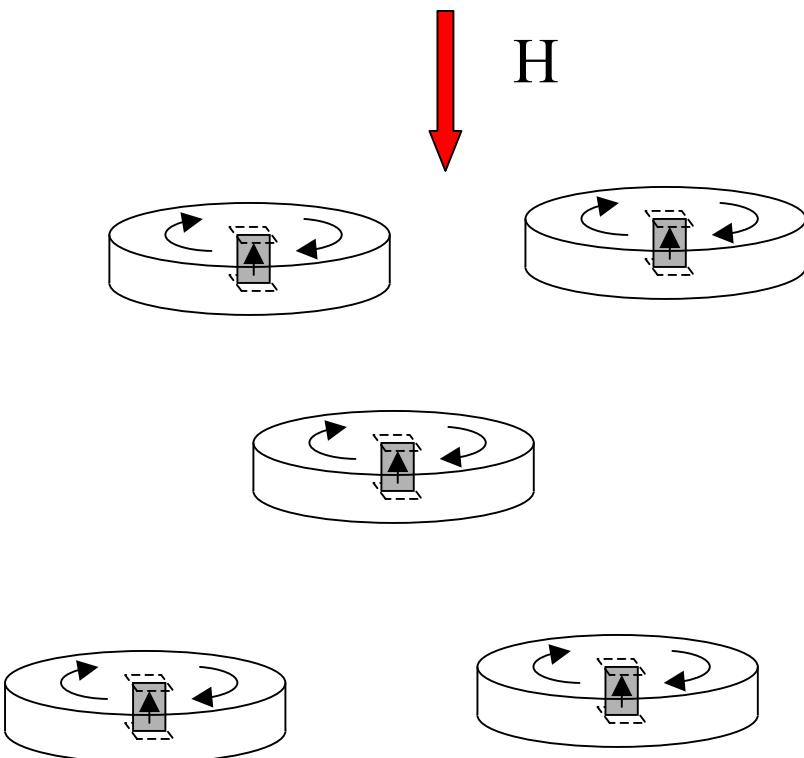
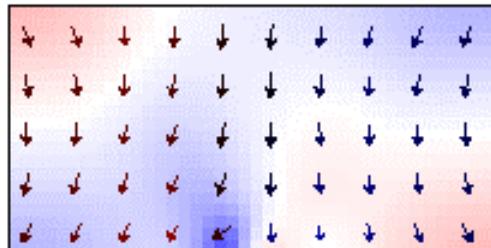


Fig. 5. Switching probability of a turned-up magnetization in circular dots with the diameter of 0.2, 0.4 and 1 μm as a function of magnetic field normal to the sample plane. The average switching field is 4100, 3900 and 3650 Oe in the sample of 0.2, 0.4 and 1 μm in diameter, respectively.

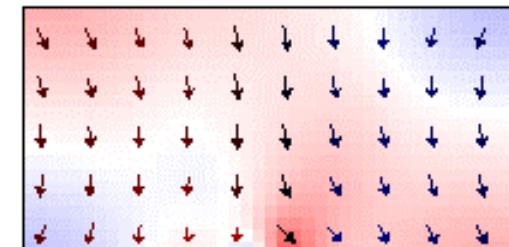
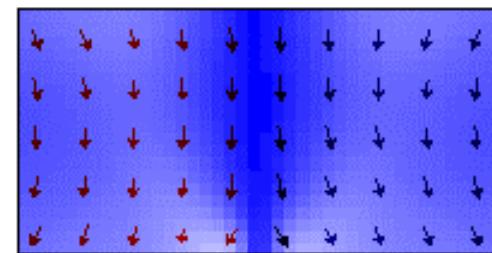
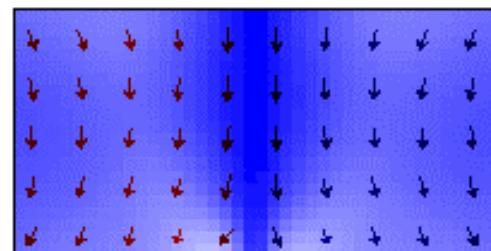
A Bloch point mediates the vortex core switching

B : from 331 to 332 mT
at $t=0$

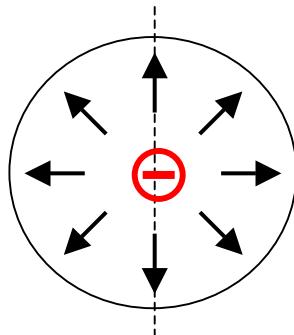
$d=100$ nm
thickness=50 nm
mesh: 4x4x5 nm
damping $\alpha=0.5$



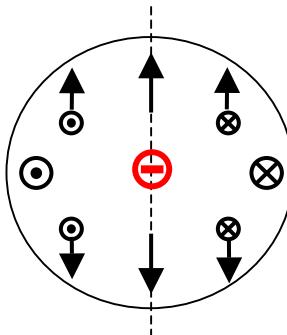
$t=1376.3$ ps



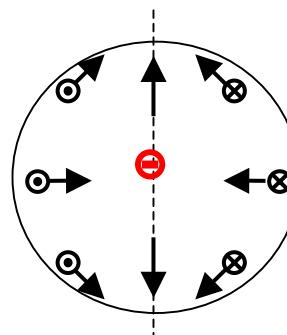
Bloch points at zero field



hedgehog



circulating



spiraling

E. Feldtkeller
Z. angew. Phys. **19** 530 (1965)

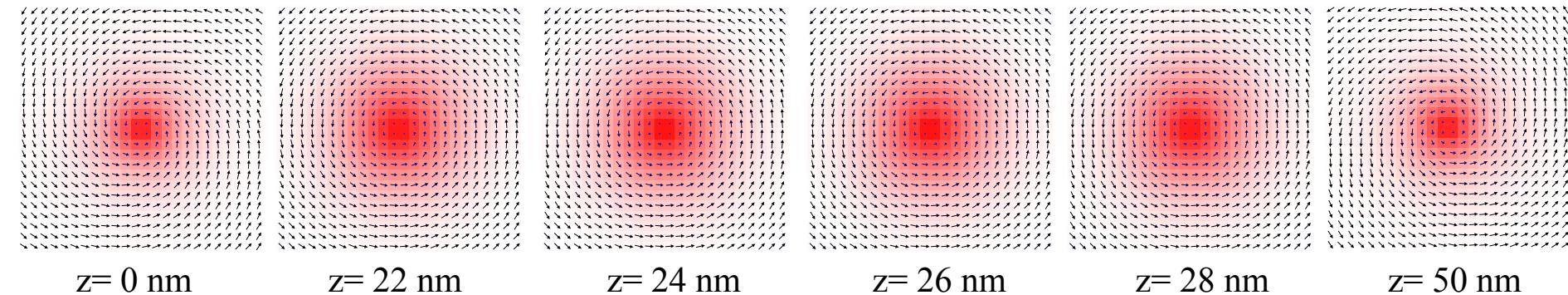
The exchange energy density diverges at the center (singularity)

It is lowest when $\vec{m} = \frac{\vec{r}}{r}$ up to a uniform rotation

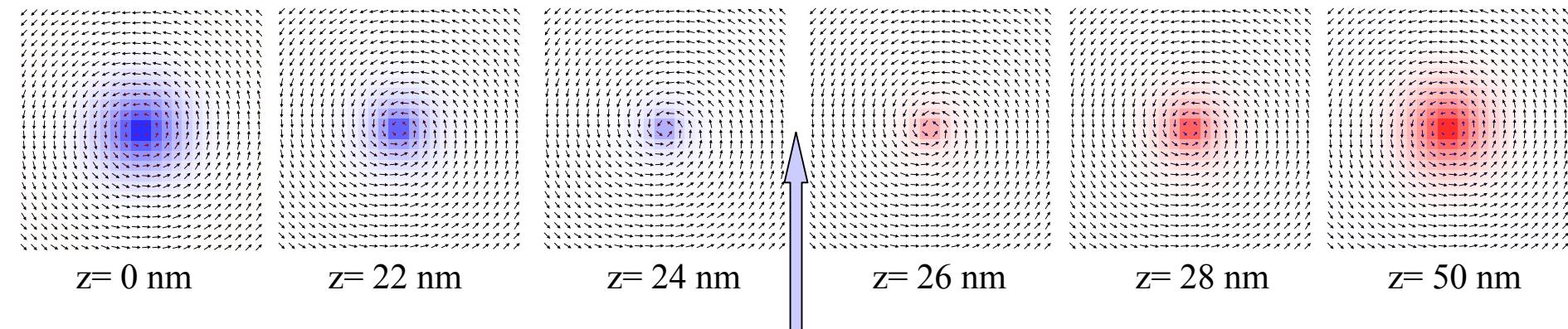
$$\varepsilon_A = (2A/r^2) \quad E_A = 8\pi A R \quad R: \text{radius of the BP structure}$$

Bloch points at zero field : calculated structure

Vortex (diameter=200 nm, thickness=50 nm, meshing=2.5 nm; image size: 60nm)



Vortex with a Bloch point in the middle



The BP is stabilized at zero H because of mesh friction; as soon as the BP is not perfectly centered it is expelled

Domain wall dynamics in nanowires



Cobalt 30 x 30 nm



diamètre 32, 64 nm

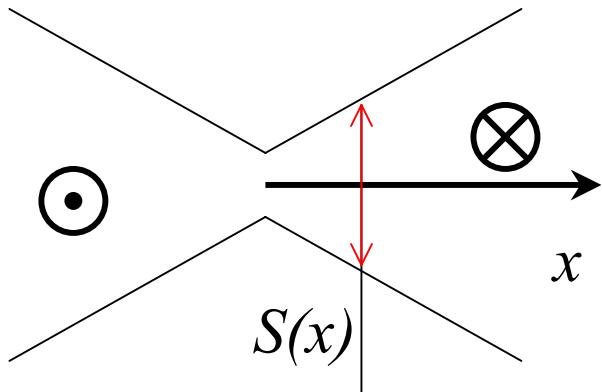
Permalloy Ni₈₀Fe₂₀



200 x 5 nm

Confinement effect on the domain wall width

P. Bruno, Phys. Rev. Lett. **83** 2425 (1999)



$$E = \int \left[A \left(\frac{d\theta}{dx} \right)^2 + K \sin^2 \theta \right] S(x) dx$$

$$\cancel{2K \sin \theta \cos \theta S - \frac{d}{dx} \left(2A \frac{d\theta}{dx} S \right) = 0}$$

$$\theta = C \int \frac{dx}{S(x)}$$

$$S = S_0 \left(1 + \left(\frac{x}{d} \right)^2 \right) \Rightarrow \theta = \text{Arctg} \left(\frac{x}{d} \right)$$

