

# Curie temperature ??

Ideally measured with low magnetic field since High field shifts the  $T_c$  of ferro to High temperature

Hypothesis mean field theory and low field

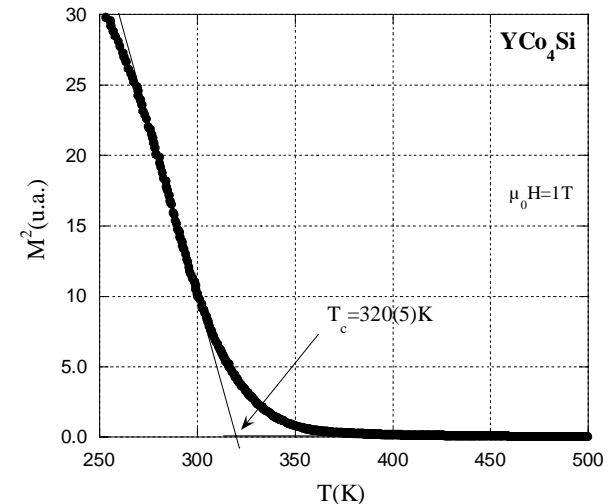
$$\begin{cases} m = \mathcal{B}_J(x) = ax(1-bx^2) \\ m = atx - \frac{H}{wM_0} \end{cases}$$

with  $t = T/T_C$  and  $b = (J^2 + (J+1)^2)/(30J^2)$

Then for  $H=0$

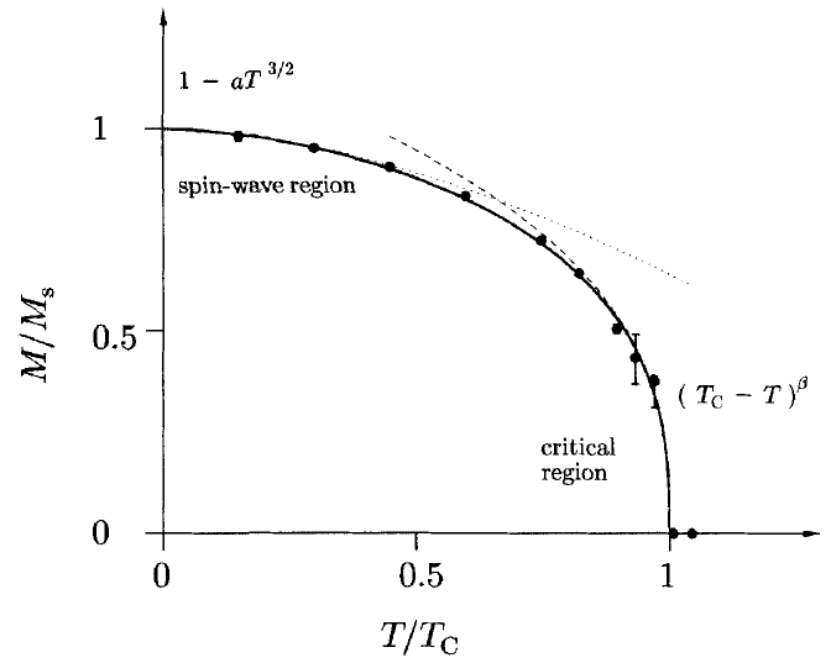
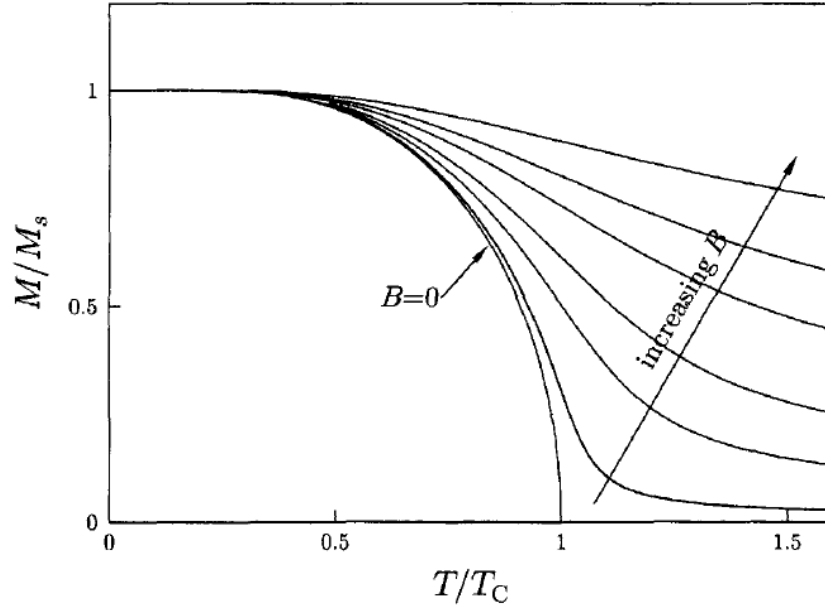
$$m_s^2 = \left( \frac{M_s}{M_0} \right)^2 = \frac{a^2}{b} t^2 (1-t) = \frac{a^2}{b} (1-t) = \frac{10}{3} \frac{(J+1)^2}{J^2 + (J+1)^2} \left( 1 - \frac{T}{T_C} \right)$$

