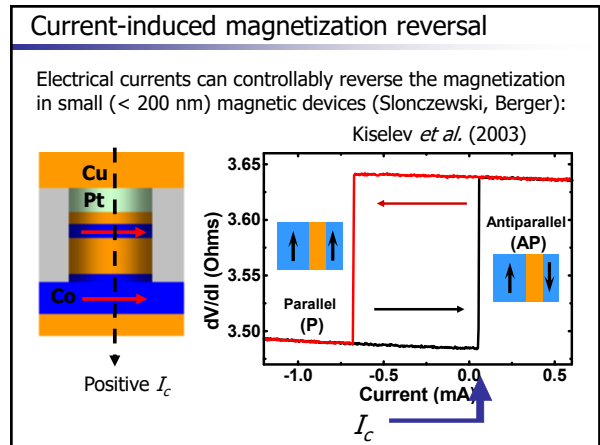


Current-induced magnetization reversal

Electrical currents can controllably reverse the magnetization in small (< 200 nm) magnetic devices (Slonczewski, Berger):

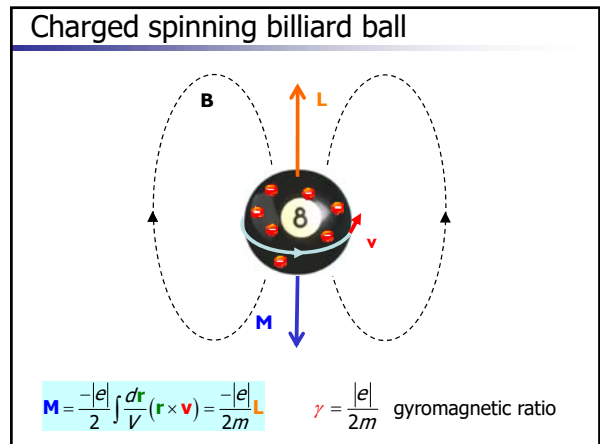


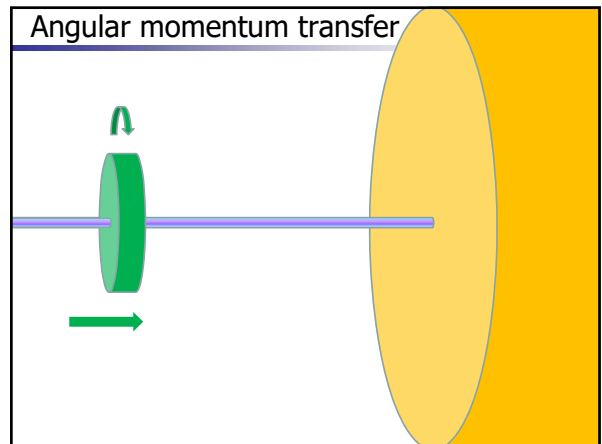
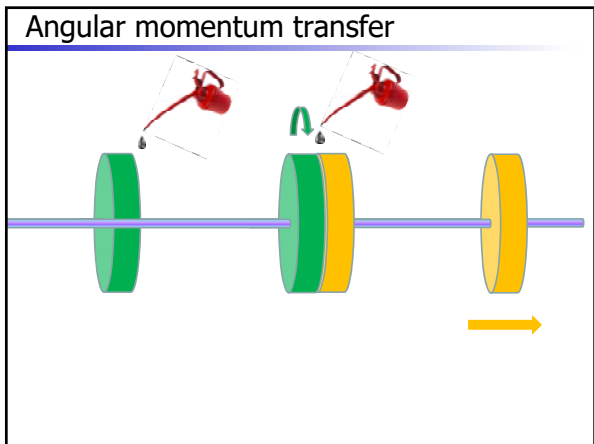
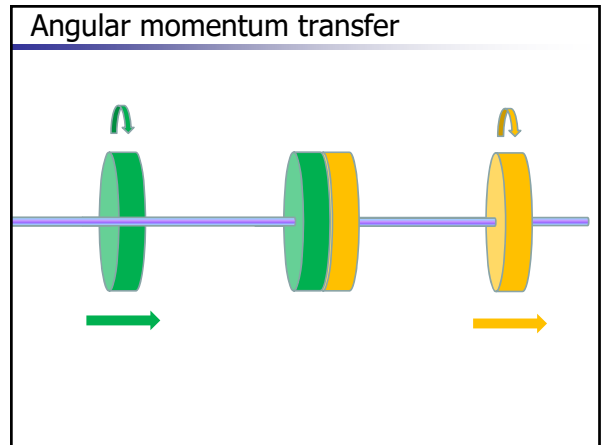
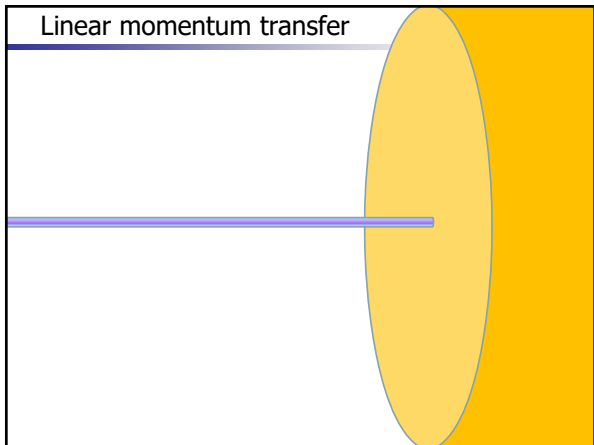
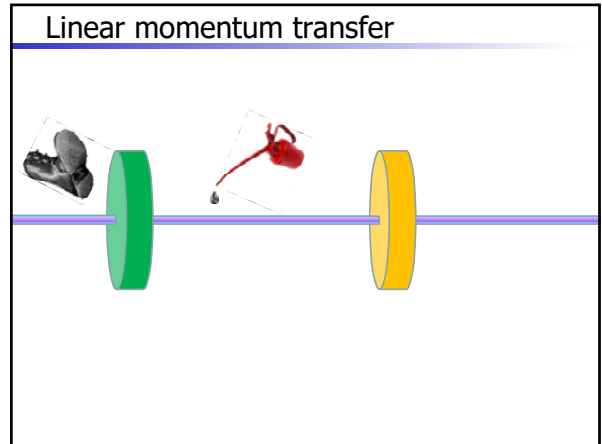
2013 Oliver E. Buckley Condensed Matter Physics Prize