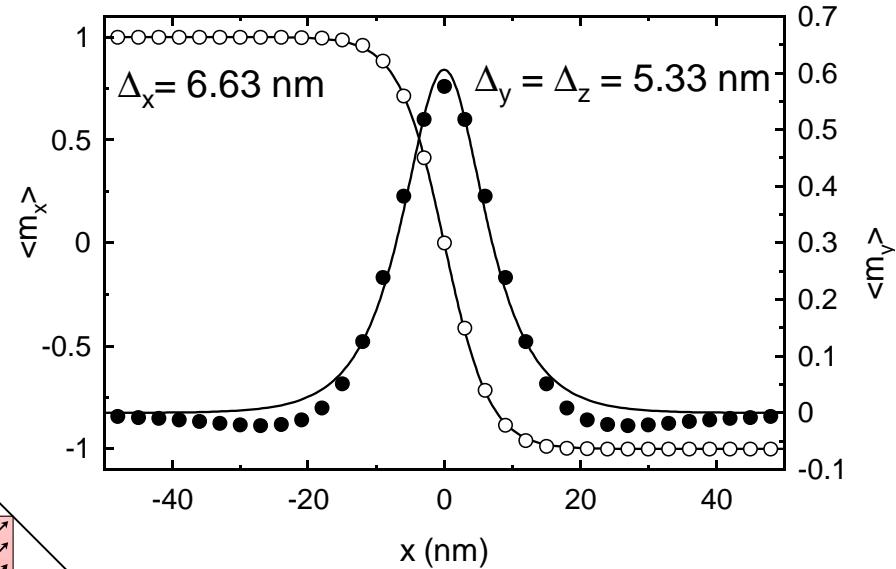
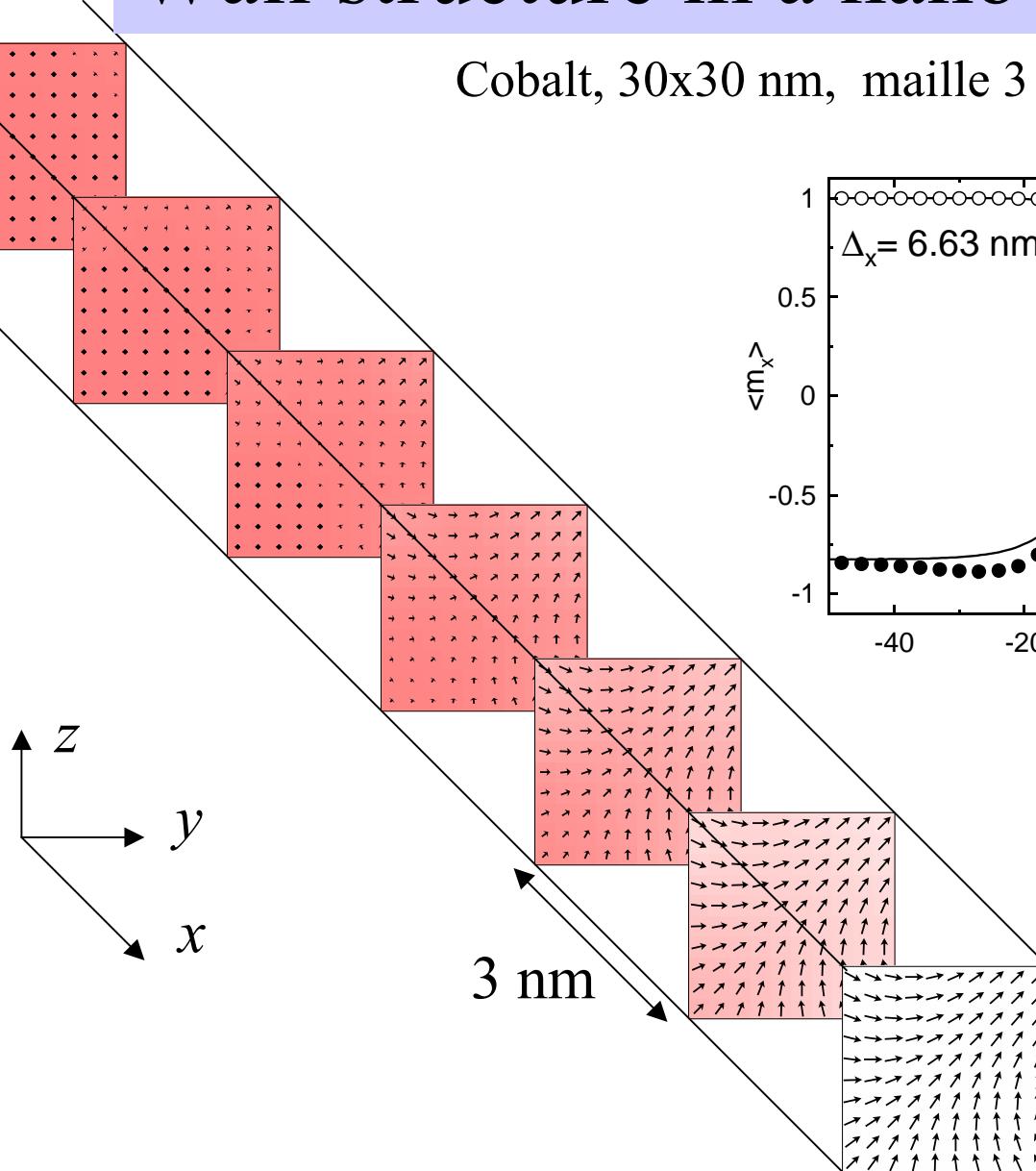
$$S = S_0 \left(1 + \frac{|x|}{d} \right)^2 \Rightarrow \theta = \frac{\pi}{2} \frac{x}{|x| + d}$$

⋮

wall width $\propto d$

Wall structure in a nanowire

Cobalt, 30x30 nm, maille 3 nm (167x 10x 10 points)

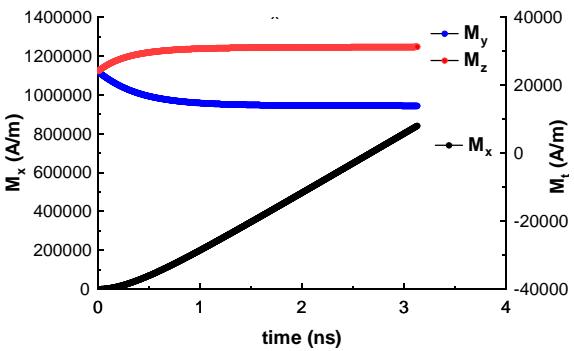


$$m_x \approx -\tanh(x / \Delta_x)$$
$$m_y \approx 1 / \text{ch}(x / \Delta_y)$$

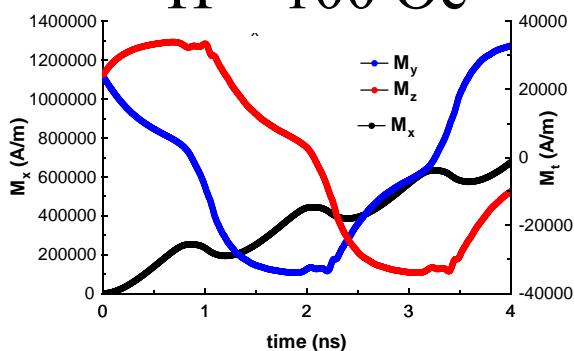
Wall dynamics under field

Damping constant $\alpha = 0.1$

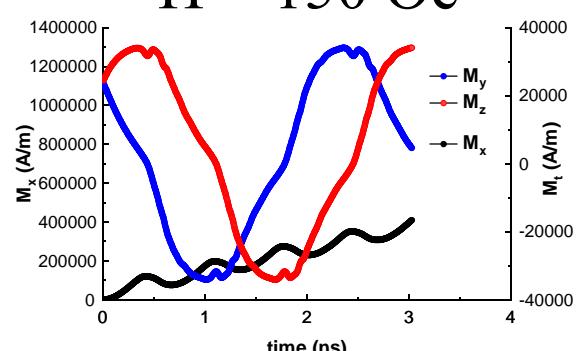
$H = 50$ Oe



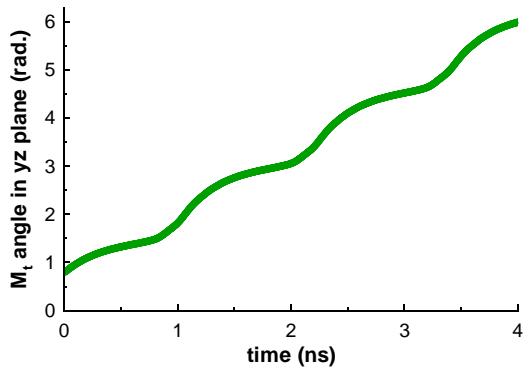
$H = 100$ Oe



$H = 150$ Oe

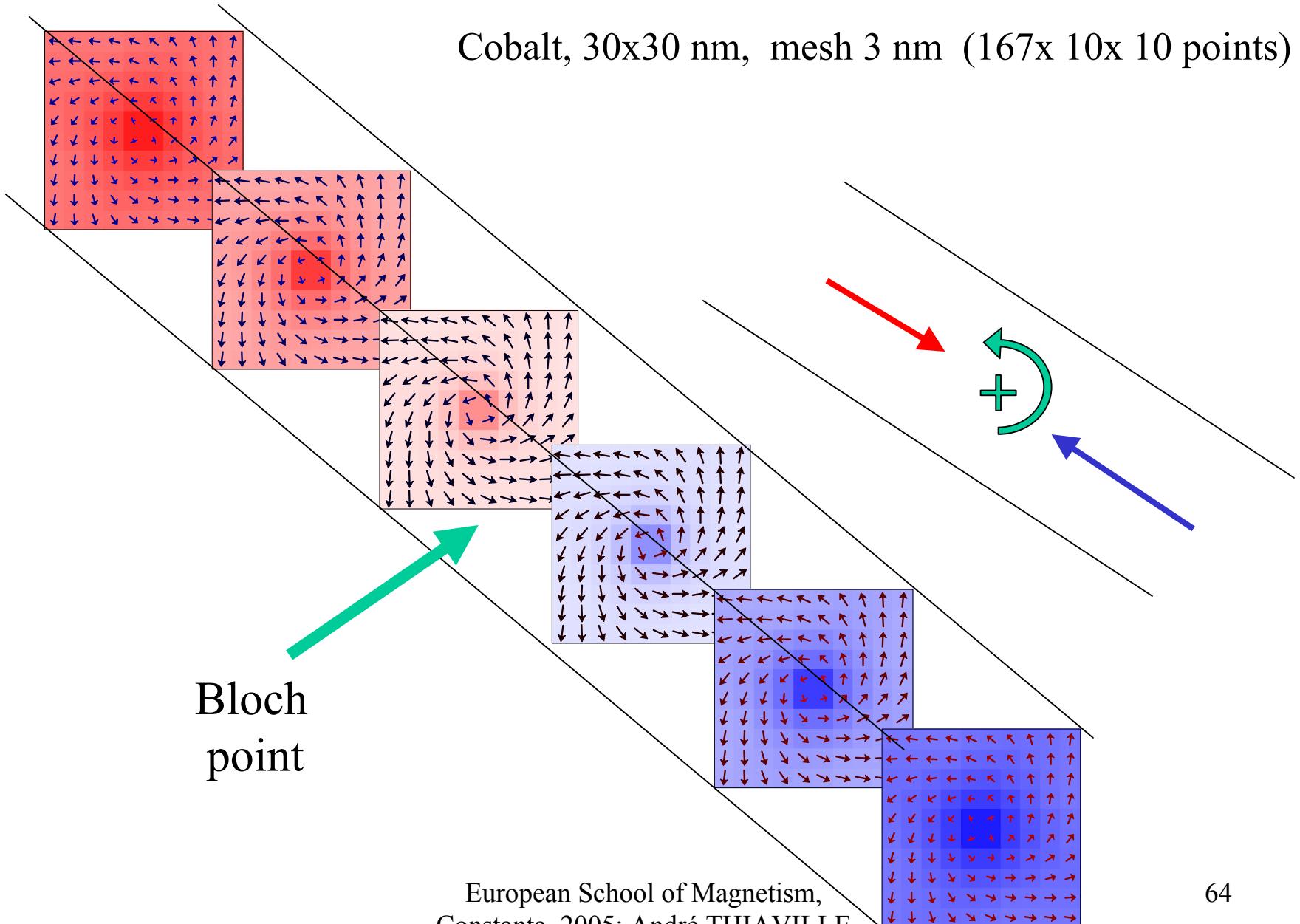


Angle of the
transverse
magnetization



Bloch point wall in a cobalt nanowire

Cobalt, 30x30 nm, mesh 3 nm (167x 10x 10 points)