So that one use  $M^2 = f(T)$  extrapolate linearly to  $T_c$



**Avoid using  $M(T)$  and the derivative**

# Low applied magnetic field necessary



Crucial when critical exponents are looked for

# Another method plot $M^2$ versus $(H/M)$

Belov K P and Goryaga A N 1956 *Fiz. Met. Metalloved.* 2 3

A. Arrott, *Phys. Rev. B* 108 (1957) 1394.

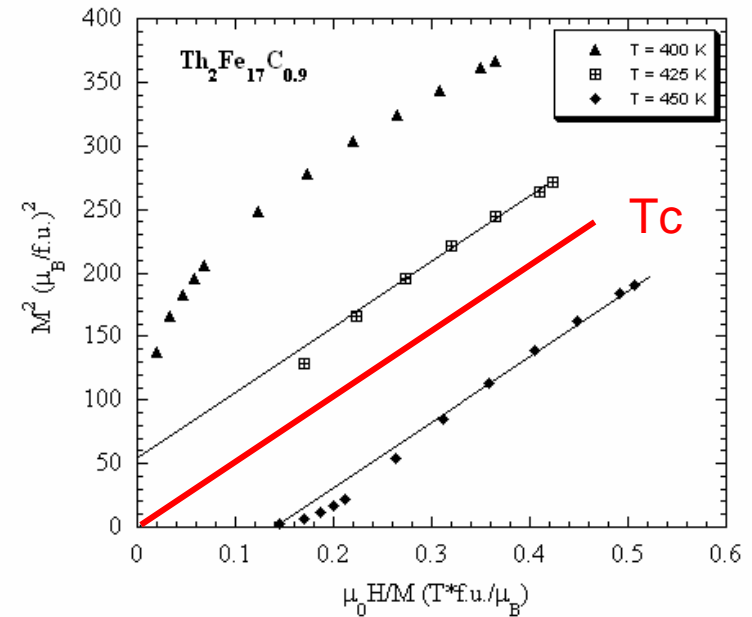
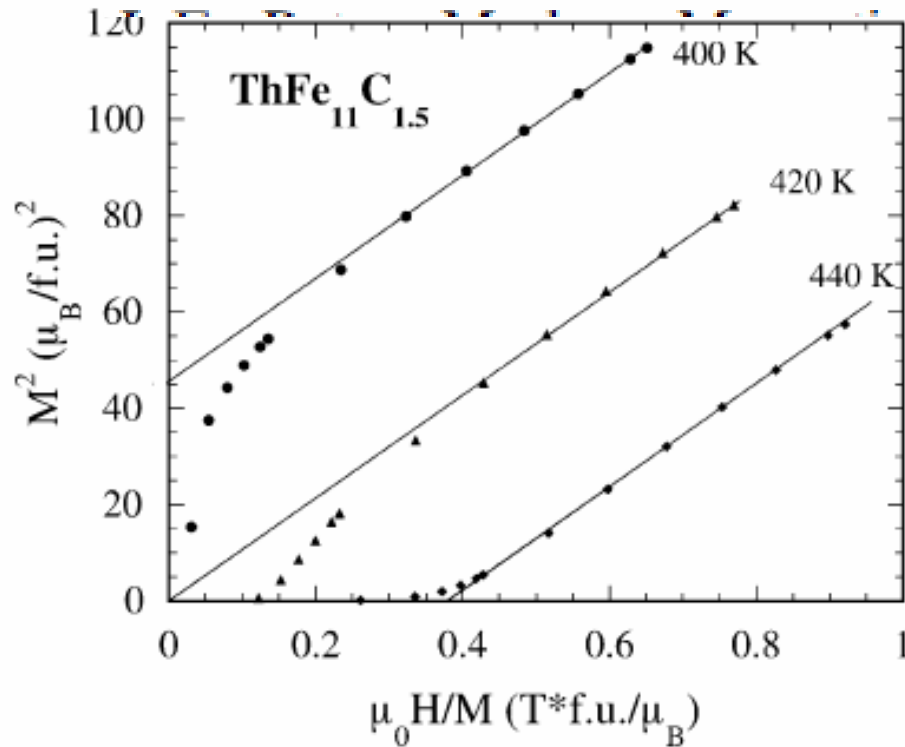


Fig. 3. Arrott plots at the indicated temperature around the Curie temperature of  $\text{ThFe}_{11}\text{C}_{1.5}$ .