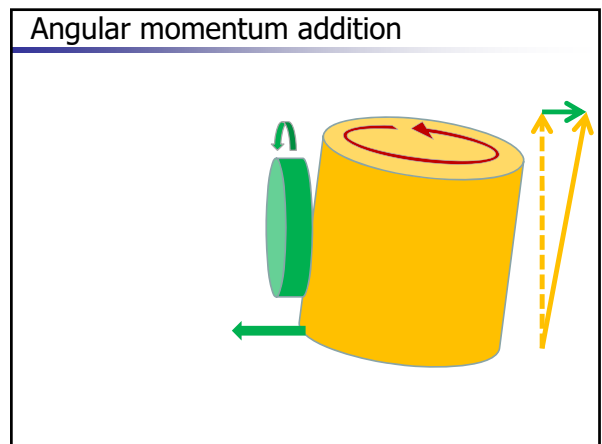
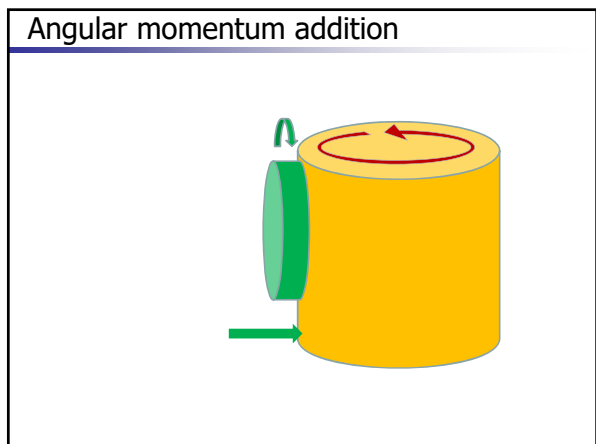
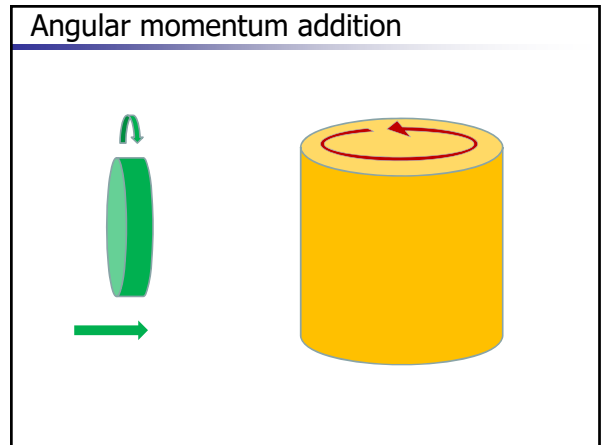
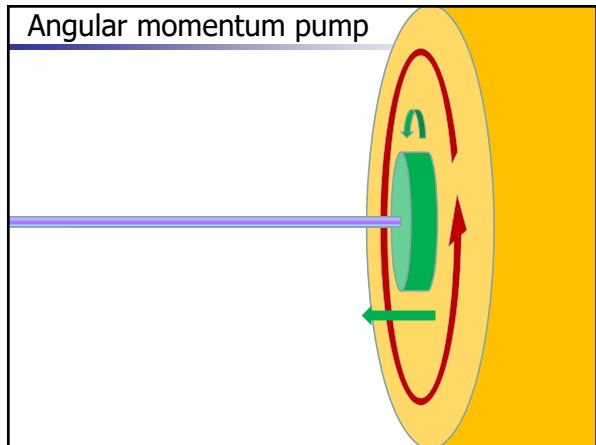
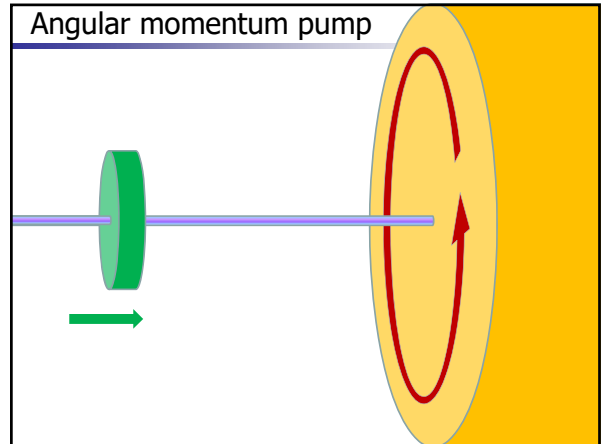
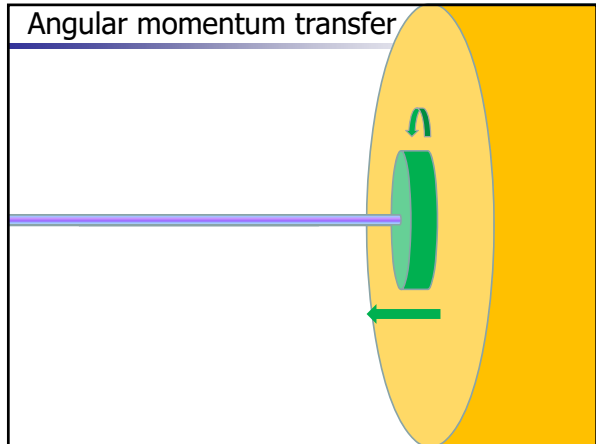
Luc Berger
Carnegie Mellon University