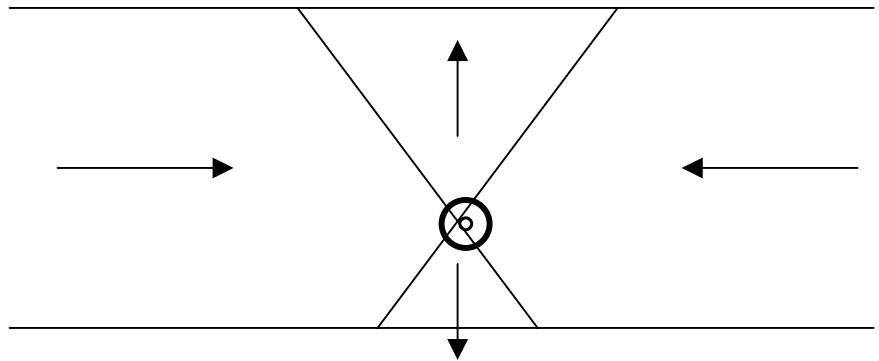
A permalloy nanostrip



$$\text{thickness } 5\text{nm} \approx \Lambda = (2A/\mu_0 M_s^2)^{1/2}$$



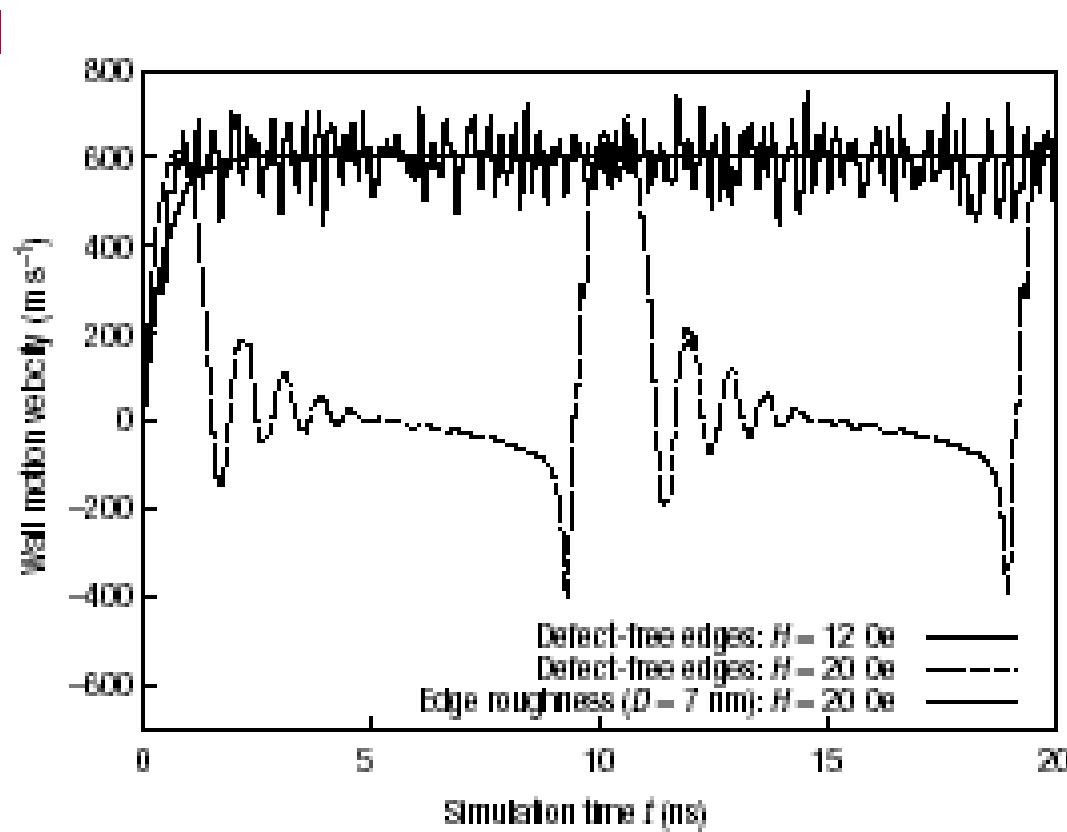
antivortex
displacement
direction



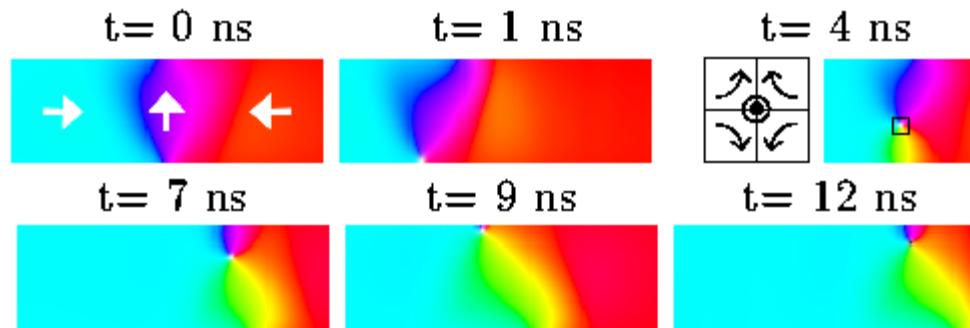
Y. Nakatani et al. Nature Mater. **2**, 521-523 (2003)

Domain wall dynamics in a permalloy nanostrip (200 x 5 nm)

Y. Nakatani et al.
Nature Mater. 2,
521-523 (2003)

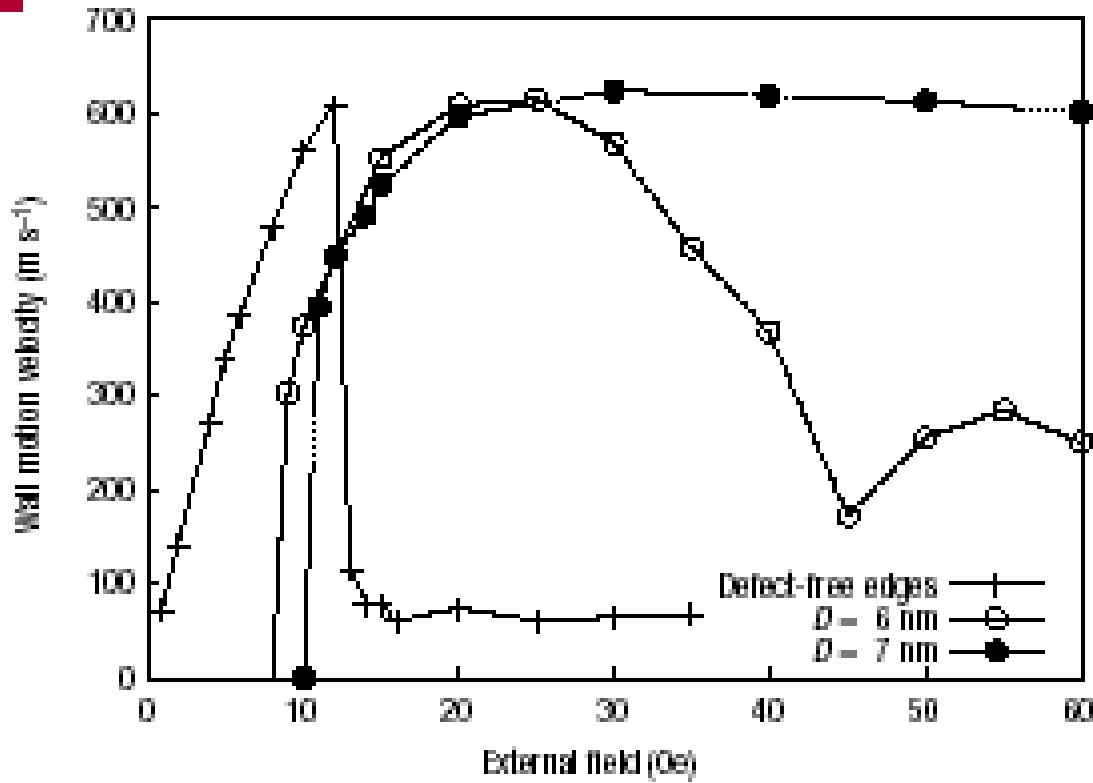


Perfect
strip



Effect of the roughness of strip edges

a



Thermodynamics of a macrospin

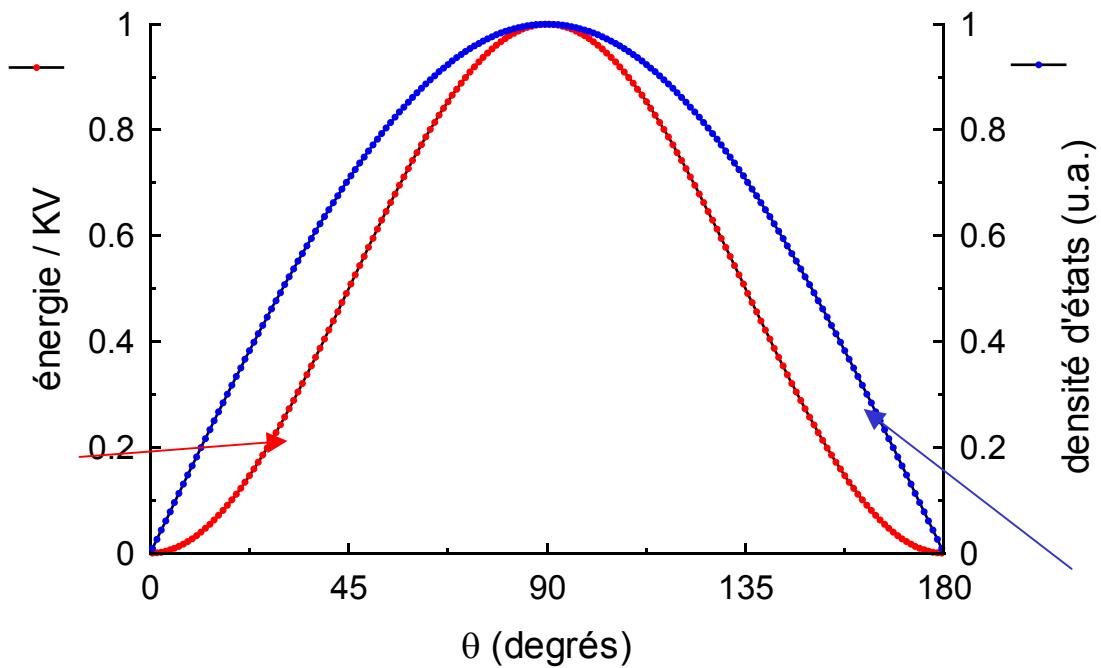
$$E = K V \sin^2\theta$$

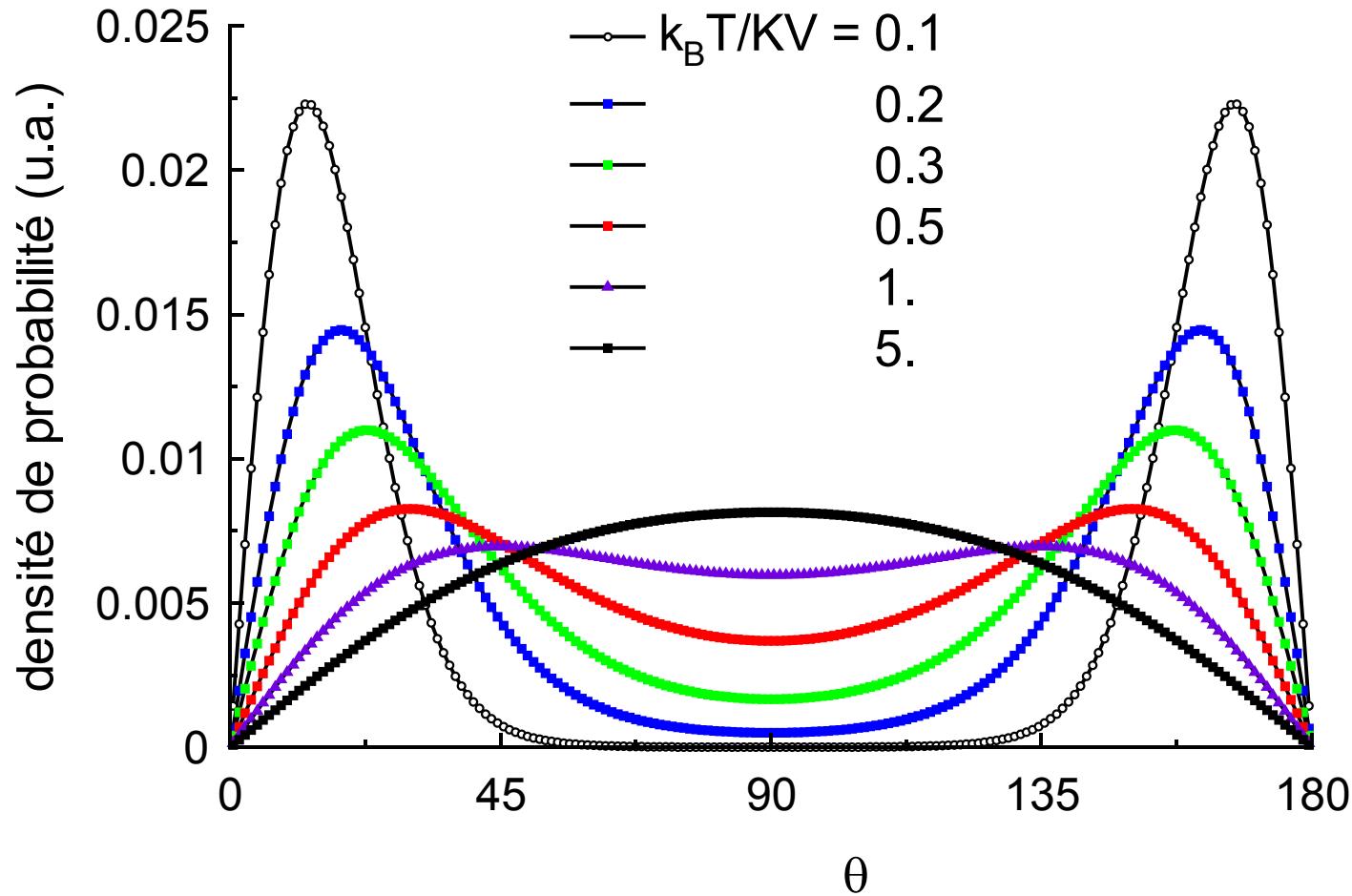
$$dS = \sin\theta \, d\theta \, d\phi / 4\pi \rightarrow \sin\theta \, d\theta / 2$$