Give similar values than  $M^2$  (T)

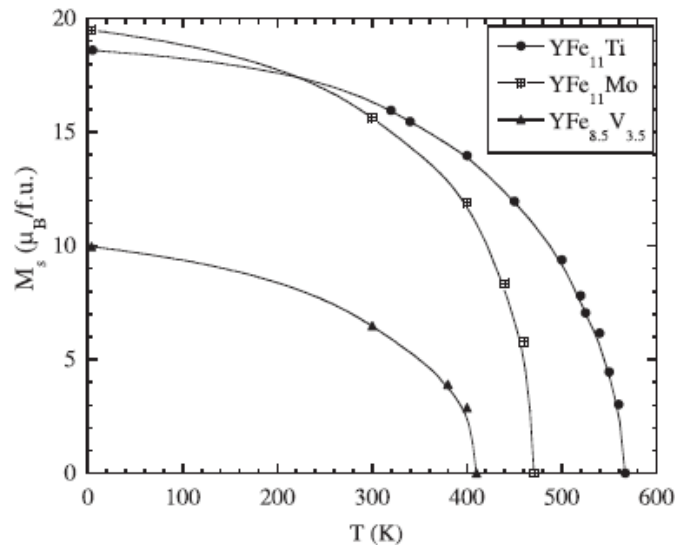
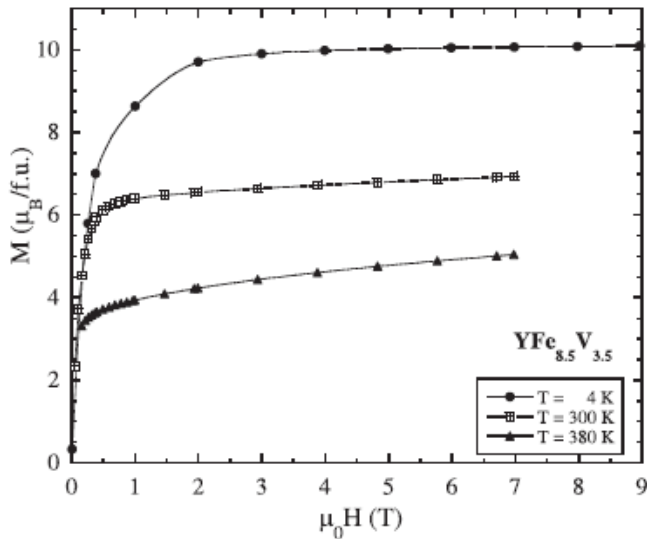
Why two magnetic moments ??

What is the difference ??

Which one do we measure experimentally ??