John Slonczewski
IBM Research Staff Emeritus

Citation:
"For predicting spin-transfer torque and opening the field of current-induced control over magnetic nanostructures."







Rotation in quantum mechanics

$\hat{R}_z(d\varphi)f = f(x+dx, y+dy) = f + \frac{\partial f}{\partial x}dx + \frac{\partial f}{\partial y}dy$
 $= f + \left(-y\frac{\partial}{\partial x} + x\frac{\partial}{\partial y}\right)f d\varphi = \left(1 + \frac{i}{\hbar}\hat{L}_z d\varphi\right)f$

Finite rotation: $\varphi = \lim_{n \rightarrow \infty} n d\varphi$
 $\hat{R}_z(\varphi) = \lim_{n \rightarrow \infty} \left(1 + \frac{i}{\hbar}d\varphi\hat{L}_z\right)^n$
 $\log(1+x) \approx x$
 $\rightarrow \lim_{n \rightarrow \infty} \log(1+x)^n \approx \lim_{n \rightarrow \infty} nx$
 $\log \hat{R}_z(\varphi) = \lim_{n \rightarrow \infty} \frac{i}{\hbar}(nd\varphi)\hat{L}_z = \frac{i}{\hbar}\varphi\hat{L}_z \rightarrow \hat{R}_z(\varphi) = e^{i\varphi\hat{L}_z/\hbar}$