Maxwell-Boltzmann statistics :

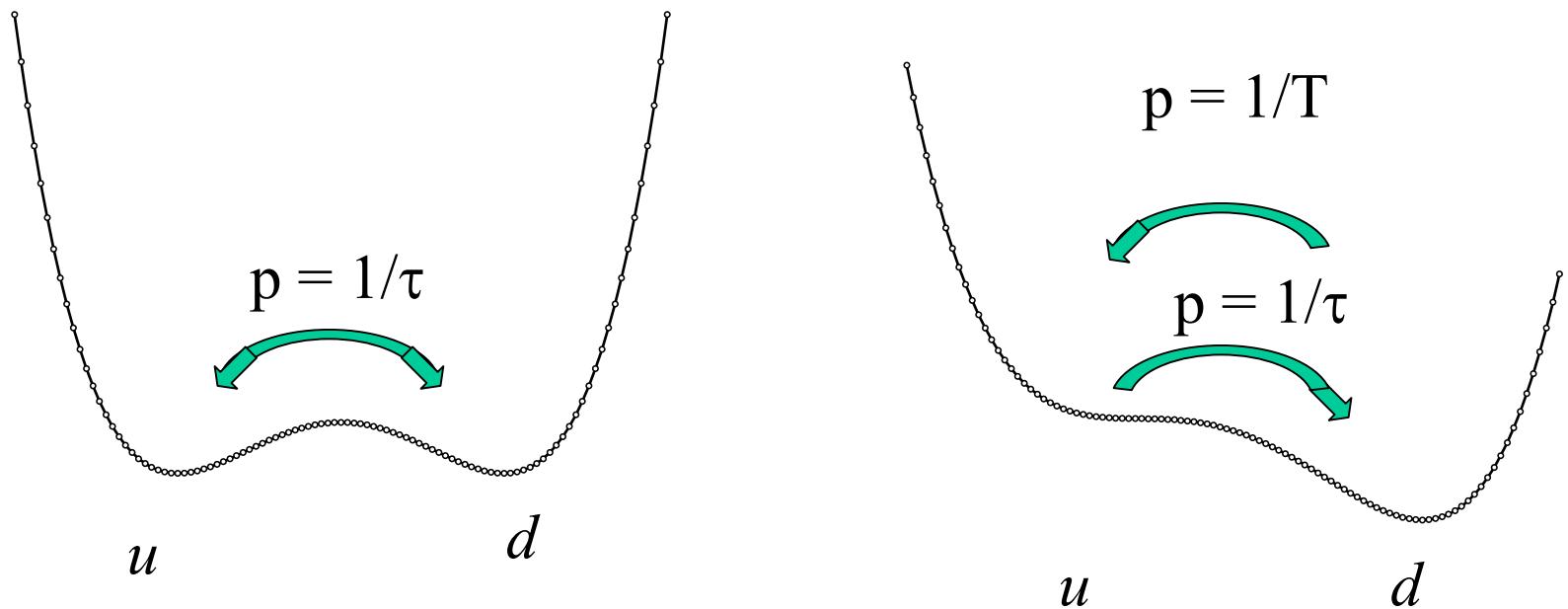
$$p(E) = \exp(-E/k_B T) / Z$$

$$\frac{K V}{k_B T} \text{ parameter}$$





Discrete orientation model (Néel-Brown)



$$\tau = \tau_0 \exp[(E_m - E(u)) / kT]$$

$$T = \tau_0 \exp[(E_m - E(d)) / kT]$$

Calculation of τ_0

$$1/\tau_0 = \frac{\alpha}{1+\alpha^2} \frac{\gamma_0 \sqrt{cc'}}{\mu_0 M_s} f(\text{col})$$

$\underbrace{\qquad\qquad}_{\omega_{\text{well}}}$

formulas of Brown,
Coffey...

$$\tau_0 \approx \text{qq. } 10^{-10} \text{ s}$$

with $\tau_0 = 0.1 \text{ ns}$
one has

$\tau =$	1s	1min	1h	1 jour	1 an	10 ans
$\Delta E/kT =$	23	27	31	34	40	43

Superparamagnetism : when $\tau < \tau_{\text{measurement}}$

Langevin field description of thermal fluctuations

$$\frac{d\vec{m}}{dt} = \gamma_0 \vec{H}_{eff} \times \vec{m} + \alpha \vec{m} \times \frac{d\vec{m}}{dt} \quad \vec{H}_{eff} = -\frac{1}{\mu_0 M_s} \frac{\delta E}{\delta \vec{m}} + \vec{H}_{th}$$

$$\left\langle \vec{H}_{th} \right\rangle = \vec{0} \quad \left\langle H_{th}^i(t) H_{th}^j(t') \right\rangle = \mu \delta_{ij} \delta(t - t')$$

$$\mu = \frac{2kT\alpha}{\gamma_0 M_s V} \quad \sigma(H_{th}^i) = \sqrt{\frac{2kT\alpha}{\gamma_0 M_s V dt}}$$

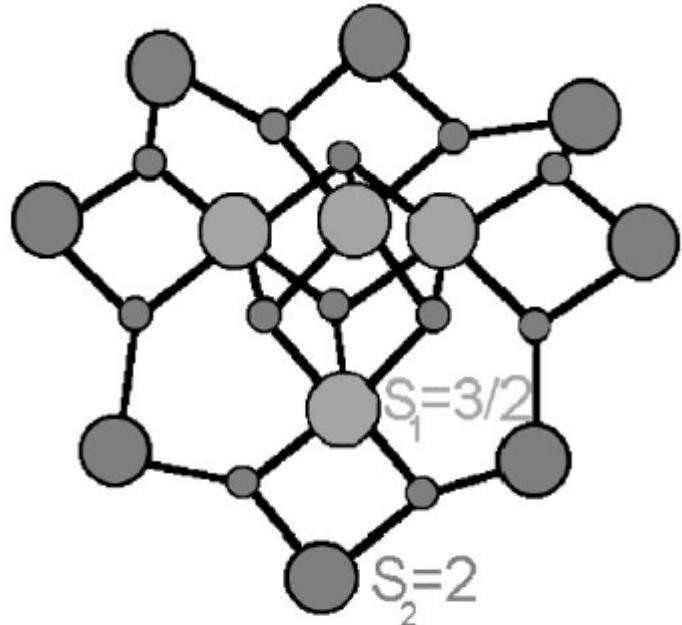
N.B. supposes a slow evolution

$$\hbar\omega < q q_\cdot kT$$

$$k/h = 2 \cdot 10^{10} \text{ Hz/K}$$

Beyond Micromagnetics

$\text{Mn}_{12}\text{-acetate}$: a molecular magnet



$$S_{\text{total}} = 8S_2 - 4S_1 = 10$$

Fig. 1. Schematic representation of the molecule of $\text{Mn}_{12}\text{-ac}$.

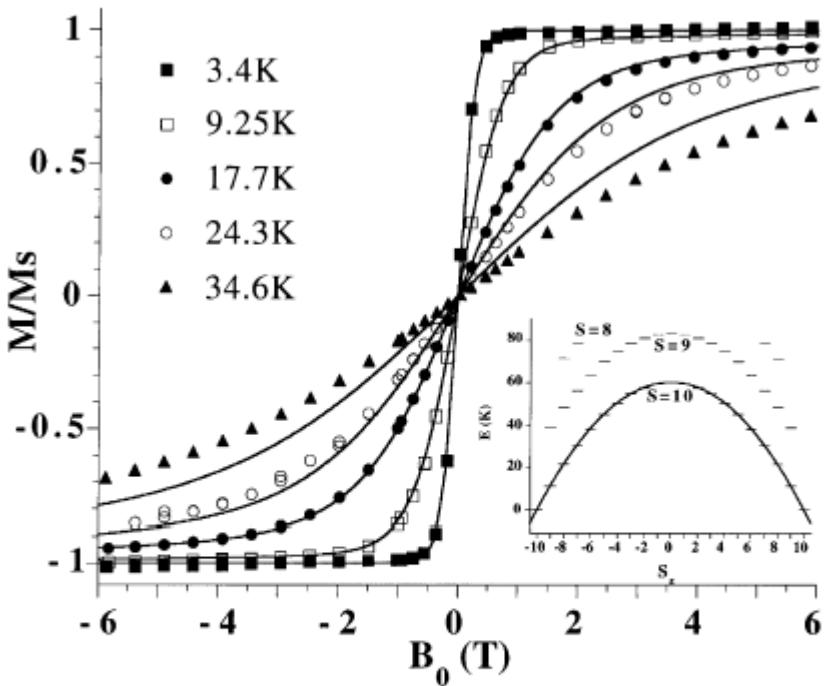


Fig. 2. Magnetization curves measured along the c -axis $M(H)$ in $\text{Mn}_{12}\text{-ac}$, above the blocking temperature. Fit to the $S = 10$ Hamiltonian. Inset: calculated energy levels $S = 10, 9, 8, \dots$

B. Barbara et al., JMMM 200, 167 (1999)

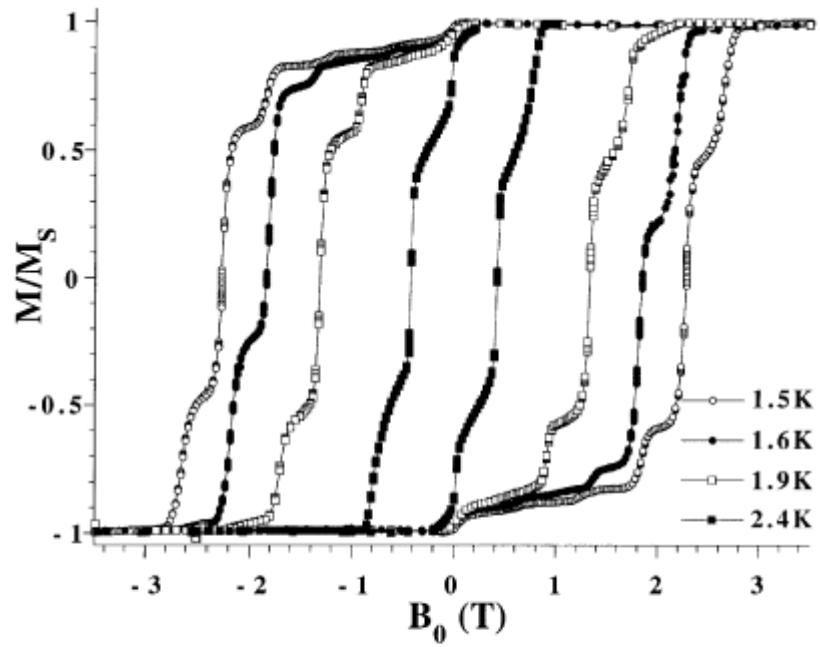


Fig. 3. Hysteresis loops of $\text{Mn}_{12}\text{-ac}$, with the field along the c -axis. Alternations of plateaux and steps suggest a ‘macroscopic quantization’ of the longitudinal magnetization component. This in fact simply reminiscient of the quantization of S_z of individual molecules + tunneling in the presence of a complex environment.