$$m_0 = g J$$

$$m_{\text{eff}} = g (J (J+1))^{1/2}$$



Ordered state

$$m_0 = g J$$

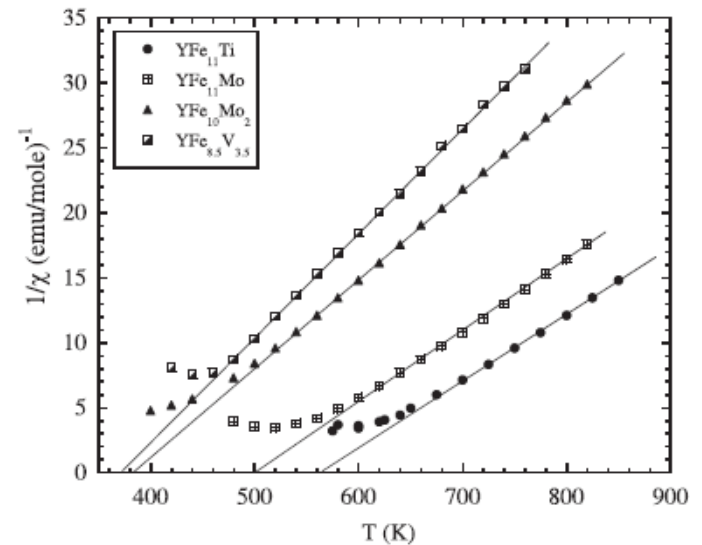
Obtained from saturation magnetization

Paramagnetic state

$$m_{\text{eff}} = g (J (J+1))^{1/2}$$

Obtained from Curie –Weiss Law

$$C = n \mu_0 \frac{\mu_{\text{eff}}^2}{3k_B}$$



# Behaviour of the transition metal ions **3d**.

Ion	3d <sup>n</sup>	2S+1L <sub>J</sub>	g	Moment effective		
				Theoretical		Experimental
				$\mu_{ef}(\mu_B) = g_J \sqrt{J(J+1)}$	$\mu_{ef}(\mu_B) = g_S \sqrt{S(S+1)}$	$\mu_{ef}(\mu_B)$
Ti <sup>3+</sup> , V <sup>4+</sup>	1	2D <sub>3/2</sub>	4/5	1,55	1,73	1,7
Ti <sup>2+</sup> , V <sup>3+</sup>	2	3F <sub>2</sub>	2/3	1,63	2,83	2,8
V <sup>2+</sup> , Cr <sup>3+</sup> , Mn <sup>4+</sup>	3	4F <sub>3/2</sub>	2/5	0,77	3,87	3,8
Cr <sup>2+</sup> , Mn <sup>3+</sup>	4	5D <sub>0</sub>	-	0	4,90	4,9
Mn <sup>2+</sup> , Fe <sup>3+</sup>	5	5S <sub>5/2</sub>	2	5,92	5,92	5,9
Fe <sup>2+</sup> , Co <sup>3+</sup>	6	5D <sub>4</sub>	3/2	6,70	4,90	5,4
Co <sup>2+</sup> , Ni <sup>3+</sup>	7	4F <sub>9/2</sub>	4/3	6,64	3,87	4,8
Ni <sup>2+</sup>	8	3F <sub>4</sub>	5/4	5,59	2,83	3,2
Cu <sup>2+</sup>	9	2D <sub>5/2</sub>	6/5	3,55	1,73	1,9
Cu <sup>+</sup> , Zn <sup>2+</sup>	10	2S <sub>0</sub>	-	0	0	0

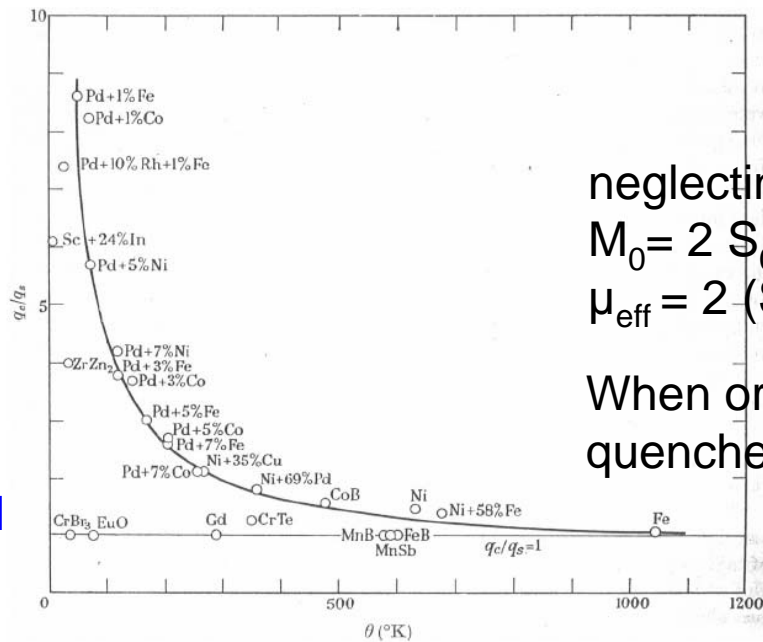
## Behaviour of the rare-earth metal ions 4f