$x' = x + dx = x - yd\varphi$
 $y' = y + dy = y + xd\varphi$

Rotation in quantum mechanics

Rotation of a state $|\Psi\rangle$ by an angle θ around an axis with unit vector \mathbf{n} : $|\Psi\rangle_R = \hat{R}_n(\theta)|\Psi\rangle$
 Rotation operator: $\hat{R}_n(\theta) = \exp(i\theta\mathbf{n} \cdot \hat{\mathbf{L}}/\hbar)$
 Electron spin: $\hat{\mathbf{L}} = \mathbf{s} = \frac{\hbar}{2}\boldsymbol{\sigma}$

$\hat{R}_n(\theta) = e^{i\mathbf{n}\cdot\boldsymbol{\sigma}\theta/2}$

With $\mathbf{n} = (\cos\varphi, \sin\varphi, 0)$
 $\psi(\varphi, \theta) = \mathbf{R}(\varphi, \theta) \begin{pmatrix} 1 \\ 0 \end{pmatrix}$
 generates all possible spin states.
 Example:
 $|\rightarrow\rangle_x = \mathbf{R}\left(\frac{\pi}{2}, \frac{\pi}{2}\right) \begin{pmatrix} 1 \\ 0 \end{pmatrix}$

Spins on the Bloch sphere

$\mathbf{R}\left(\frac{\pi}{2}, \theta\right) = e^{i\sigma_y\theta/2} = e^{\begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}\theta/2} = \sum_{m=0}^{\infty} \frac{1}{m!} \begin{pmatrix} 0 & 1 \\ -1 & 0 \end{pmatrix}^m \left(\frac{\theta}{2}\right)^m$
 $= \begin{pmatrix} \cos\frac{\theta}{2} & -\sin\frac{\theta}{2} \\ \sin\frac{\theta}{2} & \cos\frac{\theta}{2} \end{pmatrix}$

$\mathbf{R}\left(\frac{\pi}{2}, 2\pi\right) = -\begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}$

Spin-up state in x -direction is obtained by rotation about y -axis with $\theta = \pi/2$.
 $|\rightarrow\rangle_x = \frac{1}{\sqrt{2}} \begin{pmatrix} 1 \\ 1 \end{pmatrix}$

Check: ${}_x\langle\rightarrow|\mathbf{s}|\rightarrow\rangle_x = \frac{\hbar}{2}(1, 0, 0)$

Slonczewski torque in half metals

Normal **HMF**
 $|\uparrow\rangle \rightarrow (|\rightarrow\rangle + |\leftarrow\rangle)/\sqrt{2}$
 longitudinal spin current
 transverse spin current = torque

$\tau = \beta$
 $\tau\left(\theta = \frac{\pi}{2}\right) = \frac{Ne}{2\pi}(V_{\uparrow} - V_{\downarrow})$
 $N = \text{number of incoming channels}$

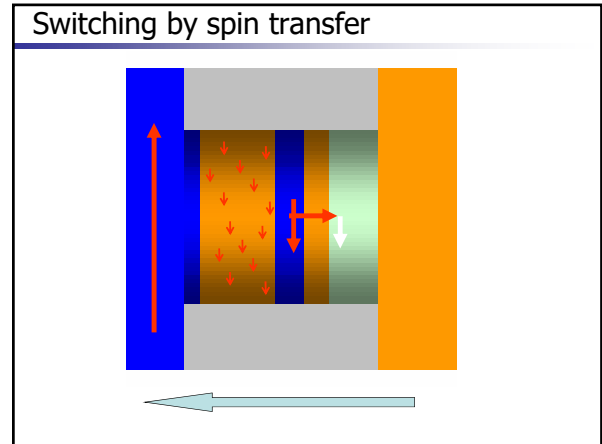
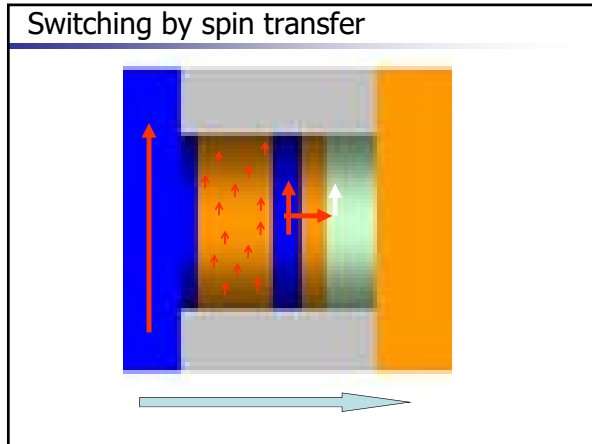
Spin-mixing conductance