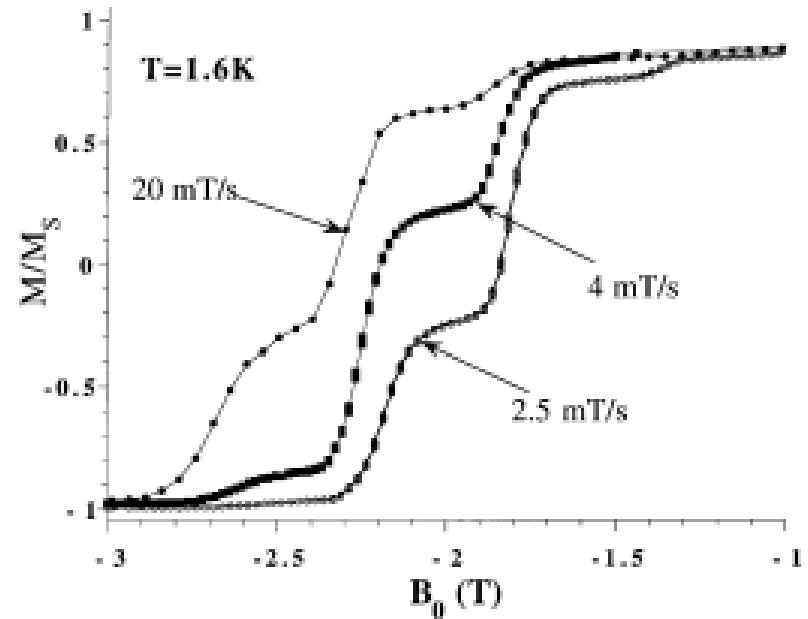


Fig. 4. Magnetization curves at different sweeping fields in $\text{Mn}_{12}\text{-ac}$.

B. Barbara et al., JMMM 200, 167 (1999)

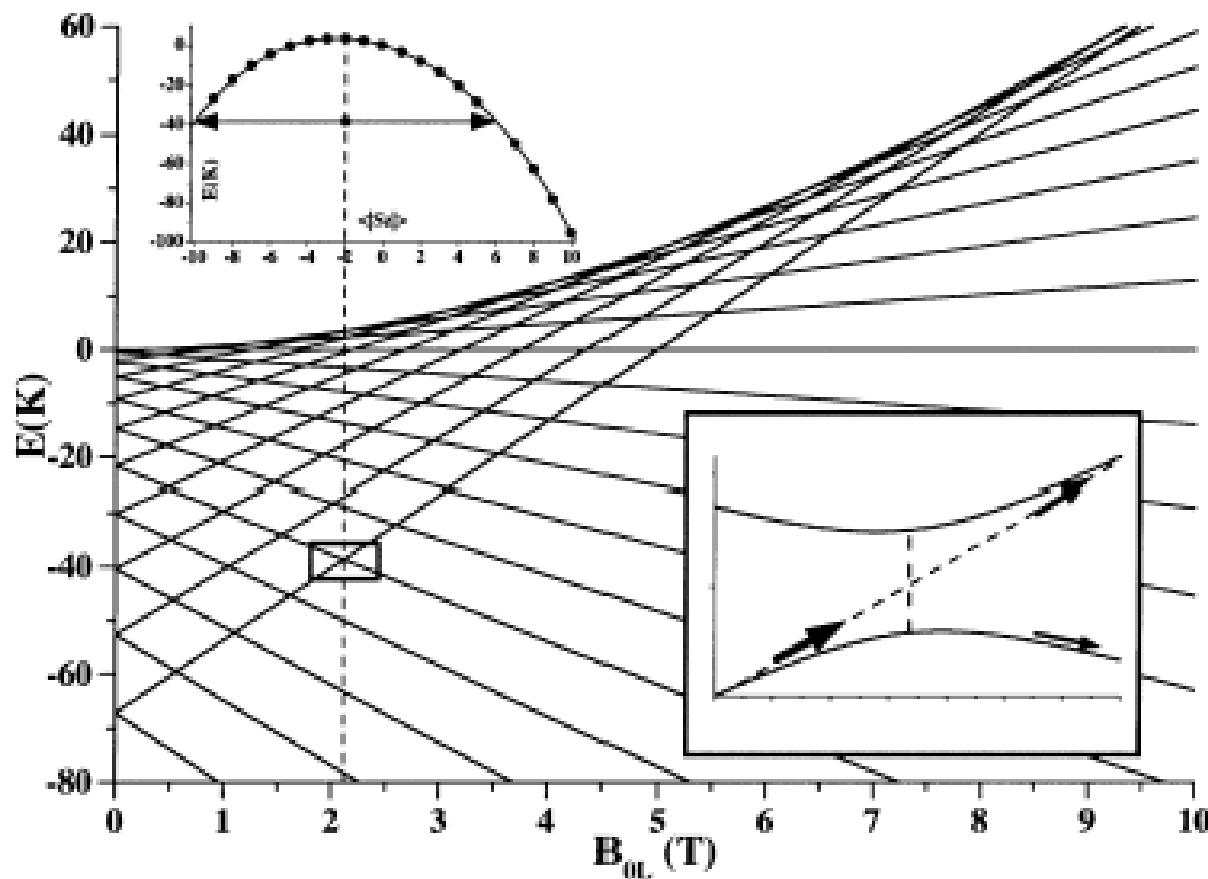
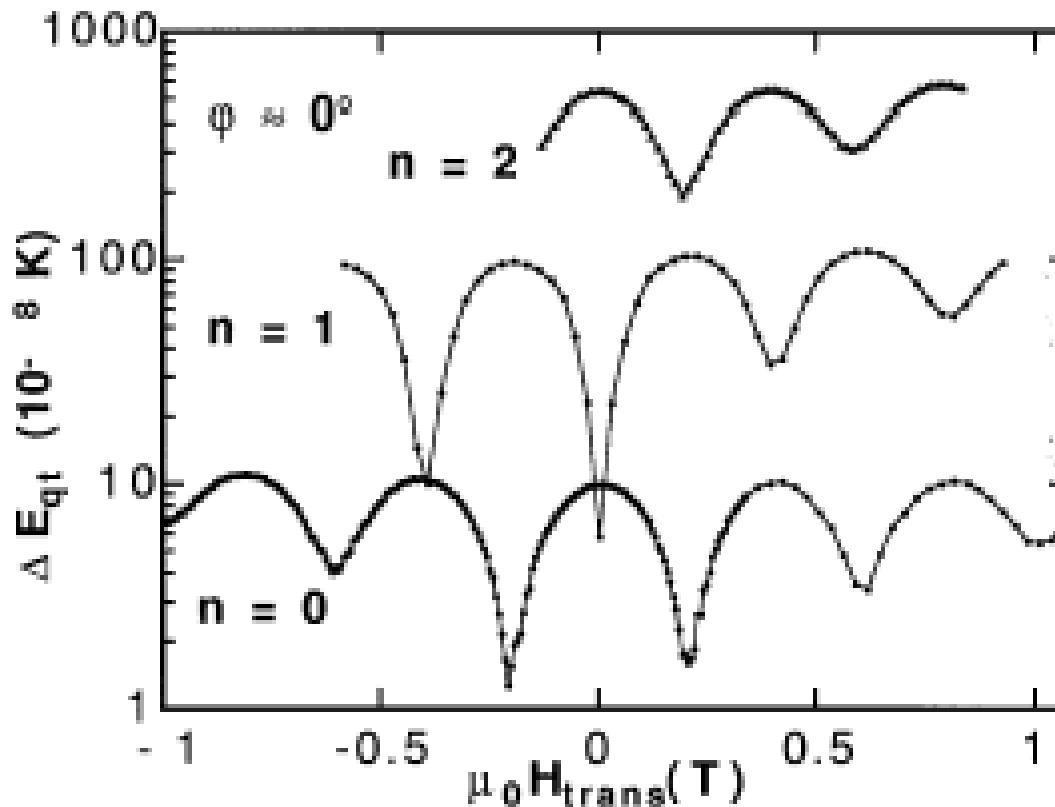


Fig. 6. Energy spectrum versus longitudinal field, calculated with the parameters given in the Appendix. Inset: enlargement of the $n = 4$ and $m = -10$ level anti-crossing with the tunneling gap and a representation of the adiabatic Landau-Zener mechanism. Top: energy barrier calculated for a field corresponding to $n = 4$.

Parity effect in tunneling



A. Caneschi et al.
Jmmm 200, 182
(1999)

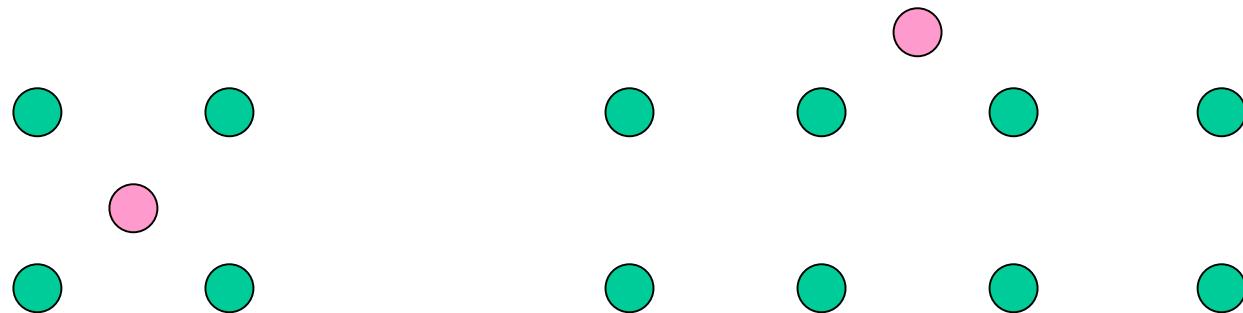
Fig. 12. Measured tunnel splitting $\Delta E_{q,t}$, at $T = 40$ mK, as a function of transverse field for $\phi \approx 0^\circ$, and for quantum transition between $M = -10$ and $(S - n)$. Note the parity effect when n is odd which is analog to the suppression of tunneling predicted for half-integer spins.