Z	Ion	4f <sup>n</sup>	S	L	J	<sup>2S+1</sup> L <sub>J</sub>	g	m=gJ (μ <sub>B</sub> )	$\mu_{ef}(\mu_B) = g_J \sqrt{J(J+1)}$	$\mu_{eff}(\mu_B)$ experimental
57	La <sup>3+</sup>	4f <sup>0</sup>	0	0	0	<sup>1</sup> S <sub>0</sub>	0	0	0	0
58	Ce <sup>3+</sup>	4f <sup>1</sup>	1/2	3	5/2	<sup>2</sup> F <sub>5/2</sub>	6/7	2,14	2,54	2,4-2,7
59	Pr <sup>3+</sup>	4f <sup>2</sup>	1	5	4	<sup>3</sup> H <sub>4</sub>	4/5	3,2	3,58	3,4-3,6
60	Nd <sup>3+</sup>	4f <sup>3</sup>	3/2	6	9/2	<sup>4</sup> I <sub>9/2</sub>	8/11	3,27	3,62	3,5-3,7
61	Pm <sup>3+</sup>	4f <sup>4</sup>	2	6	4	<sup>5</sup> I <sub>4</sub>	3/5	2,4	2,68	-
62	Sm <sup>3+</sup>	4f <sup>5</sup>	5/2	5	5/2	<sup>6</sup> H <sub>5/2</sub>	2/7	0,71	0,85	1,4-1,7
63	Eu <sup>3+</sup>	4f <sup>6</sup>	3	3	0	<sup>7</sup> F <sub>0</sub>	-	0	0	3,6
63	Eu <sup>2+</sup>	4f <sup>7</sup>	7/2	0	7/2	<sup>8</sup> S <sub>7/2</sub>	2	7	7,94	7,98
64	Gd <sup>3+</sup>	4f <sup>7</sup>	7/2	0	7/2	<sup>8</sup> S <sub>7/2</sub>	2	7	7,94	7,98
65	Tb <sup>3+</sup>	4f <sup>8</sup>	3	3	6	<sup>7</sup> F <sub>6</sub>	3/2	9	9,72	9,0-9,8
66	Dy <sup>3+</sup>	4f <sup>9</sup>	5/2	5	15/2	<sup>6</sup> H <sub>15/2</sub>	4/3	10	10,6	10,5-10,8
67	Ho <sup>3+</sup>	4f <sup>10</sup>	2	6	8	<sup>5</sup> I <sub>8</sub>	5/4	10	10,6	10,3-10,5
68	Er <sup>3+</sup>	4f <sup>11</sup>	3/2	6	15/2	<sup>4</sup> I <sub>15/2</sub>	6/5	9	9,58	9,4-9,6
69	Tm <sup>3+</sup>	4f <sup>12</sup>	1	5	6	<sup>3</sup> H <sub>6</sub>	7/6	7	7,56	7,2-7,6
70	Yb <sup>3+</sup>	4f <sup>13</sup>	1/2	3	7/2	<sup>2</sup> F <sub>7/2</sub>	8/7	4	4,53	4,4-4,6
71	Lu <sup>3+</sup>	4f <sup>14</sup>	0	0	0	<sup>1</sup> S <sub>0</sub>	0	0	0	0

Itinerant

May be much different for non ionic cases  
band magnetism

localize → 1



$$M_0 = g J$$

$$\mu_{\text{eff}} = g (J (J+1))^{1/2}$$

neglecting L we got

$$M_0 = 2 S_0$$

$$\mu_{\text{eff}} = 2 (S (S+1))^{1/2}$$

When orbital moment is quenched

$$\mu_{\text{eff}} = \mu_B \sqrt{q_c (q_c + 2)}$$

Figure A6-2 : Courbe de Rhodes – Wohlfarth : tracé du rapport  $r = q_c/q_s$  en fonction de la température de Curie ( $\theta$ ).

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O Isnard and V Pop

Table 2. Saturation magnetization  $M_s$ , Curie–Weiss constant  $C$ , paramagnetic effective moment  $\mu_{\text{eff}}$ , mean number of spins in the ordered  $S_0$  or paramagnetic states  $S_p$  and the corresponding ratio  $r = S_p/S_0$  for the  $\text{YFe}_{12-x}\text{M}_x$  compounds compared to that of the pure Fe.

Compound	$M_s$ 300 K ( $\mu_B/\text{f.u.}$ )	$M_s$ 4 K ( $\mu_B/\text{f.u.}$ )	$M_{\text{Fe}}$ 4 K ( $\mu_B/\text{atom}$ )	$S_0$	$\mu_{\text{eff}}$ ( $\mu_B/\text{Fe atom}$ )	$S_p$	$r$	$C$ ( $\mu_B \text{ K}/\text{f.u. T}$ )
$\text{YFe}_{11}\text{Ti}$	16.3	18.6	1.69	0.845	3.745	1.439	1.70	34.59
$\text{YFe}_{11}\text{Mo}$	15.6	19.8	1.8	0.90	3.649	1.392	1.55	32.80
$\text{YFe}_{10}\text{Mo}_2$	5.5	13.1	1.31	0.655	3.412	1.278	1.95	26.07
$\text{YFe}_{8.5}\text{V}_{3.5}$	6.5	9.96	1.17	0.586	3.409	1.277	2.18	22.12
$\alpha\text{-Fe}$	2.17	2.22	2.22	1.11	3.18	1.17	1.05	2.26