$\tau(\mathbf{m} = \hat{x}) = \frac{\hbar}{e} \frac{e^2 N}{h} (V_{\uparrow} - V_{\downarrow})$
 $G_{\text{Sharvin}} = \frac{2e^2}{h} \sum_{\mathbf{k}} 1 = \frac{2e^2}{h} N$
 $\mathbf{k} \rightarrow$ incoming wave vectors

Scattering theory: $\tau(\mathbf{m} = \hat{x}) = \frac{\hbar}{e}(V_{\uparrow} - V_{\downarrow}) \{ \hat{z} \text{Re} G_{\uparrow\downarrow} + \hat{y} \text{Im} G_{\uparrow\downarrow} \}$
 Spin mixing conductance: $G_{\uparrow\downarrow} = \frac{e^2}{h} \sum_{\mathbf{k}} \left(1 - r_{\uparrow\mathbf{k}}^{\uparrow} (r_{\uparrow\mathbf{k}}^{\downarrow})^*\right) \approx \frac{e^2 N}{h}$

Exchange-field torque

Precession by spins in evanescent states



Ohm's and Kirchoff's Laws

charge conservation
 $\sum_j I_{c,j \rightarrow i} = 0$

Charge current:
 $I_{c,1 \rightarrow 2} = G_{1 \rightarrow 2} (V_1 - V_2)$ $G_{1 \rightarrow 2}$ conductance

$G = \frac{e^2}{h} g = \frac{e^2}{h} \sum_{nm} |t_{nm}|^2$ Landauer formula

Spin currents

v_s^N spin accumulation in N
 v_s^F spin accumulation in F \parallel \mathbf{m} magnetization direction

$I_c, \mathbf{I}_{s,||}, \mathbf{I}_{s,\perp}$
transverse
collinear/longitudinal spin currents

$\mathbf{I}_{s,\perp} = 2\text{Re} G_{\uparrow\downarrow} (\mathbf{m} \times \mathbf{V}_s^N \times \mathbf{m}) + 2\text{Im} G_{\uparrow\downarrow} (\mathbf{V}_s^N \times \mathbf{m})$
 $\boldsymbol{\tau} = -\frac{\hbar}{2e} \mathbf{I}_{s,\perp}$ in-plane (damping) out-of-plane (effective field)

Spin currents

v_s^N spin accumulation in N
 v_s^F spin accumulation in F \parallel \mathbf{m} magnetization direction

$I_c, \mathbf{I}_{s,||}, \mathbf{I}_{s,\perp}$
transverse
collinear/longitudinal spin currents

$g_s = \sum_{nm} |t_{nm}^s|^2 = N - \sum_{nm} |r_{nm}^s|^2$ $s = \uparrow, \downarrow$ spin-dependent Landauer conductances for **charge and collinear** spin current

$g_{\uparrow\downarrow} = N - \sum_{nm} r_{nm}^\uparrow (r_{nm}^\downarrow)^*$ complex spin-mixing conductance for **transverse** spin current (torque + exchange field)