Magnetism of Fe : free atom vs bulk

Free atom : $Z=28 \quad 1s^2 \ 2s^2 2p^6 \ 3s^2 3p^6 \ 3d^6 \ 4s^2$

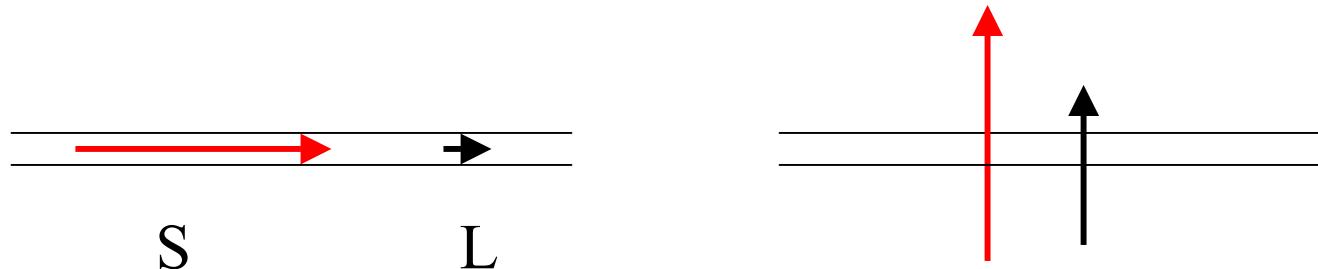
Hund's rule : $L=2$ & $S=2$: $6 \ \mu_B$ ($4 \ \mu_B$: spin + $2 \ \mu_B$: orbital)

Bulk metal : 3d & 4sp bands : $2.1 \ \mu_B$ ($2 \ \mu_B$: spin + $0.1 \ \mu_B$: orbital)



The simple model of P. Bruno (simplified)

$$H_{\text{spin-orbit}} = \lambda \vec{L} \cdot \vec{S} \quad \text{for an atom}$$

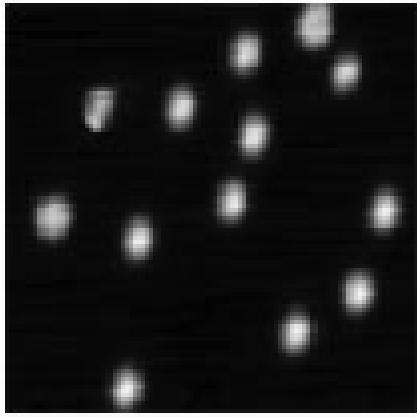


$$E_{\perp} - E_{\parallel} = \lambda S(L_{\perp} - L_{\parallel})$$

$$\lambda \approx 10 \text{ meV} : \Delta L = 1 \quad \longrightarrow \quad K = 10 \text{ meV/atom}$$

(bulk Co : $5 \cdot 10^5 \text{ J/m}^3 = 25 \mu\text{eV/atom}$)

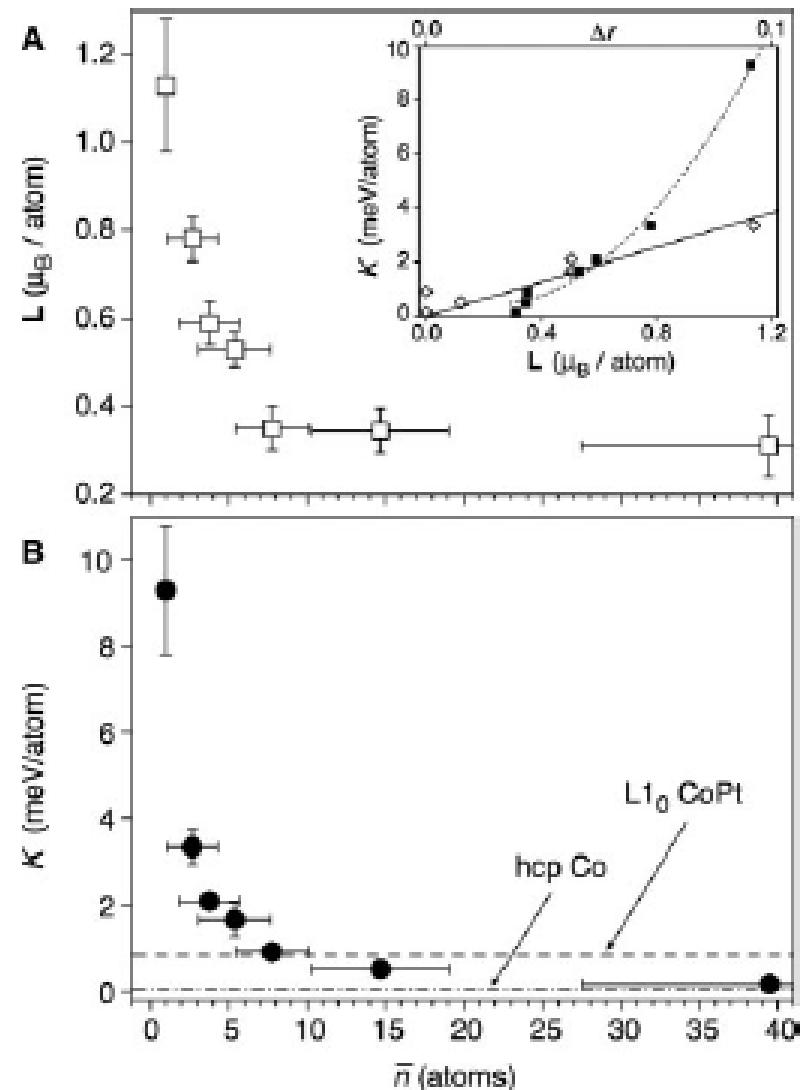
Magnetic anisotropy and orbital moment in Co clusters of a few atoms



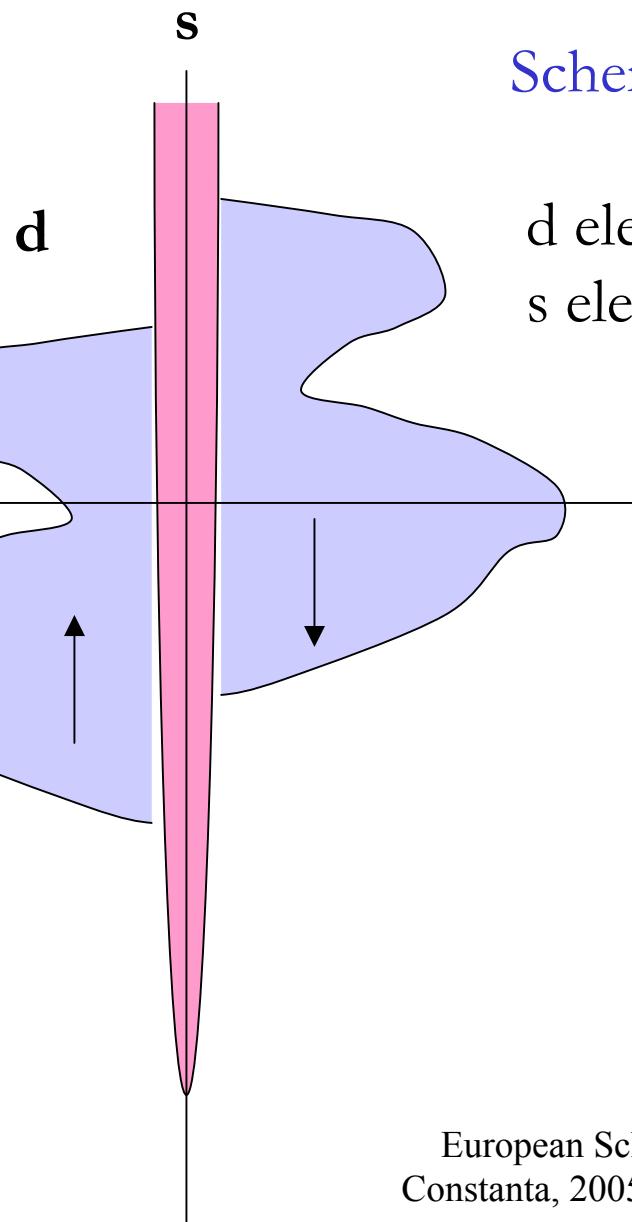
Co / Pt(111)
0.01 plan atomique
8.5 x 8.5 nm²

P. Gambardella et al.
Science 300, 1130
(2003)

Fig. 3. (A) L as a function of \bar{n} measured along the easy magnetization direction ($\theta_0 = 0^\circ$). (B) K as a function of \bar{n} . For comparison, the dashed and dashed-dotted lines show the MAE per Co atom of the L1₀ CoPt alloy and hcp-Co, respectively. The values of n were determined *in situ* by fitting the superparamagnetic response of each particle assembly by means of Eq. 3. The average sizes so obtained are within $\pm 10\%$ of those determined by STM for the same growth conditions. For a given size, the particles consist of different isomers. Particles with $5 < \bar{n} \leq 40$ have a compact shape. The Co interatomic distance is that of the underlying Pt lattice. The error bars on the horizontal scale in (A) and (B) represent the standard deviation of the size distribution determined by STM. (Inset) K is plotted as a function of L (filled squares) and as a function of $\Delta r = r(0^\circ) - r(70^\circ)$ for $\bar{n} > 1$ (open diamonds). $\Delta r = 0.1$ corresponds to about $\Delta L = 0.2 \mu_B$; the errors on Δr (not shown) are on the order of ± 0.04 . The lines are guides to the eye.



Magnetism and transport



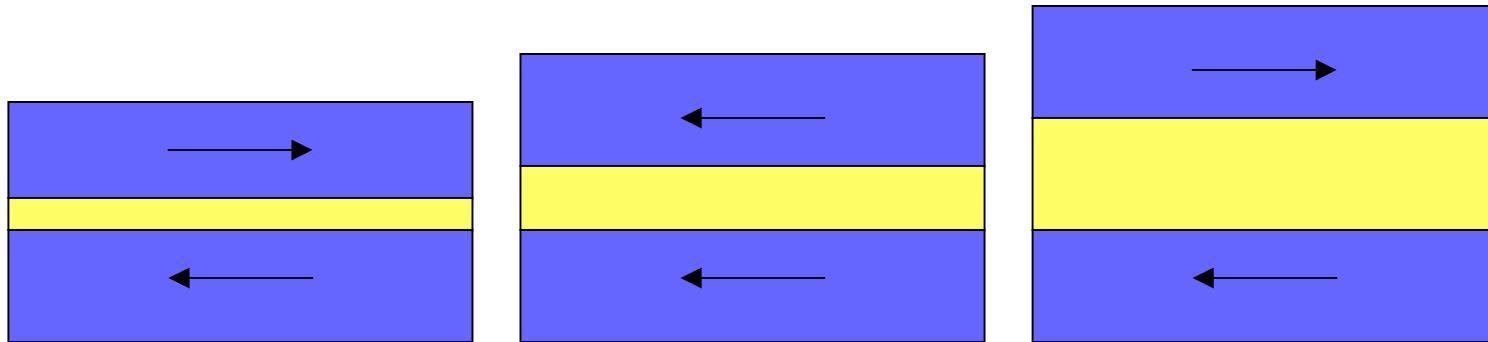
Schematic model of the 3D magnetic metals :

d electrons : localized, magnetism
s electrons : delocalized, transport

$$\sigma = \frac{ne^2\tau}{m}$$

$$\frac{1}{\tau} = \frac{2\pi}{\hbar} \left| V_{diff} \right|^2 k_B T N(E_F)$$

Interlayer exchange coupling (1986)