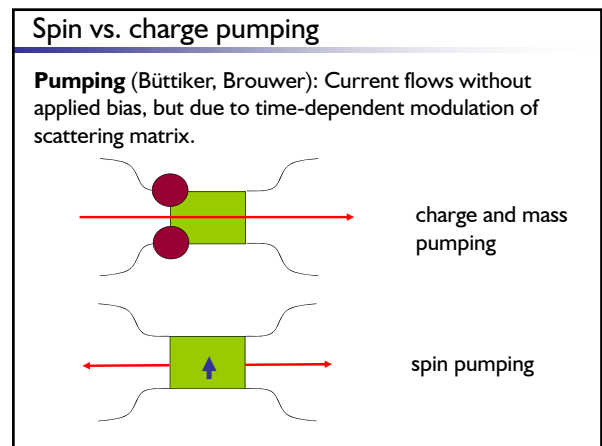
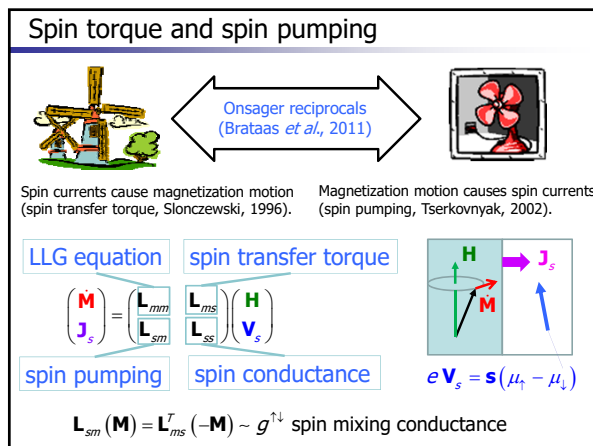
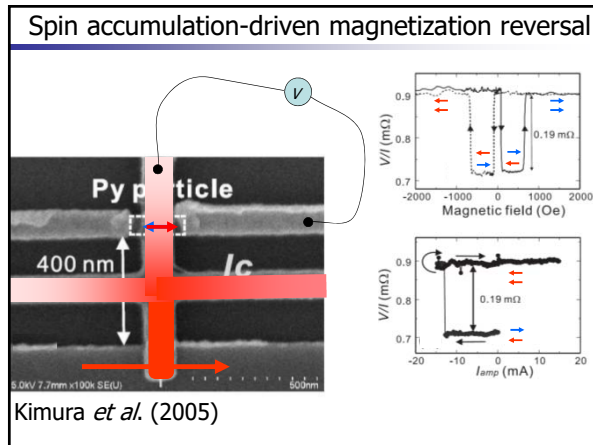
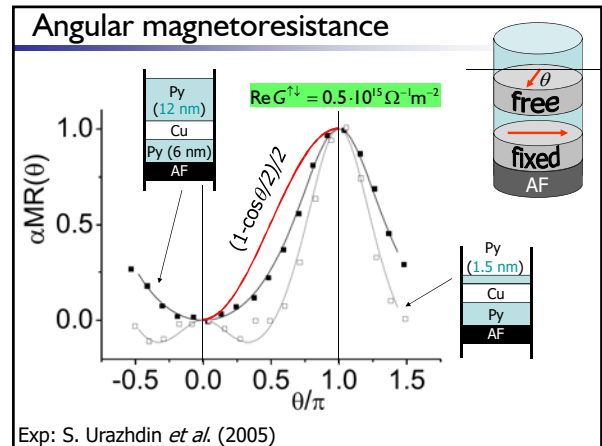
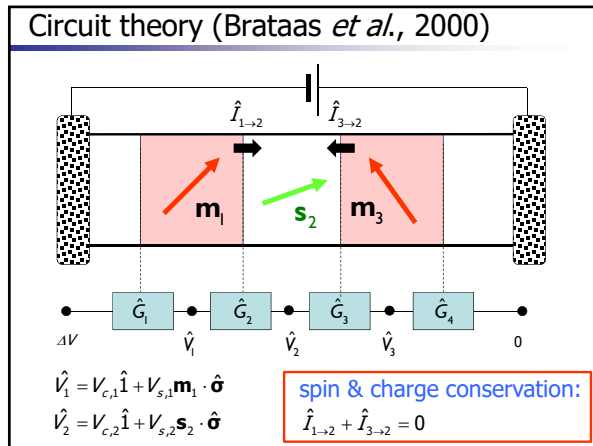
Pauli matrix notation

$(\hat{\mathbf{i}}, \hat{\boldsymbol{\sigma}}) = \left\{ \begin{pmatrix} 1 & 0 \\ 0 & 1 \end{pmatrix}, \begin{pmatrix} 0 & 1 \\ 1 & 0 \end{pmatrix}, \begin{pmatrix} 0 & -i \\ i & 0 \end{pmatrix}, \begin{pmatrix} 1 & 0 \\ 0 & -1 \end{pmatrix} \right\}$

$\hat{X} = \begin{pmatrix} X_{\uparrow\uparrow} & X_{\uparrow\downarrow} \\ X_{\uparrow\downarrow}^* & X_{\downarrow\downarrow} \end{pmatrix} = X_c \hat{\mathbf{1}} + \mathbf{X}_s \hat{\boldsymbol{\sigma}}$

$\hat{V}^N = V_c^N \hat{\mathbf{1}} + \mathbf{V}_s^N \cdot \hat{\boldsymbol{\sigma}}$
 $\hat{V}^F = V_c^F \hat{\mathbf{1}} + \mathbf{V}_s^F \cdot \mathbf{m} \cdot \hat{\boldsymbol{\sigma}}$
 $\hat{I} = I_c \hat{\mathbf{1}} + \mathbf{I}_s \cdot \hat{\boldsymbol{\sigma}}$

$\hat{G} = \begin{pmatrix} G_{\uparrow} & G_{\uparrow\downarrow} \\ G_{\uparrow\downarrow}^* & G_{\downarrow} \end{pmatrix}$



Spin pumping

$$\vec{j}_{\text{pump}}^{F \rightarrow N} = \frac{\hbar}{4\pi} \mathbf{g}_{\uparrow\downarrow} \mathbf{m} \times \frac{d\mathbf{m}}{dt}$$

Dynamics of bilayers

Landau-Lifshitz-Gilbert equation with new torque term:

$$\frac{\partial \mathbf{m}}{\partial t} = -\gamma \mathbf{m} \times \mathbf{B} + \alpha_0 \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t} + \frac{\hbar \gamma}{4\pi M} \mathbf{m} \times (\mathbf{l}_s^{\text{diss}} + \mathbf{l}_s^{\text{pump}}) \times \mathbf{m}$$

$$= -\gamma \mathbf{m} \times \mathbf{B} + \left(\alpha_0 + \frac{\hbar \gamma}{4\pi M} \mathbf{g}_{\uparrow\downarrow} \right) \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t} + \frac{\hbar \gamma}{4\pi M} \mathbf{g}_{\uparrow\downarrow} \mathbf{m} \times \mathbf{s} \times \mathbf{m}$$

spin pumping Slonczewski torque

Sources and sinks of spin currents

$$\frac{\partial \mathbf{m}}{\partial t} = -\mathbf{m} \times \gamma \mathbf{H} + \alpha_0 \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t} + \boldsymbol{\tau}$$

$$\boldsymbol{\tau} = \boldsymbol{\tau}_{\text{sp}} + \boldsymbol{\tau}_{\text{stc}}$$

enhanced damping

$\tau_{\text{sp}} \rightarrow \infty$
 $\lambda_{\text{sd}} / d_N \gg 1$
 $\frac{\partial \mathbf{m}}{\partial t} = -\mathbf{m} \times \gamma \mathbf{H} + \alpha_0 \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t}$

$\tau_{\text{sp}} \rightarrow 0$
 $\lambda_{\text{sd}} / d_N \ll 1$
 $\frac{\partial \mathbf{m}}{\partial t} = -\mathbf{m} \times \gamma \mathbf{H} + \left(\alpha_0 + \frac{\hbar \gamma}{4\pi M_s} \mathbf{g}_{\uparrow\downarrow} \right) \mathbf{m} \times \frac{\partial \mathbf{m}}{\partial t}$

Py|Pt mixing conductance

Mizukami et al. (2001)

$$G = \gamma M_s \alpha$$

$$G(d) = G_0 + \frac{(g_L \mu_B)^2 G_s^{\uparrow\downarrow}}{e^2 Ad}$$

$g_L = 2.1$ $G_0 = 10^8 \text{ Hz}$

Py|Pt:
 $\frac{G_s^{\uparrow\downarrow}}{A} = 1.0 \cdot 10^{15} \Omega^{-1} \text{ m}^{-2}$

Kato et al. (2004)

Spin current tensor, spin Hall angle

$$\vec{j}_s = (\mathbf{J}_s^x, \mathbf{J}_s^y, \mathbf{J}_s^z) = \begin{pmatrix} \mathbf{J}_{s,x} \\ \mathbf{J}_{s,y} \\ \mathbf{J}_{s,z} \end{pmatrix}$$

$\mathbf{J}_{s,x}^x$ polarization of current || x
 $\mathbf{J}_{s,x}^y$ current direction of polarization || x

$$\mathbf{J}_{s,\beta} = \theta_{SH} \hat{\beta} \times \mathbf{J}_c$$

$$\mathbf{J}_c = \theta_{SH} \sum_{\alpha} \mathbf{J}_s^{\alpha} \times \hat{\alpha}$$