Oscillation periods depend on spacer material and crystalline orientation

Calculations based on the electronic structure

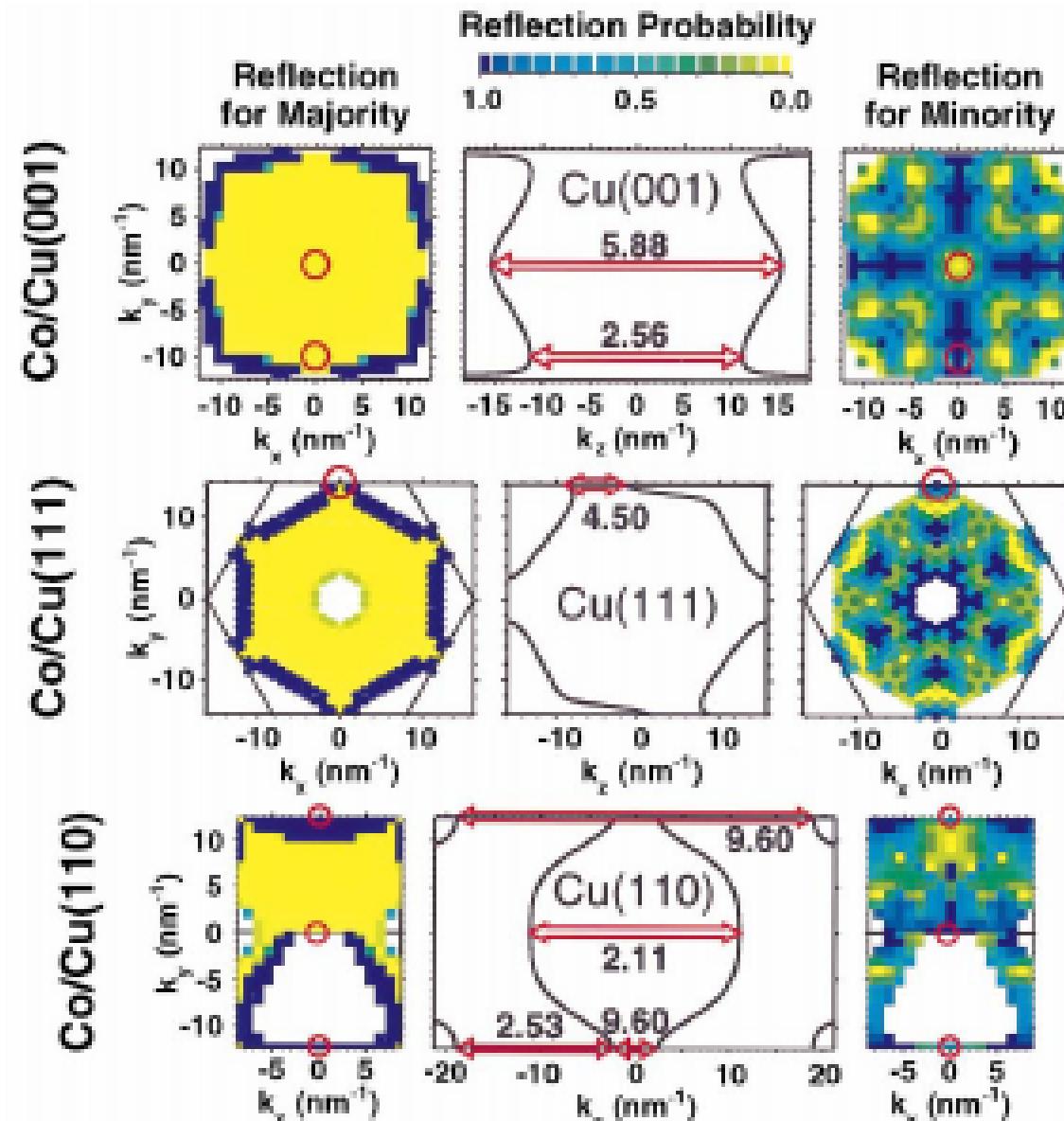


Fig. 1. Critical spanning vectors and interface reflectivities. For a series of spacer layers, magnetic materials, and interface orientations, organized in rows, the middle panels show slices through the Fermi surface of each spacer layer material for $k_z = 0$. The interface normal is the z direction in all cases. Superimposed in red on the Fermi surfaces are some of the critical spanning vectors. Each critical spanning vector is labeled by its associated coupling period in monolayers as determined from the experimental Fermi surfaces [22,114]. In the left and right panels, the Fermi surface is projected onto the $k_z = 0$ plane. It is color-coded based on the probability for an electron incident from the spacer layer material to reflect from the interface with the magnetic material. Probabilities for electrons with spins parallel to the majority and minority spin directions are shown in the left and right panels, respectively. The locations of the critical spanning vectors are labeled by red circles centered at the critical point. The Cu Fermi surface projected into a (110) interface and the Cr Fermi surface projected into a (001) interface have multiple sheets. To present these overlapping sheets, each is only shown in a fraction of the interface Brillouin zone. The full Fermi surface can be reconstructed by rotating the various partial sheets into to the other symmetric parts of the zone.

M.D. Stiles,
JMMM 200, 322 (1999)

Giant magneto-resistance (1988)

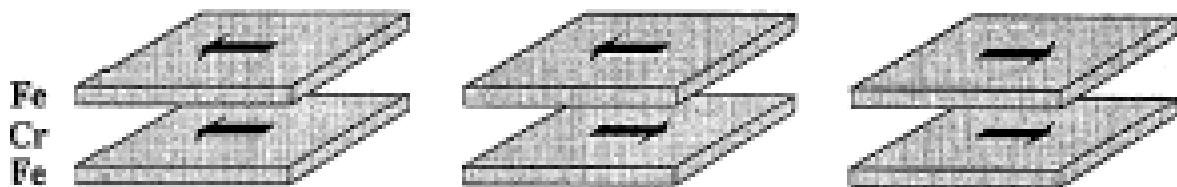
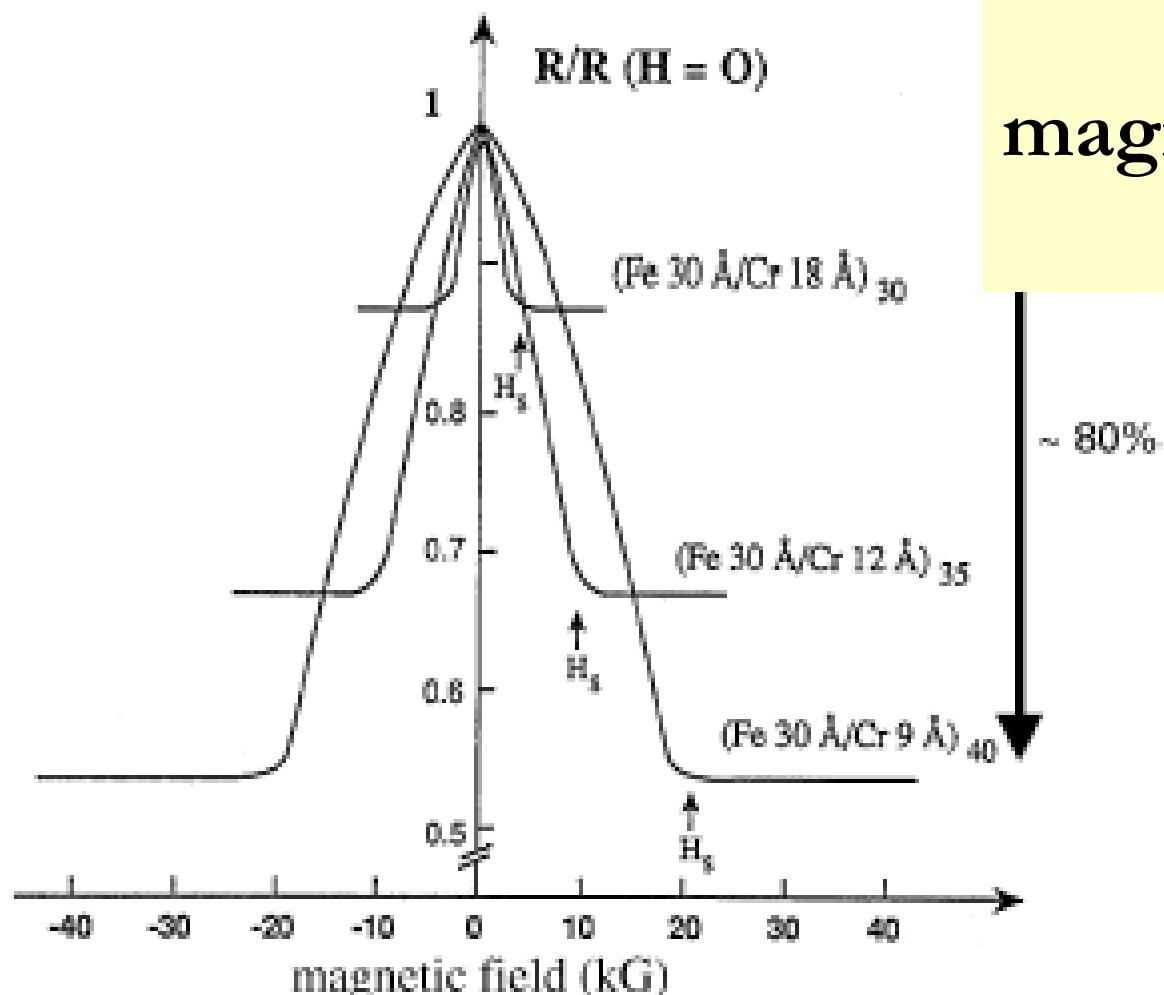


Fig. 1. Magnetoresistance curves at 4.2 K of (Fe/Cr) multi-layers [1].

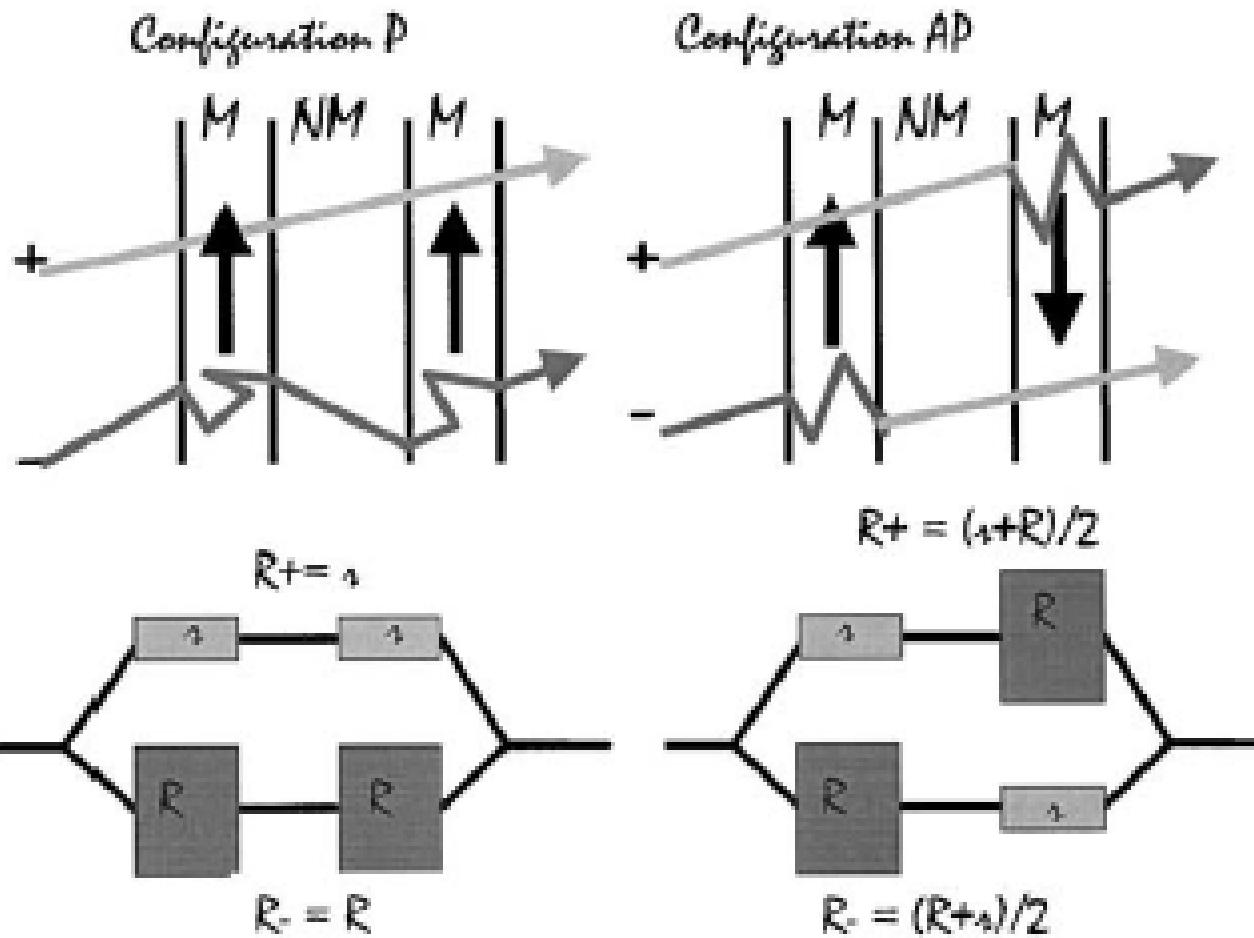
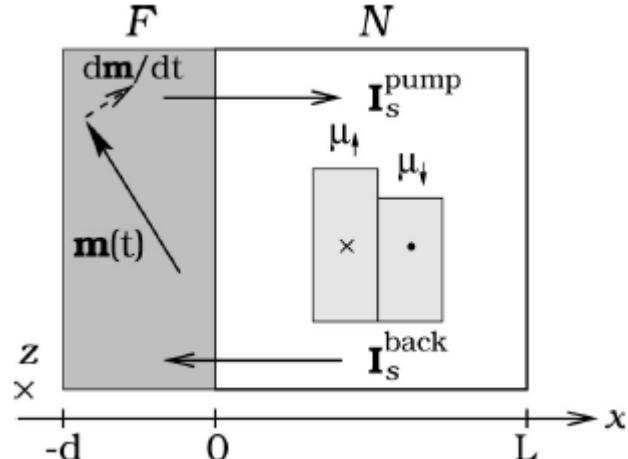


Fig. 3. Schematic picture of the GMR mechanism. The electron trajectory between two scatterings are represented by straight lines and the scattering by abrupt change in the direction. The signs + and - are for spins $S_z = \frac{1}{2}$ and $-\frac{1}{2}$, respectively. The arrows represent the majority spin direction in the magnetic layers.

Spin pumping



TSERKOVNYAK, BRATAAS, AND BAUER

PHYSICAL REVIEW B **66**, 224403 (2002)

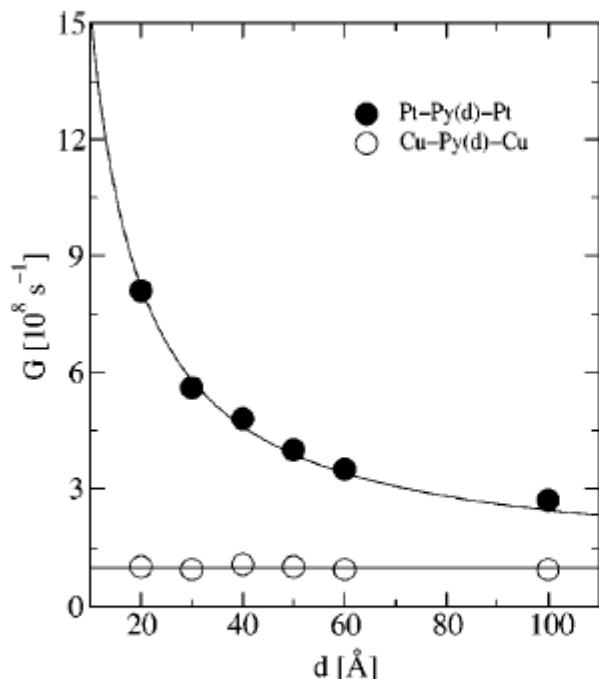


FIG. 3. Circles show measured (Ref. 6) Gilbert parameter G of a permalloy film with thickness d sandwiched between two normal-metal (Pt or Cu) layers. Solid lines are predictions of our theory with two fitting parameters, G_0 , and $g^{\uparrow\downarrow}$ -Py bulk damping and Py-Pt mixing conductance, respectively, see Eq. (22).

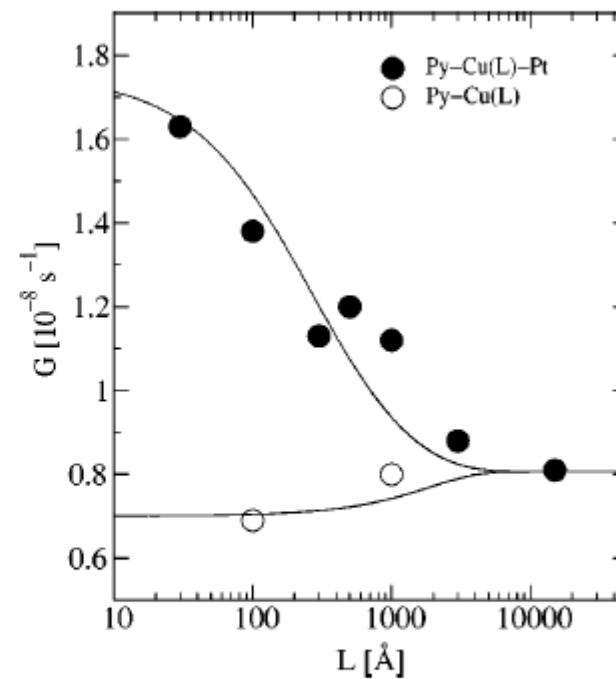
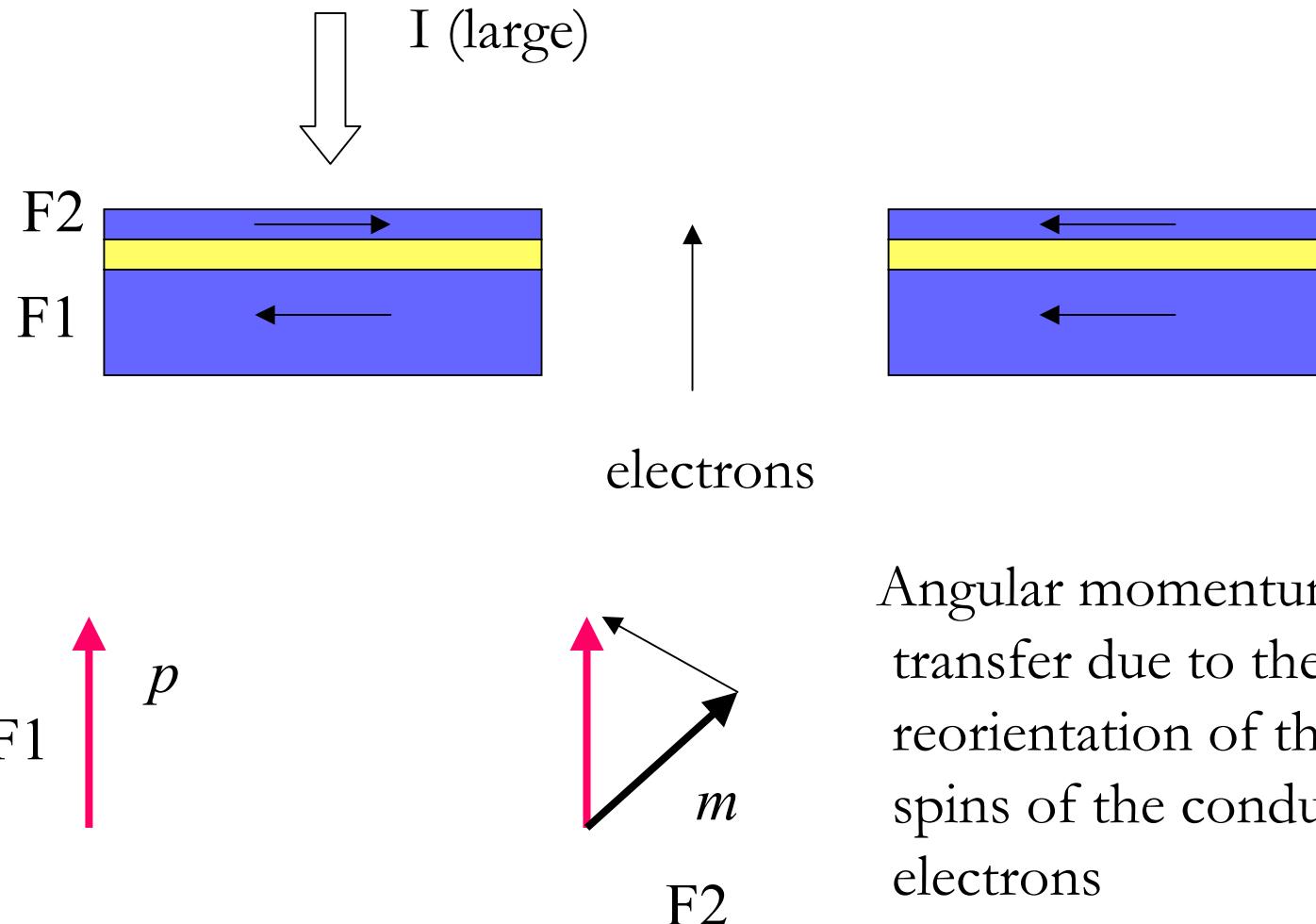


FIG. 5. Circles show the measurements by Mizukami *et al.* (Ref. 16) of the Gilbert damping in Py-Cu-Pt trilayer and Py-Cu bilayer as a function of the Cu buffer thickness L . Solid lines are our theoretical prediction according to Eqs. (26) and (27).

Spin transfer effects



Spin-polarized current switching of a Co thin film nanomagnet

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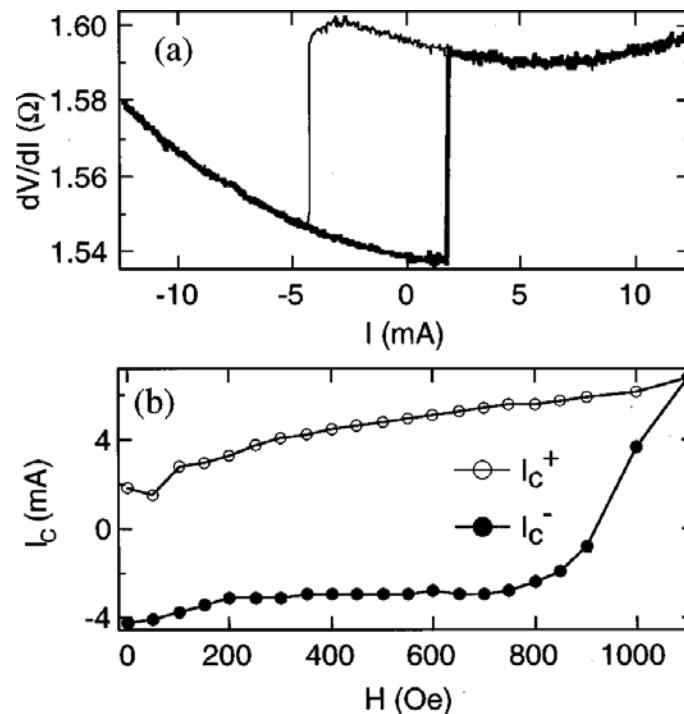
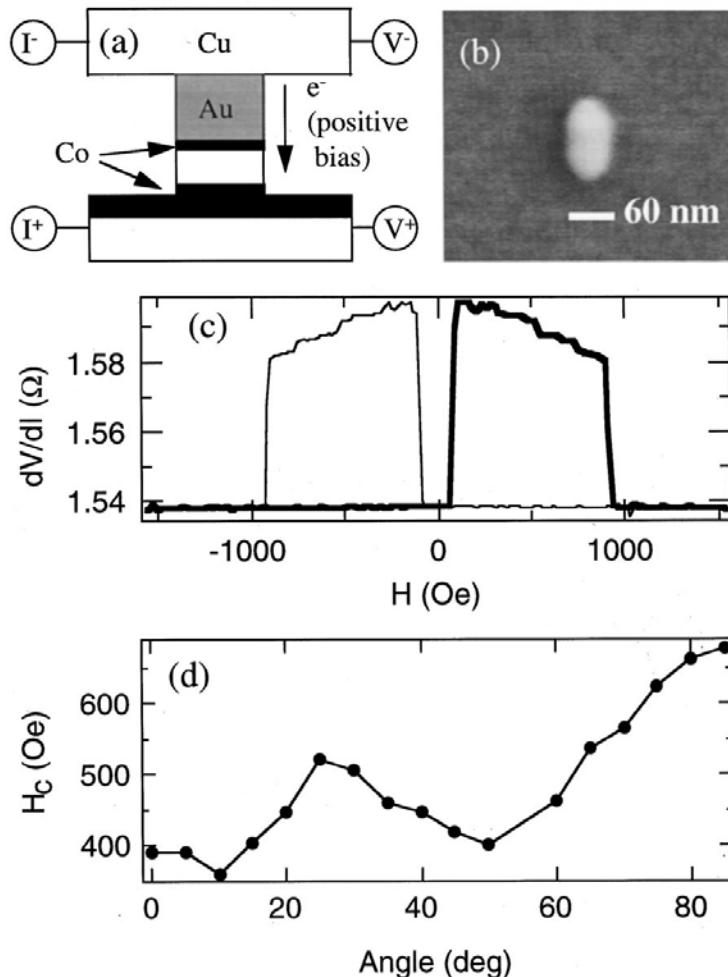
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Conclusions :

Micromagnetics

- has witnessed many decades of increasing success
- becomes more and more challenged by experiments on nanoscale samples